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# Empirical Evidence for Embodied Semantics 

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#### Abstract

This paper addresses the question whether and under which conditions hearers take into account the perspective of the speaker, and vice versa. Distinguishing between speaker meaning and hearer meaning, empirical evidence from computational modeling, psycholinguistic experimentation and corpus research is presented which suggests that literal sentence meanings result from the hearer's failure to calculate the speaker meaning. Similarly, nonrecoverable forms may result from the speaker's failure to calculate the hearer meaning.


Keywords: Bidirectional Optimality Theory, Embodied Semantics, Perspective Taking, Processing Efficiency, Pronouns, Word Order.

## 1 Introduction

If we were to interpret all sentences literally, we would frequently misunderstand others. We wouldn't understand metaphors such as The car died on me, we would have trouble responding appropriately to indirect speech acts like Can you tell me the time?, and we would fail to understand the implicated meaning 'I did not read all of her papers' for the utterance I read some of her papers. Fortunately, many hearers are quite capable of going beyond the literal meaning of these utterances to grasp the meaning that was intended by the speaker. However, despite hearers' remarkable ability to avoid misunderstanding, how hearers arrive at the intended meaning is still the subject of a lively debate.

Traditionally, a sharp distinction is made between sentence meaning (i.e., the literal meaning of the sentence) and speaker meaning (i.e., what the speaker intended to communicate) (see [1] for discussion). Sentence meaning is assumed to be explained by a theory of grammar, whereas speaker meaning is assumed to be explained by a theory of pragmatics. It is thus believed that semantics and pragmatics are distinct domains, with the only uncertainty being where exactly the distinction should be drawn. Contrasting with this traditional view on meaning, this paper argues in favor of embodied semantics, the view that meaning does not exist independently of speakers and hearers. Consequently, the relevant distinction is argued to be between speaker meanings and hearer meanings. In this paper, empirical evidence of various sorts will be provided to support this alternative view. The central claim is that interpretation always aims at calculating the speaker meaning. However, if
hearers fail to do this, perhaps because they do not have sufficient processing resources or cognitive abilities to do so, they may assign a different, for example literal, meaning instead. Similarly, sentence generation is argued to always aim at calculating the hearer meaning. This guarantees that the produced sentence conveys the intended meaning. If speakers fail to do this, they may produce a non-recoverable form instead.

A distinction between speaker meanings and hearer meanings presupposes a linguistic theory that distinguishes the speaker's perspective from the hearer's perspective. The next section introduces different approaches to perspective taking in semantics and pragmatics. Section 3 considers the question whether and under which conditions hearers calculate the speaker meaning. This question is addressed on the basis of experimental investigations of the pronoun interpretation problem in language acquisition. Section 4 considers the inverse question and asks whether speakers calculate the hearer meaning. This possibility is investigated by looking at semantic factors determining word order in Dutch.

## 2 Perspective Taking in Semantics and Pragmatics

In his influential William James lectures at Harvard in 1967, Grice [2] proposed that speakers are guided by a Cooperative Principle, backed by a set of Maxims of Conversation that specify speakers' proper conduct. For example, the Maxim of Relation tells speakers to be relevant, and the Maxim of Quantity tells speakers to make their contribution as informative as is required for the purposes of the exchange, but not more informative than that. By choosing a particular form to express their intentions, speakers assume that hearers will be able to infer the intended meaning on the basis of this form. Grice formulates this as follows: "'[Speaker] meant something by $x$ ' is (roughly) equivalent to '[Speaker] intended the utterance of $x$ to produce some effect in an audience by means of the recognition of this intention." (p. 220).

Several later studies have sought to reduce Grice's maxims, while maintaining the division of labor between speakers and hearers in the sense that speakers choose the sentence to be uttered, while hearers must do a certain amount of inferencing to determine the speaker's intended meaning. However, given Grice's formulation of the Maxim of Quantity, speakers also have to do some inferencing, as they have to determine how much information is required for the purposes of the exchange. Are the inferences that speakers draw of the same sort as the inferences that hearers draw, or are they fundamentally different?

A fully symmetric account of conversational inference, according to which hearers and speakers make similar inferences about the effects of their choices, has been proposed within the framework of optimality theory (OT) [3]. According to Blutner's definition of bidirectional optimality theory (biOT) [4], speakers select the best form for a given meaning, thereby taking into account the hearer's perspective, and hearers select the best meaning for a given form, thereby taking into account the speaker's perspective. Contrasting with Blutner's symmetric conception of bidirectional optimization, various asymmetric models have been proposed. For example, Zeevat proposes an asymmetric model according to which hearers take into account the
speaker's perspective, while speakers do not take into account the hearer's perspective to the same degree [5]. A similar position is adopted by Franke in his game theoretic model of conversational inference [6]. Jäger, on the other hand, develops a bidirectional learning algorithm in which speakers take into account hearers when evaluating form-meaning pairs, but not vice versa [7]. These different positions are mainly based on theoretical arguments and have not been tested by looking at the actual processes of speaking and understanding. Therefore, a relevant question is whether it is possible to find empirical evidence for the symmetry or asymmetry of conversational inference by considering how actual hearers and speakers comprehend and generate sentences.

A second question, which is independent of the symmetry or asymmetry of perspective taking and conversational inference but is relevant in relation to the traditionally assumed distinction between semantics and pragmatics, is whether the proposed conversational inferences are automatic word-by-word interpretational processes (as is believed to be the case for grammatical processes) or additional end-of-sentence processes (as is assumed by some to be true for pragmatic processes). Whereas unidirectional optimization may be seen as a localist incremental mechanism of interpretation, Blutner and Zeevat argue that (weak) bidirectional optimization must be seen as a global interpretation mechanism [8]. This position allows them to connect the synchronic perspective on language with the diachronic perspective, but is not supported by any empirical evidence.

The remainder of this paper aims to shed new light on these two issues by discussing evidence from computational modeling, psycholinguistic experimentation, and corpus research. Section 3 considers a phenomenon that has been argued to require hearers to take into account the speaker's perspective, and addresses the question whether this conversational inference is a local and online interpretational process, or a global and offline process. Whether speakers also take into account hearers is the topic of Section 4.

## 3 Speaker Effects on the Hearer

A well-studied phenomenon in language acquisition is the interpretation of pronouns and reflexives. Many studies have found that children make errors interpreting pronouns in sentence sequences such as This is Mama Bear and this is Goldilocks. Mama Bear is washing her until the age of five or six (see, e.g., [9]). This contrasts with children's interpretation of reflexives, which is adult-like from the age of four onward. Most explanations of children's pronoun interpretation delay appeal to nonsyntactic factors, such as children's inability to compare pronouns and their meanings with alternative forms such as reflexives and their meanings (see [10] for an influential approach).

### 3.1 A Bidirectional Account of Pronoun Interpretation

In [11], an explanation is proposed of children's delay in pronoun interpretation in terms of biOT. Whereas the distribution of reflexives is subject to Principle A, which
requires reflexives to corefer with the local subject, it is argued that pronouns are not subject to a complementary Principle B which forbids pronouns to corefer with the local subject. Rather, pronouns are essentially free in their interpretation. As a consequence, children will allow both a coreferential and a disjoint interpretation for pronouns. This would explain children's guessing behavior with pronouns in experimental tasks. In contrast to children, adults are argued to optimize bidirectionally (see also [12]) and hence block the coreferential meaning for the pronoun. Adults reason that a speaker, due to a weaker constraint preferring reflexives to pronouns, would have used a reflexive to express a coreferential meaning. As a consequence, the coreferential meaning is blocked as the meaning of the pronoun. This leaves only the disjoint meaning as the meaning of the pronoun.

This biOT explanation of children's errors in pronoun interpretation predicts children's production of pronouns to be adult-like. If Principle A is stronger than the constraint that expresses a preference for reflexives over pronouns, a disjoint meaning is expressed best by a pronoun in unidirectional as well as bidirectional OT. Choosing a reflexive to express a disjoint meaning would violate the strongest of the two constraints, Principle A. Consequently, a pronoun is the optimal form. On the other hand, if the meaning to be expressed is a coreferential meaning, a reflexive is the optimal form. Indeed, in an experiment that tested comprehension and production of pronouns and reflexives in the same children, it was found that children who made errors interpreting pronouns performed correctly on pronoun production [13].

### 3.2 A Cognitive Model of Pronoun Interpretation

Although the biOT explanation accounts for children's delay in pronoun interpretation, it is compatible with a local as well as a global view on bidirectional optimization. Children may compare the pronoun to the alternative reflexive form as soon as the pronoun is encountered, or they may wait until the end of the sentence to compare the sentence containing the pronoun with the alternative sentence containing a reflexive.

To test the biOT explanation and to compare it to non-OT accounts of children's delay in pronoun interpretation, the biOT explanation was implemented in the cognitive architecture ACT-R [14][15]. The cognitive architecture ACT-R is both a theory of cognition and a computational modeling environment. The cognitive architecture imposes cognitive constraints on the computational models, based on a wide range of experimental data on information processing, storage and retrieval. By constructing a cognitive model, concrete and testable predictions can be generated regarding children's development and online comprehension of pronouns.

Two aspects of ACT-R are of crucial importance to constructing a cognitive model of pronoun interpretation. First, every operation in ACT-R takes a certain amount of time. Because operations can be executed in parallel if they belong to different modules of the architecture, the total time that is necessary to perform a cognitive process is not simply the sum of the durations of all constituting operations. Rather, the total time critically depends on the timing of the serial operations within a module, and how the various modules interact. To generate predictions about the timing of cognitive processes, computational simulation models can be constructed and run. A
second aspect of ACT-R that is essential to constructing a cognitive model of pronoun interpretation is that higher processing efficiency can be obtained through the mechanism of production compilation. If two cognitive operations are repeatedly executed in sequence, production compilation integrates these two operations into one new operation. This new operation will be faster than the two old operations together. This process of production compilation can continue until the cognitive process has been integrated into a single operation. As a consequence of production compilation, cognitive processes become faster with experience.

Bidirectional optimization combines the speaker's direction of optimization with the hearer's direction of optimization. In the cognitive model, bidirectional optimization is therefore implemented as two serial processes of unidirectional optimization:
(1) $f \rightarrow m \rightarrow f^{\prime}$

Interpreting a pronoun thus consists of a first step of interpretation $(f \rightarrow m)$, followed by a second step of production ( $m \rightarrow f^{\prime}$ ), in which the output of the first step (the unidirectionally optimal meaning) is taken as the input. If the output of production $f$ ' is identical to the initial input in interpretation $f$, a (strong) bidirectionally optimal pair results. If the output of the production step is different, the unidirectionally optimal meaning $m$ must be discarded and another meaning $m$ ' must be selected in the first optimization step. Because pronouns are ambiguous according to the biOT explanation discussed in Section 3.1, discarding the coreferential meaning results in selection of the disjoint meaning.

If unidirectional optimization needs a given amount of time, the serial version of bidirectional optimization in (1) will initially need about twice this amount of time. When time for interpretation is limited, the model will initially fail to complete the process of bidirectional optimization. So at first, the output of the model will be a unidirectionally optimal meaning rather than a bidirectionally optimal meaning. However, over time the model's performance will become more and more efficient as a result of the mechanism of production compilation. As soon as processing efficiency is high enough to perform bidirectional optimization within the given amount of time, the model will do so, resulting in a bidirectionally optimal meaning as the output. As production compilation results from the repeated sequential execution of particular operations, such as retrieval of particular lexical items from declarative memory, it is dependent on the frequency of these lexical items in the language spoken to the child. As a consequence, the speed of development of bidirectional optimization is different for different lexical items.

Simulations of the cognitive model show a pattern of interpretation that is similar to the pattern displayed by English- and Dutch-speaking children [14]. Already from the beginning of the simulated learning period, when the constraints are already in place but bidirectional optimization is not mastered yet, the interpretation of reflexives is correct. In contrast, the proportion of correct interpretations for pronouns hovers around $50 \%$ during the first half of the simulated learning period, and then gradually increases to correct performance. The model's correct performance on reflexives is not surprising because unidirectional and bidirectional optimization both yield the correct meaning. The model's performance on pronouns follows from the
gradual increase in processing efficiency, as a result of which bidirectional optimization can be performed more frequently.

### 3.3 Testing the Cognitive Model

In incremental interpretation, time limitations arise from the speed at which the next word of the sentence arrives. In the previous section it was argued that children need less time for interpretation if their processing has become more efficient. If bidirectional optimization is a local process which takes place as soon as the pronoun is encountered, there is a second way to facilitate bidirectional optimization: by slowing down the speech rate, so that it takes longer for the next word to arrive. This prediction was tested in a study with 4 - to 6 -year-old Dutch children, who were presented with sentences at a normal speech rate as well as sentences in which the speech rate was artificially slowed down [15]. It was found that slower speech improved children's performance with pronouns but not with reflexives, and only improved children's performance with pronouns if they made errors with pronouns at normal speech rate. In all other situations, slowing down the speech rate had a negative effect. Because children who make errors in pronoun interpretation succeed in arriving at the correct interpretation when they are given more time, the experimental results suggest that insufficient processing speed is the limiting factor in children's comprehension of pronouns. If this is true, children's interpretation is already aimed at computing the speaker's meaning before they have acquired sufficient processing speed to actually do so.

Apparently, taking into account the speaker as a hearer requires sufficient processing efficiency. If, initially, children's processing is too slow, they may fail to optimize bidirectionally and select a unidirectionally optimal meaning instead. With experience in pronoun interpretation, children's processing of pronouns becomes more efficient until correct performance is reached. It is hard to see how these results can be explained by alternative accounts of children's pronoun interpretation delay that attribute children's errors to lack of pragmatic knowledge [9], insufficient working memory capacity [10], or task effects (see [16] for more references and discussion). Furthermore, these results indicate that children's errors with pronouns are not caused by their limitations in perspective taking, as the same children show better performance with slower speech than with normal speech. Also, these results suggest that bidirectional interpretation of pronouns must be viewed as a local rather than a global process, since slowing down the speech rate gave the child participants in the experiment more time within the sentence, while they still had the same amount of time at the end of the sentence.

## 4 Hearer Effects on the Speaker

In the previous section, empirical evidence was presented for the view that hearers take into account the speaker's perspective to arrive at the intended meaning for object pronouns. If conversational inference is fully symmetric, we expect speakers to take into account the hearer's perspective, perhaps in the following way:
(2) $m \rightarrow f \rightarrow m$,

According to (2), producing a form $f$ consists of a first step of production, followed by a second step of interpretation, in which it is checked whether the initial meaning $m$ is recoverable on the basis of form $f$. This possibility is investigated by looking at constituent fronting in Dutch.

### 4.1 Constituent Fronting in Dutch

Word order in Dutch is characterized by the fact that in declarative main clauses the finite verb must occur in second position. In addition, however, Dutch allows for a moderate amount of word order variation with respect to what can appear in front of this finite verb. Although the first position of the sentence is most frequently (in roughly $70 \%$ of cases, according to an estimation [17]) occupied by the subject, this position can also be occupied by direct objects, indirect objects and other constituents.

In a large scale corpus study, Bouma [17] investigated the factors determining what constituent comes first in a Dutch main clause. To this end, Bouma conducted a logistic regression analysis of data from the spoken Dutch corpus Corpus Gesproken Nederlands (CGN). The factors grammatical function, definiteness and grammatical complexity were found to independently influence the choice of constituent in first position. With respect to grammatical function, subjects have the strongest tendency to occur in first position, followed by indirect objects and direct objects. With respect to definiteness, definite full NPs are more likely to appear in first position than indefinite full NPs. Although pronouns as a group show a strong tendency to appear in first position, this is only visible in the fronting behavior of demonstrative pronouns, which front more often than definite full NPs. Reduced personal pronouns are strongly discouraged from appearing in first position, perhaps because they express highly predictable material. Finally, more complex material is preferably placed at the right periphery of the clause, thus resulting in an avoidance of the first position.

### 4.2 Partial Word Order Freezing

Although speakers of Dutch may place non-subjects in first position under the influence of factors such as the ones mentioned above, in certain situations placing a non-subject in first position makes it difficult for the hearer to infer the intended meaning. If a hearer encounters a sentence such as Fitz zag Ella ('Fitz saw Ella'), he can in principle assign an SVO or an OVS interpretation to this sentence, as both word orders are possible in Dutch. Under the first interpretation, Fitz is the subject; under the second interpretation, Fitz is the object. However, presented out of context and in the absence of any intonational clues, most hearers will interpret this sentence as conveying an SVO interpretation. Their preferred interpretation thus reflects the observation that the first constituent most likely is the subject. This observation about hearers' preference may have consequences for speakers' freedom of word order
variation. If the speaker wishes to convey the meaning that Ella did the seeing, the sentence Fitz zag Ella is a poor choice because hearers will have a preference for Fitz as the subject.

This type of conversational inference is explicit in the biOT model of word order variation proposed by Bouma [17] (cf. [18]). In this model, the speaker's choice for a particular word order is influenced by the hearer's ability to recover the subject and object. If speakers take into account the perspective of the hearer, they are expected to limit the freedom of word order variation in situations such as the one sketched above, where subject and object can only be distinguished on the basis of word order. On the other hand, if other clues are present that allow the hearer to distinguish the subject from the object, speakers are expected to have more freedom of word order variation. Such clues may include definiteness. Subjects tend to be highly definite, whereas direct objects tend to be indefinite. Indeed, Bouma's analysis of the transitive sentences in the CGN confirmed the prediction that a non-canonical word order occurs more frequently in sentences with a definite subject and an indefinite object [17]. A preliminary analysis of a manually annotated subset of the CGN suggests that animacy may have a similar effect [17]. A non-canonical word order occurs more frequently in sentences with an animate subject and an inanimate object. These hearer effects on the speaker's choice of word order were found on top of the factors discussed in Section 4.1. So the possibility of word order variation is increased if subject and object can be distinguished on the basis of other clues than word order. Speakers limit word order variation in situations where a non-canonical word order would make it more difficult for the hearer to recover the intended meaning.

Bouma's corpus study thus provides evidence for a tendency toward partial freezing of word order variation in spoken Dutch discourse, parallel to the observation of partial blocking in the domain of interpretation. In the previous section, we saw that hearers restrict the interpretational possibilities of pronouns in situations where a better form is available to the speaker for expressing one of the meanings. The corpus study provides evidence for the assumption that speakers also take into account the hearer's perspective, and hence supports a symmetric conception of biOT.

Bouma's corpus study only addressed the end product of sentence generation, namely the sentences spontaneously produced by speakers of Dutch. Based on the same reasoning as that used with pronoun interpretation, it is predicted that avoiding non-recoverable forms in production will require extra processing resources and hence will be acquired relatively late in language development. For reasons of space, however, I cannot go into this issue here.

## 5 Embodied Semantics

Section 3 addressed the question whether hearers take into account the speaker's perspective in interpretation. A biOT account of conversational inference in pronoun interpretation, according to which hearers also consider alternative forms the speaker could have used but did not use, was shown to be supported by results from cognitive modeling and psycholinguistic experimentation. Section 4 addressed the inverse question whether speakers take into account the hearer's perspective when producing
a sentence. Bouma's corpus study of word order in Dutch seems to provide evidence that speakers consider how hearers will interpret potential forms. Empirical evidence of various sorts thus suggests that hearers take into account speakers, and vice versa.

In this paper, it was argued that an important distinction is that between speaker meaning and hearer meaning. Hearers aim at computing the speaker meaning, but in certain situations the meaning they select (i.e., the hearer meaning) is different from the meaning a speaker would have intended to convey by choosing the heard form (i.e., the speaker meaning). Under the proposed view, the speaker meaning is the meaning resulting from bidirectional optimization in interpretation. In situations where the hearer meaning is different from the speaker meaning, the hearer meaning usually is what is traditionally called the literal meaning, but which under the proposed account is the unidirectionally optimal meaning. However, if the hearer has a non-adult grammar or under strong contextual pressure, the hearer meaning may be a different meaning altogether. Note, furthermore, that the speaker meaning not necessarily is the meaning that is actually intended by the speaker. Rather, it is the meaning that the hearer assumes is intended by the speaker by considering the speaker's perspective. The same two meanings, hearer meaning and speaker meaning, also play a role in production, with speakers aiming to compute the hearer meaning but sometimes failing to do so. Given this distinction between speaker meaning and hearer meaning, it seems that there is no need to distinguish a separate sentence meaning. Under the proposed view, sentences do not have meanings by themselves. Rather, sentences have meanings only in so far as these meanings are assigned to them by speakers and hearers. This view of semantics as embodied in speakers and hearers and their tasks of speaking and understanding is a departure from traditional thinking about meaning.

If no distinction is assumed between sentence meaning and speaker meaning, it becomes difficult to distinguish semantics and pragmatics. The difference between assigning a literal meaning to a sentence and assigning a speaker meaning to this sentence is argued to lie in the hearer's processing efficiency. As acquiring higher processing efficiency is a gradual process, the distinction between semantics and pragmatics (if there is any) must also be gradual. The traditional distinction between semantics and pragmatics is blurred even more by the fact that this paper addressed two phenomena that are not immediately associated with conversational inference, namely pronoun interpretation and constituent fronting. Nevertheless, evidence was presented that seemed to support analyses of these phenomena in terms of conversational inference. Cognitive modeling of the development of pronoun interpretation illustrated that it is possible for these processes of conversational inference to become automatic in such a way that their output cannot be distinguished from the output of regular grammatical processes. Given these results, an important question is whether the same mechanisms are able to explain phenomena that are traditionally viewed as belonging to the domain of pragmatics, such as scalar implicatures.

To conclude, this paper addressed the question whether and how hearers take into account the speaker's perspective, and vice versa. By showing how empirical evidence can elucidate important theoretical issues such as those regarding the relation between sentence interpretation and sentence generation, this paper illustrates the need for semantic theory to consider empirical data.

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# Natural color categories are convex sets 

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#### Abstract

The paper presents a statistical evaluation of the typological data about color naming systems across the languages of the world that have been obtained by the World Color Survey. In a first step, we discuss a principal component analysis of the categorization data that led to a small set of easily interpretable features dominant in color categorization. These features were used for a dimensionality reduction of the categorization data. Using the thus preprocessed categorization data, we proceed to show that available typological data support the hypothesis by Peter Gärdenfors that the extension of color category are convex sets in the CIELab space in all languages of the world.


## 1 Introduction: The World Color Survey

In their seminal study from 1969, Berlin and Kay investigated the color naming systems of twenty typologically distinct languages. They showed that there are strong universal tendencies both regarding the extension and the prototypical examples for the meaning of the basic color terms in these languages.

This work sparked a controversial discussion. To counter the methodological criticism raised in this context, Kay and several co-workers started the World Color Survey project (WCS, see Cook et al. 2005 for details), a systematic large-scale collection of color categorization data from a sizeable amount of typologically distinct languages across the world.

To be more precise, the WCS researchers collected field research data for 110 unwritten languages, working with an average of 24 native speakers for each of these languages. During this study, the Munsell chips were used, a set of 330 chips of different colors covering 322 colors of maximal saturation plus eight shades of gray.

The main chart is a $8 \times 40$ grid, with eight rows for different levels of lightness, and 40 columns for different hues. Additionally there is a ten-level column of achromatic colors, ranging from white via different shades of gray to black. The level of granularity is chosen such that the difference between two neighboring chips is minimally perceivable.

For the WCS, each test person was "asked (1) to name each of 330 Munsell chips, shown in a constant, random order, and (2), exposed to a palette of these chips and asked to to pick out the best example(s) ('foci') of the major terms

## Invited Speakers

elicited in the naming task" (quoted from the WCS homepage). The data from this survey are freely available from the WCS homepage http://www.icsi.berkeley.edu/ wcs/data.html.

This invaluable source of empirical data has been used in a series of subsequent evaluations that confirming Berlin and Kay's hypothesis of universal tendencies in color naming systems across languages (see for instance Kay and Maffi 1999), even though the controversy about universality vs. relativism continues.

## 2 Feature extraction

For each informant, the outcome of the categorization task defines a partition of the Munsell space into disjoint sets - one for each color term from their idiolect.

An inspection of the raw data reveals - not surprisingly - a certain level of noise. This may be illustrated with the partitions of two speakers of a randomly chosen language (Central Tarahumara, which is spoken in Mexico). They are visualized in Figure 1. In the figure, colors represent color terms of Cen-


Fig. 1. Partitions for two speakers of Central Tarahumara
tral Tarahumara. We see striking similarities between the two speakers, but the identity is not complete. They have slightly different vocabularies, and the extensions of common terms are not identical. Furthermore, the boundaries of the extensions are unsharp and appear to be somewhat arbitrary at various places. Also, some data points, like the two blue chips within the green area in the center of the upper chart, seem to be due to plain mistakes. Similar observations apply to the data from other participants.

To separate genuine variation between categories (of the same or of different speakers, from the same or from different languages) on one hand from random
variation due to the method of data collection on the other hand, I employed principal component analysis (PCA), a standard technique for feature extraction and dimensionality reduction that is widely used in pattern recognition and machine learning.

The extension of a given term for a given speaker is a subset of the Munsell space. This can be encoded as a 330-dimensional binary vector. Each Munsell chip corresponds to one dimension. The vector has the value 1 at a dimension if the corresponding chip belongs to the extension of the term in question, and 0 otherwise. By using this encoding I obtained a collection of 330 d vectors, one for each speaker/term pair.

PCA takes a set of data points in a vector space as input and linearly transforms the coordinate system such that (a) the origin of the new coordinate system is at the mean of the set of points, and (b) the new dimensions are mutually stochastically independent regarding the variation within the data points. The new dimensions, called principal components, can be ordered according to the variance of the data points along that dimension.

One motivation for performing a PCA is dimensionality reduction. Suppose the observed data points are the product of superimposing two sources of variation - a large degree of "genuine" or "interesting" variation and a small degree of irrelevant noise (and the latter is independent of the former). Then PCA is a way to separate the former from the latter. If the observed data live in an $n$-dimensional vector space but the genuine variation is $m$-dimensional (for $m<n$ ), then the first $m$ principal components can serve as an approximation of this genuine variation.

In our domain of application, "interesting" variation is the variation between the extensions of different categories, like the difference between the extensions of English "red" and English "green" or between the extensions of English "blue" and Russian "galubòj" (which denotes a certain light blue). Inessential variation is the variation between the extensions that two speakers (of the same dialect of) the same language assign to the same term. It is plausible to assume the latter to be small in comparison to the former. So as a heuristic, we can assume that the first $m$ principal components (for some $m<330$ that is yet to be determined) capture the essence of the "interesting" variation.

Figure 2 depicts the proportion of the total variance in the data explained by the principal components. The graphics does not motivate a specific choice of $m$. For the time being, I will choose $m=10$ because, as we will see shortly, the first ten principal components can be interpreted straightforward, while the others can't. The main result of the paper does not depend on this choice though. The first ten principal components jointly explain about $62.0 \%$ of the total variance in the data. Each of the following 320 principal components only explains a small additional proportion of variance of less than $1 \%$.

It is worthwhile to look at the first ten principal components in some detail. Figure 3 gives a visualization. Please note that each principal component is a vector in the 330d space defined by the Munsell chips. The degree of lightness of each chip in the visualization corresponds to the value of the principal component


Fig. 2. Proportion of total variance explained by prinicpal components


Fig. 3. Visualization of the first ten principal components
in question in the corresponding dimension. The values are scaled such that black stands for the maximal and white for the minimal value, whatever their absolute numerical value may be. Also note the directionality of principal components is arbitrary - so inverting a chart would result in a visualization of the same principal component. The important information is where the regions of extreme values (black or white) are located, in opposition to gray, i.e. the non-extreme values.

In all ten charts, we find clearly identifiable regions of extreme values. They are listed in Table 1. With very few exceptions, the thus identified regions ap-

Table 1. Oppositions defined by the first ten principal components

| PC extreme negative values extreme positive values |  |
| :--- | :--- |
| 1 red, yellow | green, blue |
| 2 white | red |
| 3 black | white, red |
| 4 black, red, blue, purple | yellow |
| 5 black, brown | red, green, blue |
| 6 blue | red, black, green |
| 7 purple | red, orange, blue |
| 8 pink | red, orange, yellow, white, purple |
| 9 pink, orange | black |
| 10 brown | black, light green, light blue |

proximately correspond to (unions of) ten of the eleven universal basic color terms identified by Berlin and Kay (1969). (The only universal basic color that does not occur is gray. This is likely due to the fact that shades of gray are under-represented in the Munsell chart in comparison to shades of other basic colors. The absence of gray is thus likely an artefact of the way the data in the WCS were collected.) Remarkably, the first six principal components jointly define exactly the six primary colors black, white, red, green, blue and yellow. (Purple has extreme values for PC4, but it is not distinguished from the neighboring red and blue.) The 7th - 10th principal components additionally identify the composite colors purple, brown, orange and pink. The 10th prinicipal component furthermore identifies another composite color between green/blue and white.

As can be seen from this discussion, the 10th principal component is less clearly interpretable than the first nine. The remaining principal components starting with the 11th lend themselves even less to an intuitive interpretation.

## 3 Dimensionality reduction

The first ten principal componentens define a linear 10d subspace of the original 330d space. We are operating under the assumption now that most of the "interesting" variation between color categories takes place within this low-dimensional
subspace, while variation outside this subspace is essentially noise. As the next step, I projected the original 330d data points to that subspace. Technically this means that in the transformed coordinate system defined by PCA, only the first ten dimensions are considered, and the values of all data points for the other 320 dimensions are set to 0 . The resulting vectors are transformed back into the original coordinate system.

If visualized as a chart of gray values, the original data points correspond to black-and-white pictures where the extension of the corresponding category is a black region with jagged edges. After dimensionality reduction, we get dark regions with smooth and fuzzy gray borders. Put differently, while the original data points are classical binary sets with sharp and jagged boundaries, the projected data points are fuzzy sets with smooth boundaries. ${ }^{1}$ (Technically speaking this is not entirely true because the values of the vectors after dimensionality reduction may fall slightly outside the interval $[0,1]$, but the notion of a fuzzy set is still a good conceptual description.) Figure 4 contains two randomly chosen examples of data points before and after dimensionality reduction.


Fig. 4. Dimensionality reduction

For a given speaker, we can now determine for each Munsell chip which category has the highest value (after dimensionality reduction). In this way we

[^0]can assign a unique category to each chip, and we end up with a partition of the color space again. The boundaries of the categories are sharp again, but in most cases not jagged but smooth. As an illustration, the cleaned-up versions of the partitions from Figure 1 are given in Figure 5.


Fig. 5. Cleaned-up partitions for the two speakers of Central Tarahumara

## 4 Convexity in the CIELab space

The visualizations discussed so far suggest the generalization that after dimensionality reduction, category extensions are usually contiguous regions in the 2 d Munsell space. This impression becomes even more striking if we study the extensions of categories in a geometrical representation of the color space with a psychologically meaningful distance metric. The CIELab space has this property. It is a 3d space with the dimension $L^{*}$ (for lightness), a* (the green-red axis) and $b^{*}$ (the yellow-blue axis). The set of perceivable colors forms a three-dimensional solid with approximately spherical shape. Figuratively speaking, white is at the north pole, black at the south pole, the rainbow colors form the equator, and the gray axis cuts through the center of the sphere. The CIELab space has been standardized by the "Commission Internationale d'Eclairage" such that Euclidean distances between pairs of colors are monotonically related to their perceived dissimilarity.

The 320 chromatic Munsell colors cover the surface of the color solid, while the ten achromatic chips are located at the vertical axis. Visually inspecting CIELab representations of the (dimensionality-reduced) partitions led to the hypothesis that boundaries between categories are in most cases approximately linear, and extensions of categories are convex regions. This is in line with the main
claim of Gärdenfors' (2000) book "Conceptual Spaces". Gärdenfors suggests that meanings can always be represented geometrically, and that "natural categories" must be convex regions in such a conceptual space. The three-dimensional color space is one of his key examples.

We tested to what degree this prediction holds for the partitions obtained via dimensionality reduction. The algorithm we used can be described as follows. Suppose a partition $p_{1}, \cdots, p_{k}$ of the Munsell colors into $k$ categories is given.

1. For each pair of distinct categories $p_{i}, p_{j}$ (with $1 \leq i, j \leq k$ ), find a linear separator in the CIELab space (i.e. a plane) that optimally separates $p_{i}$ from $p_{j}$. This means that the set of Munsell chips is partitioned into two sets $\tilde{p}_{i / j}$ and $\tilde{p}_{j / i}$, that are linearly separable, such that the number of items in $p_{i} \cap p_{j / i}$ and in $p_{j} \cap p_{i / j}$ is minimized.
2. For each category $p_{i}$, define

$$
\tilde{p}_{i} \doteq \bigcap_{j \neq i} p_{i / j}
$$

As every $p_{i / j}$ is a half-space and thus convex, and the property of convexity is preserved under set intersection, each $\tilde{p}_{i}$ is a convex set (more precisely: the set of Munsell coordinates within a convex subset of $R^{3}$ ).

To perform the linear separation in a first step, I used a soft-margin Support Vector Machine (SVM). An SVM (Vapnik and Chervonenkis 1974) is an algorithm that finds a linear separator between two sets of labeled vectors in an $n$-dimensional space. An SVM is soft-margin if it tolerates misclassifications in the training data. ${ }^{2}$ As SVMs are designed to optimize generalization performance rather than misclassification of training data, it is not guaranteed that the linear separators found in step 1 are really optimal in the described sense. Therefore the numerical results to be reported below provide only a lower bound for the degree of success of Gärdenfors' prediction.

The output of this algorithm is a re-classification of the Munsell chips into convex sets (that need not be exhaustive). The degree of convexity "conv" of a partition is defined as the proportion of Munsell chips not re-classified in this process. If $p(c)$ and $\tilde{p}(c)$ are the class indices of chip $c$ before and after re-classification, and if $\tilde{p}(c)=0$ if $c \notin \bigcup_{1 \leq i \leq n} \tilde{p}_{i}$, we can define formally:

$$
\mathrm{conv} \doteq|\{c \mid p(c)=\tilde{p}(c)\}| / 330
$$

The mean degree of convexity of the partitions obtained via PCA and dimensionality reduction is $93.9 \%$, and the median is $94.5 \%$ (see the first boxplot in Figure 6). If the above algorithm is applied to the raw partitions rather than to those obtained via dimensionality reduction, the mean degree of convexity is $77.9 \%$.

[^1]

Fig. 6. Degrees of convexity (in \%) of 1. cleaned-up partitions, 2. raw partitions, and 3. randomized partitions

Since the difference between these values is considerable, one might suspect the high degree of convexity for the cleaned-up data actually to be an artifact of the PCA algorithm and not a genuine property of the data. This is not very plausible, however, because the input for PCA were exclusively categorization data from the WCS, while the degree of convexity depends on information about the CILab space. Nevertheless, to test this hypothesis, I applied a random permutation of the category labels for each original partition and applied the same analysis (PCA, dimensionality reduction, computation of the degree of convexity) to the thus obtained data. The mean degree of convexity for these data is as low as $65.3 \%$ (see the third boxplot in Figure 6). The fact that this value is so low indicates the high average degree of convexity to be a genuine property of natural color category systems.

The choice of $m=10$ as the number of relevant principal component was motivated by the fact that only the first ten prinicpal components were easily interpretable. As this is a subjective criterion, it is important to test to what degree the results from this section depend on this choice.

Therefore I performed the same analysis with the original data for all values of $m$ between 1 and 50 . The dependency of the mean degree of convexity on $m$ is displayed in figure 7 . It can be seen that the degree of convexity is not very sensitive to the choice of $m$. For all values of $m \leq 35$, mean convexity is above $90 \%$. The baseline is the degree of convexity of $77.9 \%$ for the raw data (or, equivalently, for $m=330$ ), which is indicated by the horizontal line.

So I conclude that the data from the WCS provide robust support for Gärdenfors' thesis.

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Fig. 7. Mean degree of convexity as a function of $m$

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# Pluralities in Concealed Questions, Interrogative Clauses and Individuals Maribel Romero <br> University of Konstanz 

Concealed question Noun Phrases (NPs) like the capital of Italy in (1) have been analysed as contributing their intension --an individual concept-- to the semantic computation, as sketched in (2)-(4) (Heim 1979, Romero 2005, Aloni 2008):
(1) Mary knows / guessed / revealed / forgot the capital of Italy.
(2) 【the capital of Italy】 =
$\lambda$ w. $\mathrm{xx}_{\mathrm{e}}$ [capital-of-Italy $(\mathrm{x}, \mathrm{w})$ ]
(3) $\llbracket k n o w_{C Q} \rrbracket\left(\mathrm{x}_{\mathrm{s}, \mathrm{e}\rangle}\right)(\mathrm{z})(\mathrm{w})=1$
iff $\quad \forall w^{\prime \prime} \in \operatorname{Dox}_{z}(w)[x(w ")=x(w)]$
(4) Know $_{C Q}+$ Intension of the NP:
$\llbracket$ Mary knows the capital of Italy $\rrbracket=$
$\lambda \mathrm{w} . \forall \mathrm{w}^{\prime} \in \operatorname{Dox}_{\mathrm{m}}(\mathrm{w})\left[\mathrm{tx}_{\mathrm{e}}\left[\right.\right.$ capital-of-Italy $\left.\left(\mathrm{x}, \mathrm{w}^{\prime}\right)\right]=\mathrm{tx}_{\mathrm{e}}[$ capital-of-Italy $\left.(\mathrm{x}, \mathrm{w})]\right]$
However, the individual concept approach encounters problems when we consider concealed question NPs with quantifiers: (5). Combining the generalized quantifier's intension with the verb does not yield the correct truth conditions (Nathan 2005, Frana to appear). This has lead researchers to deviate from the core individual concept approach in different ways (Schwagger 2007, Roelofsen and Aloni 2008, Frana to appear).
(5) a. Mary knows / guessed / revealed / forgot most European capitals.
b. Mary knows / guessed / revealed / forgot few / some European capitals

The present paper proposes a solution to this problem within the invididual concept line. The key idea is that, in the same way that adverbials like to some extent and for the most part quantify over subquestions of an embedded question (Berman 1991, Lahiri 2002, Beck and Sharvit 2002), some and most can quantify over sub-individual concepts of a concealed question, as sketched in (6). Furthermore, it will be shown that certain constraints on determiner and adverbial quantification over concealed questions are parallel to those on determiner and adverbial quantification over (plain) plural individuals.
(6) The waiter knows / remembers [CQ some / most dishes you ordered].

The waiter to some extent / for the most part knows / remembers [IntercP what dishes you ordered].

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# Specific, Yet Opaque 

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#### Abstract

In her dissertation, Janet Fodor has argued that the quantificational force and the intensional status of certain quantifier phrases can be evaluated independently. The proposal was only halfway accepted: the existence of non-specific transparent readings is well-established today, but specific opaque readings are deemed illusory. I argue that they are real and outline a semantic framework that can generate them. The idea is to permit two types of quantifier raising: one that carries the restrictor of the determiner along and another that does not. When the second is applied, the restrictor can be stranded within the scope of an intensional operator as the quantificational determiner itself takes wider scope.


## 1 Fodor's Readings

Assume Alex, Bart, and Chloe are three distinct people and consider the following inference:
(1) Ralph thinks Alex is an American spy

Ralph thinks Bart is an American spy
Ralph thinks Chloe is an American spy
Ralph thinks at least three spies are American
This looks valid but under standard assumptions it can't be. The conclusion, under its de re reading, entails the existence of spies. But the premises don't: they are compatible with Ralph having false beliefs about Alex, Bart, or Chloe. Under the de dicto reading, the conclusion entails that Ralph has a general belief about the number of American spies. But the premises don't: they are compatible with him thinking nothing more than that Alex is an American spy, and Bart is, and Chloe is. It is certainly likely that if Ralph has these three specific beliefs he will also come to have the general one. But logic alone cant force him to live up to his commitments.

It would not be fair to dismiss this problem by pointing out that if propositions are taken to be sets of possible worlds then the inference is valid on the de dicto construal. True enough, if in all of Ralph's belief worlds Alex, Bart, and Chloe are American spies then all those worlds contain at least three spies. But we should not forget that given the high-flying idealization of a Hintikka-style semantics for attitude verbs, (2) is also supposed to be a valid inference:
(2) Ralph thinks Alex is an American spy

Ralph thinks Bart is an American spy
Ralph thinks Chloe is an American spy
Ralph thinks arithmetic is incomplete
Semanticists tend concede that (2) is not valid. Attitude verbs are hyper-intensional but for many purposes they can be treated as if they were merely intensional. Fair enough, we all like to keep things simple when we can. But if we don't want to take the blame when the simplifying assumption of logical omniscience leads to unacceptable predictions we should not take credit when it accidentally delivers the right result - as it happens in (1).

The real reason (1) is valid has nothing to do with logical omniscience. It is rather that the conclusion can be read in a way that differs from both the usual de re and de dicto interpretations. The relevant reading can be paraphrased as (3):
(3) There are at least three people Ralph thinks are American spies.

That intensional constructions may give rise to such readings has been conjectured before. Fodor [4] argued that the quantificational force and the intensional status of certain quantified phrases can be evaluated independently. Thus, she claimed that a sentence like (4) has four distinct readings:

Mary wants to buy an inexpensive coat.
a. Non-specific, opaque (de dicto): Mary wants this: that she buys an inexpensive coat.
b. Specific, transparent (de re): There is an inexpensive coat which Mary wants to buy.
c. Non-specific, transparent: There are inexpensive coats of which Mary wants to buy one.
d. Specific, opaque: There is a thing which Mary wants to buy as an inexpensive coat.

It is easy to imagine conditions under which the non-specific transparent reading is true but the de re and de dicto readings are false. Mary could have a certain type of coat in mind and have the desire to purchase an instance of that type, while being completely unaware of the fact that such coats are inexpensive. That (4-c) is a genuine reading of (4) has been generally recognized by semanticists; many have taken it as evidence that the scope theory of intensionality is either completely mistaken or in need of a thoroughgoing revision. ${ }^{1}$ But the reading that corresponds to (4) is (4-d) - it is specific (in the sense that it makes a claim about a particular object) yet opaque (in the sense that it characterizes this object not as it is but as it is thought to be).

Alas, the consensus these days is that the existence of the specific opaque reading is an illusion. One reason for this is the difficulty of paraphrase. The

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reading is sometimes rendered as 'There is a thing which Mary wants to buy under the description inexpensive coat' but this is quite artificial. I used an asphrase but that too is a rather obscure construction. Perhaps the best we can do is (5):
(5) There is a thing Mary wants to buy. She thinks it is an inexpensive coat.

Can (4) have a reading like (5)? Here is a widely-accepted argument that it cannot. ${ }^{2}$ (4) and (5) do not permit the same continuations; while (5+) is coherent $(4+)$ is not:
(4+) Mary wants to buy an inexpensive coat. \# But it is actually quite expensive.
(5+) There is a coat Mary wants to buy. She thinks it is inexpensive. But it is actually quite expensive.

But then (4) and (5) cannot be synonyms, and thus, (4) lacks a specific opaque reading. I think the argument is too quick. The presence of the anaphoric pronoun forces a specific reading on the preceding sentences in both $(4+)$ and (5+). In (5+) the anaphoric pronoun can pick out the coat Mary wants to buy and thinks is inexpensive. In (4+) the the anaphoric pronoun must pick out the inexpensive coat Mary wants to buy, which leads to inconsistency. But this contrast could be explained by the fact that the word thinks is present in (5) but missing from (4). Thus, we should not jump to the conclusion that (4) and (5) cannot have the same truth-conditions. ${ }^{3}$ Consider (6):
(6) Mary thinks she bought an inexpensive coat. It is actually quite expensive.

I think this sequence is perfectly consistent; it is certainly much better than $(4+)$. If there is no such thing as a specific opaque reading, the contrast is a bit of a mystery.

The intuitive validity of (1) and the intuitive coherence of (6) suggest that the dismissal of Fodor's specific opaque reading is a mistake. But generating such a reading within the standard quantificational framework using QR is far from trivial. To get a non-specific transparent reading we need to find a way

[^3]to evaluate the restrictive predicate of a quantificational DP "higher up" while interpreting the quantificational force of the DP "downstairs". There are various mechanisms that can do this - we can, for example, use overt world-variables. ${ }^{4}$ Then the simplified logical forms of the two non-specific readings of (4) would differ only in the choice of the world variable associated with the DP:
\[

$$
\begin{array}{ll}
\mathrm{a}^{\prime} . & \left.\lambda w \text { Mary wants }\left[\lambda w^{\prime} \text { to buy [an inexpensive coat in } w^{\prime}\right]\right]  \tag{4}\\
\mathrm{c}^{\prime} . & \left.\lambda w \text { Mary wants }\left[\lambda w^{\prime} \text { to buy [an inexpensive coat in } w\right]\right]
\end{array}
$$
\]

To get the corresponding specific readings we would need to raise the DP, which results in the following logical forms:
(4) $\quad \mathrm{b}^{\prime} . \lambda w[\text { an inexpensive coat in } w]_{i}$ Mary wants $\left[\lambda w^{\prime}\right.$ to buy $\left.\left.i\right]\right)$
$\mathrm{d}^{\prime} . \lambda w$ [an inexpensive coat in $\left.w^{\prime}\right]_{i}$ Mary wants $\left[\lambda w^{\prime}\right.$ to buy $\left.\left.i\right]\right)$
$\left(4 \mathrm{~b}^{\prime}\right)$ is a perfectly adequate way to capture the specific transparent (de re) reading, but $\left(4 \mathrm{~d}^{\prime}\right)$ says nothing like (4d). It would if the world-variable within the raised DP could be bound "from below" - but that is not how variable binding works.

To bypass this problem, we need to change the standard framework more radically. Before proposing such a change in section 4 , I will try to provide more robust evidence that the specific opaque readings are real.

## 2 Summative reports

Let's start with the core example. Alex is a somewhat paranoid - he thinks that his neighborhood is full of terrorists. He spends much of his time observing comings and goings, following people around, and making inquiries. One day he goes to the police. The police officer who interviews Alex hands him a pile of photographs of people who live in his neighborhood. When Alex looks at a photograph he is asked first whether the person is a terrorist and if he answers affirmatively he is then asked where the person lives. When he is done looking through the photographs he is asked whether there are terrorists in the neighborhood who are not on any of the photographs he has seen. He says that there are not. He is also asked whether he knows how many terrorists he has identified. He says that there were quite a few but he does not know precisely how many. Fortunately, the police officer took tally. It turns out that Alex has identified 17 photographs as showing terrorists, and of those 11 as showing ones that live in the apartment building across the street from him. When the police officer who conducted the interview later reports this to his superiors he says the following:
(7) Alex believes that eleven terrorists live across the street from him.

Assuming Alex was honest in expressing his beliefs this seems like a true report. It is neither a de re claim (Alex's accusations need not be true) nor a de dicto one

[^4](Alex did not count up his accusations). Rather, it is what I will call a summative report. Alex's answers express a number of de re beliefs regarding the people on the photographs and the police officer summarizes those beliefs in his report. The words 'terrorist' and 'lives across the street' show up in Alex's answers, so they are to be taken to reflect how Alex thinks of the people on the pictures. The police officer need not think that either of these predicates applies to any of those people. By contrast, the word 'eleven' is the police officer's contribution to the report. He is the one keeping tally. Alex need not have any belief about the number of people he takes to be terrorists across the street. The summative reading of (7) is what Fodor called specific opaque.

We could clearly replace 'eleven' in (7) with any other numerical determiner and preserve the summative reading. Other intersective determiners work as well. (8), for example, can be used to make a true report under the circumstances described above, even if Alex thinks that eleven terrorists across the street are but a pittance. (Perhaps he thinks most neighborhoods have a lot more terrorists than his own.)
(8) Alex believes that many terrorists live across the street from him.

When the report is summative 'many' is the police officers contribution, and the report is true because Alex in fact identified eleven people as terrorists living across the street from him and eleven terrorists across the street are in fact many.

Here is another example, this time using a non-intersective quantifier. Imagine that Bob, who lives in the same neighborhood, also comes to the police and claims that there are a number of terrorists living there. The police officer goes to his supervisor and they discuss the new development, comparing Bob's accusations with those made by Alex. The police officer observes that there is not much agreement between Alex and Bob about where the terrorists are concentrated in the neighborhood. He says:
(9) Alex believes that most terrorists live across the street from him.

Given that Alex has identified 17 people as terrorists and 11 of them as living across the street from him and that he also said that there are no terrorists in the neighborhood who are not on any of the photographs he has seen, this report seems true. The report quantifies restrictedly - the context makes clear that only people in Alex's neighborhood are at issue. With the obvious changes in the pattern of responses Alex gave, we can confirm the existence of summative readings involving other non-intersective quantifiers, such as 'every', 'two thirds of', or 'no'.

Given the character of summative reports one might expect that we can lump together not only de re beliefs of a single person, but also de re beliefs of multiple people. This expectation is borne out. Imagine that besides the 17 people Alex accuses of terrorism, Bob accuses another 9 . The police officer could report the outcome of the two interviews as (10):
(10) Alex and Bob believe that twenty-six terrorists live in their neighborhood.

The summative reading of (10) is cumulative - it is like saying that Alex and Bob ate twenty-six cookies if they jointly devoured that much. The difference is that those twenty-six things Alex and Bob ate had to be really cookies while the twenty-six people they have beliefs about needn't be really terrorists.

I conclude that summative readings are available for quantified belief reports no matter what quantifier is used. This strenghtens the evidence for the existence of specific opaque readings provided by the inference under (1).

## 3 Modals, tense, and aspect

Similar readings arise with modals, tense, and aspect as well. They are relatively easy to find, once one knows where to look.

Imagine that Anna is taking a course and the term paper is due next Monday. She has three outlines and she is trying to decide which one to work on. She doesn't have time to write more than one paper before next Monday. Under these circumstances (11) seems true.
(11) Anna could write three papers. Now she has to decide which one to write.

Note that it is false that three papers are such that it is possible that Anna writes them and equally false that it is possible that Anna writes three papers. The true reading is summative: three things (i.e. the outlines) are such that each could be a paper written by Anna.

Ben is in the same class but his situation is different. He has been working steadily for a long time but he tends to be unhappy with what he writes. On Friday he finishes a paper and burns it, on Saturday he finishes another and burns that too, and on Sunday he finishes the third but that one doesn't make it to Monday either. Still, when Monday comes (12) seems true:
(12) Ben wrote three papers. Unfortunately, he burned them all.

On the de re construal, three papers would scope above the tense and thus there would have to be three papers in existence on Monday for the sentence to be true then. On the de dicto construal, three papers is interpreted within the scope of the past tense and thus there would have to be some time before Monday when three papers were in existence. But there never were three papers Ben wrote in existence. The true reading is again summative: three things (i.e. the past papers) are such that each was a paper written by Ben. ${ }^{5}$

[^5]
## Invited Speakers

What summative readings involving attitude verbs, modals and tense have in common is that they express the results of counting across certain boundaries. In (7), we count across Alex's de re beliefs: he believes of this guy that he is a terrorist and also that he lives across the street, and he believes the same of this other guy, ..., and of this eleventh guy as well, ergo Alex believes eleven terrorists live across the street. In (11), we count across worlds: there is a possible world where Anna finishes this outline, a different possible world where she finishes this other one, and a third where she finishes this third one, ergo Anna could write three papers. In (12), we are summing up what is the case at different times: there is a time when Ben finished this paper, another when he finished this other one, and a third when he finished this third one, ergo Ben wrote three papers. ${ }^{6}$

In the cases hitherto considered, the specific opaque reading had to be teased out by constructing the appropriate contexts in which the sentence is plausibly used with that intended reading. But there are also cases where this reading is arguably the dominant one. Consider Chris who is in the same class as the other two. Chris is a show-off - he intends to hand in not one but three papers on Monday. On Saturday he is sitting at his computer working simultaneously on all three drafts. (13) describes the case correctly:
(13) Chris is writing three papers. All three are up on his screen.

There is a long-standing debate in the semantics literature about the status of things in progress. The establishment view is that a sentence like (13) does not entail the existence of any actual paper Chris is writing. This is the de dicto construal, where three papers is interpreted below the aspect. The antiestablishment view denies this and says that (13) entails that there are three papers such that Chris is writing them. This is the de re reading, where aspect takes narrow scope with regard to three papers. ${ }^{7}$ The establishment has the upper hand - it seems clear that while Chris is working on the papers there are no papers yet. But the anti-establishment makes a good point too - it seems equally clear that there are three things that are the objects of Chris's writing. They are actual drafts stored on the computer, not mere possibilia. Thus, the normal reading of (13) is, I think, neither de re nor de dicto. Rather, it is specific opaque one: there are three things (i.e. the drafts) such that each is becoming a paper written by Chris.

[^6]
## 4 Split quantifiers

How can specific opaque readings be generated? Within a QR-based approach to quantification, the task comes down to specifying a mechanism that splits quantificational determiners from their restrictors. Then the former can move above an intensional operator while the latter is evaluated "downstairs". I will present such a mechanism within the standard framework of Heim and Kratzer [5].

The idea is that raising of a quantified DP is more akin to copying: the syntactic structure remains in its original position while an identical one is attached above a higher $S$ node. The quantificational determiner moves to the higher position leaving an ordinary trace below. For the restrictor there are two possibilities: it can move or it can stay. The unfilled restrictor position - whether it is the higher one or the lower one - is filled by a default predicate whose extension is $\mathrm{D}_{e}$. Finally, we need a new rule that combines the trace with a predicate and delivers what I call a restricted trace. The semantic value of a restricted trace is undefined whenever the trace is assigned a value that in not within the extension of the restrictor.

Here is a small fragment of a language that allows split raising. It contains just one verb (run), two nouns (dog, thing), three quantificational determiners (every, some, most) and traces indexed by natural numbers ( $t_{\iota}$, where $\iota \in \omega$ ). The semantic types of lexical items are the usual: the nouns and the verb are of type $\langle e, t\rangle$, the quantificational determiners of type $\langle\langle e, t\rangle,\langle\langle e, t\rangle, t\rangle\rangle\rangle$, and the traces of type $e$. Semantic values of lexical items are standard (since only traces have assignment-dependent semantic values the superscript is suppressed elsewhere):

```
\(\llbracket t_{\iota} \rrbracket^{a} \quad=a(\iota)\)
\(\llbracket r u n s \rrbracket=\lambda x \in D_{e} x\) runs
\(\llbracket \operatorname{dog} \rrbracket=\lambda x \in D_{e} x\) is a dog
\(\llbracket t h i n g \rrbracket=\lambda x \in D_{e} x=x\)
\(\llbracket\) every】 \(=\lambda f \in D_{\langle e, t\rangle} . \lambda g \in D_{\langle e, t\rangle}\). for all \(x \in D_{e}\) if \(f(x)=1\) then \(g(x) \neq 0\)
\(\llbracket s o m e \rrbracket=\lambda f \in D_{\langle e, t\rangle} . \lambda g \in D_{\langle e, t\rangle}\). some \(x \in D_{e}\) is such that \(f(x)=1\) and \(g(x)=1\)
\(\llbracket m o s t \rrbracket=\lambda f \in D_{\langle e, t\rangle} . \lambda g \in D_{\langle e, t\rangle}\). more \(x \in D_{e}\) are such that \(f(x)=1\) and \(g(x)=1\)
        than are such that \(f(x)=1\) and \(g(x)=0\)
```

The only slightly unusual thing here is the interpretation of every; normally the clause ends with ' $g(x)=1$ ' rather than ' $g(x) \neq 0$ '. The semantics allows partial functions, so this will make a difference, which will be explained below.

Concatenation is interpreted as functional application except in the following two cases (the first is Heim \& Kratzer's, the second is new).
(PA) If $\iota$ is an index and $\sigma$ is a sentence then $[\iota \sigma]$ is a predicate abstract of type $\langle e, t\rangle$, and $\llbracket \iota \sigma \rrbracket^{a}=\lambda x \in D_{e} \llbracket \sigma \rrbracket^{a[x / \iota]}$
(RT) If $t_{\iota}$ is a trace and $\nu$ is a noun then $\left[t_{\iota} \nu\right]$ is a restricted trace of type $e$, and $\llbracket t_{\iota} \nu \rrbracket^{a}=a(\iota)$ if $\llbracket \nu \rrbracket(a(\iota))=1$; otherwise undefined.

## Invited Speakers

The syntax has two rules of quantifier-raising: one that carries along the restrictor and another that does not. (Like indices, the noun thing is phonologically null.)

$$
[\mathrm{S} \xi[\mathrm{DP}[\delta][\nu]] \psi] \Rightarrow\left[\mathrm{S}[\mathrm{DP}[\delta][\nu]]\left[[\iota]\left[\mathrm{s} \xi\left[\left[t_{\iota}\right][\text { thing }]\right] \psi\right]\right]\right]
$$

$\left(\mathrm{QR}^{\downarrow}\right) \quad[\mathrm{S} \xi[\mathrm{DP}[\delta][\nu]] \psi] \Rightarrow\left[\mathrm{S}[\mathrm{DP}[\delta][\right.$ thing $\left.]]\left[[\iota]\left[\mathrm{S} \xi\left[\left[t_{\iota}\right][\nu]\right] \psi\right]\right]\right]$
Let me illustrate how all this works on (14). The sentence could be obviously interpreted without quantifier raising and the results of applying $\left(\mathrm{QR}^{\uparrow}\right)$ or $\left(\mathrm{QR}^{\downarrow}\right)$ will not change the truth-conditions. What they do is allow some intensional operator (attitude verb, modality, tense, aspect, etc.) to intervene between the quantificational determiner and its trace. (To keep things simple, I did not include these in the fragment but they could be introduced without complications.) If the restrictor of the DP is upstairs we get a specific transparent reading; if it is left downstairs we obtain the specific opaque one.

$$
\begin{align*}
& {[\mathrm{S}[\mathrm{DP}[\mathrm{D} \text { every }][\mathrm{N} d o g]][\mathrm{VP} \text { runs }]]}  \tag{14}\\
& {\left[\mathrm{S}[\mathrm{DP}[\mathrm{D} \text { every }][\mathrm{N} d o g]]\left[5\left[\mathrm{~S}\left[\left[t_{5}\right][\mathrm{N} \text { thing }]\right][\mathrm{VP} \text { runs }]\right]\right]\right]} \\
& {\left[\mathrm{S}[\mathrm{DP}[\mathrm{D} \text { every }][\mathrm{N} \text { thing }]]\left[8\left[\mathrm{~S}\left[\left[t_{8}\right][\mathrm{N} d o g]\right][\mathrm{VP} \text { runs }]\right]\right]\right]}
\end{align*}
$$

Since $\llbracket$ thing $\rrbracket$ is the total identity function on $D_{e}$, according to (RT) $\llbracket\left[t_{5}\right][\mathrm{N}$ thing $] \rrbracket^{a}$ $=a(5)$, and according to (PA) $\llbracket\left[5\left[\mathrm{~S}\left[\left[t_{5}\right][\mathrm{N}\right.\right.\right.$ thing $\left.]\right][\mathrm{vP}$ runs $\left.\left.]\right]\right] \rrbracket=\llbracket$ runs $]$. So, obviously, $\llbracket(14) \rrbracket=\llbracket\left(14^{\uparrow}\right) \rrbracket$. By contrast, $\llbracket\left[t_{8}\right][\mathrm{N} d o g] \rrbracket^{a}$ is only defined for those values
 $=\llbracket r u n s \rrbracket$ only if $a(8)$ is a dog; otherwise it is undefined. Now it is clear why the interpretation of every had to be modified: had we used the standard one ( $14{ }^{\downarrow}$ ) would come out as false when there are no dogs in $D_{e}$. But with the modified rule we have $\llbracket(14) \rrbracket=\llbracket\left(14^{\downarrow}\right) \rrbracket$, as desired.

The interpretations of some and most did not have to be adjusted. In order for the predicate abstract to yield a truth-value for some assignment, the assignment must map its index to a member of $D_{e}$ that satisfies the restrictor below. This requirement becomes part of the truth-conditions. Thus, the lower reading of 'Some dog runs' (i.e. the one obtained via $\left(\mathrm{QR}^{\downarrow}\right)$ ) is true iff there is some $x \in D_{e}$ such that $\llbracket t h i n g \rrbracket(x)$ and $\mathbb{[}\left[8\left[\mathrm{~S}\left[\left[t_{8}\right][\mathrm{N} d o g]\right][\mathrm{VP} r u n s]\right]\right] \rrbracket(x)=1$, where the latter requirement boils down to $\llbracket \operatorname{dog} \rrbracket(x)=1$ and $\llbracket r u n s \rrbracket(x)=1$. The lower reading of 'Most dogs run' is true just in case there are more $x$ 's $\in D_{e}$ such that $\llbracket$ thing $\rrbracket(x)$ $=1$ and $\llbracket\left[8\left[\mathrm{~S}\left[\left[t_{8}\right][\mathrm{N} d o g]\right][\mathrm{VP}\right.\right.$ runs $\left.\left.]\right]\right] \rrbracket \rrbracket(x)=1$ than $x$ 's $\in D_{e}$ such that $\llbracket t h i n g \rrbracket(x)$ $=1$ and $\llbracket\left[8\left[\mathrm{~S}\left[\left[t_{8}\right][\mathrm{N} d o g]\right][\mathrm{Vp}\right.\right.$ runs $\left.\left.]\right]\right] \rrbracket \rrbracket(x)=0$. This is equivalent to the condition that there be more $x$ 's $\in D_{e}$ such that $\llbracket \operatorname{dog} \rrbracket(x)=1$ and $\llbracket r u n s \rrbracket(x)=1$ than $x$ 's $\in D_{e}$ such that $\llbracket d o g \rrbracket(x)=1$ and $\llbracket r u n s \rrbracket(x)=0$. All as it should be.

If there is an intensional operator that intervenes between a raised determiner and a stranded restrictor we can get a specific opaque reading. But in an extensional setting $\left(\mathrm{QR}^{\uparrow}\right)$ and $\left(\mathrm{QR}^{\downarrow}\right)$ are semantically indistinguishable. Here is a sketch of a proof.

Let $\sigma$ be a sentence in an extensional language containing the restricted quantifier $\delta \varrho$ (where $\delta$ is the determiner and $\varrho$ is the restrictor). Let's say that
the output of $\left(\mathrm{QR}^{\uparrow}\right)$ applied to an occurrence of $\delta \varrho$ is $\sigma^{\uparrow}$ and that an application of ( $\mathrm{QR}^{\downarrow}$ ) yields $\sigma^{\downarrow}$; let the index of the resulting restricted trace in both cases be $\iota$. I want to show that $\llbracket \sigma^{\uparrow} \rrbracket=\llbracket \sigma^{\downarrow} \rrbracket$. Suppose $\varepsilon^{\uparrow}$ is an arbitrary constituent of $\sigma^{\uparrow}$ and $\varepsilon^{\downarrow}$ the corresponding constituent of $\sigma^{\downarrow}$. (The two sentences have the same syntactic structure.) Call an assignment function that assigns a member of $D_{e}$ to $\iota$ that satisfies $\varrho$ good. I claim that if $a$ is a good assignment then $\llbracket \varepsilon^{\dagger} \rrbracket^{a}$ $=\llbracket \varepsilon^{\downarrow} \rrbracket^{a}$. This is enough to prove what we want because (assuming $\delta$ satisfies conservativity and extension) assignments that aren't good make no difference when it comes to the truth-conditions of $\sigma$. That $\llbracket \varepsilon^{\uparrow} \rrbracket^{a}=\llbracket \varepsilon^{\downarrow} \rrbracket^{a}$ for all good assignments can be proved by induction. When $\varepsilon$ is the restricted trace left behind as a result of raising $\delta \varrho$ this follows from (RT). When $\varepsilon$ is a lexical constituent of $\sigma$ that is not part of the restricted trace $\varepsilon^{\uparrow}=\varepsilon^{\downarrow}$. And the inductive steps involving functional application, predicate abstraction, and restricted trace formation (using a different index) are trivial. (It matters here that we don't have intensional operators in the language. $)^{8}$

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[^7]
# Affective demonstratives and the division of pragmatic labor* 

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## 1 Introduction

Building on [1] and [2], [3] argues for a 'division of pragmatic labor': as a result of general pragmatic interactions, unmarked expressions are generally used to convey unmarked messages and marked expressions are generally used to convey marked messages (see also $[4,5]$ ). [6] explicitly splits this into two separate pressures ("What is expressed simply is stereotypically identified" and "What's said in an abnormal way isn't normal"), and [7], [8], [9], and [10] seek to characterize the opposition in terms how form-meaning pairs are optimally chosen.

In [3], Horn argues that the division of pragmatic labor is at work in a wide range of places: pronoun choice, lexicalization, indirect speech acts, and clausemate negations, as well as issues in language change. Since then, the field has largely stayed within these empirical confines, exploring in more detail the specific pragmatic interactions Horn identified. With the present paper, we seek to branch out, by finding an important role for Horn's division of pragmatic labor in affective (uses of) demonstratives [11-18]. We focus on proximal demonstratives in Japanese, German and English, and begin to make the case that our generalizations are cross-linguistically robust.

Our evidence comes largely from a newly expanded version of the UMass Amherst Sentiment Corpora [19]. These are collections of informal online product reviews, in Chinese, English, German, and Japanese. The English and Japanese portions contain a total of 643,603 reviews and $72,861,543$ words. We use these corpora to sharpen our empirical understanding of affective demonstratives and to substantiate the claims about markedness, for forms and meanings, that underlie our treatment in terms of the division of pragmatic labor.

Section 2 introduces Lakoff's [11] notion of affective demonstratives, arguing that the basic claims are true for English and Japanese. Section 3 presents our corpora and experiments, which address not only demonstratives but also a wide range of exclamatives and related items, as a way of building a general picture of the kinds of pragmatic generalizations that the data support. Finally, in section 4, we reconnect with pragmatic theory, arguing that the division of pragmatic labor is responsible for the patterns we see in our large corpora.

[^8]
## 2 Affective demonstratives cross-linguistically

Lakoff [11] identifies a range of uses of English demonstratives that involve 'emotional deixis', as in (1).
(1) a. This Henry Kissinger is really something!
b. How's that toe?
c. There was this travelling salesman, and he ...

Lakoff's central generalization is that affective demonstratives are markers of solidarity, indicating the speaker's desire to involve the listener emotionally and foster a sense of shared sentiment. She also ventures a direct connection with exclamativity. [13] argue that similar effects arise for generic demonstratives, which "mark the kind being referred to as a relatively subordinate or homogeneous kind located among the speaker's and hearer's private shared knowledge". [17] (and commentators) apply some of these findings to then-U. S. Vice-Presidential candidate Sarah Palin's noteworthy demonstrative use.

Lakoff does not really take a stand on whether affective uses represent an ambiguity in demonstrative phrases or some kind of pragmatic extension of the basic meanings, and her own characterization suggests that the issue could be decided either way. Cross-linguistic investigation could provide important evidence in deciding the matter. If it is an ambiguity, then we have no expectation for it to arise consistently out of the more basic demonstrative meanings. Conversely, if it is a natural extension of deixis into the emotive realm, then it should turn up again and again in language. [18] address precisely this question, arguing, on the basis of parallels between English and German, that this is not an accidental lexical ambiguity, but rather an emergent property of deixis.

Correspondences between German and English are perhaps unsurprising. Even stronger evidence comes from work on Japanese demonstratives. [12, 14, 15] argue that demonstratives in Japanese can contribute an affective or expressive meaning component by indexing a kind of emotional deixis, echoing the Lakoff's suggestions for affective uses of the English demonstrative.

These characterizations of affective demonstratives are intriguing, but we have so far seen limited evidence in favor of them. So, the first task before us is to see if we can find more robust and extensive empirical evidence for affectivity in the demonstrative realm across languages. The next section seeks to provide such evidence, building on the methods of [18]. Following that, we address the question of where these effects come from, arguing that they follow from Horn's division of pragmatic labor.

## 3 Corpus experiments

### 3.1 Data

Our data for this paper come from an expanded (and soon to be released) version of the UMass Amherst Sentiment Corpora [19]. The English texts are online

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reviews at Amazon.com (reviews of a wide range of products), Tripadvisor.com (hotel reviews), and GoodReads.com (book reviews). The Japanese collection comes from Amazon.co.jp (reviews of a wide range of products). Every review included in this collection has some text and an associated star rating, which the author of the text has assigned to the product in question. Table 1 breaks down the corpora into categories based on these star-ratings, a perspective that we rely on heavily throughout this paper. (The substantial five star bias is a common feature of informal, user-supplied product reviews; see section 3.2 for our way to manage it.)

| English |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  1 star 2 star 3 star 4 star 5 star total <br> Reviews 39,383 48,455 90,528 148,260 237,839 564,465 <br> Words $3,419,923$ $3,912,625$ $6,011,388$ $10,187,257$ $16,202,230$ $39,733,423$  <br> Japanese       <br>  1 star 2 star 3 star 4 star 5 star total <br> Reviews 3,973 4,166 8,708 18,960 43,331 79,138 <br> Words $1,612,942$ $1,744,004$ $3,908,200$ $8,477,758$ $17,385,216$ $33,128,120$ Table 1. Summary of the data sets used in this paper. |  |  |  |  |  |  |  |

In contrast to professional reviews, these texts are informal and heavily emotive. Authors writing 1 -star or 5 -star reviews either loved or loathed the product they are reviewing, and this shines forth from their language, which tends to emphasize subjective experience. This makes the texts ideal for studying perspectival and emotional information of the sort that is at issue for affective demonstratives. Reviews in the middle of the scale (2-4 stars) tend to be more balanced and objective, which further helps to bring out the linguistic contrasts we are after. For more on the nature of corpora like this, as well as examples, we refer to [20-23].

### 3.2 Methods

Our statistical method is simple: we track the frequency of words, phrases, and constructions across the five star-rating categories and study the resulting distributions. Because the rating categories are so imbalanced, with the bulk of the reviews assigning 5 -stars, we always consider relative frequencies: let count $\left(w_{n}, R\right)$ be the number of tokens of $n$-gram $w$ in reviews in rating category $R \in\{1,2,3,4,5\}$, and let $\operatorname{count}_{n}(R)$ be the total count for all $n$ grams in rating category $R$. Then the frequency of $w_{n}$ in rating category $R$ is count $\left(w_{n}, R\right) / \operatorname{count}_{n}(R)$. We center the rating values, so that a rating of 3 corresponds to a value on the $x$ axis of 0 , and other rating values are shifted appropriately, so that a rating of 1 maps to -2 and a rating of 5 maps to 2 . Centering the data in this way allows us to test positive and negative biases in words and constructions, as explained just below.

We also fit logistic regression models to the log-odds versions of these distributions, in order to gain further insight into their structure. There is not space
here to review the technical details of these statistical models (we refer to [24, $25]$ for gentle introductions and [26, 27] for motivation and extension to mixedeffects models). However, we think it is worth giving the basic mathematical form for the model we use, (2), and we offer many graphical depictions in later sections to try to bring out the intuitions behind them.

$$
\begin{equation*}
P(y)=\operatorname{logit}^{-1}\left(\alpha+\beta_{1} x+\beta_{2} x^{2}\right) \tag{2}
\end{equation*}
$$

These profiles are curved. Where $\beta_{2}$ is large and positive, we have U-shaped profiles, i.e., profiles in which the bulk of the usage is at the extreme ends of the rating scale. Where $\beta_{2}$ is large and negative, we have Turned-U profiles, i.e., profiles in which the bulk of the usage is in the middle of the scale. Figure 1 illustrates each of these basic cases. The coefficient $\beta_{1}$ tells us the slope of the curve when $x=0$; since we have centered our rating values so that a middle value of 3 is mapped to 0 , we can use the value of $\beta_{1}$ to test the size and significance of any positive or negative bias in an item's distribution. A significant positive value of $\beta_{1}$ indicates a positive rating bias, while a significant positive value of $\beta_{1}$ indicates a negative rating bias, as discussed in [22].



Fig. 1. Example of (2) with the rating scale centered around 0 . The fitted models are $P($ wow $)=\operatorname{logit}^{-1}\left(-10.30-.016+.24 x^{2}\right)$, and $P($ however $)=\operatorname{logit}^{-1}(-6.70-.094 x-$ $\left..19 x^{2}\right)$. The sign of the quadratic coefficients $(.24$ and -.19$)$ determine the direction of the turn ( U or Turned U ) as well as its depth.

In figure 1 and throughout, we have included $p$ values for the coefficients. However, given the large amount of data we have and the small number of empirical points involved, $p$ values are not all that informative about the quality of the models. For present purposes, it is often more useful to compare the empirical points (black) against the models' predictions.

### 3.3 Exclamatives and anti-exclamatives

By way of building towards our results for demonstratives, we now present, in figure 2, the statistical profiles for a series of markers of exclamativity, as well as some of their 'anti-exclamative' counterparts. Exclamatives are much more frequent at the extreme ends of the rating scale than in the middle. This is consistent with the notion that they are generalized markers of unusualness or surprise [28-30]. Whatever lexical polarity they have comes from the predicates

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around them (What a pleasure/disappointment!). With the intensives (e.g., absolutely, total; [31]), we seem also to be seeing a connection between the rating scale's endpoints and endpoint modification, as well as a potential argument for the degree-based approach to exclamativity that underlies most treatments of exclamative constructions.

### 3.4 Affective demonstratives

The above picture of exclamatives in our corpora strongly suggests that our statistical approach can detect affectivity. The rating scale brings out their generalized heightened emotion, placing them in opposition to more balanced expressions like somewhat and but. The approach can also detect rich modifier scales [32] and a wide range of expressive meanings [23]. Thus, if [11-17] are correct in claiming that demonstratives have (at least in English and Japanese) affective uses, then we should see this in our corpora. And this is in fact what we find for proximate demonstrative markers; figure 3 again gives results for English, German, and Japanese. The English data are for a 18,659,017 word, 118,395 review, subset of our data that we have part-of-speech tagged using [33] and NP chunked using [34] in order to get at the distinction between determiner this (I'll have this cake) and pronominal this (I'll have this.) For Japanese, we have the three morphologically complex proximal demonstratives, formed from the proximal demonstrative morpheme ko- combining with -re to form a pronominal demonstrative, -no to form an adnominal demonstrative determiner, and -nna to form an adnominal demonstrative determiner meaning "this kind of". The proximal demonstratives form part of the paradigm summarized in Table 2.

|  | pronominal -re | determiner -no | kind determiner -nna |
| :---: | :--- | :--- | :--- |
| proximal ko- | kore | kono | konna |
| distant from speaker so- | sore | sono | sonna |
| distant from both $a$ - | are | ano | anna |
| indefinite ('which') do- | dore | dono | donna |

Table 2. The Japanese demonstrative paradigm.
We should emphasize that the U shapes for these demonstratives are not nearly as deep as those for prototypical exclamatives; the quadratic coefficient for what $a$, for example, is 0.27 (figure 2), which is more than three times bigger than the coefficient for the English determiner this (0.078). Thus, it is not as though the model is (wrongly) predicting that proximal demonstratives typically pack as much of an emotive punch as exclamatives. We believe that they can do that, but the majority of uses do not, so the overall effect is relatively mild.

## 4 (Un)Marked forms and meanings

Now that we have some quantitative evidence for the reality of affective demonstratives (for proximates) we can move to asking why such meanings arise. The consistency of the effects across languages seems to rule out a treatment in terms


Fig. 2. Exclamatives and anti-exclamatives. Exclamatives are given in the top row of each language's panel, anti-exclamatives in the bottom row. As we move from left to right, the exclamativity (anti-exclamativity) grows more pronounced as measured by the absolute size of the quadratic coefficient $\left(\beta_{2}\right)$.

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Fig. 3. Proximal demonstratives in Japanese, English, and German.
of lexical ambiguity. As Lakoff observes, the affectivity has a metaphoric connection with the more basic meaning; it is perhaps no surprise that a marker of physical closeness would be extended into the emotive realm where it would foster, or gesture at, shared sentiment. However, while this makes intuitive sense, it is hard to make the argument rigorously. It has the feel of a 'just-so' story.

Horn's division of pragmatic labor gives us a richer perspective on the problem. It is fairly easy to argue that this is a case in which marked forms associate with marked meanings. [35] argues that English demonstratives are, at the meaning level, strictly more complex morphosemantically than the. They are also significantly less frequent than definite articles. In our data, there are 977,637 tokens of the, but only 171,432 of this and another 13,026 of these. ${ }^{3}$ This is no quirk of our corpora, either. In the Google $n$-gram corpus, the is 8.5 times more frequent than this.

When we look at the profiles for the English and German definite determiners in our corpora (in the leftmost column of figure 2), we find that they are the mirror images of the profiles of the proximal demonstratives, exhibiting a significant inverse- U shape. We explain this finding as the result of competition between marked and unmarked meanings. The more marked proximal demonstratives generate an exclamative profile, with uses concentrated in the extreme regions of the scale. Since demonstratives compete for the same syntactic slot as the definite determiner, we get an inverse implicature arising from the use of the definite. This is a species of upper-bounding implicature; the speaker used a form (definite) whose meaning contribution is strictly weaker than a competing form (demonstrative) [6]. This gives rise, in certain contexts, to a kind of implicature whereby the proximal emotional deixis we saw to be generated by the proximal demonstratives is negated, so that use of the definite determiner can implicate a negation of strong emotional commitment. The strength of the effect is weak, as

[^9]seen in the small size of the quadratic term in our models. We are not predicting that use of the definite determiner is inconsistent with exclamativity; instead, we argue that competition with demonstratives generates a small but significant tendency for anti-exclamativity in the use of the definite determiner.

Japanese does not have a definite determiner to play the role of the unmarked-to-unmarked counterpart. Its demonstrative system, however, is more articulated than that of English and thus allows us to see the expressive effects of relative semantic markedness within the demonstrative paradigm itself. It is reasonable to hypothesize that the proximal demonstrative ending in -nna is more semantically marked than the one ending in -no, since the proximal demonstrative ending in -no refers only to the entity ultimately picked out by the construction kono $N P$, while the one ending in -nna makes reference not only to the entity directly indexed by the demonstrative, but also to a set of 'similar' entities. There is thus an intuitive sense in which a sentence including the -nna series proximal demonstrative konna is stronger, and hence more marked, than the same sentence in which -nna is replaced with -no.
[14] argues that the -nna series can be used to contribute both a note of "surprise" and "negative emotion". In a discussion of the -nna demonstratives, she says that most researchers concentrate on the physical deictic uses, but she continues:

Conversational data, however, indicates that the usage described above is scarcely seen in informal conversation. Rather than solely referring to the characteristics of an object, most of the usage overtly expresses the following speaker's modality: 1) negative emotion or rejection, and 2) surprise. These emotions and attitudes are toward the object, the interlocutor, or the whole utterance or action that includes the object.
We can relate the note of "surprise" that [14] identifies to the U-shaped distributions we identified earlier. In the case of proximal demonstratives, we saw that this U-shape characterized both the -no series proximal demonstrative kono and the -nna series proximal demonstrative konna. We conclude, on the basis of collaborating evidence from English and German, that this exclamative or "surprisal" value is derived by metaphorical extension of the proximity encoded by $k o$-. This leaves negativity. In our corpus, expressive negativity is reflected in a bias toward the negative end of the review scale. When we look at the distribution of konna, we see not only a U-shape, but also a negative bias, reflected in the significantly negative value of the linear coefficient ( $\beta_{1}=-0.081$, $p<0.001$ ). This contrasts with the significant positive bias for sono, reflected in the significantly positive value of its linear coefficient ( $\beta_{1}=0.071, p<0.001$ ). Graphically, the profiles of these two items appear to be mirror images of each other, in the horizontal dimension.

In line with our previous discussion of the complementary use of proximal demonstratives and the definite determiner, we posit a competition-based explanation of the contrast between kono and konna. Using konna tends, through the influence of -nna, to contribute a hint of negativity, as argued by [14]. The less marked kono has a complementary positive shift in its profile, as a result

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of competition between forms. The presence of a significant U-shape in both proximal demonstratives is due to the proximal morpheme ko-. This suggests an additive model of pragmatic enrichment, in which the ko- morpheme contributes a tendency for extremity, and the competition between unmarked -no and marked -nna is reflected in a distinct positive and negative bias.

## 5 Conclusion

Using large-scale corpus evidence, we began to make a case for the idea that affective uses of demonstratives are a robust, cross-linguistically stable phenomenon. We also addressed the question of where affective readings come from, arguing that they trace to Horn's division of pragmatic labor: the morphosyntactically complex, relatively infrequent (marked) demonstratives associate with the emotionally deictic (marked) messages. In English, we argued that the definite article plays the unmarked role for form and meaning, and the Japanese data support nuanced oppositions within the demonstrative system.

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# Experimental detection of embedded implicatures ${ }^{\star, \star \star}$ 

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## 1 Theories of scalar implicatures: globalism vs. localism

According to the Gricean approach to scalar implicatures (SIs for short), SIs are pragmatic inferences that result from a reasoning about the speaker's communicative intentions. In recent years, an alternative view of SIs (let us call it the 'grammatical view' of SIs) has been put forward, according to which they result from the optional presence of a covert so-called exhaustivity operator in the logical form of the relevant sentences and are thus reducible to standard semantic entailment (cf. Chierchia 2006, Fox 2007, Chierchia et al. in press, a.o).

While these two radically different approaches do not make distinct predictions in simple cases, they do for more complex ones. In particular, if the 'grammatical approach' is correct, then the exhaustivity operator should be able to occur in an embedded position (just like only), so that the strengthening, say, of 'some' into 'some but not all' could occur 'locally', under the scope of linguistic operators. This approach is often called 'localist', as opposed to pragmatic, so-called 'globalist' approaches (See also Landman 1998, Chierchia 2004).

Consider for concreteness the following example:
(1) Every student solved some of the problems.

The standard neo-Gricean mechanism predicts that (1) should be interpreted as implying the negation of its scalar alternative, i.e. the negation of 'Every student solved all of the problems'. Hence, (1) should give rise to the following reading (henceforth, we'll refer to this reading as the 'global reading'):
(2) Every student solved some of the problems and at least one student didn't solve them all.

If, however, the strengthening of 'some' into 'some but not all' can occur at an embedded level, as predicted by localist approaches, one expects that another possible reading for (1) is the one expressed by (3) below (which we will henceforth call the 'local reading'):

[^10](3) Every student solved some but not all the problems.

It thus seems that determining the possible readings of sentences like (1) should provide decisive evidence in the debate between localism and globalism. This is unfortunately not so. For several formalized globalist theories of SIs (e.g., Spector 2003, 2006, van Rooij and Schulz 2004, Chemla 2008, 2009b) also predict that (3) is a possible reading of (1). ${ }^{3}$

The first goal of this paper is to provide new experimental data which show, contrary to claims put forward in a recent paper by Geurts and Pouscoulous (Geurts and Pouscoulous 2009), that (3) is a possible reading for (1). A second goal of this paper is to examine a case where localism and globalism are bound to make different predictions, and to test it with a similar experimental paradigm.

## 2 Geurts and Pouscoulous' results

G\&P collected truth-value judgments for sentence-picture pairs, asking subjects to evaluate the relevant sentence as true, false, or ambiguous between a true and a false reading. One of their crucial conditions consisted of the sentence 'All the squares are connected with some of the circles', paired with the picture in Fig. 1.


Fig. 1: Item from Geurts and Pouscoulous's (2009) experiment 3 (their Fig. 2)

Here are the three relevant potential readings for the sentence they used:
(4) a. Literal Reading. Every square is connected with at least one circle.
b. Global Reading. Every square is connected with at least one circle, and it's not the case that every square is linked with all the circles.
c. Local Reading. Every square is connected with at least one circle, and no square is connected with all the circles.

G\&P found that virtually all the subjects considered the sentence to be true in Fig. 1, even though it is false under the local reading (the top square is linked to all the circles), and concluded that the local reading does not exist. We challenge this interpretation, by pointing out that there are several reasons why the strong reading, even if it existed, might have been very hard to detect:

[^11]
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- (i) G\&P's pictures are hard to decipher; in particular, the unique falsifier of the local reading (i.e. the top square) is hard to identify as such.
- (ii) Note that the local reading a-symmetrically entails the global reading, which in turn asymmetrically entails the literal reading. Meyer and Sauerland (2009), among others, argue that subjects, due to some kind of a charity principle, tend to interpret ambiguous sentences under their weakest readings, unless a stronger available reading is particularly 'accessible' (see also, e.g., Crain and Thornton 2000, Abusch 1993, Reinhart 1997). If the global and the local readings are equally accessible, it follows that the local reading will be be hard to detect experimentally even if it exists.


## 3 Our experimental design

Like G\&P, we used a sentence-picture matching task, but with some crucial modifications. We believe that our design improve on that of G\&P's in the following respects:

- (re i) The falsifiers of the strong reading are easy to identify (see Fig. 2 below, and in particular the weak condition which is the counterpart of G\&P's item represented in Fig. 1).
- (re ii) Instead of asking for absolute judgments of truth or falsity, we asked for graded judgments: subjects were asked to position a cursor on a continuous line going from 'No' (i.e. 'false') on the left, to 'Yes' (i.e. 'true') on the right. ${ }^{4}$ By offering subjects more options, we hoped to get more fine-grained results, which could reveal differences that remained hidden when subjects were given only two or three options, and thus to overcome some of the consequences of the charity principle. More specifically, we hypothesized that given a sentence $S$ and two distinct pictures $P 1$ and $P 2$, if the set of available readings for S that are true in $P 1$ is a proper subset of those that are true in $P 2$, then the degree to which S will be judged true will be lower in the case of $P 1$ than with $P 2$.


## 4 Experiment 1: scalar items in universal sentences

In this experiment, we showed that the local reading is available for sentences like (1) above: French scalar items like 'certains' (some) ${ }^{5}$ and 'ou' (or), when embedded under universal quantifiers, can give rise to readings in which they seem to be equivalent to, respectively, 'some but not all' or an exclusive disjunction.

[^12]
### 4.1 Experimental items

The items explicitly discussed in the instructions were presented first to allow participants to get used to the display and to the task. ${ }^{6}$ After that, participants ran a first block of items in which all target conditions were repeated several times (in pseudo-random order). Participants then could take a short break before moving to a second block of items instantiating the same experimental conditions (with superficially different pictures). In a last experimental block of items, some control conditions were administered.

Target conditions: universal sentences. Each item consisted of a sentence and a picture. We used the two distinct sentence-types, illustrated in (5) and (6). For each of them, we were interested in the availability of three distinct potential readings, namely the literal, the global and the local readings:
(5) Chaque lettre est reliée à certains de ses cercles.

Each letter is connected to some of its circles.
a. Literal Reading: Each letter is connected to at least one of its circles.
b. Global Reading: Each letter is connected to at least one of its circles, and it is not the case that each letter is connected to all its circles.
c. Local Reading: Each letter is connected to at least one of its circles, and no letter is connected to all its circles.
(6) Chaque lettre est reliée à son cercle rouge ou à son cercle bleu. Each letter is connected to its red circle or to its blue circle.
a. Literal Reading: Each letter is connected to its red circle, its blue circle or both.
b. Global Reading: Each letter is connected to at least one of its circles, and it is not the case that each letter is connected to both the red and the blue circle.
c. Local Reading: Each letter is connected to its red circle or its blue circle but none is connected to both.

Each of these sentences was paired with various pictures, giving rise to the following four target conditions (see Fig. 2): false: no reading is true, literal: only the literal reading is true, weak: both the literal and the global readings are true but the local reading is false, strong: all readings are true.

Control conditions: downward entailing (DE) environments. When scalar items are embedded in the scope of 'No' as in (7a) or (8a), it is uncontroversial that the potential 'local' readings described in (7b) and (8b) are only marginally available at best.

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Fig. 2: Illustrative examples of the images used in the different conditions false, literal, weak and strong for the test sentence (5). We also reported below each image whether the literal, global and local readings are true (T) or false (F).
(7) a. Aucune lettre n'est reliée à certains de ses cercles. No letter is connected to some of its circles.
b. Potential local reading: No letter is connected to some but not all of its circles.
(8) a. Aucune lettre n'est reliée à son cercle rouge ou à son cercle bleu. No letter is connected to its red circle or its blue circle.
b. Potential local reading: No letter is connected to exactly one of its two circles.

Sentences like (7a) and (8a) were thus used as controls, to check that participants do not access the 'local' reading for such sentences, or do so only marginally (given the marginal availability of the local reading). They were paired with pictures instantiating the following three conditions: false: no reading is true ?local: only the local reading is true, both: both the local and the literal readings are true.

### 4.2 Results and interpretation

Main result: detection of the local reading. Fig. 3 reports the mean ratings in the target conditions. The relevant $t$-tests show that all differences between two consecutive bars are significant. ${ }^{7}$

The crucial result is that the ratings are higher in the strong condition than in the weak condition, even though the two conditions differ only according to the truth value of the local reading. This difference provides important support

[^14]

Fig. 3: Main results: Mean position of the cursor in the target conditions of Exp. 1. Error bars represent standard errors to the mean.
for the existence of the local reading. Indeed, these results are fully explained if we assume that a) the target sentence is ambiguous between the literal reading, the global reading and the local reading, and b) the more readings are true, the higher the sentence is rated. They are not expected if only the literal and the global readings exist.

Control result : downward-entailing environments Fig. 4 reports the results for the control conditions. For the scalar item 'some', the relevant $t$-tests show a significant difference between all pairs of conditions, while for the scalar item 'or', there is no difference between the false condition and the ?local condition. ${ }^{8}$


Fig. 4: Mean responses for the DE control conditions in exp. 1 (see §4.1).

In the case of 'some', we cannot exclude that participants perceived the 'local' reading, because the ?local condition is judged a little higher than the false condition. But this result is not terribly disturbing for two reasons. First, it does not generalize to the scalar item 'or'. Second, the control sentences receive a much lower rating in the condition ?local than in conditions where it is uncontroversial that the target sentence has a true reading. Note that even with the scalar item 'some', the condition ?local is rated at a radically lower level than the condition both ( $25 \%$ vs. $92 \%$ ); more importantly, in the case of 'some', the condition ?local is rated much lower than conditions in which it is uncontroversial that the target sentence has a true reading (consider for instance the important difference between this ?local condition and the weak condition - which involved the target sentences. This difference is statistically significant: $F(1,15)=22, p<.001)$.

[^15]
## 5 Experiment 2: non-monotonic environments

In this second experiment, we tested cases for which pragmatic and grammatical theories are bound to make different predictions. This happens with sentences where a scalar item like 'some' or 'or' occurs in a non-monotonic environment:
(9) Exactly one letter is connected to some of its circles.
(10) Exactly one letter is connected to its blue circle or its red circle.

The relevant potential readings (i.e. those that the sentence could in principle have according to various theories) can be paraphrased as follows: ${ }^{9}$
(11) Potential readings of (9)
a. Literal meaning: one letter is connected to some or all of its circles, the other letters are connected to no circle.
b. Global reading: one letter is connected to some but not all of its circles, the other letters are connected to no circle.
c. Local reading: one letter is connected to some but not all of its circles, the other letters may be connected to either none or all of their circles.
(12) Potential readings of (10)
a. Literal meaning: one letter is connected to its blue circle or its red circle or to both, the other letters are connected to no circle.
b. Global reading: one letter is connected to exactly one of its two circles, the other letters are connected to no circle.
c. Local reading: one letter is connected to exactly one of its two circles, the other letters may be connected to either none or both of their circles.

Because the scalar item now occurs in a non-monotonic environment, the local reading does not entail the global reading. In fact, it does not even entail the literal reading. This is of major importance for three reasons. First, globalist theories are bound to predict readings that entail the literal reading. Hence they cannot predict local readings like (11c) or (12c) in these non-monotonic cases. Second, the fact that the local reading does not entail any of the other two potential readings could automatically make it easier to detect (according to a charity principle). Finally, this very fact allowed us to construct cases where only the local reading is true and to assess its existence independently of the other readings.

### 5.1 Experimental items

The task and the instructions were essentially the same as in experiment 1.The items were presented just like in experiment 1: the examples from the instructions were presented first; then came two blocks of target conditions, and finally

[^16]came a block with exactly the same control conditions as in experiment 1 . The target conditions involved French translations of (9) and (10). Each of these sentences was paired with various pictures, giving rise to the following four target conditions, which represent all the possible combinations of true and false readings, and are illustrated in Fig. 5: false: no reading is true, literal: only the literal reading is true, local: only the local reading is true and all: all three readings literal, global and local - are true.

$$
\text { Global }=\mathrm{F}
$$
$$
\text { Local }=\mathrm{F}
$$


Fig. 5: Illustrative examples of the images used to illustrate the different conditions false, literal, local and all for the test sentence (9). We also reported below each image whether the literal, global and local readings are true ( T ) or false (F).

### 5.2 Results

Main result: the local reading exists. Fig. 6 reports the mean ratings of the target conditions. ${ }^{10}$ All 2 by 2 differences are significant, except for the local vs. literal conditions in the case of 'or'. ${ }^{11}$


Fig. 6: Mean responses in the target conditions of experiment 2.

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This first set of data qualifies the local reading as a possible interpretation for our target sentences (involving non-monotonic operators), since 1) the local condition is rated much higher than in the false condition and ii) the local reading is rated significantly higher than the literal condition, a fact which is totally unexpected under the globalist approach, but can be understood within the localist approach.

Control result: downward entailing environments. Fig. 7 reports the results for the DE control conditions (which were the same as in Exp. 1). All 2 by 2 differences are statistically significant with both 'some' and 'or'. ${ }^{12}$


Fig. 7: Mean responses for the control conditions when administered at the end of experiment 2 .

Surprisingly, the rates for the ?local condition are higher than they were in the first experiment (compare Fig. 7 to Fig. 4), which calls for an explanation. A possible hypothesis is the following: subjects become much better at perceiving 'local' readings even in cases where they are normally dispreferred once they have experienced cases in which the local reading is salient. The target conditions of the second experiment seem to have precisely this property, given the results we have just presented.

## 6 Conclusions

Our first experiment showed that sentences in which a scalar item is embedded under a universal quantifier can be interpreted according to what we called the 'local' reading, contrary to Geurts and Pouscoulous' (2009) conclusions. We pointed out that this result is nevertheless not sufficient to establish the existence of embedded scalar implicatures (because the local reading in such a case can be predicted by a globalist account). In our second experiment, we focussed on a case where the local reading cannot be derived by globalist means - sentences where a scalar item occurs in a non-monotonic environment - , and we were able to detect experimentally genuinely local readings. The existence of embedded scalar implicatures is unexpected from a Gricean perspective. The grammatical approach to SIs provides one possible way of making sense of these data.

[^18]
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# Local and Global Implicatures in Wh-Question Disjunctions 

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#### Abstract

It has been observed that wh-questions cannot be joined disjunctively, the suggested reasons being semantic or pragmatic deviance. We argue that wh-question disjunctions are semantically well-formed but are pragmatically deviant outside contexts that license polarity-sensitive (PS) items. In these contexts the pragmatic inadequacy disappears due to a pragmatically induced recalibration of the implicature triggered by or (as argued in [2]). Importantly, the licensing of the PS property of wh-disjunctions cannot be reduced to the licensing of a lexical property of a single item but also depends on the semantics of the disjoined questions. We propose that the alternativeinducing property of or has as its syntactic correlate the feature [ $+\sigma$ ] (cf. [3]), thus forcing the insertion of the operator $\mathrm{O}_{\mathrm{ALT}}$, which is responsible for the computation of implicatures at different scope sites.


Keywords: wh-question disjunction, global implicatures, local implicatures, polarity-sensitive items, strengthening, weakening

## 1 Introduction: The Deviance of Wh-Question Disjunctions

Wh-question disjunctions have been observed to be deviant, e.g. [18], [16]: Whereas a conjunction of two questions is fine, s. (1), a disjunction is unacceptable, s. (2).

Which dish did Al make and which dish did Bill make?
Which dish did Al Make or which dish did Bill make?

According to [8], the reason for the deviance of $w h$-question disjunctions is semantic. In [8]'s question theory, a question defines a partition of the logical space. A disjunction of two questions is then a union of two partitions, which is not again a partition: There are overlapping cells. Thus the disjunction of two questions is not a question. According to [16], the reason for the deviance of $w h$-question disjunctions is also pragmatic, the underlying assumption being that speech acts cannot be coordinated disjunctively. Speech acts are operations that, when applied to a
commitment state, deliver the commitments that characterize the resulting state. Speech act disjunction would lead to disjunctive sets of commitments, which are difficult to keep track of. According to [16], a question like (2) could only ${ }^{1}$ be interpreted in the way indicated in (3), where the speaker retracts the first question and replaces it by the second. As a result there is only one question to be answered.

Which dish did Al make? Or, which dish did Bill make?

In this paper we propose that wh-question disjunctions do denote proper semantic questions but are pragmatically deviant outside specific contexts. We identify these specific contexts as contexts that license polarity-sensitive items (PSIs). In PSIlicensing contexts, the pragmatic inadequacy disappears due to a pragmatically induced recalibration of the implicature triggered by or (cf. [2]). The account developed here does not carry over to alternative questions, which can be viewed as a disjunction of yes-no-questions. For recent accounts of these, cf. [17], [1], [10].

## 2 The Semantics of Wh-Questions and Wh-Question Disjunctions

For the semantics of $w h$-questions we follow [14] and assume that a question denotes the set of its true answers. For instance, the question How did Paul get home has the denotation in (4). Assuming that in the evaluation world Paul got home by bus and by train, the set in (4) is the set given in (5). The weakly exhaustive answer to (4) is the conjunction of all the propositions in the set of true answers, see (6).
$\llbracket$ How did Paul get home? $\rrbracket \|=\left\{p \mid \exists m\left(\vee \mathrm{p} \wedge \mathrm{p}={ }^{\wedge}(\right.\right.$ Paul got home in manner m$\left.\left.)\right)\right\}$
$\{\llbracket$ Paul got home by bus $\rrbracket, \llbracket$ Paul got home by train $\rrbracket\}$
Paul got home by bus and Paul got home by train.

For easier exposition we only consider singleton sets in what follows.

[^19]For the disjunction of $w h$-questions we propose that such a disjunction denotes the set of propositions that results from the pairwise disjunction of any two propositions from the respective disjuncts, s. (7). Thus every proposition in the answer set of the first question is conjoined disjunctively with every proposition in the answer set of the second question. For (8) this delivers (9) if in fact Paul got home by bus at 3 a.m. and in no other way and at no other time.

$$
\begin{align*}
& \text { where } \mathrm{p} \vee \mathrm{q}={ }^{\wedge}\left({ }^{\vee} \mathrm{p} \vee{ }^{\vee} \mathrm{q}\right) \text { for } \mathrm{p}, \mathrm{q} \text { of type }<s, t,> \tag{8}
\end{align*}
$$

$\llbracket\left[{ }^{0} 1\right.$ How did Paul get home?] or [Q2 When did Paul get home?]』
$\{\llbracket$ Paul got home by bus $\rrbracket \vee \llbracket$ Paul got home at 3 a.m. $\|\}$
The deviance of the question disjunction in (8) can be explained if we consider its pragmatics, more specifically, if we look at it from the point of view of Gricean reasoning [7]. By [14], the weakly exhaustive answer to (8) - viz. (6) above - is a coordination of two propositions that are true in the evaluation world. Conjoining these by or violates Grice's Maxim of Quantity: and would be more informative without violating Quantity. We suggest that this is the reason for the unacceptability of $w h$-question disjunctions: $w h$-question disjunctions are unanswerable and therefore deviant. This result can be derived 'more directly' without Gricean reasoning if we consider strongly exhaustive (= enriched) answers, s. section 4.
Before closing this section, we would like to point out that our proposal might be rejected on the assumption that the over-informative and-answer should pose no problems because it is generally possible to give over-informative answers to questions, cf. (10). So this should be possible for disjoined $w h$-questions as well.

Q: Has someone called for me? A: Yes, Paul did.

We argue below (section 4) that wh-question disjunctions do not have a true strongly exhaustive answer and therefore the existence presupposition of $w h$-questions - that there should be such a true strongly exhaustive answer - cannot be satisfied. In this sense there is no such thing as an over-informative answer in these cases.

## 3 Non-Deviant Wh-Question Disjunctions

In the previous section we discussed the observation that $w h$-question disjunctions are deviant and gave an account for why this should be. Note that we only considered matrix questions in that section. Moving on to embedded questions at first sight does not change the picture: Speakers judge the sentence in (11) to be unacceptable.
*The police found out how or when Paul got home that night.

For some speakers, (11) improves if the question words are heavily accented and if there also is an intonational phrase break after the first question word, as indicated in (12). These phonological means, we suggest, indicate the readings in (12a) or (12b):
\%The police found out HOW, or WHEN Paul got home that night.
a. The police found out HOW, or rather WHEN Paul got home that night.
b. The police found out HOW, or the police found out WHEN Paul got home that night.
(12a) is a retraction reading, similar to the one in (3) discussed in section 1. (12b) is an instance of right node raising, i.e. ellipsis, so that we are not dealing with a question disjunction here but with a disjunction of the matrix clause assertions. These readings are irrelevant for the present discussion. As for the (surface) coordination of the question words how, when, s. below.

Now, digging a bit deeper we find that there are actually instances of embedded disjoined questions that are acceptable. As a matter of fact, there are quite a number of contexts that license embedded disjoined questions:

The police did not find out how or when Paul got home that night. (negation)
If the police find out how or when Paul got home that night they can solve the crime. (antecedent of conditional)

Few detectives found out how or when Paul got home that night. (downward-
entailing quantifier)
The police hoped to find out how or when Paul came home that night. (strong
intensional predicate)
The police might have found out how or when Paul came home that night. (modalized context)

The police refuse to find out how or when Paul came home that night.
(adversative predicate)
Have the police found out how or when Paul got home that night? (question)
Find out how or when Paul came home that night! (imperative)

These contexts are all contexts that license PS items. Thus, wh-question disjunctions can be classified as polarity-sensitive:

Generalization: The PS Property of Wh-Question Disjunctions. Wh-question disjunctions are licensed in downward-entailing contexts and in non-downwardentailing contexts that are non-veridical.

A context is non-veridical if for any sentence $\mathrm{C}(\phi)-1 \rightarrow \phi(=$ if $\phi$ occurs in a nonveridical context the truth of $\phi$ does not follow). Some non-veridical contexts, like negation, are also anti-veridical, which means that if $\phi$ occurs in such a context the falsity of $\phi$ follows [5].

Before we proceed we would like to point out that the question word disjunctions considered above indeed correspond to the disjunction of full questions. This can be seen quite easily from the fact that it is possible to coordinate disjunctively the complementizer if with a $w h$-word, see (21). Such a disjunction must involve ellipsis as it cannot be derived semantically as a term conjunction.

The police did not find out if or when Paul got home that night.

What about matrix clause ellipsis? -- For the unacceptable example in (11) above, which involved a matrix context that did not license PSIs, we considered the possibility that it might improve for some speakers if the intonational means signal matrix clause ellipsis. For the felicitous examples in (13) through (20) this option is not available. Let us illustrate this for the negation context in (13). If this sentence is assumed to be derived from matrix clause ellipsis its meaning is different:

The police did not find out how or when Paul got home that night.
The police did not find out how Paul got home that night or when Paul got home that night.

$$
\Leftarrow / \Rightarrow
$$

The police did not find out how Paul got home that night or the policedid not find out when Paul got home that night.

We conclude from this that ellipsis of the matrix clause is not available as a general point of departure for a unified analysis of disjoined embedded questions. The ellipsis is confined to the embedded clauses. Thus, for the sentence in (13) we assume a syntactic structure like the one below:
[CProot The police did not find out [orP [CP1 how Paul got home that night]
[or' or [CP2 when Paul got home that night]]]]

The (unenriched) meaning of (13) is given in (24), where ans corresponds to the Hamblin-style answer operator in [11]. We assume that predicates like find out do not embed questions directly: They embed answers to the question, whence the
application of ans, which delivers the intersection of the propositions in the answer set to the question.

$$
\begin{align*}
& \left.\neg \text { find_out (the_police, } \operatorname{ans}\left(\left\{\mathrm{p}_{1} \vee \mathrm{p}_{2} \mid \mathrm{p}_{1} \in \mathbb{\mathbb { L }} \mathrm{Q}_{1} \rrbracket \wedge \mathrm{p}_{2} \in \mathbb{\mathbb { L }} \mathrm{Q}_{2} \rrbracket\right\}\right)\right)  \tag{24}\\
& \text { where } \operatorname{ans}(\mathrm{Q})=\cap_{\mathrm{p} \in \mathrm{Q}} \mathrm{p}
\end{align*}
$$

## 4 Computing Local and Global Implicatures: Explaining the PS Property of Wh-Disjunctions

In section 2 we explained the deviance of matrix $w h$-question disjunctions by appealing to Gricean reasoning: The disjunctive operator or gives rise to a scalar alternative - the conjunctive operator and - , which would have been the better choice by the Maxims of Quantity and Quality. In the previous section we proposed that whquestion disjunctions are polarity-sensitive. Now, scalar implicatures have also been argued to play an important role in the licensing of PS items like any. [13] suggest that any-NPs are indefinites which come with an instruction to the hearer to consider domains of individuals that are broader than what one would usually consider, i.e. any-NPs are domain wideners. In downward-entailing contexts like negation domain widening strengthens a statement because excluding a larger domain of individuals leads to a more informative statement than excluding a smaller domain of individuals. [15] links these consideration directly to quantity implicatures and suggests that a NPI like any activates alternatives with smaller domains, which triggers the implicature that the alternative selected is the strongest one the speaker has evidence for. The fact that $w h$-question disjunctions are licensed in exactly those contexts that license PS items is thus very suggestive of a close link along these lines of reasoning.

What will be important for the data we consider here is the observation that implicatures can also arise in embedded contexts. This is somewhat unexpected if pragmatic reasoning is assumed to follow all syntactic and semantic computations, and it has led [2] to argue for a 'more grammatical' view of implicatures, which we take our findings to be supporting evidence for. To start with, consider the following embedded disjunction:

The police found out that Paul got home by bus or that he got home at 3 a.m.

The preferred reading of or in (25) is the exclusive one: (25) could describe the findings of the police if the busses stop at $12 \mathrm{p} . \mathrm{m}$. - Paul would have been home by 12 if he took the bus, or later (such as at 3 a.m.) if he did not take the bus. The implicature in (25) is a local scalar implicature, see (26), the global implicature would be the one in (27), and it is weaker than the local implicature: it is compatible with the police attaining the knowledge that it is possible that $(\mathrm{p} \wedge \mathrm{q})$.

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$$
\begin{equation*}
\text { find_out(the_police, }(\mathrm{p} \vee \mathrm{q}) \wedge \neg(\mathrm{p} \wedge \mathrm{q})) \tag{26}
\end{equation*}
$$

find_out(the_police, $(p \vee q)) \wedge \neg$ find_out(the_police, $(p \wedge q))$
$\cong$ The police found out that $(p \vee q)$ and the police did not find out anything with respect to $(\mathrm{p} \wedge \mathrm{q})$
[2], [3] suggest that the difference between local and global implicatures can be put down to an operator $\mathrm{O}_{\mathrm{ALT}}$ for scalar enrichment that can attach at various scope sites:

$$
\begin{equation*}
\mathrm{O}_{\mathrm{ALT}}(\mathrm{p})=\mathrm{p} \wedge \forall \mathrm{q} \in \operatorname{ALT}\left[{ }^{\vee} \mathrm{q} \rightarrow \mathrm{p} \subseteq \mathrm{q}\right] \tag{28}
\end{equation*}
$$

$O$ is a mnemonic for only : p and its entailments are the only members of ALT that hold. In the case of or: $\operatorname{ALT}=\left\{\mathrm{p}_{1} \vee \mathrm{p}_{2}, \mathrm{p}_{1} \wedge \mathrm{p}_{2}\right\}$ for $\mathrm{p}=\mathrm{p}_{1} \vee \mathrm{p}_{2}$. In the case of (25), $\mathrm{O}_{\mathrm{ALT}}$ applies to the embedded orP, yielding the enriched meaning given below:

$$
\begin{align*}
& \text { find_out(the_police, } \left.O_{\text {ALT }}\left(p_{1} \vee q_{2}\right)\right)  \tag{29}\\
& \Leftrightarrow \\
& \text { find_out(the_police, }(p \vee q) \wedge \neg(p \wedge q))
\end{align*}
$$

where $\mathrm{p}_{1}=\llbracket$ Paul got home by bus $\rrbracket, \mathrm{p}_{2}=\llbracket$ Paul got home at 3 a.m. $\rrbracket$

Turning to embedded $w h$-question disjunctions like (11) from section 3 above, repeated below for convenience, the insertion of $\mathrm{O}_{\mathrm{ALT}}$ at the level of orP yields the following equivalence:
*The police found out how or when Paul got home that night. (= (11))

$$
\begin{gather*}
\text { find_out(the_police, } \left.\mathrm{O}_{\text {ALT }}\left(\operatorname{ans}\left(\left\{\mathrm{p}_{1} \vee \mathrm{p}_{2} \mid \mathrm{p}_{1} \in \llbracket C \mathrm{P}_{1} \rrbracket \wedge \wedge \mathrm{p}_{2} \in \llbracket \mathrm{CP}_{2} \rrbracket\right\}\right)\right)\right)  \tag{30}\\
\Leftrightarrow \\
\text { find_out(the_police, } \left.\left(\mathrm{p}_{1} \vee \mathrm{p}_{2}\right) \wedge \neg\left(\mathrm{p}_{1} \wedge \mathrm{p}_{2}\right)\right)
\end{gather*}
$$

where (by our assumptions on the meaning of questions) $\mathrm{p}_{1}$ and $\mathrm{p}_{2}$ are true in the actual world

Importantly, the strongly exhaustive answer to the embedded question in (11) is false in the actual world. This produces a presupposition failure under the factive verb find out, and more generally, a failure of the existence presupposition of the embedded $w h$-question Q , viz. $\exists \mathrm{p}\left({ }^{\vee} \mathrm{p} \wedge \mathrm{p}=\mathrm{O}_{\mathrm{ALT}}(\operatorname{ans}(\mathrm{Q}))\right)$, which explains why $w h$-disjunctions neither can be embedded under non-factive verbs like tell (not illustrated). Furthermore, this also explains the matrix case without Gricean reasoning: In the
matrix case, $\mathrm{O}_{\text {aLt }}$ can only be inserted at the matrix level. This produces a violation of the presupposition that there must be a true strongly exhaustive answer.

If the local insertion of $\mathrm{O}_{\text {ALT }}$ produces an unacceptable sentence we might wonder, of course, why it is not global insertion that is applied. The resulting enriched meaning would be the following (cf. (27) above).

$$
\begin{align*}
& \text { find_out }\left(\text { the_police, }\left(\mathrm{p}_{1} \vee \mathrm{p}_{2}\right)\right) \wedge \neg \text { find_out }\left(\text { the_police, }\left(\mathrm{p}_{1} \wedge \mathrm{p}_{2}\right)\right)  \tag{31}\\
& \cong \text { where } \mathrm{p}_{1} \text { and } \mathrm{p}_{2} \text { are true in the actual world \& where } \neg \text { find_out } \\
& \text { means did not acquire knowledge about. }
\end{align*}
$$

Inserting $\mathrm{O}_{\text {ALT }}$ at the root level leads to a rather weak interpretation but it does not lead to deviance. Still, this reading does not seem to be available. This is surprising given that $\mathrm{O}_{\mathrm{AlT}}$ generally can be inserted at any scope site (cf. [4]). We have some preliminary evidence that under very specific contextual conditions the preference for the local implicature can be overridden. Unfortunately we do not have the space to discuss this here (see [11]).
Let us turn next to felicitous embedded wh-question disjunctions starting with downward-entailing contexts, e.g. (13) with negation. [2] observes that the downward-entailing property of an operator like negation in the matrix clause typically induces a recalibration of the implicature because local enrichment would lead to weakening in these contexts. Thus, $\mathrm{O}_{\text {alt }}$ applies to the matrix clause, s . (32). The equivalence in (32) holds because $\neg$ find_out $\left(x, \mathrm{p}_{1} \vee \mathrm{p}_{2}\right) \subseteq \neg$ find_out $\left.\left(x, \mathrm{p}_{1} \wedge \mathrm{p}_{2}\right)\right)$.

The police did not find out how or when Paul got home that night. ( = (13))

$$
\begin{gather*}
\mathrm{O}_{\text {ALT }}\left(\neg \text { find_out }\left(\text { the_police, } \operatorname{ans}\left(\left\{\mathrm{p}_{1} \vee \mathrm{p}_{2} \mid \mathrm{p}_{1} \in \llbracket C \mathrm{P}_{1} \rrbracket \rrbracket \wedge \mathrm{p}_{2} \in \llbracket \mathrm{CP}_{2} \rrbracket\right\}\right)\right)\right)  \tag{32}\\
\Leftrightarrow
\end{gather*}
$$

$\neg$ find_out(the_police, $\mathrm{p}_{1} \vee \mathrm{p}_{2}$ ), where $\mathrm{p}_{1}$ and $\mathrm{p}_{2}$ are true in the actual world

In the present case, application of $\mathrm{O}_{\text {ALT }}$ to the matrix clause does not produce an implicature. That the result in (32) is correct can be seen from the fact that The police do not believe that Paul came home by bus or that he came home at 3 a.m. is equivalent with The police believe neither that Paul came home by bus nor that he came home at 3 a.m. (with embedded declaratives we must use a non-factive matrix predicate to avoid interfering presuppositions). This result carries over to all other downward-entailing contexts.

Turning to contexts that are not downward-entailing but nevertheless license embedded $w h$-question disjunctions, let us consider questions. That questions are not downward entailing can be see from the fact that the positive answer to an or-question like the one in (33), is entailed by the positive answer to an and-question like the one in (34). In other words, the or-question is actually weaker than its alternative.

A: Have the police found out how or when Paul got home that night? B: Yes.

A: Have the police found out how and when Paul got home that night? B: Yes.
Why would or be licensed if the semantics of the disjoined questions licenses the use of $a n d$ ? Asking weaker questions often is pragmatically advantageous [15]. First observe that positive yes-no questions come with no particular bias as to the expected answer (yes or no). In order to optimize the information gain from both possible answers, the speaker will try to maintain an equilibrium between the informational value of the positive and the negative answer ([15], also cf. [19]'s notion of entropy). Importantly, the weaker a question is the more balanced the answers are, and the better the information gain is in proportion to the likelihood of the answer. This can be seen quite easily when considering guessing games where participants must guess e.g. the occupation of an invited person. In such a game, asking the rather weak question in (35) maximizes the information gain because the likelihood of receiving the yes- vs. the no-answer is roughly the same. This is different in a strong question like (36), where the no-answer would yield hardly any information gain.

Are you involved in the production/ distribution of a product?
Are you a hearing aid audiologist?

For questions as licensing contexts, inserting $\mathrm{O}_{\text {ALt }}$ at the root level rather than at the embedded level yields the weaker question.

## 5 Conclusion

Our analysis lends strong support to the central claim of [2] that the syntactic distribution of PS items is determined by grammatically conditioned pragmatic principles. The PS property of wh-disjunctions is semantically composed of two independent properties: the semantic/pragmatic property of or to induce (scalar) alternatives, and the semantics of the disjoined questions. This means that the licensing of the PS property cannot be reduced to the licensing of a lexical property of a single item (as has been suggested e.g. for any as having the property of denoting a 'dependent variable', cf. [6]. If there is a syntactic feature involved in the licensing of the PS property it must be the syntactic correlate of the alternative-inducing property of an element like or, cf. the feature $[+\sigma]$ in [2]. This is what we assume here: or always comes with $[+\sigma]$, which forces the insertion of $\mathrm{O}_{\text {ALT }}$ as discussed above.

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# Supplements <br> Within a Unidimensional Semantics ${ }^{1}$ 

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#### Abstract

Potts $(2005,2007)$ claims that Grice's 'conventional implicatures' offer a powerful argument in favor of a multidimensional semantics, one in which certain expressions fail to interact scopally with various operators because their meaning is located in a separate dimension. Potts discusses in detail two classes of phenomena: 'expressives' (e.g. honorifics, ethnic slurs, etc.), and 'supplements', especially Non-Restrictive Relative Clauses (= NRRs). But the former have been re-analyzed in presuppositional terms by several researchers, who have suggested that expressives trigger presuppositions that are i. indexical and ii. concern the speaker's attitudes - hence the fact that i. they appear to have matrix scope, and ii. they are automatically accommodated (Sauerland 2007, Schlenker 2007). Thus supplements arguably remain the best argument in favor of a separate dimension for conventional implicatures. We explore an alternative in which (1) NRRs can be syntactically attached with matrix scope, despite their appearance in embedded positions; (2) NRRs can in some cases be syntactically attached within the scope of other operators, in which case they semantically interact with them; (3) NRRs are semantically conjoined with the rest of the sentence, but (4) they are subject to a pragmatic rule that requires that their content be relatively easy to accommodate - hence some non-trivial projection facts when NRRs do not have matrix scope. (1), which is in full agreement with the 'high attachment' analysis of NRRs (e.g. Ross 1967, Emonds 1979, McCawley 1998, Del Gobbo 2003), shows that Potts's semantic machinery is redundant: its effects follow from more conservative semantic assumptions once an adequate syntax is postulated. (2), which disagrees with most accounts of NRRs, shows that Potts's machinery makes incorrect predictions when NRRs have a non-matrix attachment. (4) explains why NRRs sometimes display a projection behavior similar to presuppositions.


Keywords: supplements, appositives, non-restrictive relative clauses, bidimensional semantics

[^20]
## 1 Bidimensional vs. Unidimensional Analyses

The contrast between (1)a and (1)b suggests that appositive relative clauses are 'scopeless', i.e. that they do not interact semantically with operators in whose scope they appear.
(1) a. I doubt that John, who is smart, is competent.
=> John is smart.
b. I doubt that John is smart and competent.
$\neq>$ John is smart
This behavior was taken by Potts 2000, 2005 and Nouwen 2006 to argue for a bidimensional semantics, one in which 'supplements' (= the semantic content of appositives) are computed in a separate dimension from assertive content. Their analysis is sketched in (2)
(2) Bidimensional Analysis (Potts 2000, 2005; Nouwen 2006)
(i) Syntax: Appositives are attached in their surface position.
(ii) Semantics: Supplements are computed in a separate dimension, which has two effects.
A. They appear to have 'wide scope'.

Version 1 (Potts): They do not interact scopally with other operators.
Version 2 (Nouwen): They only interact scopally with operators to the extent that unembedded E-type pronouns do (e.g. in John invited few people, who had a good time, the NRR does interact with the quantifier; but the truth conditions are similar to those of the discourse John invited few people. They had a good time).
B. Supplements have a special epistemic status (they are not 'at issue').

We explore an alternative account within a unidimensional semantics. In brief, we take NRRs to be preferably attached to the matrix level, although lower attachments are also possible; we take NRR to have a conjuntive semantics; and we take them to be subject to a pragmatic constraint that requires that their content be both non-trivial and not too surprising. These assumptions are stated more precisely in (3).
(3) Unidimensional Analysis
(i) Syntax (see McCawley 1988, Del Gobbo 2003)
-A NRR can be attached to any node of propositional type that dominates its associated NP.
-Preferences: highest attachment >> lower attachment - attitudinal >> lower attachment - non attitudinal
(ii) Semantics (Del Gobbo 2003)
a. A NR pro can be interpreted as an E-type or referential pronoun.
b. An NRR is interpreted conjunctively.

## (iii) Pragmatics

The content of a NRR must be 'easy to accommodate', but non-trivial which gives rise to non-trivial pattern of projection.
We provide three arguments in favor of our approach:
(i) Bidimensionalism is unnecessary because there are independent arguments for postulating that high syntactic attachment is possible.
(ii) Bidimensionalism is undesirable because there are other cases in which low attachment is possible (though often dispreferred). Potts \& Harris 2009 allow for such a possibility, but only in the context of implicit or explicit attitude reports; we display examples that do not involve those.
(iii) Pragmatics: some supplements give rise to non-trivial patterns of projection which are formally similar to presupposition projection. This suggests that there is a non-trivial interaction between the appositive content and other operators.

## 2 The Possibility of High Syntactic Attachment

Cinque 2008 distinguished between two types of nonrestrictive relative clauses:
(5) a. 'Integrated NRRs' are 'essentially identical to the ordinary restrictive construction (as such part of sentence grammar)'. Such NRRs are not available in English. In French, these are exemplified by relative clauses intorduced by qui.
b. 'Non-integrated NRR' are 'distinct from the ordinary restrictive construction (with characteristics of the grammar of discourse)'. All English NRRs are of this type. In French, it is represented by relative clauses introduced by lequel.

Focusing on French, we show that even integrated NRRs have the ability to attach syntactically at the matrix level when their surface position appears to be embedded.

### 2.1. Ellipsis

Our first argument replicates in French a paradigm discussed by McCawley 1988 for English:
(6) John sold a violin, which had once belonged to Nathan Milstein, to Itzhak Perlman, and Mary did too.

McCawley 1988 observed that the second sentence does not imply that the violin that Mary sold to Perlman had once belonged to Nathan Milstein. On the assumption that ellipsis targets a constituent, this suggests that the NRR can be attached outside the constituent which is the antecedent of the elided VP. This reasoning lead McCawley to posit the structure in (7), which crucially involves a discontinuous constituent. (We do not need in the present discussion to adopt McCawley's ternary branching structure for the VP; all that matters for our purposes is that the NRR can be attached must higher than its surface position).


The same conclusion must be reached about NRRs introduced by qui in French; in this respect, they contrast rather clearly with restrictive relative clauses:
(8) Context: In each generation, the most famous cellist gets to meet the most talented young musicians.
a. Yo Yo Ma a présenté ses élèves préférés, qui vivent à Cambridge, à

Rostropovitch. Paul Tortelier aussi, bien sûr.
Yo Yo Ma introduced his favorite students, who live in Cambridge, to
Rostropovich. Paul Tortelier did too, of course
$\neq>$ Tortelier has students in Cambridge.
b. Yo Yo Ma a présenté ses élèves qui vivent à Cambridge, à Rostropovitch.

Paul Tortelier aussi, bien sûr.
Yo Yo Ma introduced his students who live in Cambridge to Rostropovich.
Paul Tortelier did too, of course.
=> Tortelier has students in Cambridge.

### 2.2. Condition C Effects

Our second argument concerns Condition C effects, which are weakened or obviated in some cases that involve NRRs, as in (9).
(9) $[\text { Le Président }]_{i}$ est si compliqué qu' [The President $_{i}$ is so complicated that
a. * $\mathrm{il}_{\mathrm{i}}$ a donné au ministre qui n' aime pas Sarkozy $\mathrm{y}_{\mathrm{i}}$ une tâche impossible. he ${ }_{i}$ gave the minister who doesn't like Sarkozy $y_{i}$ an impossible task.
b. (?) $\mathrm{il}_{\mathrm{i}}$ a donné au ministre de la Justice, qui n'aime pas Sarkozy $\mathrm{y}_{\mathrm{i}}$, une tâche impossible.
$h_{i}$ gave the minister the minister of Justice, who doesn't like Sarkozy ${ }_{i}$, an impossible task.
(10) $\quad[\text { Le Président }]_{i}$ est si compliqué qu' [The President] is so complicated that
a. ${ }^{*} \mathrm{il}_{\mathrm{i}} \mathrm{n}$ 'a envoyé qu'à un seul journaliste qui adore $\operatorname{Sarkozy}_{\mathrm{i}} \operatorname{Son}_{\mathrm{i}}$ dernier livre. he $e_{i}$ sent to only one journalist who loves Sarkozy his $_{i}$ latest book.
b. $\mathrm{il}_{\mathrm{i}} \mathrm{n}$ 'a envoyé qu'à un seul journaliste, qui adore Sarkozy $_{\mathrm{i}}$, , $\mathrm{Son}_{\mathrm{i}}$ dernier livre. he $e_{i}$ sent to only one journalist, who loves Sarkozy, his latest book.
The data involving high syntactic attachment show that an analysis that posits a separate semantic dimension in order to handle the apparent 'wide scope' behavior of NRRs is not necessary, since these are sometimes syntactically attached to the matrix level. Of course it remains to understand why such high attachments are possible, given that they would seem to violate standard syntactic constraints. We leave this question for future research.

## 2 The Possibility of Low Syntactic Attachment

We will now suggest that the bidimensional analysis in its usual form - which implies that NRRs always display wide scope behavior - is not just unnecessary, but also undesirable because there are cases in which NRRs display a narrow scope behavior.

Proving this is usually difficult if one accepts the hypothesis that the wh pronoun of a NRR has the semantics of a donkey pronoun. This hypothesis, developed by Del Gobbo 2003, is certainly compatible with a bidimensional approach, and it was in fact implemented in great detail in Nouwen 2006. The difficulty is that E-type pronouns that have wide scope can often 'imitate' the behavior of variables that are bound under other operators. Thus an example such as (11)a cannot really show that NRRs may have scope under a quantifier, because the control sentence in (11)b doesn't sound too bad, and suggests that some semantic or pragmatic mechanism (call it 'quantificational subordination') allows the pronouns in the second sentence to be interpreted as if they had scope under the universal quantifier in the first sentence.
(11) a. On Mother's day, every little boy calls his mother, who tells him she loves him.
b. On Mother's day, every little boy calls his mother. She tells him that she loves him.

Still, other cases cannot be explained away in this fashion. Thus (12)a-b gives rise to a very sharp contrast between the NRR and the case of anaphora in discourse.
(12) Context: There was incident at school ${ }^{2}$.
a. Il est concevable que Jean ait appelé sa mère, qui ait appelé son avocat. It's conceivable that Jean has-sub called his mother, who had-subj called her

[^21][^22]The reason for the contrast between (12)a and (12)b is not hard to find: the subjunctive is always ungrammatical unless it is embedded under operators with a particular semantics - in the case at hand it is conceivable that. This suggests that (12)a is not a case in which the NRR has wide scope syntactically. Furthermore, the truth conditions of the sentence suggest that the NRR really is interpreted within the scope of the existential modal. This can be seen by contrasting the truth conditions of (12)a with those of (12)a'-b': the latter imply that if John had called his mother, she would have called her lawyer; this, in turn, is unsurprising if the mood corresponding to would behaves like an E-type world pronoun, which picks out those (relevant) worlds in which John calls his mother. But no such effect is obtained in (12)a, where the NRR genuinely appears to be interpreted within the scope of the existential modal.

## 3 Patterns of Projection

We will now suggest that the bidimensional fails to account for some non-trivial patterns of projection with NRRs that do not have wide scope. We will sketch in Section 4 a pragmatic account of these patterns, but for the moment we will describe them and show that they are formally analogous to some patterns of presupposition projection.

Let us start by reminding ourselves of patterns of presupposition projection in conjunctions and disjunction. The important point is that in a conjunction the first conjunct must entail (given the shared assumptions of the conversation) the presupposition of the second conjunct. And in disjunctions, a presupposition must be entailed by the negation of the other disjunct.

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(13) Projection in conjunctions

Is it true that John is over 60 and that he knows that he can't apply?
=> If John is over 60, he can't apply
(14) Projection in disjunctions

## a. Canonical Order

John isn't over 60, or he knows that he can't apply. b. Inverse Order

John knows that he can't apply, or he isn't over 60.
$\Rightarrow$ If John is over 60, he can't apply.
Let us turn to supplements. We start by noting that (15) gives rise to a conditional inference that if the President murdered his wife, he will be indicted; one does not have to derive the unconditional (and implausible) inference that the President will in fact be indicted.
(15) Est-il vrai que Sarkozy vient d'assassiner sa femme, et que le Président, qui va être mis en examen, est sur le point de démissionner?
Is is true that Sarkozy has just murdered his wife, and that the President, who will be indicted, is about to resign.
$\neq>$ Sarkozy will be indicted.
$=>$ If Sarkozy murdered his wife, he will be indicted.
The case of disjunctions is similar, except that we obtain a conditional inference that involves the negation of one of the disjuncts - as is the case in presupposition projection.
(16) a. Tu ne vas pas épouser Sam, ou ta mère, qui sera furieuse, te déshéritera.

You will not marry Sam, or your mother, who will be furious, will disown you.
=> If you don't marry Sam, your mother will be furious
b. Est-il vrai que tu ne vas pas épouser Sam, ou que ta mère, qui sera furieuse, te déshéritera?
Is is true that you will not marry Sam, or that your mother, who will be furious, will disown you?
=> If you don't marry Sam, your mother will be furious.
I believe that the same patterns hold when the order of the disjuncts is reversed although the conditional inference is certainly more natural when the NRR appears in the second disjunct. This patterns is also reminiscent of presupposition projection: when the negation of a disjunct is needed to satisfy the presupposition of the other, one tends to prefer the order in which the presupposition trigger appears in the second disjunct.
(17) a. (?) Ta mère, qui sera furieuse, te déshéritera, ou alors tu n'épouseras pas Sam.
Your mother, who will be furious, will disown you, or you will not marry Sam. => If you don't marry Sam, your mother will be furious
b. ?Est-il vrai que tu que ta mère, qui sera furieuse, te déshéritera, ou alors que tu n'épouseras pas Sam?
Is it true that your mother, who will be furious, will disown you, or that you will not marry Sam?
=> If you don't marry Sam, your mother will be furious
We conclude that some supplements do in fact give rise to non-trivial patterns of projection, and that these are formally analogous to presupposition projection.

## 4 Epistemic Status

As was forcefully argued in Potts 2005, there are clear differences between the epistemic status of supplements and that of presuppositions: the latter are normally trivial (i.e. entailed by their local context), while the former usually make a non-trivial contribution, as is suggested by the contrast in (18).
(18) a. Armstrong survived cancer. \#Lance, who survived cancer, won the Tour de France (after Potts 2005)
b. Armstrong survived cancer. Mary knows he did (after Potts 2005)

Still, NRRs should not be too informative, as is suggested by the contrast in (19):
(19) a. Sarkozy, qui est le chef des armées, vient d'assassiner sa femme. Sarkozy, who is the commander in chief, has just murdered his wife. b. (\#)Sarkozy, qui vient d'assassiner sa femme, est le chef des armées. Sarkozy, who has just murdered his wife, is the commander in chief. Ok if the news that S. murdered his wife is already out.
(19)b is rather odd if I am breaking the news that the President has just murdered his wife. The sentence becomes fine if the news is already out - in which case the function of the NRR is to remind the addressee of a fact that is already well-known. By contrast, (19)a could well be used to announce that the President has murdered his wife; the content of the NRR can in this case be taken to be uncontroversial, since the Constitution stipulates that the President is the commander in chief.

A similar contrast is found in cases that involve non-trivial patterns of projection, as was discussed above.
(20) a. Est-il vrai que Sarkozy vient d'assassiner sa femme, et que le Président, qui va être mis en examen, est sur le point de démissionner?
Is it true that Sarkozy just murdered his wife, and that the President, who will be indicted, is about to resign?
=> If the President murdered his wife, he'll be indicted.
b. ?Est-il vrai que Sarkozy est sur le point de démissionner, et que le Président, qui vient d'assassiner sa femme, va être jugé?
Is it true that S. is about to resign and that the President, who has just

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## murdered his wife, will be indicted?

? unless the news is already out that S. murdered his wife.
(20)a gives rise to the inference that if the President murdered his wife, he will be indicted - an uncontroversial claim in normally functioning democracies. If it were acceptable, (20)b would yield the inference that if the President is about to resign, he has murdered his wife - a conditional which is by no means uncontroversial; this, in turn, explains the deviance of the sentence.

So we end up with a dual conclusion:
-Supplements that do not have matrix scope may give rise to patterns of projection that are reminiscent of presuppositions.
-How they have a different epistemic status: supplements generally make a contribution which is neither entirely trivial, nor too controversial.

The generalization can be stated as follows:

## (21) Presuppositions vs. Supplements

a. A presupposition must usually be locally trivial, i.e. it must follow from its local context.
b. A supplement should not be locally trivial. But the minimal revision $\mathrm{C}+$ of the global context C which guarantees that it is trivial should not be too surprising given C . In other words, the assumptions that should be added to C in order to get C+ should be 'weak'.

A bit more specifically, supplements can be handled within a pragmatics that is based on the notions in (22).

## (22) Pragmatics of Supplements

i. $\mathrm{C}+$

In a global context C , define $\mathrm{C}+$ to be the most conservative (weakest) strengthening of C which guarantees that the supplement is locally trivial.

## ii. Felicity

A supplement is felicitous only if $\mathrm{C}+$ is (i) different from C , and (ii) not too surprising given C .

## iii. Update

If Felicity is satisfied, update C to $\mathrm{C}+$.
These assumptions explain why supplements project in the same way as presuppositions: in both cases, the crucial notion is that of being entailed by a local context. At the same time, we also understand why supplements do not have the same epistemic status as presuppositions, since the requirement for supplements is not that they should be entailed by their local context given the global context C , but rather given a modified (strengthened) global context $\mathrm{C}+$. The fact that the latter must neither be equivalent to C nor too surprising given C accounts for the special epistemic status of supplement.

# Natural Logic and Semantics 

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#### Abstract

Two of the main motivations for logic and (model-theoretic) semantics overlap in the sense that both subjects are concerned with representing features of natural language meaning and inference. At the same time, the two subjects have other motivations and so are largely separate enterprises. This paper returns to the topic of language and logic, presenting to semanticists natural logic, the study of logics for reasoning with sentences close to their surface form. My goal is to show that the subject already has some results that natural language semanticists should find interesting. At the same time it leads to problems and perspectives that I hope will interest the community. One leading idea is that the target logics for translations should have a decidable validity problem, ruling out full rst-order logic. I also will present a fairly new result based on the transitivity of comparative adjective phrases that suggests that in addition to 'meaning postulates' in semantics, we will also need to posit 'proof principles'.


If we were to devise a logic of ordinary language
for direct use on sentences as they come,
we would have to complicate our rules of inference
in sundry unilluminating ways.

W. V. O. Quine, Word and Object

## 1 Natural Logic

By natural logic, I mean the study of inference in natural language, done as close as possible to the "surface forms". This work has various flavors and associated projects, and my goal in this talk is to present it to semanticists who know nothing about it. I would like to make the case that natural logic should be of interest in semantics, both the results that we have so far and the problems on the research agenda. I also want to comment at various points on the quote above from Quine, as just one example of an opinion that casts doubt on the whole enterprise of natural logic in first place.

My interest in the topic began in 2005 when I taught an introductory course in semantics for graduate students mainly from our linguistics department, with a few from philosophy and other subjects as well. One motivation for semantics found in textbooks is that it should be the study of inference in language: just
as syntax has grammaticality judgments to account for, semantics has inference judgments. Now I happen to be mainly a logician, and this point resonates with me as a motivation for semantics. But from what I know about the semantics literature, it almost never gives a full account of any inferences whatsoever. It is seriously concerned with truth conditions and figuring out how semantics should work in a general way. But it rarely goes back and figures out, for various fragments, what the overall complete stock of inferences should be. I wanted to do just this, to introduce logic as another study of inference. In particular, I wanted to give examples of completeness theorems that were so elementary that they could be done without the comparatively heavy syntax of first-order logic.

Let me give an example of this, a real "toy." Consider sentences All $X$ are $Y$, where $X$ and $Y$ are plural nouns. This is a very tiny fragment, but there certainly are inferences among sentences in it. For example,

$$
\begin{array}{ll}
\text { All frogs are reptiles. } \\
\text { All reptiles are animals. } &
\end{array} \quad \begin{aligned}
& \text { All sagatricians are maltnomans. } \\
& \hline \text { All frogs are animals. }
\end{aligned}
$$

The inference on the left is valid, of course, and the one on the right is invalid. On the right, I have made up the nouns to hammer home the point that the validity or non-validity is not a matter of the nouns themselves, but rather comes from the form All $X$ are $Y$. For sentences in this fragment, we can give an exact semantics: interpret each noun $X$ as a subset $\llbracket X \rrbracket$ of an underlying universe $M$. This gives models. Given such a model, say $\mathcal{M}$, we say that All $X$ are $Y$ is true in $\mathcal{M}$ if $\llbracket X \rrbracket \subseteq \llbracket Y \rrbracket$. We can go on to define $\Gamma \models S$, for $\Gamma$ a set of sentences and $S$ a sentence, by saying that every model of all sentences in $\Gamma$ is again a model of $S$. We can ask whether this semantics is adequate in the sense that intuitive judgments of valid inferences, presented in English, are matched by formal statements of the form $\Gamma \models S$. For this fragment, the semantics is basically adequate; the main issue with it is that sentences All $X$ are $X$ come out as valid even when the speaker knows or believes that there are no $X$ s. But putting this aside, the semantics is adequate ${ }^{1}$. Further, one can go on and ask for a proof-theoretic characterization of the relation $\Gamma \models S$. Here, it turns out that one can build proof trees using the following rules:

$$
\begin{equation*}
\overline{\text { All } X \text { are } X} \quad \frac{\text { All } X \text { are } Z \quad \text { All } Z \text { are } Y}{\text { All } X \text { are } Y} \tag{1}
\end{equation*}
$$

We write $\Gamma \vdash S$ if there is a tree all of whose nodes are either labeled from $\Gamma$ or else match one of the two rules above, and whose root is labeled by $S$. Then one has the following completeness theorem:

Theorem 1 ([12]). For all $\Gamma$ and $S, \Gamma \models S$ if and only if $\Gamma \vdash S$

[^23]The completeness means that every valid semantic assertion is matched by a formal proof. Nothing is missing. This is not only the simplest completeness theorem in logic, but (returning to the motivations of semantics), it is a full account of the inferential behavior in a fragment. One would think that semanticists would have done this early on.

Then we can ask: given both a semantic account and a proof-theoretic account, why should we prefer the former? Why would we not say that the prooftheory is the semantics? After all, it covers the same facts as the semantic account, and it is an account of language use to boot. In addition, it is amenable to a computational treatment.

My suspicion is that inference as such is not what really drives semanticists. Just as getting the raw facts of grammaticality right is not the driving force for syntacticians, there are other matters at play. At the end of the day, one wants an explanation of how meaning works in language. And one wants a field that leads to interesting questions. Finally, there are all sorts of theory-internal questions that come up, and for semantics, these questions are not so close to the matter of inference.

In any case, I am interested in asking how far one can go with natural logic. A step up from the tiny fragment of all are the classical syllogisms. Here one can return to Aristotle, asking whether his system for all, some, and no (thought of as a formal system) is complete. The completeness of various formulations of syllogistic logic has already been shown, for example by in Łukasiewicz [9] (in work with Słupecki), and the basic completeness result was also rediscovered by Westerståhl [24]. There are also different formulations of what Aristotle was doing, and these lead to different completeness results: see Corcoran [4] and Martin [10].

In between the all fragment and full syllogistic logic, our paper [12] contains a series of completeness theorems: i) the fragment with All $X$ are $Y$; (ii) the fragment with Some $X$ are $Y$; (iii) $=(\mathrm{i})+(\mathrm{ii}) ;(\mathrm{iv})=(\mathrm{iii})+$ sentences involving proper names; $(\mathrm{v})=(\mathrm{i})+$ No $X$ are $Y ;(\mathrm{vi})$ All + Some + No; (vii) $=(\mathrm{vi})+$ proper nouns; (viii) boolean combinations of (vii); (ix) $=(\mathrm{i})+$ There are at least as many $X$ as $Y ;(\mathrm{x})=$ boolean combinations of (ix) + Some $+N o$. In addition, we have a completeness for a system off the main track: (xi) All $X$ which are $Y$ are $Z$; (xii) Most $X$ are $Y$; and (xiii) $=($ ii) + (xii).

Note that the fragments with Most are not expressible in first-order logic. So in this sense, looking at weak fragments gives one more results.

We can go further, in a few ways. First, we can ask about negation on nouns, using set complement as the semantics. Then there is the matter of verbs, and as an initial step here we would look at transitive verbs, using arbitrary relations in the semantics. One could then mix the two enterprises by allowing negation on verbs alone, or on both nouns and verbs. The complete logic of all, transitive verbs, and negation on nouns may be found in Figure 1 below. Third, we could study adjectives in various ways, especially comparative phrases. We shall see some of this work later.

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### 1.1 Objections to natural logic

I want to return to the quote from Quine at the beginning, and to put forth several reasons ${ }^{2}$ why one might agree with it.
A. The logical systems that one would get from looking at inference involving surface sentences would contain many copies of similar-looking rules. Presenting things in this way would miss a lot of generalizations.
B. The systems would contain 'rules' that are not really rules at all, but instead are more like complex deduction patterns that need to be framed as rules only because one lacks the machinery to break them down into more manageable sub-deductions. Moreover, those complex rules would be unilluminating.
C. The systems would lack variables, and thus they would be tedious and inelegant.
D. Turning to the standard topic of quantifier-scope ambiguities, it would be impossible to handle inferences among sentences exhibiting this phenomenon in an elegant way.

My feeling is that all of these objections are to some extent apt, and to some extent miss the mark.

The first two points might be illustrated by the logic in Figure 1, a logic for sentences in the fragment shown. I have used see as a generic transitive verb just to simplify the presentation. I also have used the prime symbol ' for complement. But I intend this as a kind of variable over transitive verbs. We could as well write All $X V$ all $Z$.

Here is an example of the kind of inference which could be captured in the system:

$$
\begin{align*}
& \text { All xenophobics hate all actors } \\
& \text { All yodelers hate all zookeepers } \\
& \text { All non-yodelers hate all non-actors }  \tag{2}\\
& \text { All wardens are xenophobics } \\
& \hline \text { All wardens hate all zookeepers }
\end{align*}
$$

Here is formal derivation corresponding to (2), using the rules in Figure 1:

Figure 1 itself does not list all of the rules; the monotonicity rules are missing. For this fragment, there would be two of them: the first is the transitivity of all noted in (1) and also called Barbara in traditional syllogistics. The second is

$$
\begin{equation*}
\frac{\text { All } X \text { are } U}{} \text { All } U \text { see all } Z \quad \text { All } Y \text { are } Z ~(A l l ~ \text { see all } Y \tag{3}
\end{equation*}
$$

[^24]\[

$$
\begin{gathered}
\frac{\text { All } Y \text { are } Y^{\prime}}{\text { All } Y \text { All } Y^{\prime} \text { are } Y} \text { All } X \text { are } Y \\
\text { One } \\
\frac{\text { All } Y \text { are } X^{\prime}}{\text { All } X \text { are } Y^{\prime}} \text { Antitone } \quad \frac{\text { All } Y \text { are } Y^{\prime}}{\text { All } X \text { see all } Y} \text { Zero-VP } \\
\frac{\text { All } X \text { see all } Y \text { All } X^{\prime} \text { see all } Y}{\text { All } Z \text { see all } Y} \text { LEM } \\
\frac{\text { All } X \text { see all } Y \text { All } X \text { see all } Y^{\prime}}{\text { All } X \text { see all } Z} \text { LEM' } \\
\frac{\text { All } X \text { see all } A \text { All } Y \text { see all } Z \text { All } Y^{\prime} \text { see all } A^{\prime}}{\text { All } X \text { see all } Z} 3 p r
\end{gathered}
$$
\]

Fig. 1. The All syllogistic logic with verbs and noun-level complements, leaving off the rules in (1) and the monotonicity rules All $X^{\downarrow}$ are $Y^{\uparrow}$ and All $X^{\downarrow}$ see all $Y^{\downarrow}$.

This is captured in the notation

$$
\text { All } X^{\downarrow} \text { see all } Y^{\downarrow} \text {. }
$$

It was Johan van Benthem who first used this notation in [2]. (His work, and work influenced by it, is an important source of results and inspirations in the area, but I lack the space to discuss it.) Even more importantly, it was he who first recognized the importance of monotonicity rules for fragments of this form. The similarity of (3) and the Barbara rule from (1) illustrates objection (A): having both rules misses a generalization. At the same time, there is a rejoinder: using the arrow notation, or other "meta-rules", we can say what we want. Nevertheless, for some more complicated systems it is an open issue to present them in the "optimally informative" way. Indeed, it is not even clear what the criteria for such presentations should be.

Objections (A) and (B) are illustrated in the last rule in the figure, and to some extent in the two rules above it. The last rule says, informally, that if all $X$ see all $A$, all $Y$ see all $Z$, and all non- $Y$ see all non- $Z$, then all $X$ see all $Z$ as well. Why is this rule sound? Well, take some $x \in X$. Then if this $x$ is also a $Y$, then it sees all $Z$. Otherwise, $x$ is a non $Y$. But then $x$ sees all non- $A$ 's. And since $x$ was an $X$, it sees all $A$ as well. Thus in this case $x$ sees absolutely everything, a fortiori all $Z$.

This is not a familiar rule, and I could think of no better name for it than (3pr), since it has three premises. It is hard to take this to be a single rule, since it lacks the intuitively obvious status of some of the monotonicity rules. When presented to audiences or classes, hardly anyone believes that it is sound to begin with. Moreover, like the two law of the excluded middle rules, it really depends on the semantics of $X^{\prime}$ giving the full complement; so it might not even be the rule one always wants in the first place. But if one is committed to the semantics, one has to take it as a rule on its own because it cannot be

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simplified any further. In any case, I agree that the rule itself is probably not so illuminating.

Objection (C) is that systems for natural logic lack variables. I must again say that this is my point, and I make it to advance the discussion. It should be of interest in semantics to know exactly where variables really are needed, and to formulate logical systems that do involve variables.

It would take us too far afield in this short report to discuss objection (D). But one could see syllogistic logics capable of handling the different scope readings in ambiguous sentences, and yet do not have much in the syntax besides the disambiguation: Nishihara et al. [15], and Moss [13].

## 2 The Aristotle Boundary

Ian Pratt-Hartmann and I determined in [18] what I'll call the Aristotle boundary. This is the limit of how far one can go with purely syllogistic systems. We need some notation for logical systems taken from the paper.
$\mathcal{S} \quad$ classical syllogistic: all/some/no $X$ are $Y$
$\mathcal{S}^{\dagger} \quad \mathcal{S}$ with negation on nouns: non-X
$\mathcal{R} \quad$ relational syllogistic: add transitive verbs to $\mathcal{S}$
$\mathcal{R}^{\dagger} \quad$ relational syllogistic with noun-negations
$\mathcal{R}^{*} \quad$ relational syllogistic, allowing subject NPs to be relative clauses
$\mathcal{R}^{* \dagger}$ relational syllogistic, again allowing subject NPs to be relative clauses and full noun-negation

In more detail, the syntax of $\mathcal{R}$ is

```
All }X\mathrm{ are Y All }X\mathrm{ aren't }Y\equiv\mathrm{ No }X\mathrm{ are }
Some X are Y Some }X\mathrm{ aren't }
All X see all Y All X don't see all }Y\equivNo X sees any Y
All X see some Y All X don't see some Y \equivNo X sees all Y
Some X see all Y Some X don't see any Y
Some X see some Y Some X don't see some Y
```

$\mathcal{R}^{*}$ allows the subject noun phrases to contain relative clauses of the form

```
who see all X who see some X
who don't see all X who don't see some X
```

Finally, $\mathcal{R}^{* \dagger}$ has full negation on nouns.
Theorem 2 ([18]). There are complete syllogistic systems for $\mathcal{S}$ and $\mathcal{S}^{\dagger}$.
There are no finite, complete syllogistic systems for $\mathcal{R}$. However, allowing reductio ad absurdum, there is a syllogistic system for $\mathcal{R}$.

Even allowing reductio ad absurdum, there are no finite, complete systems for $\mathcal{R}^{\dagger}$ or for $\mathcal{R}^{* \dagger}$.

These results begins to delimit the Aristotle boundary. It has much to do with negation, especially noun negation in connection with verbs.

Despite the negative results at the end of Theorem 2, the systems involved are decidable. This means that in principle one could write a computer program to decide whether a purported inference was valid or not. The complete story here is that the complexity of the validity problem for these logics is known.

Theorem 3 ([18]). The validity problems for $\mathcal{S}, \mathcal{S}^{\dagger}$, and $\mathcal{R}$ are complete for nondeterministic logspace; for $\mathcal{R}^{\dagger}$, it is complete for deterministic exponential time $; \mathcal{R}^{*}$ for co-NPtime [11], and $\mathcal{R}^{* \dagger}$ for nondeterministic exponential time.

Now, one can ask several questions. First, do the complexity results have any cognitive relevance? This seems to me to be a very good question, and it seems completely open. Second, one could ask for the average-case complexity results and to again ask for their cognitive relevance.

My feeling overall is that the Aristotle boundary should be of interest in semantics partly because of the prominence of variables in contemporary semantics. It would be good to pinpoint the features of language that necessitate going beyond a syllogistic presentation. This is what the results in [18] say. However, it should be noted that they do not say that one must use variables in the traditional way, only that one cannot do with a purely syllogistic presentation. In fact, one can also define logical systems for fragments like $\mathcal{R}^{*}$ and $\mathcal{R}^{* \dagger}$ which use something like variables, but with more restrictions. These restrictions correspond to the decidability of the system, a point which I return to in Section 3.

### 2.1 Fitch's "Natural Deduction Rules for English"

I would like to mention Fitch [6] as an early source on natural logic. This paper is not very well-known among people in the area, and I have seen few references to it by semanticists or anyone else for that matter. Frederic Fitch was one of the first people to present natural deduction proofs in what we call 'Fitch style'; Stanisław Jaśkowski also did this. For a good discussion of the history, see Pelletier [17]. Fitch's paper of 1973 presents a set of natural deduction rules for English. Figure 2 contains an example taken directly from his paper.

It should be noted that there is no formal syntax in the paper. His rules for any are thus ad hoc, and certainly there is more that one should say beyond his rules; they do show that he was aware of what we now call polarity phenomena. This lack of syntax is not terribly surprising, since he might not have known of Montague's work. But in addition there is no formal semantics either. From the point of view of natural logic, one can return to Fitch's paper and then ask whether his rules are complete. This question is open.

## 3 The Force of Decidability

I mentioned above that the Aristotle boundary should be of some interest in semantics. I want to end with discussion of the corresponding "Turing boundary". This would be the boundary between decidable and undecidable fragments.


Fig. 2. An example from Fitch [6]

My feeling is that this boundary should be even more important to investigate. Formally-minded linguists should be more used to the rejection of undecidable frameworks following the Peters-Ritchie Theorem in formal language theory. There are certainly some who feel that semantics should make use of the strongest possible logical languages, presumably on the grounds that human beings can understand them anyways. But a wealth of experience stemming from computer science and cognitive science leads in the opposite direction. The feeling is that "everyday" deduction in language is not the same as mathematics, it might not call on the same mental faculty as deep reasoning in the first place. So one should investigate weak systems with an eye towards seeing what exactly can be said in them, before going on to more expressive but undecidable systems.

All of the logical systems mentioned so far in this paper have been decidable, including ones which need variables. (Incidentally, these fragments sometimes do not have the finite model property.) I am interested in finding yet stronger decidable fragments, and so this is how I end this paper. (For other work in the area, see Pratt-Hartmann [19, 19] and Pratt-Hartmann and Third [21].) One source of such stronger systems is comparative adjective phrases, such as bigger than, smaller than, and the like. These are always interpreted by transitive relations on a domain:

$$
\begin{equation*}
\text { If } a \text { is bigger than } b \text {, and } b \text { is bigger than } c \text {, then } a \text { is bigger than } c \text {. } \tag{4}
\end{equation*}
$$

(The interpretations are also irreflexive: nobody is bigger than themselves. But this fact will not be relevant to our point in this section.) The transitivity corresponds to the validity of arguments like the following:

Every sweet fruit is bigger than every kumquat
Every fruit bigger than some sweet fruit is bigger than every kumquat
That is, (5) is semantically valid, but only on the class of models which interpret bigger than by a transitive relation.

Now one might at first thing that what we need is a logical system which directly expresses transitivity using variables in some version of (4). We are
already heading towards the use of variables, so what is the problem with (4)? The hitch is that (4) uses three variables, and it is known that a a logical system which can express all sentences in three variables is undecidable. Even more, a system which can express all of the two-variable sentences plus assertions of transitivity (as atomic sentences) is again undecidable, by a theorem of Grädel, Otto, and Rosen [8]. So if we believe that "simple" fragments of language should lead to decidable logics, then we cannot use a language which states (4) in a "first-class" way. Here is how this is done in [14]. The system uses variables, and also natural-deduction style rules. For transitivity, it uses

$$
\frac{a\left(t_{1}, t_{2}\right) \quad a\left(t_{2}, t_{3}\right)}{a\left(t_{1}, t_{3}\right)} \text { trans }
$$

Here $a$ is an adjective phrase (it will be bigger below), and the t's are terms (variables, roughly). The derivation corresponding to (5) is

In the derivation, sentences like $\forall(\exists($ sw, bigger $), \forall($ kq, bigger $))$ stand for "everything which is bigger than some sweet fruit is bigger than every kumquat." The derivation also uses variables and temporary hypotheses. For example, $\exists($ sw, bigger $)(x)$ corresponds to a proof step like "let $x$ be bigger than some sweet fruit." Even with all of this, the system is decidable. But again, the point I wish to make is that transitivity is a rule, not an axiom. This suggests an issue for semantics: what other constructions work this way?

Transitivity also plays a role in the recent literature on (of all things) avian cognition: see Guillermo Paz-y-Miño C et al [16]. For a different cognitive science connection of monotonicity rules to the modeling of inference (in humans), see Geurts [7].

Note on the references I have included in the references below many more papers than I actually reference in this, as a way of indicating much of what has actually been done in the area. Much of the history appears in van Benthem [3].

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# Dutch from logic (and back) 

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## 1 A Generator

In this paper, we present a non-deterministic procedure to generate Dutch sentences with a predefined, fully specified formal meaning. The procedure is grafted on the Delilah parser and generator (http://www.delilah.eu). The input to the procedure is a formula in Flat Logical Form, a fully specified level of semantic representation ([7]). The formula contains only semantic information. The output is a well-formed Dutch sentence with a full grammatical representation, providing again a formula in Flat Logical Form. The logical relation between the input formula and the output formula can be computed.

The main characteristics of the procedure are:

- the input constraint is not biased towards the syntax or the lexicon;
- the generation procedure is non-deterministic, but finite;
- the result can be logically validated: input and output semantics are formulas in the same language
The paper describes the structure of Delilah's generator and the nature of Flat Logical Form. It specifies a method to relate Flat Logical Form to the lexicon and the (categorial) grammar by extracting semantic networks from it. These networks are shown to be able to steer lexical selection and grammatical unification. Finally, the logic of validating the result is explained and demonstrated.

The Delilah system entertains a generator which is driven by a multimodal combinatory categorial grammar of Dutch, dubbed Minimal Categorial Grammar (MCG) in [3]. Its categorization is rigid in that it does not exploit slash introduction the combinatorial force of Lambek categorial grammars ([5]). The combinatorics of MCG are governed by a limited number of compositional modalities, not unlike the modalities proposed in [6] for Lambek categorial grammars and by [1] for Combinatory Categorial Grammar. The Delilah system applies MCG is also for deep parsing. Both in parsing and in generation, the grammar steers the unification of complex symbols. The unified graph is the main derivational result, apart from a derivational tree (when parsing) and a spell-out of logical forms. An underspecified semantic representation emanates from this unification ([4]).

The generator is hypothesis-driven: it tries to construct a well-formed and meaningful phrase of a given category, with a complete parse in the form of a unified graph representing a complex symbol. The generation procedure is strictly meaning driven
without any structural preconditions, as in [2] and [9]. It proceeds by selecting appropriate phrases from the lexicon after inspecting an agenda and by testing their unification. The agenda is fed by the categories of phrases already selected, und updated after successful unification. The generation succeeds if the hypothesis can be checked, no item is left at the agenda and some non-empty structure has been created.

Basically, the algorithm tries to find templates and to unify them according to an agenda which is set by an initial hypothesis and updated by applying combinatory categorial rules. The agenda consists of two parts: given, corresponding with complex symbols already adopted, and to_find, corresponding to structures still to be checked. A succesful unification of complex symbols according to the agenda is the proper result of the procedure.

## 2 Flat Logical Form

The input to the generation procedure is a formula in Flat Logical Form (FLF). As an example of an FLF formula, see (1),representing elke vrouw probeerde te slapen 'each woman tried to sleep'. Variables are formatted as a quadruple Variable + Monotone + Quantifier + Governors. In this index, Monotone gives a value for upward or downward entailment for that variable with respect to its predicate, Quantifier identifies the binding regime and Governors is a (possibly empty) list of variables the valuation of which co-determines Variable's valuation.

```
state(S+\uparrow+some+[A], woman) &
theme_of(S+\uparrow+some+[A], A+\downarrow+every+[]) &
event(B+\uparrow+some+[A], try) &
property(C+\uparrow+some+[A]) &
event(D+\uparrow+some+[C], sleep) &
experiencer_of(D+\uparrow+some+[C], A+\uparrow+every+[]) &
attime(D+\uparrow+some+[C], E)
agent of (B+\uparrow+some+[A], A+\uparrow+every+[]) &
theme_of(B+\uparrow+some+[A], C+\uparrow+some+[]) &
attime(B+\uparrow+some+[A], F)
&
tense (B+\uparrow+some+[A], past).
```

The classifiers state, event and property normally come with variable arguments produced by context-dependent, but wide-scoped choice functions; this complication is here left out for the ease of explanation. Lexical concepts are arguments of classifiers and are italicized.

FLF is designed for inference. Here is a, yet incomplete, set of inference rules. The predicates are represented as one-place, by schönfinkelization, for ease of exposition. The inference is given in standard predicate logic, for the same reason, but has an evident counterpart in FLF. In that representation, $P \uparrow$ and $P \downarrow$ represent a super- and a sub-predicate to $P$, respectively, according to a model or an ontology where $P \downarrow \leq P \leq P \uparrow$. The valuation of variables that are referentially dependent, is handled by wide- scope choice functions (cf. [8]).
(2) FLF logic

| Premisse | to infer |
| :---: | :---: |
| $\varphi \& P(x+\uparrow+Q+[]) \& \psi$ | Qz.P (z) |
|  | $\exists y \cdot P(y)$ |
|  | $\exists \mathrm{w} . \mathrm{P} \uparrow(\mathrm{w})$ |
| $\varphi$ \& $P\left(x+\uparrow+Q+\left[y_{1} \cdot y_{n}\right]\right) \& \psi$ | $\exists f_{y} \cdot P\left(f_{y}(x)\right)$ |
|  | $\exists f_{y} \cdot P \uparrow\left(f_{y}(x)\right)$ |
| $\varphi \& P(x+\downarrow+n o+[]) \& \psi$ | $\neg \exists \mathrm{z}$. P (z) |
|  | $\neg \exists \mathrm{z} \cdot \mathrm{P} \downarrow(\mathrm{z})$ |
| $\begin{aligned} & \varphi \& P(x+\downarrow+Q+[]) \& \psi \\ & (Q=/=n o) \end{aligned}$ | Qz.P(z) |
|  | QY. P_(y) |
|  | $\exists \mathrm{z} \cdot \mathrm{P}(\mathrm{z})$ |
| $\varphi \& P\left(x+\downarrow+Q+\left[y_{1} \cdot y_{n}\right]\right) \& \psi$ | $\exists f_{y} \cdot P\left(f_{y}(x)\right)$ |

According to this table, the entailment $\mathfrak{J} \Longrightarrow_{\text {eLF }} \mathfrak{R}$ is defined iff both $\mathfrak{J}$ and $\mathfrak{R}$ are in FLF and every clause in $\mathfrak{\Re}$ can be inferred from $\mathfrak{J}$.

Moreover, every FLF can be described as a connected graph, the small clauses being the vertices which are connected when they share a variable.
(3) the semantic graph of (1)


The sets contain clauses that share a variable. The union of these sets defines the lexical space for the generation procedure, to be described in the next section. Each set specifies the constraints on one lexical phrase. An FLF can only be verbalized into one sentence if it is connected in the sense described above and if every small clause (node) has all of its specified variables connected.

## 3 From meaning to form (and back)

The generation procedure is driven by a categorial hypothesis - a hypothesis as to the category of the phrase to be produced. The conceptual agenda strictly limits the freedom of the generator. Every concept is addressed exactly once in a successful generation procedure. Infinite looping is excluded under this simple cancellation agenda.

The procedure sketched above is essentially non-deterministic in at least two senses:

- the (structure of the) FLF is not determining the structure of the sentence;
- the output FLF may not match the input FLF according to a semantic standard.
FLF underdetermines not only its own verbalization - the syntax of sentences realizing that FLF. Because of this 'inverse underspecification', the generation procedure cannot fix all the characteristics of the produced semantics in the logical space in advance or on the fly. There are two reasons for the indeterminacy:
- FLF may itself contain less specifications than any verbalization would introduce;
- FLF cannot predict which logical dependencies between variables are blocked or enhanced by following a certain construction mode for the sentence.
The first aspect of semantic underspecification is evident: one cannot be sure that an FLF contains all the information that a full sentence will produce, as it may originate from other sources than language itself. Real-language complex symbols may introduce additional meanings to those mentioned in the conceptual agenda, e.g. by default specifications like tense on finite verbs. The concepts in the input are a subset of those in the output. Moreover, the input FLF may not specify semantic dependencies that are inherent to sentential construal. The following FLF, for example, gives rise to the generation of sentences meaning Every man invites a woman in a generic reading, but the FLF neither specifies tense nor scope.

The second incongruence between input and output FLF is due to the form-driven nature of sentence meaning. Whether or not a certain operator can scope over another, depends partly, if not mainly, on its syntactic embedding. For example, an operator embedded in a nominal construction has fewer scope options than an operator embedded in a non-nominal, but conceptually equivalent construction. In the same vain, intensional domains are not predictable. Generally, weak and strong islands of any sort are induced by syntax, and the syntax is underspecified, by definition and inevitably. Consequently, the generation procedure cannot be enriched with an additional agenda controlling possible scopal dependencies. Scope can only be checked or compared post hoc.

Since FLF - in fact, every purely semantic logical form - contains too little information to fully determine the generation procedure, generating from logic is a trial, by necessity. The outcome of the process can or must be checked against the input constraint. It is important to realize, however, that the input constraint and the output FLF may differ only in a limited number of ways. For example, the output may contain concepts that are not present in the input, but only if these concepts are introduced by default when applying certain complex symbols and if they passed the restrictions on unification imposed by the semantic networks. The output is far from being in free variation with the input.

As was argued above, it is unwise to check for strict identity or equivalence of input and output FLFs. But the analytical structure of FLF offers several options for a well-defined semantic relation to be imposed. Here are a few, for the InputFLF and OutputFLF:

- InputFLF is a (proper) sub-formula of OutputFLF;
- InputFLF and OutputFLF share a (proper) sub-formula containing predefined key-clauses;
- InputFLF and OutputFLF do not entail each other's denials.

Checking a sub-formula property is simple, given FLF's conjunctivist structure. Moreover, it reflects a relatively liberal attitude towards the notion 'sentence meaning' - possibly too liberal. Though the reciprocal denial test is logically much heavier, but decidable on the basis of logic (2), it is even more liberal: accept the output if is does not run contrary against the input.

Taking into account the considerations given above with respect to the 'inverse underspecification', we would propose that the normal check would be as in

## (4) Accept $S$ with OutputFLF as a translation of InputFLF into Dutch iff OutputFLF entails InputFLF.

Informally, this means that the generated sentence is at least as specific as the input, or that a model for OutputFLF is also a model for InputFLF, but not necessarily the other way around. Again, it must be noted that the conceptual difference between InputFLF and OutputFLF will be very limited, given the restriction of the lexical resources to those induced by the semantic nets of InputFLF.

If a produced sentence cannot comply to (4), the generator can backtrack or start again. Backtracking has the advantage that all grammatical possibilities will show up, with a degree of efficiency that is determined by the structure of the grammar and the lexicon. A disadvantage of backtracking for the generation task may be that success may require quite a few trials if the source of the incongruence is in early choices. Of course, starting again may follow another track, but every control over the trials disappears.

Under both strategies, the proposed generation procedure guarantees definite qualifications of the result. This is a major advantage of meaning-driven generation with a semantic grammar.

## 4 Conclusion

In order to generate natural language from full logic, there needs to be no intrinsic relation between the semantic input constraint and the generating grammatical device. The input constraint only requires its concepts to be retrievable in the lexicon. It does not impose syntactic or morphological requirements; they are induced by the generator. Notwithstanding this flexibility, the correctness or effectiveness of the generation can be computed in a formal way, by exploring the logical relation between the input constraint and the output's logical form. But then, there is always Gauß meeting Wilhelm von Humboldt in the early days of the 19th century, according to Daniel Kehlman's Die Vermessung der Welt; Von Humboldt - a diplomat - starts masochistically.
...Er sei übrigens auch Forscher ! (...) Er untersuche alte Sprache.
Ach so, sagte Gauß.
Das, sagte der Diplomat, habe enttäuscht geklungen.
Sprachwissenschaft. Gauß wiegte den Kopf. Er woll ja keinem zu nahe treten.
Nein, nein. Er solle es ruhig sagen.
Gauß zuckte die Achseln. Das sei etwas für Leute, welche die Pedanterie zur Mathematik hätten, nicht jedoch die Intelligenz. Leute die sich ihre eigene notdürftige Logik erfänden.
Der Diplomat schwieg.

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# Tableaus for Natural Logic 

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#### Abstract

In this paper we develop the beginnings of a tableau system for natural logic, the logic that is present in ordinary language and that us used in ordinary reasoning. The system is based on certain terms of the typed lambda calculus that can go proxy for linguistic forms and which we call Lambda Logical Forms. It is argued that proof-theoretic methods like the present one should complement the more traditional model-theoretic methods used in the computational study of natural language meaning.


## 1 Introduction

A standard approach to the semantics of natural language [17] provides language, or rather fragments of language, with a truth definition by means of translation into the language of some logic (such as Montague's IL) that already comes with one. The truth conditions of a translated sentence will then be identified with those of its translation. This also induces a relation of entailment on the translated fragment, for a sentence $S$ can be taken to entail a sentence $S^{\prime}$ if and only if the translation of the former entails that of the latter.

This provides a way to do automated inference on natural language. In order to check whether a given argument stated in ordinary language holds, its premises and conclusion are translated into logic with the help of some form of the typed lambda calculus, after which a theorem prover is invoked to do the actual testing. This procedure is described in [5] with great clarity and precision.

Here we will follow another route and define a tableau system that directly works on representations that are linguistically relevant. We will also place in focus tableau rules that are connected with certain properties of operators that seem important from a linguistic point of view. Our aim will not so much be to provide a proof system that is complete with respect to the semantics of our representations, but to provide rules that can be argued to come close to the rules implemented in human wetware. The purpose of this paper, therefore, is to contribute to the field of natural logic. ${ }^{1}$

[^25]
## 2 Lambda Logical Forms

For our purpose it will be of help to have representations of natural language expressions that are adequate both from a linguistic and from a logical point of view. At first blush, this may seem problematic, as it may be felt that linguistic and logic require completely different and competing properties from the representations they use, but in fact the typed lambda calculus provides what we need, or at least a good approximation to it. In order to obtain a class of terms with linguistic relevance we will restrict attention to those (simply typed) lambda terms that are built up from variables and non-logical constants, with the help of application and lambda abstraction and will delimit this class further by the restriction that only variables of individual type are abstracted over. The resulting terms, which will be called Lambda Logical Forms (LLFs), are often very close to linguistic expressions, as the following examples illustrate.
(1) a. ((a woman)walk)
b. ((if ((a woman)walk)) ((no man)talk))
c. (mary (think ((if ((a woman)walk)) ((no man)talk))))
d. $((\operatorname{a}$ woman $)(\lambda x(\operatorname{mary}(\operatorname{think}((i f(\operatorname{walk} x))((\operatorname{noman}) t a l k)))))$
e. (few man) $\lambda x$.(most woman) $\lambda y$.like $x y$

The terms in (1) were built up in the usual way, but no logical constants, such as $=, \forall, \exists, \rightarrow, \wedge, \vee, \neg$ and the like, were used in their composition. The next section will make a connection between some of the non-logical constants used in (1) and logical ones, but this connection will take us from natural representations of linguistic expressions to rather artificial ones. Lambda terms containing no logical constants will therefore continue to have a special status.

Lambda Logical Forms come close to the Logical Forms that are studied in generative grammar. For example, in [13] trees such as the one in (2a) are found, strikingly similar to the $\lambda$-term in (2c).
(2) a. $\left[\mathrm{s}[\mathrm{Dp}\right.$ every linguist $]\left[1\left[\mathrm{~S}\right.\right.$ John[Vp offended $\left.\left.\left.\left.t_{1}\right]\right]\right]\right]$
b. ((every linguist) $\left(\lambda x_{1}\left(\right.\right.$ john $\left(\right.$ offend $\left.\left.\left.\left.x_{1}\right)\right)\right)\right)$

## 3 A Natural Logic Tableau System

In this section we will discuss a series of rules for a tableau system directly based on LLFs. While tableau systems usually only have a handful of rules (roughly two for each logical operator under consideration), this system will be an exception. There will be many rules, many of them connected with special classes of expressions. Defining a system that comes even close to adequately describing what goes on in ordinary language will be a task far greater than what can be accomplished in a single paper and we must therefore contend ourselves with giving examples of rules that seem interesting. Further work should lead to less incomplete descriptions. Since the rules we consider typically are connected
to some algebraic property or other (such as monotonicity or anti-additivitysee below), it will also be necessary to specify to which class of expressions each rule applies. Describing exactly, for example, which expressions are monotone increasing in any given language requires a lot of careful linguistic work and for the moment we will be satisfied with providing examples (here: some, some N , every N, many N, and most N).

Familiarity with the method of tableaus will be assumed. Our tableaus will be based upon a (signed variant of) the KE calculus ([6]).

### 3.1 Tableau Entries

We will work with signed tableaus in which entries can have one of the following forms. ${ }^{2}$

- If $A$ is an LLF of type $\langle\vec{\alpha}\rangle$ and $\vec{C}$ is a sequence of constants or LLFs of types $\vec{\alpha}$, then $T \vec{C}: A$ and $F \vec{C}: A$ are tableau entries;
- If $A$ and $B$ are LLFs of type $\langle\vec{\alpha} \vec{\beta}\rangle$ and $\vec{a}$ is a sequence of constants of types $\vec{\beta}$ then $T \vec{a}: A \subset B$ and $F \vec{a}: A \subset B$ are tableau entries.

An entry $T \vec{C}: A(F \vec{C}: A)$ intuitively states that $A \vec{C}$ is true (false), while $T \vec{a}: A \subset B(F \vec{a}: A \subset B)$ states that it is true (false) that $(\lambda \vec{x} \cdot A \vec{x} \vec{a}) \subset(\lambda \vec{x} \cdot A \vec{x} \vec{a})$ (where the $\vec{x}$ are of types $\vec{\alpha}$ ). For example, $T i: \operatorname{man} \subset$ talk states that, as a matter of contingent fact, in world $i$ all men are talking, while $T$ : sparrow $\subset$ bird says that, in all worlds, all sparrows are birds.

### 3.2 Closure Rules

There will be two cases of outright contradiction in which a branch can be closed.


### 3.3 Rules Deriving from the Format

The format we have chosen also validates some rules. First, we are only interested in LLFs up to $\beta \eta$ equivalence and lambda conversions can be performed at will. Second, the $X \vec{C}: A$ format (where $X$ is $T$ or $F$ ) validates the following rules.

$$
\begin{array}{ll}
X \vec{C}: A B & X B \vec{C}: A  \tag{4}\\
\mid \vec{C}: A & X \vec{C}: A B
\end{array}
$$

So we can shift arguments to the front and shift them back again.

[^26]
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### 3.4 The Principle of Bivalence

The KE calculus, which we base ourselves upon, allows for a limited version of the cut rule, called the Principle of Bivalence (PB). It runs as follows.

provided $A$ and all $\vec{C}$ are already in the tableau.

The provision here is essential in order to maintain analyticity of the method. $A$ should be a subterm of a term that already occurs in the tableau and all the $C$ should also already be present (not as subterms).

Splitting a tableau is a very costly step in view of memory resources and if we want to devise a system that comes close to human reasoning (at the moment we are just exploring the logic behind such a system not developing such a system itself) we should start investigating under what conditions the human reasoner in fact takes this step. Here we have opted to let PB be our only tableau-splitting rule, as it is in the calculus KE.

### 3.5 Rules for $\subset$

The following rules seem reasonable for our inclusion statements.

| $T \vec{a}: A \subset B$ | $T \vec{a}: A \subset B$ | $F \vec{a}: A \subset B$ |
| :--- | :---: | :---: |
| $T \vec{a}: B \subset C$ | $T \vec{C} \vec{a}: A$ | $\mid$ |
| $T \vec{a}: A \subset C$ | $T \vec{C} \vec{a}: B$ | $T \vec{b}: A$ |
|  |  | $F \vec{b} \vec{a}: B$ |

While the first two rules in (6) do not introduce any new material, the second does. The witnesses $\vec{b}$ that are introduced here must be fresh to the branch.

### 3.6 Hyponomy Rule

We will suppose that many basic entailments between words ${ }^{3}$ are given in the lexicon and are freely available within the tableau system. This leads to the following rule.
(7) If $A \subset B$ is lexical knowledge:

$$
T \vec{a}: \stackrel{\mid}{A} \subset B
$$

Tableau validity will thus be a notion that is dependent on the set of entailments that are considered lexical knowledge.

[^27]
### 3.7 Boolean Rules

We can now give rules for the operators and, or and not, the first two of which we write between their arguments, much as the rules for $\wedge, \vee$ and $\neg$ would be in a signed variant of the KE calculus. What is different here is that these rules are given for conjunction, disjunction and complementation in all categories, not just the category of sentences.

$$
\begin{gather*}
T \vec{C}: A \text { and } B  \tag{8}\\
\overrightarrow{\mid}: A \\
T \vec{C}: B
\end{gather*}
$$

$F \vec{C}: A$ and $B$
$F \vec{C}: A$ and $B$
$T \vec{C}: A$
$F \vec{C}: B$
$T \vec{C}: B$
$F \vec{C}: A$
(9)

$T \vec{C}: A$ or $B$
$T \vec{C}: A$ or $B$
$F \vec{C}: A$
$F \vec{C}: B$
$T \vec{C}: A$

$$
\begin{gather*}
T \vec{C}: \operatorname{not} A  \tag{10}\\
F \vec{C}: A
\end{gather*}
$$

$$
\begin{gathered}
F \vec{C}: \operatorname{not} A \\
T \vec{C}: A
\end{gathered}
$$

Here is a tableau showing that not (man or woman) entails (not man) and (not woman).


In order to refute the possibility that some object $c$ and some world $i$ satisfy not (man or woman) but do not satisfy (not man) and (not woman) a tableau was developed which starts from the counterexample set

$$
\{T c i: \operatorname{not}(\text { man or woman), } F c i:(\text { not man) and (not woman) }\} .
$$

Since the tableau closes the possibility is indeed refuted.
While and, or and not seem to be operative in all categories, if is sentential. We formulate its rules as follows. Note that sentences still need a parameter (here: $i$ ) since their type is $\langle s\rangle$, not just $\rangle$.

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$$
\begin{gather*}
T i: \text { if } A B  \tag{12}\\
T i: A \\
\text { : } \\
T i: B
\end{gather*}
$$

$F i:$ if $A B$
$T i: A$
$F i: B$

### 3.8 Rules for Monotonic Operators

The rules we have discussed until now were either completely general or operated on specific words (constants), but it has been observed that natural reasoning hinges on properties that attach to certain groups of expressions. Let us write $\subset_{i}$ for the relation that obtains between relations $M$ and $M^{\prime}$ of the same type $\langle\vec{\gamma} s\rangle$ if $(\lambda \vec{x} \cdot M \vec{x} i) \subset\left(\lambda \vec{x} . M^{\prime} \vec{x} i\right)$. A relation $A$ of type $\langle\langle\vec{\alpha} s\rangle \vec{\beta} s\rangle$ is called upward monotone if $\forall X Y \forall i\left(X \subset_{i} Y \rightarrow A X \subset_{i} A Y\right)$ (where $X$ and $Y$ are of type $\langle\vec{\alpha} s\rangle$ ). Examples of upward monotone expressions (already mentioned above) are some, some N , every N , many N , most N (where N varies over expressions of type $\langle e s\rangle$ ), but also Mary. Here is a tableau rule for upward monotone (mon $\uparrow$ ) expressions.
(13) If $A$ is mon $\uparrow$ :

$$
\begin{gathered}
T \vec{C} i: A B \\
T i: B \subset B^{\prime} \\
T \vec{C} i: A B^{\prime}
\end{gathered}
$$

And here is a dual rule for expressions that are downward monotone, i.e. that satisfy the property $\forall X Y \forall i\left(X \subset_{i} Y \rightarrow A Y \subset_{i} A X\right)$. Examples are no, no n, every, few, and few N .
(14) If $A$ is mon $\downarrow$ :

$$
\begin{gathered}
T \vec{C} i: A B \\
T i: B^{\prime} \subset B \\
\mid \vec{C} i: A B^{\prime}
\end{gathered}
$$

Using the second of these rules, the first tableau in Table 1 shows, by way of example, that no bird moved entails no lark flew. ${ }^{4}$

A central theme of [19] is that monotonicity reasoning is at the hart of traditional logic. The second tableau in Table 1 shows the validity of the syllogism known as Disamis.

The crucial step here makes use of the upward monotonicity of some. We have used a rule to the effect that all essentially is $C_{i}$ (where $i$ is the current world) which will be introduced below.

### 3.9 Other Rules Connected to Algebraic Properties

Upward and downward monotonicity are not the only algebraic properties that seem to play a pivotal role in language. There is a literature starting with [23]

[^28]| $T i:$ no bird moved | $T i:$ some AB |
| :---: | :---: |
| $F i:$ no lark flew | $T i:$ all AC |
| $T i:$ flew $\subset$ moved | $F i:$ some CB |
| $T i:$ no bird flew | $T i: \mathrm{A} \subset \mathrm{C}$ |
| $T \mathrm{flew}, i:$ no bird | $T \mathrm{~B} i:$ some A |
| $F \mathrm{flew}, i:$ no lark | $T \mathrm{~B} i:$ some C |
| $T i: l a r k \subset$ bird | $T i:$ some CB |
| $T \mathrm{flew}, i:$ no lark | $\times$ |
| $\times$ |  |

Table 1. Two Tableaus
singling out anti-additivity, as linguistically important. An operator $A$ is antiadditive if it is downward monotone and satisfies the additional property that $\forall X Y((A X \cap A Y) \subset A(X \cup Y))$. Rules for anti-additive operators, examples of which are no-one and without, but also not, are easily given:
(15) If $A$ is anti-additive:

$$
\begin{array}{cc}
F \vec{C}: A\left(B \text { or } B^{\prime}\right) & F \vec{C}: A\left(B \text { or } B^{\prime}\right) \\
T \vec{C}: A B & T \vec{C}: A B^{\prime} \\
F \vec{C}: A B^{\prime} & F \vec{C}: A B
\end{array}
$$

We can continue in this vein, isolating rules connected to semantic properties that have been shown to be linguistically important. For example, [7] mentions splittingness, $\forall X Y(A(X \cup Y) \subset(A X \cup A Y))$, and having meet, $\forall X Y((A X \cap$ $A Y) \subset A(X \cap Y))$, which we can provide with rules as follows.
(16) If $A$ has meet:

$$
\begin{array}{cc}
F \vec{C}: A\left(B \text { and } B^{\prime}\right) & F \vec{C}: A\left(B \text { and } B^{\prime}\right) \\
T \vec{C}: A B & T \vec{C}: A B^{\prime} \\
F \vec{C}: A B^{\prime} & F \vec{C}: A B
\end{array}
$$

(17) If $A$ is splitting:

$$
\begin{gathered}
T \vec{C}: A\left(B \text { or } B^{\prime}\right) \\
F \vec{C}: A B \\
T \vec{C}: A B^{\prime}
\end{gathered}
$$


no $N$ and every $N$ have meet, while some $N$ is splitting.

### 3.10 Getting Rid of Boolean Operators

Many of the rules we have seen thus far allow one to get rid of Boolean operators, even if the operator in question is not the main operator in the LLF under consideration. Here are a few more. If a Boolean is the main connective in the functor of a functor-argument expression it is of course always possible to distribute it over the argument and Booleans can likewise be pulled out of lambda-abstractions.

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$$
\begin{align*}
& X \vec{C}:\left(A \text { and } A^{\prime}\right) B  \tag{18}\\
& X \vec{C}: A B \text { and } A^{\prime} B
\end{align*}
$$

$$
\begin{gathered}
X \vec{C}:(\lambda x . A \text { and } B) \\
X \vec{C}:(\lambda x \cdot A) \text { and }(\lambda x \cdot B)
\end{gathered}
$$

These rules were given for and, but similar rules for or and not are also obviously correct.

Other rules that help removing Booleans from argument positions are derivable from rules that are already present, as the reader may verify. Here are a few.
(19) If $A$ is mon $\uparrow$ :

| $T \vec{C}: A\left(B\right.$ and $\left.B^{\prime}\right)$ | $F \vec{C}: A\left(B\right.$ or $\left.B^{\prime}\right)$ |
| :---: | :---: |
| $T \vec{C}: A B$ | $F \vec{C}: A B$ |
| $T \vec{C}: A B^{\prime}$ | $F \vec{C}: A B^{\prime}$ |

(20) If $A$ is mon $\downarrow$ :

$$
\begin{gathered}
T \vec{C}: A\left(B \text { or } B^{\prime}\right) \\
T \vec{C}: A B \\
T \vec{C}: A B^{\prime}
\end{gathered}
$$

$$
F \vec{C}: A\left(B \text { and } B^{\prime}\right)
$$

$$
F \vec{C}: A B
$$

$$
F \vec{C}: A B^{\prime}
$$

It is clear that not all cases are covered, but the rules allow us to get rid of and and or at least in some cases.

### 3.11 Rules for Determiners

Let us look at rules for determiners, terms of type $\langle\langle e s\rangle\langle e s\rangle s\rangle$. It has often been claimed that determiners in natural language all are conservative, i.e. have the property $\forall X Y(D X Y \equiv D X(X \cap Y))([1])$. Leaving the question whether really all determiners satisfy this property aside, we can establish that for those which do we can use the following tableau rule.
(21) If $D$ is conservative:

$$
\begin{gathered}
X i: D A(A \text { and } B) \\
\quad \stackrel{\mid}{D i}: D A B
\end{gathered}
$$

This again is a rule that removes a Boolean operator from an argument position. Here is another. If determiners $D$ and $D^{\prime}$ are duals (the pair some and every are prime examples), the following rule can be invoked. (We let $\bar{T}=F$ and $\bar{F}=T$.)
(22) If $D$ and $D^{\prime}$ are duals:

$$
\begin{gathered}
X i: D A(\operatorname{not} B) \\
\bar{X} i: D^{\prime} A B
\end{gathered}
$$

The following rule applies to contradictory determiners, such as some and no.
(23) If $D$ and $D^{\prime}$ are contradictories:

$$
\begin{aligned}
X i & : D A B \\
\bar{X} i & \stackrel{\mid}{D^{\prime} A B}
\end{aligned}
$$

There must also be rules for the logical determiners every and some. The first of these determiners is of course closely related to $\subset$ and we obtain the following.

$$
\begin{gather*}
X i: \text { every } A B  \tag{24}\\
X i: A \subset B
\end{gather*}
$$

The second may be given its own rules.

$$
\begin{gather*}
\text { Ti: some } A B  \tag{25}\\
\mid \\
T b i: A \\
T b i: B
\end{gather*}
$$

Fi: some $A B$
$T c i: A$
$\vdots$
$F c i: B$

$$
\begin{aligned}
& X i: \text { some } A B \\
& \\
& X i: \text { some } B A
\end{aligned}
$$

Fci: B

The $b$ in the first rule must again be fresh to the branch. Such taking of witnesses typically leads to undecidability of the calculus and it would be an interesting topic of investigation how the linguistic system avoids the 'bleeding and feeding' loops that can result from the availability of such rules.

### 3.12 Further Rules

In a full paper we will add rules for the modal operators may and must, think and know. We will also consider rules that are connected to comparatives and other expressions.

## 4 Conclusion

One way to describe the semantics of ordinary language is by means of translation into a well-understood logical language. If the logical language comes with a model theory and a proof theory, the translation will then induce these on the fragment of language that is translated as well. A disadvantage of this procedure is that precise translation of expressions, taking heed of all their logical properties, often is difficult. Whole books have been devoted to the semantics of a few related words, but while this often was done with good reason and in some cases has led to enlightening results, describing language word by word hardly seems a good way to make progress. Tableau systems such as the one developed here provide an interesting alternative. They interface with the usual model theory, as developing a tableau can be viewed as a systematic attempt to find a model refuting the argument, but on the other hand they seem to give us a better chance in obtaining large coverage systems approximating natural logic. The format allows us to concentrate on rules that really seem linguistically important and squares well with using representations that are close to the Logical Forms in generative syntax.

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# The Data Complexity of the Syllogistic Fragments of English 

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#### Abstract

The syllogistic fragments of English (syllogistic FOEs) express syllogistic reasoning. We want to know how suitable they would be as front-end languages for ontology-based data access systems (OBDASs), front-ends that have been proposed to rely on controlled fragments of natural language. In particular, we want to know how well syllogistic FOE-based data management tasks for OBDASs scale to data. This, we argue, can be achieved by studying the semantic complexity of the syllogistic FOEs and by considering those computational properties that depend on the size of the data alone.


Keywords: Syllogistic fragments of English, tree-shaped questions, ontologybased data access, semantic and data complexity

## 1 Introduction

A fragment of English (FOE) is any (grammatical) subset of English. Montague, back in the 1970's [9] showed how to define a compositional, formal semantics for a FOE by means of compositional translations $\tau(\cdot)$ that recursively assign to each English syntactic constituent a HO meaning representation (MR), where HO can be conceived of as the extension of FO with the $\lambda$-abstraction, $\lambda$-application, $\beta$-normalization and, eventually, the types of the simply-typed $\lambda$-calculus [9]. Since HO (FO) possesses a formal semantics, embodied by an interpretation function ${ }^{\mathcal{I}}$, we can, modulo $\tau(\cdot)$, apply $\cdot{ }^{\mathcal{I}}$ to FOEs. Such formal semantic analysis gives rise to the notion of semantic complexity, proposed by Pratt in [11], viz., the computational properties of their MRs (which define fragments of FO ) and, a fortiori, the FO reasoning decision problems expressible by such FOEs.

An important family of FOEs are the syllogistic FOEs studied by Pratt and Third in [11]. These FOEs capture common-sense syllogistic reasoning, which was (with Aristotle) the starting point of all research in formal logic. The syllogistic FOEs capture also wide classes of common-sense constraints and, as a result, overlap in expressiveness with well-known knowledge representation formalisms such as conceptual modelling (e.g., ER-diagrams) and ontology (e.g., OWL) languages.

Recently $[3,6,8]$ FOEs (in particulat, controlled FOEs, viz., fragments devoid of structural or semantic ambiguity) have been proposed as front-end (natural) languages for OBDASs. An OBDAS $[13,4]$ is a pair $(\mathcal{O}, \mathcal{D})$, where $\mathcal{O}$ is an ontology (a set of,
ultimately, FO axioms) and $\mathcal{D}$ is a database (DB), meant to specify partially the knowledge we have of a given domain (DBs are FO structures). Scalability in OBDASs can be understood through the data complexity of data management tasks, i.e., though their (computational) complexity measured w.r.t. the size of $\mathcal{D}$ alone, which is crucial insofar as real-world DBs may contain giga or terabytes of data, if not more [4,15]. Modulo $\tau(\cdot)$, the semantic complexity of font-end fragments for OBDASs can impact the performance (the scalability to data) of the back-end data management tasks and routines.

In this paper we study the suitability of the syllogistic FOEs as front-end languages for OBDASs by considering their scalability to data. To understand such scalability we study the data complexity of syllogistic FOE-based data management tasks for OBDASs. We focus on the two main OBDAS management tasks, namely, declaring and accessing information, which can be each represented, accordingly, by a FO decision problem: (i) knowledge base satisfiability and (ii) query evaluation. To infer such data complexity bounds we adopt as main strategy resolution-based saturation decision procedures for fragments of FO as outlined by Joyner in [7].

## 2 The Fragments of English and Tree-Shaped Questions

The syllogistic FOEs are defined incrementally. The idea is to start with a FOE, called COP, that covers: (i) copula ("is"), (ii) verb-phrase negation ("is not"), (ii) the determiners "some", "every" and "no", together with common and proper nouns. The fragment and the translation $\tau(\cdot)$ are defined at the same time, by means of a semantically annotated context-free grammar. Standard HO MRs are used. Thereafter, by extending coverage to a new English construct, viz., transitive verbs (e.g., "likes"), ditransitive verbs (e.g., "gives"), relatives (e.g., "that") and anaphors (e.g., "him"), the other members of the family are defined. See Table 1. For the detailed definition of the fragments, we send the reader to [11]. See Table 2 for their MRs.

The information that we can express/store in such fragments can be queried/accessed by questions. A relevant interrogative FOE is that of tree shaped questions (TSQs), which express some of the most common queries to relational databases (which intersect with SELECT-PROJECT-JOIN SQL queries [1]), while remaining quite natural for speakers. They are built through query words (e.g., "who"), relatives, transitive verbs, copula, common nouns, the determiner "some", the pronoun "somebody", passives (e.g., "is loved by") and conjunction ("and"). See Table 1. For their formal definition we send the reader to [14]. See Table 2 for their MRs.

We intend to understand the computational properties of the syllogistic FOEs in the size of the data. We consider sets $\mathcal{S}$ of quantified and $\mathcal{F}$ of ground sentences. The pair $(\mathcal{S}, \mathcal{F})$ is a KR knowledge base (KB). Notice that, modulo $\tau(\cdot), \mathcal{S}$ maps into ("expresses") and ontology $\mathcal{O}$ and $\mathcal{F}$ into a DB $\mathcal{D}$, and thus a $\mathrm{KB}(\mathcal{S}, \mathcal{F})$ into an OBDAS $(\mathcal{O}, \mathcal{D})$. We study two decision problems. On the one hand, KB satisfiability (Kb-Sat):

- Given: $(\mathcal{S}, \mathcal{F})$.
- Check: is $\tau(\mathcal{S}) \cup \tau(\mathcal{F})$ satisfiable?

And, on the other hand, query answering (KB-QA):

- Given: $(\mathcal{S}, \mathcal{F})$, a question $Q$ and (possibly) a constant $c$.

| COP | Copula, common and proper nouns, negation, <br> universal, existential quantifiers |
| :--- | :--- |
| COP+Rel | COP plus relative pronouns |
| COP+TV | COP plus transitive verbs |
| COP+TV+DTV | COP+TV plus ditransitive verbs |
| COP+Rel+TV | COP+Rel plus transitive verbs |
| COP+Rel+TV+DTV | COP+Rel+TV plus ditransitive verbs |
| COP+Rel+TV+RA | COP+Rel+TV plus anaphoric pronouns (e.g., he, <br> him, it, herself) of bounded scope |
| COP+Rel+TV+GA | COP+Rel+TV plus unbounded anaphoric pronouns |
| COP+Rel+TV+DTV+RA | COP+Rel+TV+DTV plus bounded anaphoric pronouns |

Table 1. Coverage of the FOEs and of TSQs.

- Check: $\operatorname{does} \tau(\mathcal{S}) \cup \tau(\mathcal{F}) \models \tau(Q)\{x \mapsto c\}$ ?
where $\tau(Q)$ is a formula of (possibly) free variable $x$. By analogy to [15], we define the data complexity of Кв-SAT and Кв-QA as their computational complexity when $\mathcal{F}$ is the only input to the problem. The size $\#(\mathcal{F})$ of $\mathcal{F}$ is defined as the number of distinct proper names (or individual constants in $\tau(\mathcal{F})$ ) occurring in $\mathcal{F}$.


## 3 Data Complexity of the FOEs.

Resolution decision procedures. A term $t$ is (i) a variable $x$ or a constant $c$ or (ii) an expression $f\left(t_{1}, \ldots, t_{n}\right)$ where $f$ is a function symbol and $t_{1}, \ldots, t_{n}$ terms. In the latter case, we speak about function terms. A litteral $L$ is a FO atom $P\left(t_{1}, \ldots, t_{n}\right)$. By a clause we understand a disjunction $L_{1} \vee \cdots \vee L_{n} \vee \bar{N}_{n+1} \vee \cdots \vee \bar{N}_{n+m}$ of positive and negative litterals. The empty clause or falsum is denoted $\perp$. By $V(t), V(L)$ and $V(C)$ we denote the sets of variables of, resp., term $t$, litteral $L$ and clause $C$. A term, litteral, clause or set of clauses is said to be ground if it contains no free variables. A substitution $\sigma$ is a function from variables to terms. It is called a renaming when it is a function from variables to variables. Substitutions can be extended to terms and litterals in the standard way. A unifier is a substitution $\sigma$ s.t., given two terms $t$ and $t^{\prime}, t \sigma=t^{\prime} \sigma$. A most general unifier is a unifier $\sigma$ s.t. for every other unifier $\sigma^{\prime}$ there exists a renaming $\sigma^{\prime \prime}$ with $\sigma^{\prime}=\sigma \sigma^{\prime \prime}$.

The depth of a term is defined by $(i) d(x):=d(c):=0$ and (ii) $d\left(f\left(t_{1}, \ldots, t_{n}\right)\right):=$ $\max \left\{d\left(t_{i}\right) \mid i \in[1, n]\right\}+1$. The depth $d(L)$ of a litteral $L$ or $d(\Gamma)$ of set of clauses $\Gamma$ is the maximal depth of their terms. The relative depth of a variable $x$ in a term is defined by $(i) d(x, y):=d(x, c):=0$ and (ii) $d\left(x, f\left(t_{1}, \ldots, t_{n}\right)\right):=\max \left\{d\left(x, t_{i}\right) \mid\right.$ $i \in[1, n]\}+1$. The relative depth $d(x, L)$ of a variable $x$ in a litteral $L$ is its maximal relative depth among $L$ 's terms.

| COP | $\begin{aligned} \varphi_{l}(x) & \rightarrow A(x) \\ \varphi_{r}(x) & \rightarrow \pm \varphi_{l}(x) \end{aligned}$ | $\begin{aligned} & \forall x\left(\varphi_{l}(x) \Rightarrow \pm \varphi_{r}(x)\right) \\ & \exists x\left(\varphi_{l}(x) \wedge \varphi_{r}(x)\right) \end{aligned}$ | No student failed. A student failed. |
| :---: | :---: | :---: | :---: |
| COP+TV | $\begin{aligned} \varphi_{l}(x) & \rightarrow A(x) \\ \varphi_{r}(x) & \rightarrow \pm \varphi_{l}(x) \mid \forall y(A(x) \Rightarrow \pm \psi(x, y)) \\ & \mid \exists y(A(x) \wedge \psi(x, y)) \end{aligned}$ | $\begin{aligned} & \forall x\left(\varphi_{l}(x) \Rightarrow \pm \varphi_{r}(x)\right) \\ & \exists x\left(\varphi_{l}(x) \wedge \varphi_{r}(x)\right) \end{aligned}$ | No student failed. Some student follows every course. |
| COP+TV+DTV | $\begin{aligned} & \varphi_{l}(x) \rightarrow A(x) \\ & \varphi_{t v}(x) \rightarrow \\ & \pm \varphi_{l}(x) \mid \forall y(A(x) \Rightarrow \pm \psi(x, y)) \\ & \mid \exists y(A(x) \wedge \psi(x, y)) \\ & \varphi_{d t v}(x, y) \forall z(A(x) \Rightarrow \pm \chi(x, y, z)) \\ & \mid \exists z(A(x) \wedge \chi(x, y, z)) \\ & \varphi_{r}(x) \rightarrow \varphi_{t v}(x) \mid \forall y\left(A(x) \Rightarrow \pm \varphi_{d t v}(x, y)\right) \\ & \mid \exists y\left(A(x) \wedge \varphi_{d t v}(x, y)\right) \\ & \hline \end{aligned}$ | $\begin{aligned} & \forall x\left(\varphi_{l}(x) \Rightarrow \pm \varphi_{r}(x)\right) \\ & \exists x\left(\varphi_{l}(x) \wedge \varphi_{r}(x)\right) \end{aligned}$ | Every student gives no credit to some student. A student borrowed a book from some library. |
| COP+Rel | $\begin{aligned} & \varphi_{l}(x) \rightarrow A(x) \mid \pm \varphi_{l}(x) \wedge \pm \varphi_{l}(x) \\ & \varphi_{r}(x) \rightarrow \varphi_{l}(x) \end{aligned}$ | $\begin{aligned} & \forall x\left( \pm \varphi_{l}(x) \Rightarrow \pm \varphi_{r}(x)\right) \\ & \exists x\left( \pm \varphi_{l}(x) \wedge \pm \varphi_{r}(x)\right) \end{aligned}$ | Every student who is not dum is smart. |
| COP+TV+Rel | $\begin{aligned} \varphi_{l}(x) & \rightarrow A(x) \\ \varphi_{r}(x) & \rightarrow \pm \varphi_{l}(x) \mid \forall y(A(x) \Rightarrow \pm \psi(x, y)) \\ & \mid \exists y(A(x) \wedge \psi(x, y)) \end{aligned}$ | $\begin{aligned} & \forall x\left(\varphi_{l}(x) \Rightarrow \pm \varphi_{r}(x)\right) \\ & \exists x\left(\varphi_{l}(x) \wedge \varphi_{r}(x)\right) \end{aligned}$ | No student failed. Some student studies every course. |
| COP+Rel+TV+DTV | $\begin{aligned} & \hline \varphi_{l}(x) \rightarrow A(x) \mid \pm \varphi_{r} \wedge \pm \varphi_{r} \\ & \varphi_{t v}(x) \rightarrow \pm \varphi_{l}(x) \mid \forall y(A(x) \Rightarrow \pm \psi(x, y)) \\ & \mid \exists y(A(x) \wedge \psi(x, y)) \\ & \varphi_{d t v}(x, y) \rightarrow \forall z(A(x) \Rightarrow \pm \chi(x, y, z)) \\ & \mid \exists z(A(x) \wedge \chi(x, y, z)) \\ & \varphi_{r}(x) \rightarrow \varphi_{t v}(x) \mid \forall y\left(A(x) \Rightarrow \pm \varphi_{d t v}(x, y)\right) \\ & \mid \exists y\left(A(x) \wedge \varphi_{d t v}(x, y)\right) \\ & \hline \end{aligned}$ | $\begin{aligned} & \forall x\left(\varphi_{l}(x) \Rightarrow \pm \varphi_{r}(x)\right) \\ & \exists x\left(\varphi_{l}(x) \wedge \varphi_{r}(x)\right) \end{aligned}$ | Every helpful student gives some aid to some student. Some diligent student borrowed every book from every library. |
| TSQs | $\begin{aligned} & \varphi(x) \rightarrow A(x)\|\exists y R(x, y)\| \varphi_{1}(x) \wedge \varphi_{2}(x) \\ & \mid \exists y(R(x, y) \wedge \varphi(y)) \end{aligned}$ | $\varphi(x)$ | Which student who attends some course is diligent? |

Table 2. The MRs generated by the FOEs and TSQs. Note that $\psi(x, y)$ (resp. $\chi(x, y, z)$ ) stands for some binary (resp. ternary) atom, while $\pm$ means that a formula may or may not be negated. Complete FOE utterances comply with the pattern Det N VP, and complete (wh-)TSQs with the pattern Intpro N VP or $\operatorname{Int}$ pro $\mathbf{S}_{g}$, where $\mathbf{S}_{g}$ denotes a (subordinate) clause.

We consider the so-called saturation-based version (or format) of the resolution calculus in which we iteratively (monotonically w.r.t. $\subseteq$ ) generate the set of all possible clauses derived from $\Gamma$ using the rules

$$
\operatorname{res} \frac{\Gamma, C \vee \bar{L} \quad \Gamma, C \vee L^{\prime}}{\left(C \vee C^{\prime}\right) \sigma} \text { fact } \frac{\Gamma, C \vee L \vee L^{\prime}}{(C \vee L) \sigma}
$$

where $\sigma$ is a most general unifier (of $L$ and $L^{\prime}$ in this case), until either (i) $\perp$ is derived or (ii) all possible clauses are generated (fixpoint computation). Formally, consider a function $\rho(\cdot)$ over sets of clauses, defined in terms of res amd fact. A resolution calculus is a function $\mathcal{R}(\cdot)$ s.t. $\mathcal{R}(\Gamma):=\Gamma \cup \rho(\Gamma)$. A derivation $\delta$ from $\Gamma$ is defined by putting (i) $\mathcal{R}^{0}(\Gamma):=\Gamma$ and $\mathcal{R}^{i+1}(\Gamma):=\mathcal{R}\left(\mathcal{R}^{i}(\Gamma)\right)$, for $i>0$. Thereafter the saturation of $\Gamma$ is defined as $\Gamma^{\infty}:=\bigcup\left\{\mathcal{R}^{i}(\Gamma) \mid i \geq 0\right\}$. The positive integer $i$ is called the depth or rank of $\delta$. The set(s) of clauses derived at each rank $i \geq 0$ of $\delta$ is (are) called the state(s) of $\delta$. The size of $\delta$ is defined as its total number of states. Resolution is sound and complete w.r.t. (un)satisfiability: $\Gamma$ is unsatisfiable iff $\perp \in \Gamma^{\infty}$. Moreover, if $\Gamma$ is satisfiable, we can build out of $\Gamma^{\infty}$ a Herbrand model of $\Gamma$ [5].

Resolution saturations are not in general computable (they may not converge finitely). However, Joyner in [7] showed that finite convergence can be achieved provided that two conditions are met: ( $i$ ) that the depth of litterals does not grow beyong a certain bound $d \geq 0$ and (ii) that the length of clauses (the number of disjunctions) does not grow beyond a bound $l \geq 0$. Several refinements can be used to ensure the existence of such bounds and a fortiori finite convergence for several fragments of FO.

To control depth, acceptable orderings (A-orderings), that is, well-founded and substitution-invariant partial orders on clause litterals and sets thereof, can be used (which force resolution on litterals that are maximal w.r.t. the ordering). The best known is the $\prec_{d}$ ordering defined by

$$
L \prec \prec_{d} L^{\prime} \text { iff } d(L)<d\left(L^{\prime}\right), V(L) \subseteq V\left(L^{\prime}\right) \text { and, for all } x \in V(L), d(x, L)<d(x, L),
$$

a refinement sound and complete w.r.t. satisfiability. To control length the splitting rule

$$
\left.\begin{array}{ccc} 
& \Gamma, C \vee L & \Gamma, C \vee L^{\prime} \\
& \vdots & \vdots \\
\text { split } \frac{\Gamma, C \vee L \vee L^{\prime}}{} & C^{\prime} \sigma & C^{\prime} \sigma \\
C^{\prime} \sigma & &
\end{array}(L) \cap V\left(L^{\prime}\right)=\emptyset\right)
$$

can be used (it is sound and complete w.r.t. satisfiability). These refinements are guaranteed to work the way we want them to in case they are applied to covering clauses. A litteral $L$ is said to be covering whenever $(i) d(L)=0$ or (ii) for every functional term $t$ in $L, V(t)=V(L)$. If all the litterals of a clause $C$ are covering, so is $C$. This property is not, however, closed under resolution or its refinements: applying them to covering clauses may result in non-covering clauses. To prevent this from happening, a further refinement is required: monadization [7]. Intuitively, what this does is to reduce the (un)satisfiability of non-covering clauses, satisfying some structural properties, into that of a set of covering clauses. The applicability of the refinements thus depends on
the FO fragments such clauses are drawn from, but, whenever all are applicable, saturations finitely converge [5].

The different systems arising from the different combinations of rules, orderings and refinements are summarized by Table 3. Note that saturations exhibit the shape of a tree (of branching factor 2 ) or of a sequence, depending on whether the calculi make use or not of the splitting rule.

In particular, the $\mathcal{R}_{2,5}$ calculus of Table 3 decides the $\mathcal{S}^{+}$class of clauses [5]. The class $\mathcal{S}^{+}$is the class where every clause $C$ satisfies: (i) $V(C)=V(t)$, for every functional term $t$ in $C$, and (ii) either $L$ has at most one variable or $V(L)=V(C)$, for every litteral $L$ in $C$.

Data Complexity of KB-QA and KB-SAT. In this section we study the data complexity of Кв-SAT and Кв-QA by applying resolution decision procedures to the syllogistic FOEs. We apply data complexity arguments to sets $\Sigma \cup \Delta$ of non-ground and ground clauses. This makes sense, because, modulo $\tau(\cdot)$ and clausification, FOE constraints $\mathcal{S}$ map to sets $\Sigma$ of non-ground clauses, FOE facts $\mathcal{F}$ map to sets $\Delta$ of ground clauses, and, in general, $\mathrm{KBs}(\mathcal{S}, \mathcal{F})$ to sets $\Sigma \cup \Delta$ of clauses.

We do as follows. For the tractable FOEs we rely on the "separation" property of resolution saturations [5] (resolution of ground clauses can be delayed to the end). For the intractable, on the "monadic reducibility" property shown by Pratt and Third in [11] that enforces a reduction to $\mathcal{S}^{+}$clauses for the fragments involved; this we combine with a data complexity of the $\mathcal{S}^{+}$class (and saturations).

- Separation: $\perp \in(\Sigma \cup \Delta)^{\infty}$ iff there exists a set $\Sigma^{\prime} \subseteq \Sigma^{\infty}$ s.t. (i) $d\left(\Sigma^{\prime}\right) \leq d(\Delta)$, (ii) $\perp \in\left(\Sigma^{\prime} \cup \Delta\right)^{\infty}$ and (iii) $\Sigma^{\prime}$ is finite.
- Monadic reducibility: every set $\Gamma$ of COP+TV+DTV+Rel clausified MRs (or any fragment thereof). can be polynomially (in the size of $\Gamma$ ) transformed into a set $\Gamma_{u}$ of unary clauses s.t. $\Gamma$ is satisfiable iff $\Gamma_{u}$ is satisfiable.

Lemma 1. Let ( $\mathbf{C}, \mathbf{F}, \mathbf{R}$ ) be a finite FO signature, where $\mathbf{C}$ is a (finite) set of constants, $\mathbf{F} a$ (finite) set of function symbols and $\mathbf{R} a$ (finite) set of predicate symbols. Consider a clause set $\Gamma$ over such signature and suppose that there exist both a term depth bound $d \geq 0$ and a clause length bound $k \geq 0$. Then

1. the number of clauses derivable by the saturation is (worst-case)
(a) exponential in the number of constants in $\mathbf{C}$ if we use the splitting rule or
(b) polynomial in the number of constants in $\mathbf{C}$ otherwise, and
2. the depth of the saturation is (worst-case) polynomial in in the number of constants in $\mathbf{C}$.

Proof. Assume that a depth bound $d$ and a length bound $l$ exist. Let $c$ be the number of constant symbols in $\mathbf{C}, v$ the number of variables in $\mathbf{V}, f$ the number of function symbols in $\mathbf{F}$, $p$ the number of predicate symbols in $\mathbf{R}, a r_{f}$ the maximum arity of the function symbols, and $a r_{p}$ the maximum arity of the predicate symbols. We can define


Table 3. Resolution calculi.
the number $t e_{i}$ of terms of depth $i \geq 0$ inductively by setting (i) te $e_{0}:=v+c$, (ii) $t e_{i+1}:=f \cdot t e_{n}^{a r_{f}}$. Thus, the number te of terms of depth $\leq d$ is

$$
\begin{equation*}
t e \leq \sum_{i=0}^{d} t e_{i}=f^{0} \cdot(v+c)^{a r_{f}^{0}}+\ldots+f^{d} \cdot(v+c)^{a r_{f}^{d}}:=\mathrm{p}_{\mathrm{te}}(c) \tag{1}
\end{equation*}
$$

which defines a polynomial $\mathrm{p}_{\mathrm{te}}(c)$. This in its turn yields as upper bound to the number $l i$ of positive and negative literals

$$
\begin{equation*}
l i \leq 2 \cdot p \cdot t e^{a r_{p}}=2 \cdot p \cdot \mathrm{p}_{\mathrm{te}}(c)^{a r_{p}}:=\mathrm{p}_{\mathrm{li}}(c) \tag{2}
\end{equation*}
$$

thus defining a polynomial $\mathrm{p}_{1 \mathrm{i}}(c)$. Finally, from $l i$ we derive an upper bound to the number $c l$ of clauses of length $\leq l$

$$
\begin{equation*}
c l \leq l l^{l}=\mathrm{p}_{1 \mathrm{i}}(c)^{l}:=\mathrm{p}_{\mathrm{cl}}(c) \tag{3}
\end{equation*}
$$

which again defines a polynomial $\mathrm{p}_{\mathrm{cl}}(c)$. The splitting rule splits saturations into two, yielding a (saturation) tree of worst-case size $\leq 2^{\mathrm{p}_{\mathrm{cl}}(c)}$, largest (derived) state of size $\leq \mathrm{p}_{\mathrm{cl}}(c)$ and that will converge after $\leq \mathrm{p}_{\mathrm{cl}}(c)$ iterations.

Theorem 1. Kb-Sat is in NP in data complexity for $\mathcal{S}^{+}$.
Proof. Let $\Sigma \cup \Delta$ be a set of $\mathcal{S}^{+}$clauses. Consider now a $\mathcal{R}_{2,5}$-saturation. Calculus $\mathcal{R}_{2,5}$ decides $\mathcal{S}^{+}$and saturations finitely converge. Assume w.l.o.g. that $\Sigma$ contains no constants and that $\Delta$ is of depth $d(\Delta)=0$ and has $c$ distinct constants (where $c \geq 0$ ). By Lemma 1 we know that the saturation will be tree-shaped, of rank $\leq \mathrm{p}(c)$, of size $\leq 2^{\mathrm{p}(c)}$ and of maximal state of size $\leq \mathrm{p}(c)$.

Outline a non-deterministic algorithm for Kb-Sat as follows. Start with $\Sigma \cup \Delta$. For each rank $i \in[0, \mathrm{p}(c)]$ of the saturation, guess/choose a state $j \in\left[0,2^{i}\right]$. Notice that the algorithm will make polynomially many choices on $c$. Finally, check, in time polynomial in $c$ whether $\perp$ is in the resulting state, and, if no, compute, in time polynomial in $c$, a Herbrand model of $\Sigma \cup \Delta$.

Theorem 2 (Kb-SAT). The data complexity for Kb-SAT is
in LSpace for $C O P, C O P+T V$ and $C O P+T V+D T V$,
2. in $\mathbf{N P}$ for $C O P+$ Rel, and
3. NP-complete for $C O P+$ Rel $+T V, C O P+$ Rel $+T V$ and $C O P+R e l+T V+D T V$.

|  | TSQs | Fragment |
| :---: | :--- | :--- |
| COP | in LSpace [Th 3] | in LSpace [Th 2] |
| COP+TV | in PTime [Th 3] | in LSpace [Th 2] |
| COP+TV+DTV | in coNP | in LSpace [Th 3] |
| COP+Rel | coNP-complete [10] | in NP [Th 2] |
| COP+Rel+TV | coNP-complete [10] | NP-complete [10] |
| COP+Rel+DTV | coNP-complete [Th 3] | $\mathbf{N P}$-complete [Th 3] |
| COP+Rel+DTV+TV | coNP-complete [Th 3] | NP-complete [Th 3] |


|  | Atomic question | Fragment |
| :---: | :---: | :--- |
| COP+Rel+TV+GA | undecidable [Th 4] | undecidable [11] |
| COP+Rel+DTV+TV+RA | undecidable [Th 4] | undecidable [11] |
| COP+Rel+DTV+TV+GA | undecidable [Th 4] | undecidable [11] |


|  | TSQs+RA | Fragment |
| :--- | :--- | :--- |
| COP+Rel+TV+RA | undecidable [Th 4] | NP-complete [Th 3] |

Table 4. Data complexity of Kb-QA and Kb-SAt (a.k.a. fragment complexity) for the syllogistic FOEs and TSQs.

Proof. (Sketch.) For the fragments COP, COP+TV and COP+TV+DTV we reason as follows. Let $(\mathcal{S}, \mathcal{F})$ be a KB and consider its MRs $\tau(\mathcal{S})$ and $\tau(\mathcal{F})$ (which can be computed in space logarithmic in $\#(\mathcal{F})$ ). Computing their skolemization and clausification does not affect data complexity, since it is the identity for $\tau(\mathcal{F})$. By inspecting the resulting clauses we can observe that they are covering: using A-ordered resolution prevents clauses from growing beyond a certain depth bound $d$. Furthermore, it can be proven that applying res and fact, does not increase clause length beyond a certain bound $l$, nor does it result in non-covering clauses. Therefore, the A-ordered resolution calculi without splitting from Table 3 decide the satisfiability of $\tau(\mathcal{S}) \cup \tau(\mathcal{F})$. In addition, we know by the "separation" property that we can "separate" data from facts provided $\tau(\mathcal{S})$ is satisfiable.

Sketch a decision algorithm for Kb-Sat as follows. Check whether $\tau(\mathcal{S})$ is satisfiable, i.e., whether $\perp \in \tau(\mathcal{S})^{\infty}$, computation that does not depend on $\#(\mathcal{F})$ (or $\#(\tau(\mathcal{F}))$ ). If the answer is negative, return "no". If the answer is positive: (i) Compute the finite model $\mathcal{D}$ of $\tau(\mathcal{F})$ (i.e., the Herbrand model defined from $\tau(\mathcal{F})$ ). (ii) Compute the FO formula $\varphi_{\mathcal{S}}:=\bigwedge\left\{C \mid C\right.$ clause of $\left.\tau(\mathcal{S})^{\infty}\right\}$. Then,

$$
\tau(\mathcal{S}) \cup \tau(\mathcal{F}) \text { is satisfiable iff } \mathcal{D} \models \varphi_{\mathcal{S}}
$$

which outlines a reduction to relational database query answering, known to be in LSpace (actually, in $\mathrm{AC}^{0}$ ) [1]. Membership in LSpace follows.

Membership in NP for COP+Rel, COP+Rel+TV and COP+Rel+TV+DTV is derived as follows. Consider a $\mathrm{KB}(\mathcal{S}, \mathcal{F})$. Consider now the resulting MRs, $\tau(\mathcal{S})$ and $\tau(\mathcal{F})$. Clausifying such MRs can be done in time constant in $\#(\tau(\mathcal{F}))$. By Pratt and Third's "monadic reducibility" property, we know that we can reduce, in time poly-
nomial in $\#(\tau(\mathcal{F}))$ their satisfiability to that of a set $\tau(\mathcal{S})_{u} \cup \tau(\mathcal{F})_{u}$ of monadic clauses. By inspection, we can, moreover, observe that such classes belong to the $\mathcal{S}^{+}$ class. We can now apply Lemma 1, whence it follows that Kb-Sat is in NP. For COP+Rel+TV+RA we observe that the "monadic reducibility" property still holds for restricted anaphoric pronouns [11], wherein we impose pronouns like "him" to co-refer with their closest antecedent noun phrase within, moreover, a single utterance (and not beyond).

Finally, NP-hardness for COP+Rel+TV and COP+Rel+TV+DTV can be inferred by a reduction from the NP-complete satisfiability problem for $2+2$ clauses [12]. A $2+2$ clause is a clause $L_{1} \vee L_{2} \vee \bar{L}_{3} \vee \bar{L}_{4}$ containing two positive litterals and two negative litterals.

Theorem 3 (Kb-Qa). If we consider TSQs, then the data complexity of Kb-QA is

1. in LSpace for COP,
2. in PTime for $C O P+T V$,
3. in coNP for $C O P+T V+D T V$, and
4. coNP-complete for $\mathrm{COP}+$ Rel, $\mathrm{COP}+$ Rel $+T V$ and $\mathrm{COP}+$ Rel $+T V+D T V$.

Proof. (Sketch.) Kb-QA for COP is in LSpace in data complexity, because it can be shown that its MRs are contained by the description logic DL-Lite, for which such result holds [2]. Similarly, it can be shown that COP+TV Kb-QA reduces to Datalog Kb-QA. Furthemore, given a $\mathrm{COP}+\mathrm{TV} \mathrm{KB}(\mathcal{S}, \mathcal{F})$ and a TSQ $Q$, such reduction proceeds in space logarithmic in $\#(\mathcal{F})$. It thus preserves data complexity. Since Datalog Kb-QA is in PTime, the result follows.

The coNP upper bound for COP + Rel and COP + Rel+TV follows from the coNPcompleteness for data complexity of $\mathrm{KB}-\mathrm{QA}$ for the two-variable fragment of FO [10]. Regarding COP+TV+DTV and COP+Rel+TV+DTV, we observe that: (i) TSQs can be expressed quite easily by COP + Rel+TV+DTV, by extending this FOE with grammar rules accounting for wh- and $\mathrm{y} / \mathrm{n}$-questions. (ii) $\mathrm{COP}+\mathrm{Rel}+\mathrm{TV}+\mathrm{DTV}$ is closed under negation. We can thus reduce Kb-QA (again, by a reduction space logarithmic in the size of the data) to COKB-QA (i.e., the complement of Kb-SAT) and apply Theorem 2.

Finally, coNP-hardness derives from the fact that we can again reduce the satisfiability of $2+2$ clauses to $\mathrm{COP}+\mathrm{Rel}$ CoKb-QA (i.e., the complement of Kb-QA). This lower bound then propagates to $\mathrm{COP}+\mathrm{Rel}+\mathrm{TV}$ and $\mathrm{COP}+\mathrm{Rel}+\mathrm{TV}$.

## Theorem 4. Kb-Qa is undecidable

> 1. for $C O P+$ Rel $+T V+R A$ with $T S Q s+R A$, and
> 2. for $C O P+$ Rel $+T V+G A$ and $C O P+R e l+T V+D T V+R A$ with atomic questions.

Proof. (Sketch.) We can define a reduction from the unbounded tiling problem, known to be undecidable, to KB-QA for COP+Rel+TV+RA with indeterminate pronouns (e.g., "Anybody who does not love somebody, hates him.") and TSQs+RA, i.e., TSQs where anaphoric pronouns have been added to the fragment (e.g., "Does some man like somebody who hates him?").

For COP+Rel+TV+GA and COP+Rel+TV+DTV+RA the result follows by reduction from unsatisfiability and by the fact that, as it was shown in [11], SAT is undecidable for these fragments. The reduction requires atomic $y / n$-questions (e.g. "Is Socrates a philosopher?").

## 4 Conclusions

We have studied the data complexity of Pratt's syllogistic FOEs w.r.t. Kb-Sat (viz., KB satisfiability) and Kb-QA (viz., answering TSQs over KBs). In so doing, we have assessed their scalability as front-end languages for OBDASs, in particular w.r.t. data and constraint declaration and querying, which the aforementioned decision problems formalize. Our results show that the data complexity of the non-recursive fragments, COP, COP+TV and COP+TV+DTV, are grosso modo, tractable (the upper bound for KB-Qa for COP+TV+DTV is not tight and could be improved), and that data complexity is grosso modo, intractable, when relatives are added (the upper bound for Kb-SAT for $\mathrm{COP}+\mathrm{Rel}$ is not tight either). Adding anaphoric pronouns either to the syllogistic FOEs alone or in combination with TSQs results, in general, in undecidability.

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# Extending Syllogistic Reasoning 

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#### Abstract

In this paper syllogistic logic is extended first to propositional logic, and then an interesting fragment of predicate logic that includes relations.


## 1 Introduction

Traditional logic, also known as term logic, is a loose term for the logical tradition that originated with Aristotle and survived until the advent of modern predicate logic in the late nineteenth century. Modern logicians used quite a number of arguments as to why traditional logic should be abandonded. First and foremost, the complaint is that traditional logic is not rich enough to account for mathematical reasoning, or to give a serious semantics of natural language. It is only a small fragment of predicate logic, which doesn't say anything about propositional logic, or multiple quantification. Russell (1900) blamed the traditional logical idea that every sentence is of subject-predicate form for giving sentences misleading logical forms. Due to the development of Montague grammar and especially Generalized Quantifier Theory in the 1960s-1980s the misleading form thesis of early proponents of modern logic is not a mainstream position anymore, and analyzing sentences in subject-predicate form is completely accepted again.

In this paper I will first quickly discuss traditional Aristotelian syllogistics, and how to extend it (also semantically) with negative and singular terms. Afterwards I will discuss how propositional logic can be seen as an extension of Aristotelian syllogistics. Thus, in distinction with polish logicians like Lukasiewicz and others, I won't assume that to understand traditional logic we have to presuppose propositional logic, but instead formulate propositional logic by presupposing syllogistic reasoning. Afterwards I will follow (the main ideas, though not the details of) Sommers (1982) and his followers
in showing how traditional logic can be extended so as to even account for inferences involving multiple quantification that almost all modern textbooks claim is beyond the reach of traditional logic: A woman is loved by every man, thus Every man loves a woman.

## 2 From syllogistics to propositional logic

Syllogisms are arguments in which a categorical sentence is derived as conclusion from two categorical sentences as premisses. As is wellknown, a categorical sentence is always of one of four kinds: $a$-type ('All men are mortal'), $i$-type ('Some men are philosophers'), $e$-type ('No philosophers are rich'), or o-type ('Some men are not philosophers'). A rather standard proof theory SYL for syllogistic reasoning with negative terms (if $P$ is a term, $\bar{P}$ is a term as well) which only makes use of $a$ and $i$ propositions can make use of the fact whether a term occurs distributively, or monotone decreasingly/negatively within a sentence, or not. Denoting a distributed term by - and an undistributed term by + , the following follows at once: $S^{-} a P^{+}$, $S^{+} i P^{+}, S^{-} e P^{-}$, and $S^{+} o P^{-}$, which we might think of now as a syntactic characterisation. The proof system then consists of the following set of axioms and rules (with sentence-negation ' $\neg$ ' defined as follows: $\neg(S a P) \stackrel{\text { def }}{=} S o P, \neg(S i P) \stackrel{\text { def }}{=} S e P, \neg(S e P) \stackrel{\text { def }}{=} S i P$, and $\neg(S o P) \stackrel{\text { def }}{=} S a P)$ :
(1) $M a P, \Gamma(M)^{+} \vdash \Gamma(P) \quad$ Dictum de Omni, where $\Gamma(M)^{+}$is a sentence where $M$ occurs undistributed.
(2) $\vdash \operatorname{TaT} \quad$ Law of identity
(3) $\vdash T \equiv \overline{\bar{T}}^{1} \quad$ Double negation
(4) $S a \bar{P} \vdash P a \bar{S} \quad$ Contraposition
(5) $\Gamma, \neg \phi \vdash \psi, \neg \psi \quad \Rightarrow \quad \Gamma \vdash \phi \quad$ Reductio per impossible ${ }^{2}$
(f) $\vdash \neg(T a \bar{T}) \quad$ (i.e. $\vdash T i T) \quad$ Existential Import

We will now slightly extend syllogistic reasoning in some seemingly innocent ways. First, we add a distinguished 'transcendental' term ' $T$ ' to our language, standing for something like 'entity'. Obviously,

[^29]the sentence $S a \top$ should always come out true for each term $S$. To reflect this, we will add this sentence as an axiom to SYL. But adding $T$ as an arbitrary term to our language gives rise to a complication once we accept existential import for all terms, including negative ones: for negative term $\bar{T}$ existential import is unacceptable. One way to get rid of this problem is to restrict existential import to positive categorical terms only. Next, we add singular, or individual terms to our language. In contrast to in standard predicate logic, we will not assume that there is a type-difference between individual terms and standard predicates. Following Leibniz (1966b) and Sommers (1982), we will assume, instead, that for singular propositions, $a$ and $i$ propositions coincide, just like $e$ and $o$ propositions. Thus, 'Plato sleeps' is represented by a sentence like ' $P a S$ ', which is equivalent with ' PiS '. Finally, we will add a rule (due to Sherperdson, 1956) saying what to do with empty terms. We will denote the system consisting of $(1),(2),(3),(4),(5)$ together with the following four rules by $\mathbf{S Y L}^{+}$.
(6) $\vdash \neg(T a \bar{T})$, for all positive categorical terms $T$
(7) $\vdash S a \top$
(8) for all singular terms $I$ and terms $P: I i P \dashv \vdash I a P$.
(9) $\bar{S} a S \vdash \bar{S} a P$ (for any $P$ )

To think of propositional logic in syllogistic terms, we will allow for 0 -ary predicates as well. We will assume that if $S$ and $P$ are terms of the same arity, $S a P, S i P$ etc. are formulas of arity 0 . Moreover, if $S$ and $P$ are 1-ary predicates, and $\phi$ a 0 -ary predicate, something like $(S i \bar{P}) a \phi$ will be 0 -ary predicates as well. Starting with a non-empty domain $D$, we will (extensionally) interpret $n$-ary terms as subsets of $D^{n}$ (thus $D^{0}=\{\langle \rangle\}$ ). If $S$ and $P$ are 0-ary or 1-ary terms, the categorical sentences are interpreted as follows: $V_{M}(S a P)=\left\{\langle \rangle: V_{M}(S) \subseteq V_{M}(P)\right\}, V_{M}(S i P)=\left\{\langle \rangle: V_{M}(S) \cap\right.$ $\left.V_{M}(P) \neq \emptyset\right\}$, and the $e$ and $o$-propositions as negations of them. It is easy to see that all types of complex propositional formulas can be expressed in categorical terms $\left([\phi] a[\psi] \equiv{ }^{'} \phi \rightarrow \psi^{\prime},[\phi] i[\psi] \equiv ' \phi \wedge \psi\right.$, $[\phi] e[\phi] \equiv{ }^{\prime} \neg \phi '$, and $\left.[[\phi] e[\phi]] a[\psi] \equiv ' \phi \vee \psi^{\prime}\right)$, and receive the correct interpretation.

Let us see now how things work from a proof-theoretic point of view. To implement the above suggestions, we will add to $\mathbf{S Y L}^{+}$ the following three ideas: (i) 0 -ary terms don't allow for existential import, (ii) $T^{0}$ is a singular term, and (iii) $P^{0}$ is equal to $T^{0} i P^{0}$. The first idea is implemented with the help of axiom (6) by stipulating that 0 -ary terms are not categorical.
(10) 0 -ary terms are no categorical and $\top^{0}$ is a singular term.
(11) $P^{0} \dashv \vdash \top^{0} i P^{0}$.

We will denote the system $\mathbf{S Y L}^{+}$together with (10) and (11) by $\mathbf{S Y L}{ }^{+} \mathbf{P L}$. The claim of this section of the paper is that this system can indeed account for all inferences in proposotional logic. It is almost immediately clear that Modus Ponens, Modus Tollens, the Hypothetical Syllogism, and the Disjunctive Syllogism can be thought of as ordinary valid syllogisms of the form Barbara, Camestres, Barbara, and Camestres, respectively. Also other 'monotonicity-inferences' follow immediately from the Dictum de Omni.

To show that $\mathbf{S Y L}{ }^{+} \mathbf{P L}$ is enough, we will show that also the following hold ' $p \vdash p \vee p$ ', ' $p \vee p \vdash p$ ', ' $p \vee q \vdash q \vee p$ ', and ' $p \rightarrow q \vdash(r \rightarrow$ $p) \rightarrow(r \rightarrow q)^{\prime}$. The reason is that we can axiomatize propositional logic by these four rules, together with modus ponens (cf. Goodstein, 1963, chapter 4). We can conclude that propositional logic follows from syllogistic logic if we (i) make the natural assumption that propositions are 0 -ary terms, (ii) assume that $T^{0}$ is a singular term, and (ii) treat singular terms as proposed by Leibniz.

It is important to realize that we represent $p \vee q$ by $\bar{p} a q$. ' $p \vdash$ $p \vee p$ ' immediately follows from the validity of $\bar{p} a \top$, the equivalence $p \equiv \top a p$ and the Dictum. As for disjunctive elimination, note that because $p \vee p \equiv \bar{p} a p$, we can conclude by (9) to $\bar{p} a \perp$. Via contraposition and double negation we derive $T^{0} a p$. Because $T^{0}$ is a singular term (rule 10)) it follows by (8) that $\top^{0} i p$, and thus via (11) that $p$. So we have validated $p \vee p \vdash p$. It is easier to validate ' $p \vee q \vdash q \vee p$ ': it immediately follows by contraposition and double negation.

Notice that ' $p \rightarrow q \vdash(r \rightarrow p) \rightarrow(r \rightarrow q)$ ' follows from the Dictum if we could make use of the deduction theorem: $\Gamma, P \vdash Q \Rightarrow$ $\Gamma \vdash P a Q$ (for this to make sense, $P$ and $Q$ have to be 0 -ary terms, obviously). But this deduction theorem follows from $\mathbf{S Y L}^{+} \mathbf{P L}$ : As-
sume $\Gamma, P \vdash Q$ and assume towards contradiction that $\neg(P a Q)$. This latter formula is equivalent to $P i \bar{Q}$. We have seen above that TiP can be derived from $P i \bar{Q}$ in $\mathbf{S Y L}{ }^{+}$. Because $\neg(P a Q) \vdash P$, it follows from the assumption $\Gamma, P \vdash Q$ that $\Gamma, \neg(P a Q) \vdash Q$. From this we derive $\top a Q$, and together with the validity of $P a \top$ we derive via the Dictum that $P a Q$. Thus, from $\Gamma$ and assuming $\neg(P a Q)$ we derive a contradiction: $\Gamma, \neg(P a Q) \vdash \neg(P a Q), P a Q$. By the reductio-rule we conclude that $\Gamma \vdash P a Q$.

## 3 Relations

Traditional logicians were well aware of an important limitation of syllogistic reasoning. In fact, already Aristotle recognized that the so-called 'oblique' terms (i.e. ones expressed in a grammatical case other than the nominative) gives rise to inferences that cannot be expressed in the ordinary categorical syllogistic. An example used by Aristotle is 'Wisdom is knowledge, Of the good there is wisdom, thus, Of the good there is knowledge'. This is intuitively a valid inference, but it, or its re-wording, is not syllogistically valid: 'All wisdom is knowledge, Every good thing is object of some wisdom, thus, Every good thing is object to some knowledge'. The re-wording shows that we are dealing with a binary relation here: 'is object of'. Aristotle didn't know how to deal with such inferences, but he noted that if there is a syllogism containing oblique terms, there must be a corresponding syllogism in which the term is put back into the nominative case.

It is generally assumed that in traditional formal logic there is no scope for relations. Thus - or so the Frege-Russell argument goes it can be used neither to formalize natural language, nor to formalize mathematics. What we need, - or so Frege and Russell argued - is a whole new logic. But the Frege-Russell argument is only partly valid: instead of inventing a whole new logic, we might as well just extend the traditional fragment. As far as semantics is concerned, it is wellknown how to work with relations. The main challenge, however, is to embed relations into the traditional theory, and to extend the inference rules such that also proofs can be handled that crucially involve relations. As it turns out, part of this work has already been done by medieval logicians, and also by people like Leibniz and de

Morgan when they were extending syllogistic reasoning such that it could account for inferences involving oblique terms, or relations.

We want to combine relations with monadic terms by means of the 'connectives' $a, i, e$, and $o$ to generate new terms. This will just be a generalization of what we did before: When we combine a monatic term $P$ with a monadic term $S$ (and connective ' $a$ ', for instance), what results is a new 0 -ary term like $S a P$. The generalization is now straightforward: if we combine an $n$-ary term/relation $R$ with a monadic term $S$ (and connective ' $a$ ', for instance), what results is a new $n-1$-ary term $\left(S^{1} a R^{n}\right)^{n-1}$. The semantics should now determine what such new terms denote. The $n-1$ ary term $\left(S^{1} a R^{n}\right)^{n-1}$, for instance, would denote $\left\{\left\langle d_{1}, \ldots, d_{n-1}\right\rangle: V_{M}(S) \subseteq\right.$ $\left\{d_{n} \in D:\left\langle d_{1}, \ldots, d_{n}\right\rangle \in V_{M}\left(R^{n}\right)\right\} .{ }^{3}$

Now we can represent the natural reading of a sentence like 'Every man loves a woman' as $M a\left(W i L^{2}\right)$. The meaning of this formula is calculated as follows:

$$
\begin{aligned}
& V_{M}\left(M a\left(W i L^{2}\right)\right)=\left\{\langle \rangle: I(M) \subseteq\left\{d \in D:\langle d\rangle \in V_{M}\left(W i L^{2}\right)\right\},\right. \\
& \quad \text { with } V_{M}\left(W i L^{2}\right)=\left\{d_{1}: I(W) \cap\left\{d_{2} \in D:\left\langle d_{1}, d_{2}\right\rangle \in I\left(L^{2}\right)\right\} \neq \emptyset\right\} .
\end{aligned}
$$

To represent the sentence 'There is woman who is loved by every man' we will follow medieval practice and make use of the passive form of 'love': being loved by. For every binary relation $R$, we represent its passive form by $R^{\cup}$, interpreted as indicated above: $V_{M}\left(R^{\cup}\right)=\left\{\left\langle d_{2}, d_{1}\right\rangle:\left\langle d_{1}, d_{2}\right\rangle \in I_{M}(R)\right\}$. ${ }^{4}$ Now we represent 'There is woman who is loved by every man' as follows: $W i\left(M a L^{\cup}\right)$. This sentence is true iff:
$V_{M}\left(W i\left(M a L^{\cup}\right)\right)=\left\{\langle \rangle: I(W) \cap\left\{d \in D:\langle d\rangle \in V_{M}\left(M a L^{\cup}\right)\right\} \neq \emptyset\right\}$, with $V_{M}\left(M a L^{\cup}\right)=\left\{\left\langle d_{1}\right\rangle: I(W) \subseteq\left\{d_{2} \in D:\left\langle d_{1}, d_{2}\right\rangle \in V_{M}\left(L^{\cup}\right)\right\}\right\}$.

[^30]Both truth conditions are intuitively correct, and correspond with those of the two first-order formulas $\forall x[M(x) \rightarrow \exists y[W(y) \wedge L(x, y)]]$ and $\exists y[W(y) \wedge \forall x[M(x) \rightarrow \wedge L(x, y)]]$, respectively.

What we want to know, however, is how we can reason with sentences that involve relations. Let us first look at the re-wording of Aristotle's example: 'All wisdom is knowledge, Every good thing is object of some wisdom, thus, Every good thing is object of some knowledge'. If we translate this into our language this becomes $W a K$, $G a(W i R) \vdash G a(K i R)$, with ' $R$ ' standing for 'is object of'. But now observe that we immediately predict that this inference is valid by means of the Dictum de Omni, if we can assume that ' $W$ ' occurs positively in ' $G a(W i R)$ '! We can mechanically determine that this is indeed the case. ${ }^{5}$ First, we say that if a sentence occurs out of context, the sentence occurs positively. From this, we determine the positive and negative occurrences of other terms as follows:
$\bar{P}$ occurs positively in $\Gamma$ iff $P$ occurs negatively in $\Gamma$.
If $(S a R)$ occurs positively in $\Gamma$, then $S^{-} a R^{+}$, otherwise $S^{+} a R^{-}$.
If $(S i R)$ occurs positively in $\Gamma$, then $S^{+} i R^{+}$, otherwise $S^{-} i R^{-}$.

Thus, first we assume that ' $G a(W i R)$ ' occurs positively. From this it follows that the ' $W i R$ ' occurs positively, from which it follows in turn that ' $W$ ' occurs positvely. Assuming that ' $W a K$ ' is true, the Dictum allows us to substitute $K$ for $W$ in $G a(W i R)$, resulting in the desired conclusion: $G a(K i R)$. Something very similar was done by medieval logicians (cf. Buridan, 1976).

As far as I know, this is how far medieval logicians went. But it is not far enough. Here is one classical example discussed by Leibniz (1966a): 'Every thing which is a painting is an art (or shorter, painting is an art), thus everyone who learns a thing which is a painting learns a thing which is an art' (or shorter: everyone who learns painting learns an art). Formally: $P a A \vdash\left(P i L^{2}\right) a\left(A i L^{2}\right)$. Semantically it is immediately clear that the conclusion follows from the premiss. But the challenge for traditional logic was to account for this inference in a proof-theoretic way. As Leibniz already observed, we can account for this inference in traditional logic if we add the extra

[^31](and tautological) premiss 'Everybody who learns a thing which is a painting learns a thing which is a painting', i.e. $\left(P i L^{2}\right) a\left(P i L^{2}\right)$. Now ( $\left.P i L^{2}\right) a\left(A i L^{2}\right)$ follows from PaA and $\left(P i L^{2}\right) a\left(P i L^{2}\right)$ by means of the Dictum the Omni, because by our above rules the second occurrence of ' $P$ ' in ( $\left.P i L^{2}\right) a\left(P i L^{2}\right)$ occurs in a monotone increasing position. ${ }^{6}$

To account for other inferences we need to assume more than just a tautological premiss. For instance, we cannot yet account for the inference from 'There is a woman who is loved by every man' represented by $W i\left(M a L^{\cup}\right)$ to 'Every man loves a woman' represented by $M a\left(W i L^{2}\right)$. In standard predicate logic one can easily prove the equivalence of $\forall x[M(x) \rightarrow \forall y[W(y) \rightarrow R(x, y)]]$ with $\forall y[W(y) \rightarrow \forall x[M(x) \rightarrow R(x, y)]]$. But in contrast to predicate logic, our system demands that the sequence of arguments of a relational term is in accordance with the scope order of the associated terms. Because of this, we have to use something like passive transformation to express 'reverse scope'. Thus, to reason with relations, we have to say which rules passive transformation obeys. To do so, we will follow medieval logicians such as Buridan and enrich our system SYL+PL with the rule of oblique conversion (12), and the passive rule (13) (for binary relations $R$, and predicates $S$ and $O$ ), and the more general formulation of the Dictum in ( $1^{\prime}$ ):
(12) Oblique Conversion: $S a(O a R) \equiv O a\left(S a R^{\cup}\right)$
from 'every man loves every woman' we infer that 'every woman is loved by every man' and the converse of this. ${ }^{7}$
(13) Double passive: $\quad R^{\mathrm{UU}} \equiv R$
(1') Dictum de Omni: $\Gamma(M a R)^{+}, \Theta(M)^{+} \vdash \Gamma(\Theta(R))$
Let us see how we can account for the inference from $W i\left(M a L^{\cup}\right)$ to Ma(WiL) :

[^32]| 1. $W i\left(M a L^{\cup}\right)$ | premiss |
| :--- | :--- |
| 2. $\left(M a L^{\cup}\right) a\left(M a L^{\cup}\right)$ | a tautology (everyone loved by every man is <br>  <br>  <br>  <br> loved by every man) |
| 3. $M a\left(\left(M a L^{\cup}\right) a L^{\cup \cup}\right)$ from 2 and $(12)\left(S=\left(M a L^{\cup}\right)\right.$ and $\left.S^{\prime}=M\right)$ <br> 4. $M a\left(\left(M a L^{\cup}\right) a L\right)$ by 3 and $(13)$, substitution of $L$ for $L^{\cup \cup}$ <br> 5. $M a(W i L)$ by 1 and 4 , by the Dictum de Omni $\left(1^{\prime}\right)^{8}$ |  |

Many other examples can be accounted for in this way as well.

## 4 Decidable Fragment of Predicate Logic

In this paper I have argued with Sommers (1982) and others that it is possible to think of logic as an extension of traditional syllogistics. Singular propositions straightforwardly fit into the system, and the syllogistics can easily be extended to account for propositional reasoning, and even for reasoning with relational terms as well. Though we used neither a distinguished relation of identity, nor make use of variables to allow for binding, we have seen that we could nevertheless adequately express many types of sentences for which these tools are normally used in predicate logic. This doesn't mean that our extended syllogistics is as expressive as standard first-order logic. What we cannot (yet) represent are sentences which crucially involve variables/pronouns and/or identity. Some examples for which these tools are crucial are the following: 'Every/some man loves himself', 'All parents love their children', 'Everybody loves somebody else', 'There is a unique king of France', and 'At least 3 men are sick'. As it turns out, we can extend our language with numerical quantifiers (cf. Murphee, 1997) and Quinean predicate functors to solve these problems, but these extensions have their price. Pratt-Hartmann (2009) shows that syllogistic systems with numerical quantifiers cannot be axiomatized, and adding Quinean predicate functors brings us over the decidability border. In the formal system we have so far, the sequence of arguments of a relational term will always be in accordance with the scope order of the associated terms. Thinking of this system as a fragment of FOL means that this logic has a very interesting property. Following an earlier suggestion of Quine, Purdy

[^33](1998) shows that the limits of decidability are indeed close to the limits of what can be expressed in (our fragment of) traditional formal logic. One can argue that (our fragment of) traditional formal logic is thus the natural part of logic. Indeed, a small contingent of modern logicians (e.g. Suppes, Sommers, van Benthem, Sanchez, Purdy, Pratt-Hartmann, Moss) try to develop a system of natural logic which is very close to what we have done in this paper in that it crucialy makes use of monotonicity (or the Dictum de Omni) and is essentially variable-free.

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# Temporal propositions as vague predicates ${ }^{\star}$ 

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#### Abstract

The notion that temporal propositions are vague predicates is examined with an eye to the nature of the objects over which the predicates range. These objects should not, it is argued, be identified once and for all with points or intervals in the real line (or any fixed linear order). Context has an important role to play not only in sidestepping the Sorites paradox (Gaifman 2002) but also in shaping temporal moments/extent (Landman 1991). The Russell-Wiener construction of time from events (Kamp 1979) is related to a notion of context given by a string of observations, the vagueness in which is brought out by grounding the observations in the real line. Moreover, that notion of context suggests a slight modification of the context dependency functions in Gaifman 2002 to interpret temporal propositions.


## 1 Introduction

Fluents, as temporal propositions are commonly known in AI, have in recent years made headway in studies of events and temporality in natural language semantics (e.g. Steedman 2000, van Lambalgen and Hamm 2005). The present paper concerns the bounded precision implicit in sentences such as ( $\dagger$ ).
$(\dagger)$ Pat reached the summit of K2 at noon, and not a moment earlier.
Presumably, a moment in $(\dagger)$ is less than an hour but greater than a picosecond. Whether or not determining the exact size of a moment is necessary to interpret or generate $(\dagger)$, there are pitfalls well known to philosophers that lurk. One such danger is the Sorites paradox, which is commonly associated not so much with time as with vagueness. Focusing on time, Landman has the following to say.

It is not the abstract underlying time structure that is semantically crucial, but the system of temporal measurements. We shouldn't ask just 'what is a moment of time', because that is a context dependent question. We can assume that context determines how precisely we are measuring time: it chooses in the hierarchy of temporal measurements one measurement that is taken as 'time as finely grained as this context requires it to be.' The elements of that measurement are then regarded as moments in that context. (Landman 1991, page 138)

[^34]The present paper considers some notions of context that can be deployed to flesh out this suggestion. We start in section 2 with the use of context in Gaifman 2002 to sidestep the Sorites paradox before returning to the special case of time. A basic aim is to critically examine the intuition that the temporal extent of an event is an interval - an intuition developed in Kamp 1979, Allen 1983 and Thomason 1989, among other works.

## 2 Sorites and appropriate contexts

The tolerance of a unary predicate $P$ to small changes is expressed in Gaifman 2002 through conditionals of the form (1).

$$
\begin{equation*}
N_{P}(x, y) \rightarrow(P(x) \rightarrow P(y)) \tag{1}
\end{equation*}
$$

$P$ is asserted in (1) to be tolerant insofar as $P$ holds of $y$ whenever $P$ holds of an $x$ that is $N_{p}$-near $y$. Repeatedly applying (1), we conclude $P(z)$, given any finite sequence $y_{1}, \ldots, y_{n}$ such that $y_{n}=z, P\left(y_{1}\right)$ and $N_{P}\left(y_{i}, y_{i+1}\right)$ for $1 \leq i<n$. A Sorites chain is a sequence $y_{1}, \ldots, y_{n}$ such that $P$ holds of $y_{1}$ but not $y_{n}$, even though $N_{P}\left(y_{i}, y_{i+1}\right)$ for $1 \leq i<n$. Gaifman's way out of the Sorites paradox is to interpret $P$ against a context dependency function $f$ mapping a finite set $C$ (of objects in a first-order model) to a subset $f(C)$ of $C$, understood to be the extension of $P$ at "context" $C$. (In effect, the predication $P(x)$ becomes $P(x, C)$, for some comparison class $C$ that contains $x$.) The idea then is to pick out finite sets $C$ that do not contain a Sorites chain

$$
\text { for every Sorites chain } y_{1}, \ldots, y_{n},\left\{y_{1}, \ldots, y_{n}\right\} \nsubseteq C
$$

Such sets are called feasible contexts. Formally, Gaifman sets up a Contextual Logic preserving classical logic in which tolerance conditionals (1) can be sharpened to (2), using a construct $[C]$ to constrain the contexts relative to which $P(x)$ and $P(y)$ are interpreted.

$$
\begin{equation*}
[C]\left(N_{P}(x, y) \rightarrow(P(x) \rightarrow P(y))\right) \tag{2}
\end{equation*}
$$

As contexts in Contextual Logic need not be feasible, (2) must be refined further to restrict $C$ to feasible contexts

$$
\text { feasible }(C) \rightarrow[C]\left(N_{P}(x, y) \rightarrow(P(x) \rightarrow P(y))\right)
$$

The formal notation gets quite heavy, but the point is simple enough:
sentences and proofs have associated contexts. Those whose contexts are feasible form the feasible portion of the language; and it is within this portion that a tolerant predicate is meant to be used. The proof of the Sorites contradiction fails, because it requires an unfeasible context and in unfeasible contexts a tolerant predicate looses [sic] its tolerance; it has some sharp cutoff. Unfeasible contexts do not arise in practice. (Gaifman 2002, pages 23, 24)

The obvious question is why not build into Contextual Logic only contexts that do "arise in practice" - viz. the feasible ones? For tolerant predicates in general, such a restriction may, as Gaifman claims, well result in a "cumbersome system." Fluents are, however, a very particular case of vague predicates, and insofar as practice is what matters, it is of interest to restrict time to practice. That said, Contextual Logic leaves open the question of what the stuff of time is - integers, real numbers or events - or how times are formed from that stuff - points, intervals or some other sets. Whatever the underlying first-order model might be, the crucial point is to pick out, for every fluent $P$, finite sets $C$ of times that validate (2), for a suitable interpretation of $N_{P}$. Such feasible contexts $C$ avoid the sharp cutoffs characteristic of unfeasible contexts, and allow us to sidestep the difficulty of pinning down the precise moment of change by bounding the granularity. Bounded granularity is crucial for making sense of talk about the first (or last) moment a fluent is true (or of claims that a fluent true at an interval is true at every non-null part of that interval).

## 3 Contexts for temporal extent

The context-dependent conception of time outlined in pages 138-140 of Landman 1991 features a discrete order at every context, subject to refinement by more fine-grained contexts. Contexts become more fine-grained as we consider further fluents side by side, not only through the variations in the truth of the fluents over time, but through the additional nearness predicates in (2). Refinements should, as pointed out in page 139, be carried out only "as long as it is sensible," as "there may be points after which refinement is no longer practically or even physically possible (these would be points where our measurement systems are not fine-grained enough to measure)." It would appear that dense linear orders such as the set of rational numbers or the set of real numbers outstrip the bounded precision of fluents in ordinary natural language discourse. Instead of such numbers, one might construct time from fluents - an approach that suggests the "actual usage" of vague predicates that Gaifman claims for feasible contexts pertains to Contextual Logic's proof system more than to any of its particular model-theoretic interpretations. The remainder of this section builds on Kamp 1979 to explore the view that as predicates, fluents range not so much over time, but over eventuality-occurrences.

The point is to make time just fine grained enough to order certain events of interest. Kamp 1979 collects such events in a set $E$, and adds binary relations (on $E$ ) of temporal overlap $\bigcirc$ and complete precedence $\prec$ to form an event structure $\langle E, \bigcirc, \prec\rangle$ satisfying $\left(\mathrm{A}_{1}\right)-\left(\mathrm{A}_{5}\right)$.

```
\(\left(\mathrm{A}_{1}\right) \quad e \bigcirc e\)
\(\left(\mathrm{A}_{2}\right) \quad e \bigcirc e^{\prime}\) implies \(e^{\prime} \bigcirc e\)
\(\left(\mathrm{A}_{3}\right) \quad e \prec e^{\prime}\) implies not \(e \bigcirc e^{\prime}\)
\(\left(\mathrm{A}_{4}\right) \quad e \prec e^{\prime} \bigcirc e^{\prime \prime} \prec e^{\prime \prime \prime}\) implies \(e \prec e^{\prime \prime \prime}\)
\(\left(\mathrm{A}_{5}\right) \quad e \prec e^{\prime}\) or \(e \bigcirc e^{\prime}\) or \(e^{\prime} \prec e\)
```


## Workshop on Vagueness

(Seven postulates are given in Kamp 1979, but two are superfluous.) Before extracting temporal moments from $\langle E, \bigcirc, \prec\rangle$, it is useful for orientation to proceed in the opposite direction, forming event structures from a relation $s \subseteq T \times E$ associating a time $t \in T$ with an event $e \in E$ according to the intuition that

$$
s(t, e) \text { says ' } e s \text {-occurs at } t \text { '. }
$$

That is, $s$ is a schedule, for which it is natural to define temporal overlap ov(s) between events $e$ and $e^{\prime}$ that $s$-occur at some time in common

$$
e \operatorname{ov}(s) e^{\prime} \stackrel{\text { def }}{\Leftrightarrow}(\exists t) s(t, e) \text { and } s\left(t, e^{\prime}\right)
$$

and to apply a linear order $<$ on $T$ to relate an event $e$ to another $e^{\prime}$ if $e s$-occurs only <-before $e$

$$
e<_{s} e^{\prime} \stackrel{\text { def }}{\Leftrightarrow}\left(\forall t, t^{\prime} \text { such that } s(t, e) \text { and } s\left(t^{\prime}, e^{\prime}\right)\right) t<t^{\prime} .
$$

Proposition 1. $\left\langle E, o v(s),<_{s}\right\rangle$ is an event structure provided
(i) $<$ is a linear order on $T$
(ii) $(\forall e \in E)(\exists t \in T) s(t, e)$, and
(iii) $s(t, e)$ whenever $s\left(t_{0}, e\right)$ and $s\left(t_{1}, e\right)$ for some $t_{0}<t$ and $t_{1}>t$.

Let us call $\langle s, T,<\rangle$ an interval schedule if it satisfies (i) - (iii).
Now for the Russell-Wiener construction in Kamp 1979 of time from an event structure $\langle E, \bigcirc, \prec\rangle$. We collect subsets of $E$ any two in which $\bigcirc$-overlap in

$$
O_{\bigcirc} \stackrel{\text { def }}{=}\left\{t \subseteq E \mid\left(\forall e, e^{\prime} \in t\right) e \bigcirc e^{\prime}\right\}
$$

and equate temporal moments with $\subseteq$-maximal elements of $O_{\bigcirc}$

$$
T_{\bigcirc} \stackrel{\text { def }}{=}\left\{t \in O_{\bigcirc} \mid\left(\forall t^{\prime} \in O_{\bigcirc}\right) t \subseteq t^{\prime} \text { implies } t=t^{\prime}\right\} .
$$

We then pass $\prec$ on to $T_{\bigcirc}$ existentially

$$
t \prec \bigcirc t^{\prime} \stackrel{\text { def }}{\Leftrightarrow}(\exists e \in t)\left(\exists e^{\prime} \in t^{\prime}\right) e \prec e^{\prime}
$$

and define sched ${ }_{\bigcirc} \subseteq T_{\bigcirc} \times E$ as the converse of membership

$$
\operatorname{sched}_{\bigcirc}(t, e) \stackrel{\text { def }}{\Leftrightarrow} e \in t
$$

for all $t \in T_{\bigcirc}$ and $e \in E$.
Theorem 2 (Kamp). $\left\langle\right.$ sched $\left._{\bigcirc}, T_{\bigcirc}, \prec \bigcirc\right\rangle$ is an interval schedule if $\langle E, \bigcirc, \prec\rangle$ is an event structure.

Applying the transformations in Theorem 2 and Proposition 1 in sequence to an event structure leads to the same event structure, but applying the transformations in reverse to an interval schedule may result in a different (reduced)
interval schedule. The notion of time obtained from events is fine enough just to determine overlap $\bigcirc$ and complete precedence $\prec$ between events. But are there not other temporal relations to consider?

Thirteen different relations between intervals are catalogued in Allen 1983, strung out below as sequences of snapshots (enclosed in boxes).


If a box must be $\subseteq$-maximal (as required by $T_{\bigcirc}$ ), only three of the thirteen strings above survive

$$
\bar{e} e^{\prime}+e^{\prime} \bar{e}+e, e^{\prime}
$$

To recover the ten other strings, it is useful to equip an event $e$ with pre- and post-events pre(e) and post(e), marrying (and mangling) ideas from Allen and Ferguson 1994 and Walker instants (Thomason 1984 as well as van Lambalgen and Hamm 2005) to take the steps
or, in terms of a schedule $s$, to enrich $s$

$$
s^{<} \stackrel{\text { def }}{=} s \cup s_{-}^{<} \cup s_{+}^{<}
$$

by

$$
\begin{aligned}
& s_{-}^{<} \stackrel{\text { def }}{=}\left\{\langle t, \operatorname{pre}(e)\rangle \mid\left(\exists t^{\prime}>t\right) s\left(t^{\prime}, e\right) \text { and }\left(\forall t^{\prime} \leq t\right) \text { not } s(t, e)\right\} \\
& s_{+}^{<} \stackrel{\text { def }}{=}\left\{\langle t, \operatorname{post}(e)\rangle \mid\left(\exists t^{\prime}<t\right) s\left(t^{\prime}, e\right) \text { and }\left(\forall t^{\prime} \geq t\right) \operatorname{not} s(t, e)\right\}
\end{aligned}
$$

where for all $e, e^{\prime}, e^{\prime \prime} \in E$, the set $\left\{e, \operatorname{pre}\left(e^{\prime}\right)\right.$, post $\left.\left(e^{\prime \prime}\right)\right\}$ has cardinality 3 . It is easy to see that if $\langle s, T,<\rangle$ is an interval schedule on $E$, then so is $\left\langle s^{<}, T,<\right\rangle$ on the extended set

$$
E_{s}^{<} \stackrel{\text { def }}{=}\left\{y \mid(\exists t) s^{<}(t, y)\right\}
$$

of events, and moreover each of the thirteen relations between $e$ and $e^{\prime} \in E$ can be determined from the overlap relation $o v\left(s^{<}\right)$induced by $s^{<}-$e.g.

$$
\begin{array}{lll}
e \text { before } e^{\prime} & \text { iff } & \operatorname{post}(e) \operatorname{ov}\left(s^{<}\right) \operatorname{pre}\left(e^{\prime}\right) \\
e \text { meets } e^{\prime} & \text { iff } & \operatorname{post}(e) \operatorname{ov}\left(s^{<}\right) e^{\prime} \text { but neither } \\
& & e \operatorname{ov}\left(s^{<}\right) e^{\prime} \text { nor } \operatorname{post}(e) \operatorname{ov}\left(s^{<}\right) \operatorname{pre}\left(e^{\prime}\right) .
\end{array}
$$

## Workshop on Vagueness

For the record,
Proposition 3. For every interval schedule $\langle s, T,<\rangle,\left\langle E_{s}^{<}, o v\left(s^{<}\right), \prec\right\rangle$ is an event structure where $\prec$ is the precedence $<{ }_{s}<$ induced by $s<$ and $<$, and for $\bigcirc \xlongequal{\text { def }} o v\left(s^{<}\right)$,

$$
\begin{equation*}
T_{\bigcirc}=\left\{\left\{y \mid s^{<}(t, y)\right\} \mid t \in T\right\} . \tag{3}
\end{equation*}
$$

According to (3), $T_{\bigcirc}$ does not discard a time $t \in T$ (as may be the case were $\bigcirc=o v(s))$ but merely identifies it with $t^{\prime} \in T$ such that for all $y$,

$$
s^{<}(t, y) \text { iff } s^{<}\left(t^{\prime}, y\right) .
$$

(This equivalence is, in general, stronger than one with $s$ in place of $s^{<}$.) The effect of $T_{\mathrm{O}}$ can be pictured on strings as block compression $\pi$ reducing adjacent identical boxes $\alpha \alpha$ to one $\alpha$ so that, for example, a string

$$
\begin{array}{|l|l|}
\hline \text { rain,dawn } & \text { rain } \\
& \text { rain,dusk } \\
\hline
\end{array}
$$

of length $n+2$ recording $n+2$ observations of rain from dawn to dusk is reduced to rain,dawn rain rain,dusk for $n \geq 1$ in accordance with the slogan "no time without change" (Kamp and Reyle 1993, page 674)
suppressing the pre and post-events. To count observations, we need only introduce them as events (e.g. ticks of a clock).

## 4 Contexts as strings

A schedule $s \subseteq T \times E$ that is finite (as a set) can always be represented as a string, given a linear order < on $T$, whether or not it meets the interval requirement (iii) in Proposition 1. For example, we can picture the schedule

$$
\left\{(0, e),(1, e),\left(1, e^{\prime}\right),\left(2, e^{\prime}\right),(3, e)\right\}
$$

under the usual ordering $0<1<2<3$ as

$$
\begin{array}{|l|l|l|l|}
\hline 0, e & 1, e, e^{\prime} & 2, e^{\prime} & 3, e  \tag{4}\\
\hline
\end{array}
$$

which restricted to $E \cup\{0\}$, projects to

$$
\begin{array}{|l|l|l|l|}
\hline 0, e & e, e^{\prime} & e^{\prime} & \bar{c}  \tag{5}\\
\hline
\end{array}
$$

obtained by discarding $1,2,3$. Restricted to $\{e\}$, (4) and (5) both become
that $\pi$ reduces to
$e \square e$.
To be more precise, some notation will be helpful to picture the construction in Proposition 3 in terms of strings. For any subset $X$ of $E$ (such as $E$ ), let

$$
X_{+} \stackrel{\text { def }}{=} X \cup\{\operatorname{pre}(e) \mid e \in X\} \cup\{\operatorname{post}(e) \mid e \in X\}
$$

and $r^{X}: E_{+}^{*} \rightarrow X^{*}$ be given by componentwise intersections with $X$

$$
r^{X}\left(\alpha_{1} \cdots \alpha_{n}\right) \stackrel{\text { def }}{=}\left(\alpha_{1} \cap X\right) \cdots\left(\alpha_{n} \cap X\right)
$$

and $\pi_{X}: E_{+}^{*} \rightarrow X^{*}$ be given by applying $r^{X_{+}}$, then $\pi$ and then $r^{E}$ (to suppress pre- and post-events)

$$
\pi_{X}\left(\alpha_{1} \cdots \alpha_{n}\right) \stackrel{\text { def }}{=} r^{E}\left(\pi\left(r^{X_{+}}\left(\alpha_{1} \cdots \alpha_{n}\right)\right)\right)
$$

Now, Russell-Wiener-Kamp applied to the restriction

$$
s\lceil X \stackrel{\text { def }}{=}\{(t, e) \in s \mid e \in X\}
$$

of a schedule $s$ to a finite set $X$ becomes the $\pi_{X}$-approximation of $s$. For example, for

$$
s=\{(r, r) \mid r \in \mathbb{R}\}
$$

and $X=\{0,1,2\}$, the $\pi_{X}$-approximation of $s$ is

$$
\boxed{0} \square \widehat{1} \square \boxed{2} \square .
$$

The reader familiar with inverse limits can carry out the construction in Proposition 3 by gluing together $\pi_{X}$ approximations of $s$, for finite subsets $X$ of $E$. For a more linguistic example, consider again the string rain,dawn | rain | rain,dusk |
| ---: | :--- | :--- | depicting the phrase rain from dawn to dusk. For $X=\{$ rain, dawn, dusk $\}$, this string can be understood as the $\pi_{X}$-approximation of a schedule $s \subseteq T \times E$ such that for some $t_{1}, t_{2} \in T$, we have for all $t \in T$,

(i) $s\left(t\right.$, dawn) if $t \leq t_{1}$
(ii) $s(t$, rain) and
(iii) $s\left(t\right.$, dusk) if $t \geq t_{2}$.

Weaker constraints on $s$ can be derived by changing the $\pi_{X}$-approximation or perhaps by experimenting with projections other than $\pi_{X}$ that stay away from pre- and post-borders in $X_{+}$. In the remainder of this section, we shall consider more drastic changes in the interpretation of a string, allowing us to drop the interval requirement on schedules (condition (iii) in Proposition 1).

## Workshop on Vagueness

Let us interpret a string $\alpha_{1} \cdots \alpha_{n}$ over open intervals in the real line $\mathbb{R}$ that have length greater than some fixed real number $\epsilon>0$. (The intuition is that an observation takes time $>\epsilon$. Let

$$
\mathcal{O}_{\epsilon} \stackrel{\text { def }}{=}\left\{(a, b) \mid a, b \in \mathbb{R}_{ \pm \infty} \text { and } b>a+\epsilon\right\}
$$

where

$$
(a, b) \stackrel{\text { def }}{=}\{r \in \mathbb{R} \mid a<r<b\}
$$

and for all $o, o^{\prime} \in \mathcal{O}_{\epsilon}$,

$$
o \prec_{\epsilon} o^{\prime} \stackrel{\text { def }}{\Leftrightarrow} o, o^{\prime} \in \mathcal{O}_{\epsilon} \text { and }(\forall r \in o)\left(\forall r^{\prime} \in o^{\prime}\right) r<r^{\prime}
$$

and for $\epsilon$-successors,

$$
o s_{\epsilon} o^{\prime} \stackrel{\text { def }}{\Leftrightarrow} o \prec_{\epsilon} o^{\prime} \text { and } \operatorname{not}\left(\exists o^{\prime \prime} \prec_{\epsilon} o^{\prime}\right) o \prec_{\epsilon} o^{\prime \prime} .
$$

An $\epsilon$-chain is a sequence $o_{1} \ldots o_{n}$ in $\mathcal{O}_{\epsilon}$ such that

$$
o_{1} s_{\epsilon} o_{2} s_{\epsilon} o_{3} \cdots s_{\epsilon} o_{n}
$$

A string $\alpha_{1} \cdots \alpha_{n}$ holds at an $\epsilon$-chain $o_{1} \ldots o_{n}$ if for $1 \leq j \leq n$,

$$
o_{j} \models \varphi \text { for every } \varphi \in \alpha_{j}
$$

for a suitable notion $\models$ of satisfaction. That is, a symbol $\alpha$ in a string is made up not just of event occurrences but of event types, allowing us to reconceive the string $\operatorname{pre}(e) \quad e \operatorname{post}(e)$ as $\alpha(e) \operatorname{oc}(e) \omega(e)$ where the negation $\neg \mathrm{Oc}(e)$ of an occurrence of $e$ is split between

$$
\begin{aligned}
& \alpha(e) \stackrel{\text { def }}{=} \neg \mathrm{oc}(e), \neg \operatorname{Past}(\mathrm{oc}(e)), \text { Future }(\mathrm{oc}(e)) \\
& \omega(e) \stackrel{\text { def }}{=} \neg \mathrm{oc}(e), \text { Past }(\mathrm{oc}(e)), \neg \text { Future }(\mathrm{oc}(e))
\end{aligned}
$$

not to mention

$$
\begin{aligned}
\text { hole }(e) & \stackrel{\text { def }}{=} \neg \mathrm{oc}(e), \operatorname{Past}(\mathrm{oc}(e)), \text { Future }(\mathrm{oc}(e)) \\
\text { never }(e) & \stackrel{\text { def }}{=} \neg \neg \mathrm{oc}(e), \neg \operatorname{Past}(\mathrm{oc}(e)), \neg \text { Future }(\mathrm{oc}(e))
\end{aligned}
$$

where as usual,

$$
\begin{array}{rll}
o \models \neg \varphi & \text { iff } & \text { not } o \models \varphi \\
o \models \text { Past } \varphi & \text { iff } & o^{\prime} \models \varphi \text { for some } o^{\prime} \prec_{\epsilon} o \\
o \models \text { Future } \varphi & \text { iff } & o^{\prime} \models \varphi \text { for some } o^{\prime} \succ_{\epsilon} o .
\end{array}
$$

Next, to step from $\epsilon$-chains to intervals, let us agree that an $\epsilon$-chain $o_{1} \ldots o_{n}$ $\epsilon$-spans $(a, b)$ if $a \in o_{1}, b \in o_{n}$ and

$$
o_{1} \cup o_{n} \subseteq(a-\epsilon, b+\epsilon)
$$

- i.e.

$$
\{a, b\} \subseteq o_{1} \cup \cdots \cup o_{n} \subseteq(a-\epsilon, b+\epsilon)
$$

Now, in general, given two $\epsilon$-chains $o_{1} \ldots o_{n}$ and $o_{1}^{\prime} \ldots o_{n}^{\prime}$ that $\epsilon$-span $(a, b)$, the strings that hold at $o_{1} \ldots o_{n}$ may differ from those that hold at $o_{1}^{\prime} \ldots o_{n}^{\prime}$. The door is left open for an analysis of vagueness (as opposed to tolerance) in Gaifman 2002 based on modal logic, with an accessibility relation $R$ (for fixed $\epsilon$ ) between $\epsilon$-chains of the same length

$$
o_{1} \ldots o_{n} R o_{1}^{\prime} \ldots o_{n}^{\prime} \stackrel{\text { def }}{\Leftrightarrow}(\exists a, b) o_{1} \ldots o_{n} \text { and } o_{1}^{\prime} \ldots o_{n}^{\prime} \text { both span }(a, b) .
$$

Borderline cases abound in which a string $\alpha_{1} \cdots \alpha_{n}$ that holds at an $\epsilon$-chain $o_{1} \ldots o_{n}$ may fail at some $o_{1}^{\prime} \ldots o_{n}^{\prime}$ such that $o_{1} \ldots o_{n} R o_{1}^{\prime} \ldots o_{n}^{\prime}$. Matters change somewhat if the accessibility relation $r$ is defined instead between intervals

$$
(a, b) R\left(a^{\prime}, b^{\prime}\right) \stackrel{\text { def }}{\Leftrightarrow}\left|a-a^{\prime}\right|<\epsilon \text { and }\left|b-b^{\prime}\right|<\epsilon
$$

where say,

$$
\begin{gathered}
(a, b) \models \alpha_{1} \cdots \alpha_{n} \stackrel{\text { def }}{\Leftrightarrow} \alpha_{1} \cdots \alpha_{n} \text { holds at every } \epsilon \text {-chain } o_{1} \ldots o_{n} \text { such that } \\
o_{1}=(a, c) \text { and } o_{n}=(d, b) \text { for some } c, d .
\end{gathered}
$$

Not to mention variations in $\epsilon \ldots$

## 5 Conclusion

Three notions of context were considered above:

- feasible contexts in $\S 2$ for Sorites (Gaifman 2002) amounting to comparison classes
- selected events in $\S 3$ that induce temporal moments (applying the Russell-Wiener-Kamp construction on event structures with pre- and post-events), and
- strings in $\S 4$ that generalize event occurrences to event types, and are interpretable as incomplete samples from open intervals in $\mathbb{R}$ of a particular granularity $\epsilon>0$.

The tension between strings that record sequences of observations and the real line $\mathbb{R}$ gives rise to vagueness, in the form of borderline cases analyzable in a modal logic, as outlined in Gaifman 2002. Focusing on the contexts that "arise in practice," recall that Gaifman interprets a tolerant unary predicate $P$ via a context dependency function $f_{P}$ mapping a context $C$ to the extension $f_{P}(C) \subseteq$ $C$ of $P$ at $C$. Similarly, we might analyze a temporal proposition $P$ as a function mapping $C$ to the set $f_{P}(C)$ of parts of $C$ that make $P$ true such that

$$
P \text { is true at } C \quad \text { iff } \quad f_{P}(C) \neq \emptyset .
$$

## Workshop on Vagueness

Building on a natural part-of relation $\sqsubseteq$ between strings where, for example,

$$
\begin{array}{|l|l|l|l|l|}
\hline \mathrm{a}, \mathrm{~b} & \mathrm{c} & \mathrm{~d} & \sqsubseteq \mathrm{a}, \mathrm{~b}, \mathrm{c} & \mathrm{a}, \mathrm{c}, \mathrm{~d} \\
\mathrm{~d} & s^{\prime}
\end{array},
$$

we can put

$$
f_{P}(C)=\{s \sqsubseteq C \mid s \in \mathcal{L}(P)\}
$$

where $\mathcal{L}(P)$ is the set of strings $s$ that make $P$ true - for example,

$$
\mathcal{L}(\text { rain from dawn to dusk })=\text { dawn, rain }^{\text {rain }}{ }^{+} \text {dusk, rain }
$$

(Fernando 2007, 2009).

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# Vagueness is Rational Under Uncertainty 

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## 1 Introduction

In this paper we show that some of the properties of vague scalar adjectives are consequences of rational communication. Traditionally, theories of vagueness are evaluated through the lens of a single cluster of philosophical desiderata: how vagueness fits into a theory of truth (or even metaphysics), the sorites, and related issues. These are important, and we will have more to say about some of them, but we also seek to refocus the analysis of vagueness, moving away from consideration of abstract philosophical problems, and towards consideration of the problems faced by ordinary language users. It is our contention that it is by considering the latter that the former can best be understood. Using standard mathematical tools, we suggest that, given a certain model of communication, what have typically been taken to be puzzles in the truth conditions of vague expressions, should just be expected consequences of communication under uncertainty.

The most basic criterion for any successful semantic theory is that it should establish when sentences are true, and when they are false. This is a tall order as regards sentences involving vague predicates. As a result, the bar is sometimes set too low in the sense that some scholars settle for giving definite truth values for only a subset of conditions in the world, or for abandoning truth in favor of some notion of acceptability. We have no a priori argument against theories which attribute partial or fuzzy truth conditions to vague sentences, ${ }^{1}$ and no a priori arguments against theories that are stated primarily in terms of acceptability, but we like and want to retain classical semantics. Ceteris paribus, a theory which attributes a definite, boolean truth value to a vague sentence is preferable to one which does not, and a theory which allows us to talk about the objective truth value of a vague sentence is preferable to one which relativizes the truth conditions to features of the utterance situation or speaker. We will not claim that it is always possible to specify objective boolean truth values for every vague sentence even with complete knowledge of the utterance situation and

[^35]speaker, but we will offer a theory which implies that every vague sentence has a boolean truth value, and we will offer a theory of how speakers can and must approximate it.

## 2 A Free Variable Theory of Scalar Adjectives

Following Cresswell [1], we analyze the semantics of "Xena is tall" simply as saying that Xena's height is greater than some standard of comparison or threshold degree $d$, where $d$ is a free variable. Thus our analysis is semantically parallel to free variable accounts of e.g. modals [2] or quantifiers [3]. However, there is a crucial difference. Consider the analysis of quantifiers: if "Everybody is happy" is analyzed as $\forall x \in C$, $\operatorname{happy}(x)$, with the restrictor $C$ being a free variable, then it is normally assumed that while the hearer may sometimes be uncertain as to the value of $C$, the speaker has a particular value in mind, and cannot in any sense be wrong about that value. However, in our free variable account of vagueness, there is no such asymmetry: when a speaker says "Xena is tall", neither the speaker nor the hearer has privileged access to $d$. Indeed, even if both speaker and hearer are clear on issues such as the comparison class for which Xena's tallness is being considered, and on normative issues such as the utility or aesthetics of various heights for this class, they still cannot be certain as to the appropriate value of $d$. The best they can do, we will suggest, is form a probabilistic model of the value of $d$, based on their prior experience of how tall has been used. ${ }^{2}$

Probabilistic, statistical, and fuzzy theories of vagueness have previously been brushed aside and discounted because of the failure of rather naive straw-man statistical approaches to account for the properties of vague predicates. Arguments against probabilistic approaches to vagueness such as those of Fine, Klein, Parikh, and Kamp and Partee $[4,5,6,7]$ argue against the use for threshold values of point estimates such as averages, geometric means, or arbitrary probability densities. ${ }^{3}$ And they're right; such analyses are inadequate. There is another way though. Instead of merely using statistics to calculate a point estimate and then

[^36]forgetting about the original statistics, we take the information conveyed by a vague sentence to be a statistical distribution. A vague meaning provides a conditional distribution over facts, a probability function dependent on the value of an unbound variable, a variable that is itself constrained by a pragmatically determined statistical distribution.

## 3 Communication Under Uncertainty

We can imagine, contrary to fact, a system of linguistic communication in which all expressions are precise, in principle assessable by language users as definitely true or definitely false, i.e. there are no vague expressions. In fact, much of semantics as well as information theory is aimed at developing ways of guaranteeing precision. However, we are taking a somewhat different approach and asking whether there are situations guaranteeing a form of imprecision, vagueness. We apply standard results from information theory to obtain a model of communication under uncertainty in which the following hold: (i) communication under uncertainty is represented as a game against a malevolent nature who's goal is to disrupt communication, (ii) even in the face of a malevolent nature, non-trivial exchange of information is possible, (iii) the information conveyed by vague expressions is not truth values or the precise facts upon which a relation over degrees is determined, but a distribution over such facts, and (iv) vagueness is rational under uncertainty. The discussion in this section is presented informally by way of example, but the concepts and results have counterparts in the formal theory of information. Readers familiar with the basics of information theory should be able to make the relevant connections through the citations provided.

Definition 1. Information channel: An information channel [8] is a system of communication between a speaker and a hearer for conveying and interpreting observations about objects. The input to an information channel is a speaker's beliefs or observations and the output is the utterance heard.

Suppose a speaker observes and believes that Xena's height is defined by a degree of height (e.g. 175 cm ) and that it exceeds some standard. Both of which are objectively true or false. The speaker communicates the observation by uttering "Xena is tall", and in this case the information channel is the one where the speaker inputs observations about Xena's height relative to this standard and the hearer receives these via the utterance "Xena is tall".

Such a communicative setup can be represented statistically [8] as a vocabulary of observations and utterances along with probability distributions relating them. For a speaker or hearer to know how to use the channel, i.e. to know the communicative conventions, they must have knowledge of the space of observations and utterances and the probabilities governing them.
"Xena is tall and she is not tall" (cf. fn. 1), whereas a statistical account predicts this unproblematically, provided the same degree distribution is assumed for both uses of tall.

Definition 2. Mutual information: Mutual information [8] is a measure of overlap between the distributions of some observations.
E.g. if a speaker knows Xena's height as the uniform distribution over the interval
$(1.7 \mathrm{~m}, 1.8 \mathrm{~m})$ but a hearer knows it as the uniform distribution over the interval $(1.75 \mathrm{~m}, 1.85 \mathrm{~m})$ then there is an overlap, a positive amount of mutual information, in the speaker and hearer's distributions. The mutual information is also larger than it would have been if the hearer knew Xena's height as the distribution over the interval $(1.3 \mathrm{~m}, 1.4 \mathrm{~m})$, but smaller than it would have been had they agreed exactly.

In order to be as precise as possible, rational speakers and hearers should strive to have channel distributions that overlap as much as possible [8]. Perfect overlap is unachievable under uncertainty, but maximizing mutual information is still the best option $[9,10,11]$.

Definition 3. Information channel game: An information channel game [11] is a game between a speaker and a malevolent nature. In an information channel game, the speaker wants utterances to convey observations as precisely as possible, as measured by mutual information, but nature counters with noise making this difficult.

Suppose again that a speaker believes Xena's true height is defined by a degree of height which exceeds some standard, and communicates this by uttering "Xena is tall". Now, though, suppose that every observation the speaker has ever made was interfered with via a series of funhouse mirrors created by a malevolent nature. Thus, when the speaker says "Xena is tall", he is likely not only to be wrong as regards Xena's height, but also to be misinformed as to what counts as tall. That is, his distribution over heights as well as the distribution over the relevant standard of comparison have been distorted by the evil nature. The hearer will then recover something which is neither Xena's true height nor what the speaker takes Xena's height to be. For rational speakers and hearers to know how to use this channel is to have sufficient information to cope with the channel's noisy distributions. Because the funhouse mirrors are not controlled by the speakers or hearers, though, the best that they can do is to jointly figure out the distributions of height and its standard that overlap as much as possible with the distributions that were distorted by nature, the true distributions plus some noise.

Notice that in the funhouse mirror game speakers and hearers do not play against each other. They play together, on the same team as it were, against the noise-introducing malevolent nature. They succeed when they maximize the overlap, the mutual information, of their communicative conventions, the channel distributions, under this uncertainty.

Proposition 1. Communication under uncertainty can be modeled as an information channel game.

Rational models of linguistic communication are often presented as Lewisian signaling games [12, 13] in which speaker and hearer play on separate teams
with separate (though perhaps related) utilities. Such games have proved very fruitful, but they bring with them the baggage of strong common knowledge and rationality (CKR) assumptions and also (in the most common applications) fail to recognize the importance of shared uncertainty in communication. Complete CKR is a non-starting position, neither possible nor wanted because of unavoidable uncertainty and variability in communicative situations. What is wanted is a model of communication that can accommodate the uncertainty, whether limited or extreme, that speakers and hearers have. If (i) what you believe or even know is like what I believe or know up to a certain point and (ii) you believe this and can make guesses about or estimate where we differ, then (iii) what really matters most is whether you can communicate according to what you believe or know plus some guesses about how that might differ from what I believe or know. Insofar as what we are interested in in this paper is completely cooperative communication in which the speaker and hearer share common goals, we might say that rational communication under uncertainty is like talking to a noisy version of yourself.

The result is reminiscent of Davidson's notion of charity [14], which "counsels us quite generally to prefer theories of interpretation that minimize disagreement" [ $15, \mathrm{p} . \mathrm{xix}] .{ }^{4}$ Davidson makes it clear that rational communication cannot and should not eliminate disagreement; it should offer a way to make disagreement possible and useful. Substituting CKR with charity, the problem rational speakers and hearers face is to do what's best with respect to certain beliefs plus some uncertain or noisy beliefs. The current paper can be seen as a way to refine Davidson's proposal, by introducing a general method for working out what is best in a precise and motivated way. To wit, we treat the disagreement between interlocutors as if it were introduced by a malevolent third party, and understanding communicative acts as part of an optimal strategy against that party.

For example, a rational speaker who tries to communicate an observation of Xena's height with an utterance of "Xena is tall", faces the problem that there is potential or actual variation in speaker and hearer beliefs about Xena, height, Xena's height, and standards of tallness. Letting these differences be our funhouse mirrors, the speaker that knows how to communicate over the channel can calculate the optimal channel distributions in the face of the uncertainty or noise created by the mirrors.

Assuming that the above model is apropos, a basic and welcome result is that even in the face of a malevolent nature, non-trivial exchange of information is possible. That is:

Proposition 2. Communication under uncertainty is possible.
It's not obvious it should be so, although many scholars implicitly assume something like the above without argument; in an information channel game, the possibility of communication under uncertainty can and must be demonstrated. Here is where standard mathematical results have a voice. In an information

[^37]channel game, provided limited amounts of uncertainty, (i) a minimax solution exists, (ii) it's value is a positive amount of mutual information or overlap, and (iii) when the noise or uncertainty becomes too large, as should be expected, communication will fail [10, 11].

Suppose that the speaker observes Xena's height and says "Xena is tall", and the hearer knows that Xena is a warrior princess and has some guesses about the heights of warrior princesses and related standards of tallness. Then the hearer will come to know something about Xena's height even if there's some disagreement about what counts as tall for a warrior princess. This follows from the existence of a minimax solution with positive mutual information for limited amounts of uncertainty. On the other hand, if the hearer does not know what sort of entity Xena is, or thinks warrior princesses are a kind of flower, things will not turn out so well. For in this case there will be a very large mismatch between the speaker and hearer's distributions of Xena's height and the relevant standard or what counts as tall. In such circumstances it is quite possible that interpretation will fail, in the sense that the communicative act will not convey any information about Xena's height: chalk up a victory to malevolent nature. Fortunately, interlocutors commonly know enough about each other that they can make use of an information channel and succeed in meaningful information exchange.

There are two kinds of distributions that rational speakers and hearers must know to use an information channel: the prior probabilities and the conditional probabilities. In our example, the former are the distributions of Xena's height and tallness and the latter are distributions relating Xena's height to tallness and vice versa. The most important of these is the posterior distribution of Xena's height given an utterance of "Xena is tall". This allows a hearer to recover (estimates of) the speaker's observations.

Proposition 3. The information conveyed ${ }^{5}$ in communication under uncertainty is the posterior probability distribution of the input observations.

Typically in an information theoretic model the hearer decodes an utterance as follows: it is the most likely input observation given the output utterance. But this is problematic if a unique best observation does not exist, since selecting one reduces to choosing randomly from the posterior. As an alternative, we suggest not worrying about decoding at all. The information conveyed by communication under uncertainty is more generally the increased knowledge that a hearer has about the possible observations a speaker made. E.g. if a speaker says "Xena is tall", what a hearer knows for sure is a distribution describing the speaker's observation of Xena's height. This even holds in the case when there is no way for the hearer to recover a unique best threshold of height! The information conveyed

[^38]in the communication is not an exact observation of Xena's height relative to the standard. Rather, the information conveyed is whatever knowledge would, in the best case, allow decoding, and, in the worst case, allow the hearer to draw conclusions about what possible observations a speaker could have made of Xena's height. This takes us to propose a working definition of what it is for a claim involving a scalar predicate to be vague:

Definition 4. Vague: A claim involving a scalar predicate about an entity is vague iff for some range of observations of the value the entity takes on the scale, the information conveyed does not reliably determine whether those observations are compatible with the truth of the claim.

To see how this applies, consider again the predicate tall, which, as noted, is typically defined as a relation between a measure of height and a standard of comparison or comparison class. Suppose that the claim "Xena is tall" is made after an observation that Xena is 1.8 m tall. Put in terms of information conveyed, the question is whether on the basis of hearing and accepting the claim "Xena is tall", a hearer would be in a position to say with complete certainty whether the observation that Xena is 2 m tall is correct or not. And the answer is no, because the hearer has only a statistical distribution for the standard of height required for tall to be predicated of an individual, and there may be a non-zero probability that the standard is higher than 2 m . Thus tall is vague.

We may contrast the case of tall with the case of taller than 1.8 m . To the extent that the degree $1.8 m$ is itself precise, the expression taller than $1.8 m$ turns out not to be vague under our definition. For any observation that Xena is X meters tall, for some X , it can reliably be determined whether the claim "Xena is taller than 1.8 m " is compatible with the observation.

We note here that the inability of the information conveyed to reveal a precise observation creates the appearance that facts underlying vague expressions are indeterminate, gappy, or simultaneously true and false. But this is only an illusion much like an observation made through a funhouse mirror. There is a fact to the matter of an observation that underlies a vague sentence, but it is not part of the information conveyed.

At this point you may think that this definition reiterates a common definition of vagueness vis-a-vis borderline cases. Crucially it does not. This is clearer if we recognize that communication games include not just the input of an observed height and standard or comparison class but the context, the situation, the goals of communication, etc. If any of these, too, can only be known up to the posterior distribution, then the cases in which the information conveyed is unreliable for the determination of truth multiply. Vagueness, here, is uncertainty in the information conveyed and whether it can be used to determine the facts.

With the definition of vagueness in hand, we come to the central result:

## Proposition 4. Vagueness is rational under uncertainty.

The rationality of vagueness follows directly from its definition and from constraints on maximizing mutual information with respect to uncertainty. If
there is any uncertainty between a speaker and hearer then the resulting channel distributions, the best or rational way for the speaker and hearer to use the channel, have a margin of error or non-negative categorization error [8]. I.e. the information conveyed by an utterance of "Xena is tall" will be a non-trivial distribution over Xena's height. Vagueness is immediate.

## 4 Conclusions

Most theories of vagueness agree, as we do, on the point that vague expressions are uncertain or imprecise $[17,18,19]$. Where we've gone further is by giving a reason for the imprecision and saying how rational speakers and hearers cope with it and why they are happy to accept it or even prefer it. And from that, we can say why the sorites and epistemic uncertainty are not surprising.

Consider Xena and Callisto in a sorites sequence: if both are tall, then Callisto may be a hair's breadth shorter than Xena and yet still tall. Without reference to heights or standards, this case seems to, incorrectly, confirm a general inductive step. In our model, the distribution by which this inference is made treats Xena and Callisto as all but indistinguishable; indeed, we may even be psychologically unable to distinguish the information conveyed about adjacent individuals in a sorites sequence. So if Xena is tall, we correctly predict an inference from the first to the second, but we also predict that the inference should not continue much further. According to the statistical model we employ, each distribution along the scale is (slightly) different, and to the extent that speakers and hearers reason with such models, it is predicted that statements made about individuals far apart on the scale convey different information, i.e. different distributions over possible observations. The confidence as well as the uncertainty that speakers and hearers have does not remain constant moving along the scale. Thus if we were to allow Callisto to be 30,000 hair's breadths shorter than Xena, then the inference from "Xena is tall" to "Callisto is tall" will not necessarily be made with the same confidence. This is, of course, precisely what we observe.

Putting aside the sorites, consider our proposal in the light of previous linguistic accounts of vagueness. The logical revisions in supervaluationist [4, 7] and dynamic accounts [20] try to eliminate imprecision rather than bringing it to the fore. Consider the issue of higher-order vagueness: the vagueness which arises in defining precise regions of vagueness. If in a certain region on a scale truth values are indeterminate, then these new boundaries themselves fail to be precise. The awkward result is that imprecision remains as ever more regions of higher-order vagueness are added. Since we embrace imprecision within our model with statistical uncertainty, we never have to make a decision about where precision stops and imprecision begins.

It is also quite common to attack vagueness with more sophisticated ways of comparing individuals to standards of comparison or comparison classes [5, 19]. This hints at the role of uncertainty and may provide an adequate modeltheoretic semantics, but these theories are silent regarding the source of the ordering relations. Are they the products of thought? Should we expect them to
be viable strategies in communication? We do not disagree with these modifications, but do believe they can be better motivated by looking at the properties of rational communication. ${ }^{6}$

Our main claim is that vague scalar adjectives convey insufficient information to decide the degrees and standards of comparison upon which they supervene. I.e. a vague predicate has truth conditions and it will be true or false but these facts are absent from the information conveyed in communication. This is similar to Williamson's $[24,25]$ epistemic view, which characterizes vagueness as a form of essential ignorance. When vague expressions are used, as speakers and hearers, we are only concerned with knowledge up to a margin of error; we are ignorant of the precise facts. Williamson's claims are merely observational, perhaps stipulative, but they can be substantiated by a formal model such as ours. ${ }^{7}$ The epistemic view, on its own, does not make it especially clear why ignorance bubbles up into communication (it's not obviously necessary; precise languages are staples in both philosophy and information theory) or why margins of error exist. In an information channel, though, we have ignorance because margins of error are unavoidable thus making ignorance rational under uncertainty. The ignorance in vagueness is strategic ignorance. Additionally, whereas Williamson $[24,25]$ gives a somewhat vague explanation for the widely accepted idea that vagueness supervenes on precision, we make it precise: vagueness is the product of limits on the information conveyed, information which supervenes on the precise facts in a statistical sense.

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# Restricted Quantification over Tastes 

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#### Abstract

This paper provides an analysis of statements with predicates of personal taste (tasty, fun, etc.) Rather than directly relativizing semantic interpretation to a judge (cf., Lasershon, 2005), this paper aims to capture the phenomenon called 'faultless disagreement' (the fact that one can deny a speaker's subjective utterance without challenging the speaker's opinion) by means of pragmatic restrictions on quantification domains. Using vagueness models, a statement like the cake is tasty is analyzed as true in a partial context c iff it is true in the set of completions t consistent with c (Kamp, 1975), wherein tasty denotes different, contextually possible, taste measures (Kennedy, 1999). Phrases like for me restrict the set of completions to those with taste measures consistent with the speaker's taste. Faultless disagreement naturally follows assuming speakers accommodate or reject implicit restrictions of this sort (Lewis, 1979).


Keywords: Taste; faultless disagreement; vagueness; context restriction.

## 1 Disagreements over Taste

One can deny an utterance like the cake is tasty or running is fun without challenging the speaker's opinion. The speaker asserts ' $\varphi$ ', his addressee ' $\neg \varphi$ ', and still neither can be blamed for making a mistake. Lasersohn (2005); MacFarlane (2005), and Egan et al. (2005), among others, illustrate that such 'faultless disagreements' characterize, beside statements about taste, also aesthetic, moral and probability statements, future contingents, vagueness, and epistemic modals. These authors aim to account for faultless disagreements by relativizing semantic interpretation to a judge (or 'context of assessment'). On this 'relative truth' approach, contexts specify in addition to a speaker, a world and a time of evaluation, also a judge. Due to variance in the judge-world-time parameters, the truth values of statements with, e.g., taste predicates, may vary between contexts (cf., (1a)), although their content remains the same (1c).
a. $\quad$ The cake is tasty $\rrbracket_{c, i, \mathrm{a}}=1$ iff $\llbracket T h e ~ c a k e ~ \rrbracket_{c, \mathrm{i}, \mathrm{a}} \in \llbracket \operatorname{tasty} \rrbracket_{\mathrm{c}, \mathrm{i}, \mathrm{a}}$ (where c is a context, i a world-time pair and a the judge).
b. $\quad$ The cake is tasty for Bill $\rrbracket_{c, i, a}=1$ iff $\llbracket$ The cake is tasty $\rrbracket_{c, i, B i l l c,, i, a}$
c. $\quad \llbracket$ The cake is tasty $\rrbracket_{c}=1$ iff $\llbracket$ The cake is tasty $\rrbracket_{c}(W(c), A(c))$ (where $W(c)$ and $A(c)$ are the world-time pair and judge in $c$. .)

In this setting, faultless disagreement arise due to shifts in the contextual parameters, usually triggered by speakers' tendency towards autocentric interpretations, e.g., while a speaker may truthfully assert the cake is tasty based on herself as a judge, her addressee may truthfully assert the cake is not tasty, with himself as the judge. Still, no cake is both tasty and not tasty in any single context.

Dominant opponents of this approach argue against it based on theoretical and empirical considerations (for a detailed discussion see von Fintel and Gilles, 2008a). Importantly, if semantics is subjective to the extent suggested by relative truth theories, then why do speakers ever bother to deny others' utterances at all?

On the other side of the spectrum, theories claim for standard, 'impersonal' interpretations for taste predicates (Nouwen, 2009; Wolf, 2009), such as those in (2).
(2) a. $\quad$ The cake is tasty $\rrbracket_{i}=1$ iff $\llbracket$ the cake $\rrbracket_{i} \in \llbracket$ tasty $\rrbracket_{i}$.
b. $\quad$ Bill finds the cake tasty $\rrbracket_{i}=1$ iff $\llbracket$ the cake $\rrbracket_{i} \in \llbracket$ tasty $\rrbracket_{i}$, for all indices i consistent with Bill's subjective experience.

Faultless disagreements are explained by virtue of the vagueness of taste predicates. We are inherently unable to reach full knowledge of the extension of expressions like tasty. Consequently, we can only base our claims on our own sensory experience (the gastronomic pleasure we feel while eating things), as well as on weak clues others give us about their experience. Thus, all edible things are always borderline of taste predicates (Nouwen, 2009).

Formally, vague predicates are often interpreted within contexts c , via a set of indices $\mathrm{T}_{\mathrm{c}}$, the worlds (Stalnaker 1978) or completions (van Fraassen, 1969; Kamp, 1975) consistent with the information in c (completions being 'classical' contexts, wherein every statement is either true or false). Truth of a statement $S$ in $c$ is defined based on these indices as follows (time indices are avoided, for simplicity sake):
(3) $\quad S$ is true in $c$ iff $S$ is true in every $t \in T_{c} ; S$ is false in $c$ iff $S$ is false in every $t \in T_{c}$, and $S$ is undetermined in $c$, otherwise.

The 'impersonal', vagueness based theory considers every taste statement always undetermined in actual contexts c. This has a variety of consequences. First and foremost, even when no attitude report or for/ to PP is present, there is still the intuition that taste predicates express someone's taste (after all, the most trustworthy source of beliefs about taste comes from our private sensory experience). Second, there is nothing scalar about taste predicates, as everything forms a borderline case. The problem is that if personal tastes do not tell us anything about the impersonal interpretation of tasty, the theory about it is impossible to refute. And if personal tastes do show anything, then, the large-scale taste differences between people prove false the idea of a single impersonal interpretation.

## 2 A New Proposal

In this paper, focusing on predicates of personal taste, I argue that relativity does not enter the semantics, except through independently-motivated, pragmatic mechanisms. While the approach developed in this paper is eventually vagueness-based, it also differs from, e.g., Nouwen (2009), in important respects. Part 2 elaborates on its different components and how they bear on the personal and public aspects of taste predicates. Part 3 presents a variety of consequences. In addition, it grounds the discussion within a broader framework of linguistic analysis of different types of expressions with 'personal' ingredients.

### 2.1 The Personal Ingredient

First and foremost, this paper claims that there is no such thing as "one true answer" when it comes to taste. Do you, the readers, like salty French fries or sweet cream cakes, both or neither? Do you prefer Mozart to Bach, or the opposite? Let alone opera sopranos or rock stars. Different readers can definitely possess different tastes, and probably more often than not, they in fact do. Thus, a single unique interpretation of, e.g., tasty or fun need not necessarily exist in the actual world. In order to formally represent this idea, interpretation in contexts $c$ can be modeled via the set $T_{c}$ of completions $t$ consistent with the information in c . These indices can be richer than worlds. For example, in Kamp (1975) completions determine cutoff points for vague adjectives, although the author holds that no such thing as a cutoff point exists in the actual world. On the present proposal, completions determine full fledged interpretations for, e.g., tasty. Each corresponds to the taste of one possible individual. Thus, different completions differ with respect to the interpretation of tatsy, while none corresponds to the actual 'objective' (inter-personal) interpretation (as such probably does not exist).

What is the basic interpretation of tasty in each completion t? Personal taste predicates P are typically gradable (cf., the felicity of tastier, as tasty as, very / too /fairly tasty, etc.), though the existence of different tastes imply different scales. Therefore, this paper associates taste predicates in each completion $t$ with degree functions, $\mathrm{f}(\mathrm{P}, \mathrm{t})$, i.e. mappings of entities to degrees (cf., Kennedy, 1999). Thus, tasty holds true of an object $x$ in $t$ iff the value $f(t a s t y, t)(x)$ exceeds the cutoff point (standard of membership) of tasty in t , standard(tasty,t), as illustrated in (4). Tastier holds true of an object pair $\langle x, y\rangle$ in $t$ iff the value $f($ tasty, $t)(x)$ exceeds the value $\mathrm{f}($ tasty, t$)(\mathrm{y})$, as illustrated in (5).

$$
\begin{equation*}
\llbracket \text { The cake is tasty } \rrbracket_{c}=1 \text { iff for all } t \in T_{c}, \| \text { the cake } \rrbracket_{t} \in \llbracket \text { tasty } \rrbracket_{t} \tag{4}
\end{equation*}
$$

Iff for all $\mathrm{t} \in \mathrm{T}_{\mathrm{c}}, \mathrm{f}($ tasty, t$)\left(\left[\right.\right.$ the cake $\left.\rrbracket_{\mathrm{t}}\right)>$ standard(tasty, t$)$.

[^40]【The cake is tastier than the ice cream】 $\mathbb{c}=1$
Iff for all $t \in T_{c},<\llbracket$ the cake $\rrbracket_{t}$, ${\text { the ice cream } \rrbracket_{t}>\in \llbracket \text { tastier } \rrbracket_{t}}$
Iff for all $t \in T_{c}, f($ tasty, t$)\left(\llbracket\right.$ the cake $\left.\rrbracket_{\mathrm{t}}\right)>\mathrm{f}($ tasty, t$)\left(\llbracket\right.$ the ice cream $\left.\rrbracket_{\mathrm{t}}\right)$
Modifiers and subordinators such as for $X$, to $X$, in $X$ 's opinion, I find $X P$ or $I$ consider $X P$, are, therefore, explicit means of subjectively restricting contexts. For example, the cake is tasty for me is true in c iff the cake is tasty is true in every completion $t$ of $c$ in which the values of $f($ tasty, t$)$ and standard $($ tasty, t$)$ are consistent with my own taste: Entities' values represent my opinion about their tastes, and so is the cutoff point between tasty and not-tasty.

$$
\begin{align*}
& \llbracket \text { The cake is tasty for Dan } \rrbracket_{c}=1 \text { iff }  \tag{6}\\
& \text { For all } t \in \mathrm{~T}_{\text {Dan }} \subseteq \mathrm{T}_{\mathrm{c}}, \mathrm{f}(\text { tasty }, \mathrm{t})\left(\llbracket \text { the cake } \rrbracket_{\mathrm{t}}\right)>\text { standard }(\text { tasty }, \mathrm{t}) \text {. }
\end{align*}
$$

As the information these constituents provide is presupposed, not asserted, it tends to be preserved under negation, e.g., It is not tasty for Sam doesn't normally mean it is tasty, but not for Sam.

### 2.2 The General (Public) Ingredient

Second, according to the present proposal, although tastes are personal, information about the interpretation of taste predicates can become publicly available.

Information about particular tastes can be gained through individual eating experiences, based on which generalizations on taste can be inferred. Thus, we can reasonably say that oil does not taste well, but chocolate does. Some people are less crazy than others about chocolate, but almost no one considers it disgusting. The opposite is the case with regard to oil. In fact, one's ability to draw generalizations about the taste of different groups of people plays an important role in one's social and cultural life. Conversations and disputes regarding utterances like, the cake is tasty are a main tool to this end. For example, it is publicly known that not everyone loves, say, avocado salads. Thus, before offering such a salad one is likely to consult with her partner about the matter. Similarly, before choosing a film to go to on a first date, one would usually try to find out whether her partner finds romantic comedies more fun than horror films, or vice versa, whether mainstream is fine, or independent cinema is preferred, and so on and so fourth. This is important because speakers order tastes in hierarchies. They argue for or against these orderings based on their cultural appropriateness or fitness to the spirit of the time and circumstances. Speakers do all that by uttering and disputing taste statements, thereby expressing or negotiating social dominance relations (thus, formally, completions are ordered by contextual relevance depending on how relevant and important the taste functions in them rank).

To recap, due to all that, if, for instance, one is to invite guests for dinner (including, say, one's bosses), one can fairly safely choose to serve pasta with a Bolognese sauce, rather than, say, an avocado with mint salad. But if some guests are vegetarian, then one may better go for a fungi cream sauce. And if some have
children, getting the simplest sort of Ketchup, or even leaving some Pasta with no sauce at all, is probably a very good idea (adults will not like it, though). Of course, these and many others descriptions of facts about tastes are non-perfect generalizations. They admit exceptions. This brings us to the next point.

### 2.3 Restricted Generalizations: Synthesis of the Personal and General

Third, quantification in natural languages is by default restricted. Consider, for example, the quantifying expression everything in (7a). The domain of the universal quantifier denoted by everything clearly does not include every possible object, only sites in Paris, or maybe even only famous or adored sites.
(7) I lived near the Seine, near Boulevard St. Germain and Rue St. Michel, near the market and the Pantheon, near everything (Haaretz, 04.01.2002).

Conventionally, contextual restrictions on quantifying expressions are represented by a context variable (say-, $\mathrm{X}_{\mathrm{t}}$ ), whose value is a set of relevant individuals (cf., von Fintel 1994). Accordingly, the truth conditions of a statement with a quantifying expression, like (8a), require that every individual, which is a duck and is in the set of relevant individuals will be in the denotation of lays whitish eggs.

$$
\begin{align*}
& \forall \mathrm{t} \in \mathrm{~T}_{\mathrm{c}}: \llbracket \mathrm{A} \text { duck lays whitish eggs } \rrbracket_{\mathrm{t}}=1 \text { iff } \forall \mathrm{x} \in\left(\llbracket \text { duck } \rrbracket_{\mathrm{t}} \cap \mathrm{X}_{\text {duck }, \mathrm{t}}\right):  \tag{8}\\
& \mathrm{x} \in \llbracket \text { ays whitish eggs } \rrbracket_{\mathrm{t}}\left(\mathrm{X}_{\text {duck,t }} \text { being the set of relevant entities in } \mathrm{t}\right) .^{2}
\end{align*}
$$

We also find restrictions in theories of conditionals (Kratzer 1979, 1986; Kadmon and Landman 1993). The conditional in (9a) is restricted via $\mathrm{X}_{\text {John subscribes to a newspaper }}$ to be only about subscriptions to a newspaper that John can read. (9b) is restricted to eventualities (or completions) in which there is no oil in the tea. This is crucial, for instance, to account for the fact that, intuitively, (9b) fails to entail (10).
(9) a. If John subscribes to a newspaper, he gets well informed.
b. If there is sugar in the tea, the tea tastes well.

If there is sugar and oil in the tea, the tea tastes well.
Thus, grammar encompasses mechanisms of implicit domain restriction (Partee, 1989; Kratzer 1979, 1986; von Fintel 1994). They can be readily used also for our present purposes. Thus, we can say that some things (e.g., oil) are tasty according to no 'relevant' taster in a given context (restricting the tasters to be human, with a typical taste bud system, etc.) Other things (e.g., Pasta Bolognese) are tasty according to all tasters in a contextually given set (we do not always have to worry about, e.g.,

[^41]children or vegetarian, anymore). Thus, in each index, tasty measures the extent of gastronomic pleasure an eating event causes a certain type of subject. The subject in question, though, is most often not specified, allowing hearers to take into account all the contextually plausible and relevant tastes. Disputes (or agreements) about taste make sense precisely because taste statements are general, rather than personal.

To be sure, denotations of predicates are often interpreted restrictively even in the absence of a quantifying expression. Consider, for example, utterances of negated predicates like not a bird or non-birds in a context of a zoo. Hearers hardly ever interpret these predicates as referring to the garbage cans or to the cages or fences; nor do they interpret them as referring to visitors in the zoo, though all these constitute members of the given denotations. Moreover, hearers do not normally assume that sentences like Tweety is a bird are about ostriches. Atypical birds are, by default, considered irrelevant. ${ }^{3}$ Finally, context restrictions are certainly at play when statements with vague predicates such as the line is long are evaluated. We can assert such statements only when we contextually restrict the set of possible cutoff points.

For the purposes of this paper (representing faultless disagreements), I make do by representing implicit context restrictions in taste statements via accommodation of, e.g., an implicit for phrase or find subordinator's interpretation (Lewis, 1979), but for alternative proposals concerning the representation of implicit context restrictions see von Fintel (1994) and Stanley and Szabo (2000).
von Fintel and Gilles (2008) argue for a 'restricted quantification' analysis of faultless disagreement in statements with epistemic modality. Epistemic modals quantify over possibilities consistent with a relevant information state, where contexts of utterance decide whose information state that is. But given a context of utterance, there are multiple ways of drawing the boundaries of the group holding the relevant information. Thus, it is indeterminate just which set of possibilities is quantified over by bare epistemic modals.

Crucially, in von Fintel and Gilles (2008), the group whose knowledge is under discussion only enters into play indirectly (the set of possibilities forming the modal base is construed of worlds consistent with the information distributed over the group members). This analysis has an appealing advantage. Epistemic modals maintain the interpretation type other modals have (quantifiers over a modal base). For the very same reason, there is no a priori reason against taking the group of judges (the subjects whose taste is under discussion) to affect the truth conditions of taste statements only indirectly. The set of possibilities based on which a vague taste adjective is interpreted is construed based on the tastes of the group members. This analysis has an appealing advantage. Adjectives of personal taste maintain the interpretation type and characteristics of other vague adjectives. Let us, then, present the main consequences of such a proposal. ${ }^{4}$

[^42]
## 3 The Consequences of Restricted Quantification over Tastes

First and foremost, the conjunction of two sentences such as those in (11a-b) is a contradiction in the absence and only in the absence of an appropriate context restriction. The contradictory interpretation illustrated in (12a-b) is that the cake is both above and below tasty's standard in any completion $t$ of $c$ (i.e., according to any possible, conceivable, taste measure and cutoff point in c.)
a. (Dan:) The cake is tasty .
b. (Sam:) No it's not.
a. $\quad \forall \mathrm{t} \in \mathrm{T}_{\mathrm{c}}, \mathrm{f}($ tasty, t$)\left(\left[\right.\right.$ The cake $\left.\rrbracket_{\mathrm{t}}\right)>$ standard $($ tasty, t$)$.
b. $\quad \forall \mathrm{t} \in \mathrm{T}_{\mathrm{c}}, \mathrm{f}($ tasty, t$)(\llbracket$ The cake $\rrbracket \mathrm{t}) \leq \operatorname{standard}($ tasty, t$)$.

Second, context restriction (e.g., via accommodation) can turn the interpretation equivalent to that of sentences (13a-b) (Lewis, 1979). When discourse participants are cooperative, striving for a non-contradictory interpretation, they are likely to assume that context is thus restricted. The result is the non-contradictory interpretation in (14a-b).
(13) a. The cake is tasty (for Dan / in Dan's opinion).
b. No it's not (for Sam / in Sam's opinion).
a. $\forall t \in T_{c}$, s.t. the values of $f($ tasty,t) and standard(tasty,t) represent Dan's taste in $\mathrm{c}, \mathrm{f}($ tasty, t$)\left(\|\right.$ The cake $\left.\rrbracket_{\mathrm{t}}\right)>$ standard $($ tasty, t$)$.
b. $\quad \forall \mathrm{t} \in \mathrm{T}_{\mathrm{c}}$, s.t. the values of $\mathrm{f}($ tasty, t$)$ and standard(tasty,t) represent Sam's taste in $\mathrm{c}, \mathrm{f}($ tasty, t$)\left(\llbracket\right.$ The cake $\left.\rrbracket_{\mathrm{t}}\right) \leq$ standard $($ tasty, t$)$.

If Dan and Sam's tastes are different, they are adequately represented by different taste functions and/or cutoff points, namely by two different, non-overlapping sets of indices ( $\mathrm{T}_{\text {Dan }} \subseteq \mathrm{T}_{\mathrm{c}}$ and $\mathrm{T}_{\mathrm{Sam}} \subseteq \mathrm{T}_{\mathrm{c}}$, but $\mathrm{T}_{\text {Dan }} \cap \mathrm{T}_{\text {Sam }}=\varnothing$ ), differing along the interpretation of tasty. Thus, it may well be the case that in every t in $\mathrm{T}_{\mathrm{Dan}}$, the cake's degree of taste exceeds the standard, but in no $t$ in $T_{\text {sam }}$, the cake's degree does so. Still, the speakers may well agree that the indices in both these sets are consistent with the common ground, i.e., the interpretation of tasty in each represents a legitimate taste in c.

At any rate, such a polite discussion, with two purely personal interpretations, is characteristic of first dates or highly official meetings with very important personalities. Let us consider Dan and Sam after some period of happy relationships. Now they are less busy being polite (rendering utterances of the partner true), and more busy getting to know one another. Now Sam is more likely to respond to utterances such as this c.d. is fun or this salad is tasty with something like C'mmon, that's teenage music! or No way! How can an Avocado-mint salad be tasty?

Luckily, given the present analysis there is a natural sense in which two speakers in a dialogue such as (11a-b) may disagree. In uttering (11b) a bit less apologetically (or more assertively) than in a first date, Sam may imply that she prefers evaluating the asserted statement relative to a different set of taste functions and/or cutoff points,
perhaps because she views them as superior (more plausible or relevant), and hence more appropriate in c (more likely to be considered part of $\mathrm{T}_{\mathrm{c}}$ ). What is more, despite our pluralism with regard to taste, we all agree that, say, soap doesn't taste. Not everything goes. Thus, Sam's non-use of an explicit restrictor (e.g., for Sam) may even convey that in c we all agree that the cake doesn't taste (let us represent this proposition as $\neg \varphi$ ), i.e., that (11b) (namely, $\forall t \in T_{c}, \llbracket \neg \varphi \rrbracket_{\mathrm{t}}=1$ ) is true, while (13a) (namely, $\forall \mathrm{t} \in \mathrm{T}_{\text {Dan }}, \llbracket \varphi \rrbracket_{\mathrm{t}}=1$ ) is inappropriate, as $\mathrm{T}_{\text {Dan }} \cap \mathrm{T}_{\mathrm{c}}=\varnothing$.

We have just illustrated a personal interpretation vs. public interpretation scenario. Alternatively, in a bad day, Sam may interpret Dan non-restrictively, as conveying (11a) (namely, $\forall \mathrm{t} \in \mathrm{T}_{\mathrm{c}}, \llbracket \varphi \rrbracket_{\mathrm{t}}=1$ ), and reject that on the basis that c is more pluralistic. It is consistent with completions in which the cake isn't tasty. Sam can take her own taste to form evidence for that $\left(\exists \mathrm{t} \in \mathrm{T}_{\mathrm{Sam}} \subseteq \mathrm{T}_{\mathrm{c}}, \llbracket \neg \varphi \rrbracket_{\mathrm{t}}=1\right)$. This is a public vs. personal scenario. It is not cooperative in that Sam's response does not render Dan's utterance true (cf., von Fintel and Gilles, 2008). Dan could have been taken to base his generalization on his personal experience alone, but he was taken to provide a more general conjecture.

Thus, disagreements are taken to be faultless in a context c iff different context restrictions (and hence different completion sets) are used, whose legitimacy both sides appreciate. This condition is not always met, in particular not in personal vs. public scenarios characteristic of 'academic' discourse about art, food, and the like. In disagreements between students and their professor or between a listener and an expert on a Radio program, the responders are taken to 'know more' about taste than the speakers, whose views might, therefore, be considered mistaken (if they are not assertive, their tastes might drop off the contextually reduced common grounds).

Conversely, the public vs. personal scenario is characteristic of, for instance, mothers trying to gently convince their children to eat healthy food. A mother may be in a position to assert a statement like This cheese is very tasty if, say, the children she knows find it tasty. She may assert the statement even if she herself does not find the cheese tasty, because adult tastes may simply be irrelevant. ${ }^{5}$ If mother cannot really tell what her child's taste is like, she can only convey that $\forall t \in\left(\cup\left\{T_{x}: x\right.\right.$ is one of the other children mother knows $\}$ ) $\subseteq \mathrm{T}_{\mathrm{c}}$, $\llbracket$ This cheese is tasty $\rrbracket_{t}=1$. At the same time, mother may conjecture or ask about the interpretation based on (i) her child's taste, or (ii) her child's taste together with the taste of the other children she knows or additional children (von Fintel and Gilles, 2008). The child, who may well be convinced that a candy is tastier to eat, may answer Yucky, this cheese is disgusting! Being the speaker, a child, and one who is expected to eat the cheese, he can legitimately consider himself part of the group whose tastes are relevant. As such, his view about the cheese gives sufficient evidence against mother's conjectures. The child can confirm or deny the strongest proposition she may have issued, whose truth value he presumes to know (von Fintel and Gilles, 2008 and references therein). Confirming her own proposition (as in \#ok, it is tasty for every child you know) is not informative enough, certainly if he considers the cheese disgusting. One appropriate

[^43]answer is then No, this cheese is disgusting, which can only be based on the child's own taste $\left(\forall \mathrm{t} \in \mathrm{T}_{\mathrm{me}} \subseteq \mathrm{T}_{\mathrm{c}}\right.$, $\llbracket$ this cheese is disgusting $\left.\rrbracket_{\mathrm{t}}=1\right)$. This interpretation is strong in that it entails that the cheese is not merely in the gap of tasty in c , but rather is in the negative denotation (which entails the falsity of (i), i.e. of "it is tasty for me"). Another appropriate answer is No, this cheese is not tasty, based on the taste of a group containing him and perhaps all other possible children. This answer conveys that $\neg \forall \mathrm{t} \in\left(\cup\left\{\mathrm{T}_{\mathrm{x}}: \mathrm{x}\right.\right.$ is a child $\left.\}\right) \subseteq \mathrm{T}_{\mathrm{c}}$, $\llbracket$ This cheese is tasty $\rrbracket_{\mathrm{t}}=1$, which entails that (ii) ("it is tasty for every child you know plus me") is not true. Denial makes sense because an interpretation based on a larger set of tastes (than those based on which mother made her assertion) is there to deny (von Fintel and Gilles, 2008).

So far we have illustrated how disagreements on the application of taste predicates may arise due to inherent indeterminacy regarding the degree function they denote. This kind of disagreements is impossible if tasty in, say, (11), is substituted by a predicate such as tall. The latter's degree function is fixed across contexts, or at least determines a context invariant ordering between entities' (based on their heights). Still, Sam and Dan can disagree about the comparison class. Sam may assert that Joe is tall based on Joe being taller than her (i.e. based on indices in which Joe and her form the comparison class), and Dan may disagree saying no, Joe is not tall!, based on Joe's being shorter than him (indices in which Joe and him form the given class).

Furthermore, again, a for phrase can provide a restriction to indices with a given comparison class, as in Mary is tall for her age/ school. In addition, in, for instance, these cookies are tasty for cats, the for phrase operates as a restrictor both at the level of the comparison class and at the level of the taste functions in question. Moreover, for phrases can restrict epistemic modal bases (as in for all that I know, ...) Finally, the same data can be found in other languages, like Hebrew and Italian. Altogether, the data support an analysis of for phrases as temporarily restricting evaluation contexts.

To sum up, the present approach captures different types of personal ingredients of interpretation and their relation to the common ground. It provides unified means to account for a variety of ingredients that grammar collapses together through the use of for phrases (e.g., personal degree functions, comparison classes, and epistemic modal bases). No new grammatical mechanisms are introduced. Independently-motivated, pragmatic mechanisms (accommodation of context restrictions) suffice. While the availability of faultless disagreements supports a classification of taste predicates as vague or indeterminate, it does not support their classification as true relative to a judge (Lasersohn, 2005). Nor does their availability depend on the way a personal ingredient may be realized (as indices, implicit indexicals, or non-indexical parameters). Rather, it depends on the existence of indeterminacy. If it is possible to interpret an ingredient affecting the truth conditions as general, the very attempt to generalize invokes disputes. If it is possible to withdraw (restrict the domain of application of the generalization) disagreement becomes faultless.

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# Vagueness Facilitates Search 

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#### Abstract

This paper addresses the question why language is vague. A novel answer to this question is proposed, which complements other answers suggested in the literature. It claims that vagueness can facilitate search, particularly in quasi-continuous domains (such as physical size, colour, temperature), given that different speakers are likely to attach subtly different meanings to words (such as "tall", "blue", "hot") defined over such domains.


## 1 Introduction

Two questions dominate theoretical research on vagueness. The first is of a logical-semantic nature: What formal models offer the best understanding of vagueness? Many answers to this question have been proposed (see e.g. Keefe and Smith 1996, Van Rooij 2009), yet it is fair to say that none of these has found general acceptance so far. The second question is of a pragmatic nature and asks Why is language vague? This question has been asked forcefully by the economist Barton Lipman, who has shown that some seemingly plausible answers are at odds with classical Game Theory (Lipman 2000, 2006). While a number of tentative answers to this question have been suggested (for an overview, see Van Deemter 2009 and Van Deemter, to appear), Lipman's is still in many ways an open question, particularly with respect to situations where there is no conflict between the speaker and the hearer (cf., Crawford \& Sobel 1982).

Our paper will focus on the second question, but in doing so we hope to obtain some insights into the first question as well. We argue, primarily, that vagueness can facilitate search; additionally we argue that Partial Logic is better placed to explain this than Classical Logic, and that theories that give pride of place to degrees (including two-valued theories that include degrees, e.g., Kennedy 2007) are even better placed than Partial Logic to do this. Having said that, we do not claim that facilitation of search is the only rationale for vagueness, or that degrees are necessary for explaining the benefits of vagueness: a non-quantitative model involving an ordinal scale might be equally suitable.

## 2 Informal outline of the argument

Let's call a domain quasi-continuous if it contains some different objects which resemble each other so much (in the relevant dimension) that they are indistinguishable in practice. Domains do not have to be mathematically continuous to
have this property: it suffices for them to contain objects that are similar enough in the relevant dimension (a person of 180.1 cm and one of 180.2 cm height, for example) that they cannot be told apart given the measurement tools at hand. Examples abound, including the heights of all the people you know, or all the colours that you have seen.

In a quasi-continuus domain, it is difficult for people to align the meanings of the predicates defined over them: there are bound to be people that one speaker calls 'tall' that another does not. Arguments to this effect can be found in many different places. Hilbert (1987), for example, who focusses on colour terms, explains how the differences in people's eyes (e.g., in terms of the density of pigment layers on the lens and the retina) make it unavoidable that one normally sighted person can often distinguish between colour patches where another cannot. Another example is Reiter et al. (2005) on temporal phrases, where it was shown that different speakers use different criteria (e.g., dinner time or the time when the sun sets) to determine the start of the evening, for example. (For discussion, see van Deemter (to appear)). Rohit Parikh has written insightfully about this phenomenon, and we shall use and adapt one of his examples. ${ }^{1}$

In Parikh's original story of Ann and Bob, Ann asks Bob to find her book on topology, adding that "it is blue" (Parikh 2000). Ann and Bob use different concepts of 'blue', but Parikh's point is that if the overlap between them, as compared to their symmetric difference, is sufficiently large then Ann's utterance may still be very useful, because it may reduce the time that Bob should expect to take before finding the referent. All the same, the mismatch between speaker and hearer does cause Bob's search for the topology book to take more time than it would otherwise have done. This is particularly true because the book, let's call it $b$, may be an element of $\|b l u e\|_{A n n}\|-\| b l u e \|_{B o b}$. In this case, Bob must first search all of $\|b l u e\|_{B o b}$, then the rest of the books (i.e., the ones he does not consider blue) until he finds $b$ there. His expected search effort in this scanario can be equated to the cardinality of the set $\|b l u e\|_{\text {Bob }}$ plus half that of the complement of this set. In this "unlucky" scenario, Ann's utterance has led Bob astray: without information about the colour of the book, he could have expected to examine only half the domain. Scenarios of this kind will play an important role in what follows.

In Parikh's story, Ann and Bob both use a crisp (i.e., non-vague) concept 'blue'. In what follows, we will argue that it would be advantageous for Bob (and, by extension, for Ann, who wants the book to be found) if Bob was able to rise above thinking in terms of a simple dichotomy between blue and non-blue. Bob might argue, for example, that if the target book is not found among the ones he considers blue, then it is most likely to be one that he considers borderline blue; so after inspecting the books he considers blue, he would be wise to inspect

[^45]these borderline cases. In a more dramatic departure from simple dichotomy, Ben might even think of the books as arranged in order of their degree of blueness, and start by searching the ones that are most typically blue, followed by the ones that are just slightly less blue, and so on.

Colours are fairly complex, multi-dimensional things. For simplicity, let us focus on the one-dimensional word tall. This will have the effect that, of any two extensions that the word may be assigned in a given situation, one must always be a subset of the other $\left(\|t a l l\|_{A n n}\|\subseteq\| t a l l \|_{B o b}\right.$ or $\|t a l l\|_{B o b}\|\subseteq\| t a l l \|_{A n n}$, or both). More crucially, let us abandon the assumption that Ann and Bob must necessarily always think of the words in question as expressing a crisp dichotomy. ${ }^{2}$ The story of the stolen diamond is set in Beijings Forbidden City, long ago:

A diamond has been stolen from the Emperor and, security being tight in the palace, the thief must have been one of the Emperors 1000 eunuchs. A witness sees a suspicious character sneaking away. He tries to catch him but fails, getting fatally injured in the process. The scoundrel escapes. With his last breath, the witness reports "The thief is tall!", then gives up the ghost. How can the Emperor capitalize on these momentous last words? (Van Deemter, to appear, Chapter 9.)

Suppose the Emperor thinks of tall as a dichotomy, meaning taller than average, for instance. In this case, his men will gather all those eunuchs who are taller than average, perhaps about 500 of them. In the absence of any further clues, he should expect to search an average of as many as 250 tall people (i.e., half of the total number). Matters get worse if the witness has used a more relaxed notion of tall than the Emperor. If this mismatch arises, it is possible that the perpetrator will not be among the eunuchs whom the Emperor considers to be tall. Since the Emperor's concept "tall" makes no distinctions between people who are not tall, (or between ones that are tall, for that matter) the Emperors men can only search them in arbitrary order. In other words, he first searches 500 eunuchs in vain, then an expected $0.5 * 500=250$, totalling 750 . Analogous to what we saw in the previous section, the Emperor would have been better off without any description of the thiefs height, in which case he should have expected to search $0.5 * 1000=500$ eunuchs. The Emperor could have diminished the likelihood of a false start (i.e., a search strategy based on a notion of tall that excludes the thief) by counting more eunuchs as tall. But in doing so, he would have increased the search times that are necessary to inspect all the eunuchs he considers tall. The only way to avoid the possibility of a false start altogether is by counting all eunuchs as tall, which would rob the witness statement of its usefulness.

[^46]If the Emperor thinks of tall as vague, however, then he might separate the eunuchs into three rather than two groups: the ones who are definitely tall, the ones who are definitely not tall, and the borderline cases characteristic of vague concepts. For concreteness, assume 100 eunuchs are definitely tall, 500 are definitely not tall, and 400 are doubtful. Surely, the eunuchs in the "definitely tall" category are more likely to be called tall than the ones in the "doubtfull" category, while no one in the "definitely not tall" category could be called tall. To put some figures to it, let the chance of finding the thief in the group of 100 be $50 \%$ and the chance of finding him in the doubtful group of 400 likewise. Under this scenario, it pays off to search the "definitely tall" eunuchs first, as one may easily verify. In other words, the Emperor benefits from regarding tall as containing borderline cases (i.e., being vague). This thought experiment suggests that borderline cases, and hence vagueness, can facilitate search, because borderline cases allow us to distinguish more finely than would be possible if all our concepts were dichotomies. If your language contains only dichotomous concepts then separating the eunuchs into three different groups does not make sense to you: there are tall eunuchs, not-tall ones, and thats it. But if you understand tall to have borderline cases then you can distinguish between the different people whom you do not consider tall, as well as between the ones you consider tall and all the others.

But if distinguishing between three different categories (tall, not-tall, and borderline tall) is better than distinguishing between just two, then it might be even better to distinguish even more finely. And indeed, the Emperor can do even better than was suggested above, if he uses a ranking strategy. Suppose he has the eunuchs arranged according to their heights. First the tallest eunuch is searched, then the tallest but one, and so on, until the diamond is found. This strategy is faster than each of the other ones if we assume that the taller a person is, the more likely the witness is to have described him as tall. Under this assumption, the same type of advantage obtains as in the previous case (where only borderline cases were acknowledged), but at a larger scale.

This argument suggests an interesting possible rationale for understanding 'tall' (or 'blue', for that matter) as involving borderline cases or degrees, namely that this allows a more efficient search than would have been possible under a dichotomous understanding of these words. But borderline cases and degrees are the hallmark of vagueness. Consequently, if the argument is correct then we have found a so-far unnoticed rationale for vagueness: vagueness can facilitate search.

## 3 Towards a formal development of the argument

In what follows, it will be useful to employ a couple of abbreviations, some of which are nonstandard. The aim of our enterprise is to show that, given a dichotomous model, it is always possible to define a closely resembling vague model, which has a higher utility than the original crisp one, where utility is formalised by the search effort that a model implies on the part of the hearer.

Let's assume that $\mathcal{A}$ is a standard two-valued model of the word 'tall' as defined on a domain $D$ of people, where some people in $D$ are tall (such people are in the extension $\|t a l l\|$ ) and others are not (such people are in the extension $\left.\|\overline{\operatorname{tall}}\|_{\mathcal{A}}\right) . \mathcal{B}$, by contrast, has a truth-value gap: according to $\mathcal{B}$, there are not only tall and not-tall people, but borderline cases as well (such people are in the extension $\| ?$ tall? $\left.\|_{\mathcal{B}}\right)$. As before, the search effort implied by a model $\mathcal{X}$ (abbreviated $s(\mathcal{X})$ ) will be formalised as the expected number of elements of $D$ that the hearer will have to examine, under the assumption that she goes on searching until the intended referent (i.e., the man with the diamond in his pocket) is found. For simplicity, assume that the models $\mathcal{A}$ and $\mathcal{B}$ call exactly the same people tall, so both assign the same extension to $\|t a l l\| .{ }^{3}$ Furthermore, we assume that all the extensions mentioned above (with the possible exception of $\|t a l l\|)$ are nonempty.

### 3.1 The advantage of allowing borderline cases

Let us compare the models $\mathcal{A}$ and $B$ above. Focussing on the witness' reference to the thief $(t)$, there are three different types of situations. (In what follows, $\operatorname{card}(X)$ abbreviates "the cardinality of $X$ ").

Type 1. $t \in\|t a l l\|$. In this case, $s(\mathcal{A})=s(\mathcal{B})$, because the same sets are searched in both cases.
Type 2. $t \in \|$ ?tall? $\|_{B}$. In this case, $s(\mathcal{A})>s(\mathcal{B})$, so $B$ leads to a lower search effort than $\mathcal{A}$. In other words, the model with borderline cases (i.e., model $B$ ) incurs an advantage over the one that does not (i.e., $\mathcal{A}$ ). The size of the advantage is $1 / 2\left(\operatorname{card}\left(\|\overline{\operatorname{tall}}\|_{\mathcal{B}}\right)\right)$.
Type 3. $t \in\|\overline{\operatorname{tall}}\|_{\mathcal{B}}$. In this case, $s(\mathcal{B})>s(\mathcal{A})$, in other words the model with borderline cases incurs a disadvantage. The size of the disadvantage is $1 / 2\left(\operatorname{card}\left(\|? t a l l ?\|_{B}\right)\right)$.

Proofs of these claims use standard reasoning about probability. Consider Type 2, for example, where the thief $t$ is borderline tall. Given our assumptions, this implies $t \in\|\overline{\operatorname{tall}}\|_{A}$. We can measure the hearer's search effort implied by the model $\mathcal{A}$ as $s(\mathcal{A})=\operatorname{card}(\|\operatorname{tall}\|)+1 / 2\left(\operatorname{card}\left(\|\overline{\operatorname{tall}}\|_{\mathcal{A}}\right)\right)$. The search effort implied by $\mathcal{B}$ is $s(\mathcal{A})=\operatorname{card}(\|\operatorname{tall}\|)+1 / 2\left(\operatorname{card}\left(\|? \operatorname{tall} ?\|_{\mathcal{B}}\right)\right)$, so $s(\mathcal{A})>s(\mathcal{B})$ if $\operatorname{card}\left(\|\overline{\operatorname{tall}}\|_{\mathcal{A}}\right)>\operatorname{card}\left(\|? \operatorname{tall} ?\|_{\mathcal{B}}\right)$, which is true given that (as we assumed) $\|\overline{\operatorname{tall}}\|_{\mathcal{B}} \neq \emptyset$. The size of the advantage is $1 / 2\left(\operatorname{card}\left(\|\overline{\operatorname{tall}}\|_{\mathcal{A}}\right)\right)-1 / 2\left(\operatorname{card}\left(\|? \operatorname{tall} ?\|_{\mathcal{B}}\right)\right)$, which equals $1 / 2\left(\operatorname{card}\left(\|\overline{\operatorname{tall}}\|_{\mathcal{B}}\right)\right)$.

What we really like to know is the expected search effort a priori, when it is not known in which of the three Types of situations (listed above) we are. Since borderline cases are advantageous in Type-2 situations but detrimental in Type3 situations, this depends on the likelihood of these two types. Let "tall(x)" (in double quotes) say that the witness calls $x$ tall, then we can write ( $p \mid$

[^47]"tall(x)") to denote the conditional probability of $p$ given that the witness calls $x$ tall. We can now prove theorems such as the following (still assuming that $\left.\|t a l l\|_{A}=\|t a l l\|_{B}\right):$

Theorem 1. If $\operatorname{card}\left(\|? \operatorname{tall} ?\|_{\mathcal{B}}\right) \leq \operatorname{card}\left(\|\overline{\operatorname{tall}}\|_{\mathcal{B}}\right)$ then

$$
\left(p\left(t \in\|? \operatorname{tall} ?\|_{\mathcal{B}} \mid " \operatorname{tall}(\mathrm{t}) "\right)>p\left(t \in\|\overline{\operatorname{tall}}\|_{\mathcal{B}} \mid " \operatorname{tall}(\mathrm{t}) "\right)\right) \Rightarrow s(\mathcal{A})>s(\mathcal{B})
$$

In words: if the number of borderline cases in $\mathcal{B}$ does not surpass the number of people who are clearly not tall in $\mathcal{B}$ then $\mathcal{B}$ has an advantage over $\mathcal{A}$ as long as a person $t$ 's being called "tall" makes it likelier that $t$ is borderline tall than clearly not tall.

The significance of this Theorem may be seen by focussing on situations where $\left.\operatorname{card}(\|\operatorname{tall}\|)=\operatorname{card}\left(\|? \operatorname{tall} ?\|_{B}\right)\right)=\operatorname{card}\left(\|\overline{\operatorname{tall}}\|_{B}\right)$, in which case the antecedent of the Theorem is met. Clearly, in such a situation, the two following things hold:

$$
\begin{aligned}
& p\left(t \in\|? \operatorname{tall} ?\|_{B} \mid " \operatorname{tall}(\mathrm{t}) "\right)>p\left(t \in \| \overline{\left.\operatorname{tall} \|_{B} \mid " \operatorname{tall}(\mathrm{t}) "\right)}\right. \\
& p\left(t \in\|\operatorname{tall}\|_{B} \mid " \operatorname{tall}(\mathrm{t}) "\right)>p\left(t \in\|? \operatorname{tall} ?\|_{B} \mid " \operatorname{tall}(\mathrm{t}) "\right)
\end{aligned}
$$

The Theorem tells us that this implies $s(\mathcal{A})>s(\mathcal{B})$, in other words, the expected search time implied by the dichotomous model $\mathcal{A}$ is greater than that implied by model $B$, which has a truth-value gap. In other words: given a dichotomous model, it is always possible to find a non-dichotomous model (i.e., with borderline cases) which agrees with it on all the positive cases (i.e., which calls exactly the same people tall), and which implies a smaller search effort on the part of the hearer.

### 3.2 The advantage of degrees and ranking

To develop a formal take on what happens when a concept like "tall" is seen as having degrees, let us contemplate a degree model $\mathcal{C}$, alongside the dichotomous model $\mathcal{A}$ and the three-valued model $\mathcal{B}$. Without loss of generality we can assume that $\mathcal{C}$ assigns real-valued truth values in $[0,1]$ to each person in $D$. As is customary in Fuzzy Logic (Zadeh 1965), among other systems, let $\mathcal{C}$ assign the value 0 to the shortest person and 1 to the tallest, while taller people are be assigned values that are not lower than those assigned to shorter ones.

In the present context, the crucial advantage of degree models over 2- or 3 -valued ones is that degree models tend to make finer distinctions. 2-valued models (i.e., dichotomous ones) are able to distinguish between two kinds of people (the tall ones and the not-tall ones), and 3 -valued models (i.e., ones with a truth-value gap) are able to distinguish between three. Degree models have the capacity to distinguish between many more people - if need be, a mathematical continuum of them. Where this happens, the advantages are analogous to the previous subsection.

Suppose, for example, that the domain contains ten individuals: $a 1, a 2, b 1$, $b 2, c 1, c 2, d 1, d 2, e 1$, and $e 2$, where $a 1$ and $a 2$ have (approximately) the same
height, so do $b 1$ and $b 2$, and so on. Assume that the Emperor assigns "fuzzy" truth values as follows:

$$
\begin{aligned}
& v(\operatorname{Tall}(a 1))=v(\operatorname{Tall}(a 2))=0.9, \\
& v(\operatorname{Tall}(b 1))=v(\operatorname{Tall}(b 2))=0.7, \\
& v(\operatorname{Tall}(c 1))=v(\operatorname{Tall}(c 2))=0.5, \\
& v(\operatorname{Tall}(d 1))=v(\operatorname{Tall}(d 2))=0.3, \\
& v(\operatorname{Tall}(e 1))=v(\operatorname{Tall}(e 2))=0.1 .
\end{aligned}
$$

Recall that the witness described the thief as "tall". It is not farfetched to think that $a 1$ and $a 2$ are more likely targets of this description than $b 1$ and $b 2$, while these two are more likely targets than $c 1$ and $c 2$, and so on. The Emperor should therefore start looking for the diamond in the pockets of the two tallest individuals, then in those of the two next tallest ones, and so on. The idea is the same as in the previous subsection, except with five rather three levels of height: under the assumptions that were made, this search strategy is quicker than the previous two.

This example suggests that the key to the success of this strategy is the ability to rank the indivuals in terms of their heights, assuming that this corresponds to a ranking of their likelihood of being called "tall". Whenever this ability results in finer distinctions than 2 - or 3 -valued models, degree models lead to diminished search effort. In other words:

Theorem 2. Suppose that, for all $x$ and $y$ in the domain $D, v(\operatorname{tall}(x))>$ $v(\operatorname{tall}(y))$ implies $p($ "tall $(\mathrm{x}) ")>p\left({ }^{\prime} \operatorname{tall}(\mathrm{y}) "\right)$. Suppose, furthermore, that $D$ contains individuals of four or more height levels (i.e., at least four different truth values of the form $v(\operatorname{Tall}(x)))$. It then follows that $s(\mathcal{C})<s(\mathcal{B})$. Proof: by induction on the number $n$ of levels, with $n=4$ as the base case.

Theorem 2 implies that the expected search time associated with the degree model $\mathcal{C}$ is smaller than that associated with model $\mathcal{B}$, which has a truth-value gap. So, given a three-valued model, it is always possible to find a degree model that respects the distinctions made by the three-valued model and that implies an even smaller search effort on the part of the hearer.

## 4 Discussion

We have argued that quasi-continuous domains (such as colours, sizes, etc., where some physically different stimuli are indistinguishable by the naked eye) make it difficult for language users to align the meanings of the predicates defined over them: there are bound to be things that one person calls 'large' (or 'blue', or 'warm') that another person does not. (In fact, even the same person is bound to judge differently on different occasions.) Given such mismatches - which do not exist in standard game-theoretical analyses of vagueness - we have argued that it is to the hearer's advantage to distinguish shades of meaning in a way that is typical for vague concepts, namely using borderline cases or degrees. I believe
that this argument offers an answer to the pragmatic question that we asked in our Introduction which is important while differing notably from the ones offered in the literature so far (see Van Deemter 2009, Van Deemter (to appear) for a survey). To the extent that it supports degree-based models, ranging from Fuzzy Logic to Kennedy-style 2-valued semantics, our analysis also appears to shed light on the logical-semantic questions surrounding vagueness.

In an effort to assess the implications of our findings, we discuss some possible objections against our argument.

Objection 1. It might be argued that the benefits that we ascribed to 3 -valued and many-valued models can, in fact, also be obtained from 2 -valued models. According to this view, the user of a 2 -valued model is just as able to make fine distinctions as the user of any other kind of model. One can imagine a semantic and a syntactic version of this argument. The semantic version would argue that an intelligent user of a 2 -valued model should be aware that other (2-valued) models may exist. She could argue, for example, that taller people are counted as tall by more models than less tall people. Clearly then, it pays to start searching amongst those people who are counted as tall by the largest set of models, that is, amongst the tallest people. The syntactic version of this argument would say that a person who is "quite" tall is a more likely to be called tall than someone is "somewhat" tall, who is more likely to be called tall than someone who is "a little bit on the tall side perhaps", and so on; therefore, after unsuccessfully searching all the people who are downright tall, the hearer should direct her attention to the people who are quite tall, somewhat tall, and so on.

I would counter that all objections of this kind presuppose that Bob's understanding of "large" goes beyond a simple dichotomous model. A language user who reasons as in the semantic version of this objection, for instance, knows that "tall" can have many different thresholds (corresponding with the different models). Where does this leave her own understanding of the word "tall"? Presumably this is just one among many. This language user's understanding of "tall" goes beyond a simple dichotomous model with one threshold: she understands that it's part of the meaning of the word that it allows different thresholds. Essentially, this amounts to understanding the word as vague. The counterargument against the syntactic version of the objection is analogous: going beyond what the witness said, by exploring the extension of qualifications like "somewhat tall", does not make sense unless one is aware that the word "tall" is used differently by different people. Once again, if the Emperor followed this strategy, we would be justified in ascribing to him an understanding of "tall" as a vague concept.

Objection 2. One might question the behaviour of the witness. Why, after all, did he keep us guessing, by using a vague concept? Why didn't he tell us directly what he saw, saying "the thief is 185 cm tall", or something precise like that? I believe this objection to rest on a misunderstanding. Perhaps the alternative utterance, "the thief is 185 cm tall" would have been more helpful, but it is most
naturally understood as vague too. Surely, an utterance of this kind would cover a person who is 184.3 cm , for instance. At what height exactly the assessment starts being false would be difficult to say. Its meaning is perhaps best captured by a Gaussian function that asserts that 185 cm is the most likely height, with other heights becoming less and less likely as they are further removed from 185 cm . If such a vague estimate of the thief's height comes more naturally to human speakers than a precise assessment (e.g., "the thief's height is 185 cm plus or minus 2 cm ") then Litman's question can be repeated: why is this the case? Why, in other words, do people's height estimates tend to be vague? This new question can be answered in an exactly analogous way as the question on which we focussed in this paper, by pointing out that a crisp concept like "height $=185 \mathrm{~cm}$ plus or minus 2 cm " suffers from the same lack of flexibility as Ann and Bob's crisp notions of blue, in Parikh's story. Like before, vagueness allows speakers to deal flexibly with the differences among each other.

Objection 3. It can be argued that a 3 -valued model such as $\mathcal{A}$ falls short of making "tall" a vague concept, given that its boundaries (i.e., between $\|$ tall $\|$, $\| ?$ tall? $? \|$, and $\| \overline{\text { tall } \|)}$ ) are crisp instead of vague. One might even go further and argue that the same is true for the many-valued models discussed in section 3.2 , since these, too, assign definite truth values to each statement of the form "Tall(x)". I would counter that, if these models are seen as failing to model genuine (i.e., higher-order) vagueness, then it is difficult to see what models do model genuine vaguenes. Certainly very few of the models on the theoretical market (see e.g. Keefe and Smith 1997) go further than many-valued models in acknowledging vagueness. Essentially, in this paper, I have taken the pragmatic question about vagueness to be "Why does language not make do with simple dichotomous concepts?"

Objection 4. Litman (2006) proves a game-theoretical theorem (framed within a standard model as proposed in Crawford and Sobel 1982) stating that, given a vague predicate $P$, there must always exist a non-vague predicate $P^{\prime}$ that has higher utility than $P$. It might be thought that this contradicts the main claim of the present paper, but this is not the case. To prove his theorem, Lipman makes various assumptions which our analysis does not share. One of these assumptions is that a a vague predicate is a probability distribution over functions that assign messages to heights. This is known as a mixed strategy, as opposed to a pure strategy, which is just a function from heights to messages. We have seen in our discussion of Objection 3 that we have adopted a different attitude towards vagueness, without probability distributions. A second, and even more crucial assumption on which Lipman's theorem rests is that there are no mismatches between speaker and hearer. In particular, when a pure strategy is adopted by the speaker, he assumes that the hearer knows what this strategy is. Our own investigations, by contrast, use a very different assumption, namely that mismatches between speaker's and hearer's understanding of words like 'tall' are unavoidable.

## Workshop on Vagueness

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# Meaning of 'now' and other temporal location adverbs 

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#### Abstract

This paper provides an analysis of the temporal location adverb now. The core data comes from free indirect discourse, where now often co-occurs with the past tense and has an affinity for stative sentences. Building on Kamp \& Reyle's (1993) analysis, I propose that now is a perspective setting anaphor: it requires an eventuality described by an aspectual phrase to hold throughout a salient event that serves as a the 'current perspective.' The proposed meaning is compatible with both the past and present tenses and it has the same semantic type and uses the same ingredients as other temporal location adverbs.


Keywords: adverbs, aspect, tense, narrative progression, free indirect discourse, anaphora, indexicals

## 1 Introduction

There is a particular use of now where it co-occurs with the past tense. This usage is often found in free indirect discourse (FID) viz. (1), where it is possible to understand the described eventualities as happening from the point of view of a particular character, rather than the speaker or narrator ([1]). This, however, is not a necessary condition for now to co-occur with the past tense. For example, the state of being unpleasant to look at in (2) must be interpreted from the point of view of the speaker.

He came to me and told me he had been dressing in my clothes whenever I wasn't home for quite a few years, and now he was ready to take the next step
and with the help of his doctor (that I didn't even know about) he wanted to start the process of becoming female ([2]).

Anna went to her plastic surgeon. She had won the beauty contest 30 years ago. Now the old bag was a sight for sore eyes! (Sam Cumming, p.c.)

Now exhibits two key properties in discourses such as (1) and (2). The first is that now is used as an anaphor. This is especially clear when one compares (2) to its counterpart without now. In such a case, the state of being unpleasant to look at would be understood to hold when Anna won the beauty contest. This would render the discourse infelicitous. With now, however, the discourse is felicitous because the described state is understood to hold throughout the event of going to the plastic surgeon. This event is chosen as an antecedent because now is an event seeking anaphor and the perfect clause in (2) makes the consequence of the winning event salient (rather than the winning event itself; see [3]). Further evidence comes from
(3), which is infelicitous with now because the series of stative sentences don't provide an antecedent of the right type.

Samsa's room, a regular human bedroom, only rather too small, lay quiet between the four familiar walls. Above the table on which a collection of cloth samples was unpacked and spread out hung a picture. It showed a lady, with a fur cap on and a fur stole, sitting upright and holding out to the spectator a huge fur muff. Samsa \{*was now/was\} intrigued by this lady (modified from [4]).

The other property of now is exemplified by discourses such as (4) and (5). Here we see that now is incompatible with eventive sentences ([5], pp. 595-596). ${ }^{1}$ In this way, now differs from all other temporal location adverbs (cf. [8]), including the seemingly similar anaphor at that point in (6).

He came to me and told me he had been dressing in my clothes whenever I wasn't home for quite a few years, and now he \{was ready to take/was taking/had taken/*took\} the next step...

Yesterday, Anna went to her plastic surgeon. She had won the beauty contest 30 years ago. Now she $\{$ wanted to replace $/ *$ replaced $\}$ her nose and upper lip with those of a donor.

The first of Weiss' explicitly autobiographical novels, Leavetaking, describes his childhood and youth until 1940. \{At that point/*now\} he essentially claimed his independence and set out to become an artist ([9]).

Based on similar observations, Kamp and Reyle propose that now refers to a temporal perspective point-i.e. the speech time or a previously mentioned discourse event ([5]). The innovation of their analysis is that now is not treated as an indexical expression (cf. [10]), but as perspective setting anaphor whose value is constrained by tense. A problem with their analysis, however, is that they posit three past tenses even though the morphology indicates otherwise: (i) a past tense that only combines with stative sentences, (ii) a past tense that only combines with eventive sentences and (iii) a past tense that is required only in the presence of now ([5], pp. 601).

An alternative hypothesis is to say that the semantics of FID explains the seemingly quirky behavior of now. For example, according to one influential analysis, FID is an operator that 'shifts' the coordinates of an indexical expression ([11], [12]). On this view, we could say that in a discourse like (2), a FID operator shifts the speech time coordinate to a past time, namely the time of Anna going to the plastic surgeon. In turn, we can maintain that now is an indexical expression; it refers to the (shifted) speech time.

While this analysis of FID may be correct ${ }^{2}$, shifting coordinates of now does not explain now's reluctance to co-occur with eventive sentences viz. (4)-(6). Moreover,

[^48]it does not explain now's anaphoric nature-i.e. that it 'chooses' a particular antecedent event to serve as the 'current perspective' viz. (2)-(3). These facts, I believe, warrant a semantic reanalysis of now.

In this paper, I build on Kamp and Reyle's proposal that now is a perspective setting anaphor whose value is constrained by tense and propose a meaning that is (i) compatible with both the past and present tenses and (ii) has the same semantic type and uses the same ingredients as other temporal location adverbs. In particular, I propose that all such adverbs have a temporal component and a discourse component. Depending on the nature of the adverb, one of these components typically plays a greater role in fixing the temporal location of an eventuality described by an aspectual phrase. In the case of now, however, both components play an instrumental role. They conspire to impose the following two requirements: (i) search for a topical event that serves as the "current perspective" and (ii) describe what took place throughout this topical event. These two requirements capture now's anaphoric nature and-given aspectual constraints on narrative progression discussed in the next section-they lead to a contradiction with eventive, but not stative verb phrases. All in all, the proposed analysis makes the correct predictions about the discourses considered in this section without "postulating apparently spurious ambiguities" ([5], pp. 599).

## 2 Background assumptions

### 2.1 Event structure

Following [3], I assume that events have a tripartite structure, consisting of a preparatory process that leads up to an event's culmination, which in turn transitions into an event's consequent state. Accomplishment verb phrases (VPs) like write a letter are the most complex event types because they describe events consisting of I and II in Fig. 1; achievement VPs like arrive describe events consisting of II, while activity VPs like run describe events consisting of I.


Fig. 1. Moens and Steedman's tripartite event structure.

### 2.2 Narrative progression and aspect

It is generally held that temporal anaphora depends in part on the aspectual distinction between events and states (see [15], [16], [17], [18]). For example, consider the discourse below in (7), modeled after Partee's famous example in [17]. Here, the times of the described events (i.e. John's getting up, raising the blind and pulling the blind down) correlate with the order of appearance, i.e. a narrative progression is invoked. On the other hand, the state described in (7) (i.e. being light out) holds throughout the described events, i.e. a narrative halt is invoked.

[^49]John got up at 8 and raised the blind. It was light out. He pulled the blind down. (7)

Narrative discourses like (7) motivate a notion of a reference time-i.e. a placeholder for where the narrative has developed. According to one influential analysis proposed by Bonnie Webber in [19], a reference time is either the time described by temporal location adverbials or the duration of the consequent state of a previously mentioned discourse event (cf. Partee's "time right after"). Moreover, following [15]-[18], Webber proposed that aspect constrains the temporal location of an eventuality described by a verb phrase (VP) in the following way: Whereas events occur within a reference time, states hold throughout that time.

Such an analysis accounts for the inferred temporal ordering in (7) as follows. The event of John getting up is located within the time denoted by at 8 , which serves as the reference time. Subsequently, the event of John raising the blind is located within the duration of the consequent state of John getting up, which serves as the new reference time. This correctly predicts that John raised the blind after he got up. With regard to the state described in (7), i.e. being light out, it holds throughout (rather than within) the reference time, namely the duration of the consequent state of John raising the blind. This correctly predicts that it was light out when John raised the blind. Moreover, the state of being light out does not serve as an antecedent for the next sentence, thus triggering the narrative halt effect.

In sum, Webber's analysis is elegant because (i) it makes use of an independently motivated event structure and (ii) it relates events to times specified by an adverbial in the same way it relates events to times provided by the discourse context, thereby preserving Reichenbach's unified notion of a reference time ([20]).

Despite its elegance, however, I argued in [21] and [22] that Webber's analysis cannot account for the Russian imperfective aspect, which relates distinct event parts to the reference time. Which event part is at play depends on how the reference time is specified. If it is specified by an adverbial expression, then the Russian imperfective locates an event relative to a reference time. However, if it is specified by the discourse context, then the Russian imperfective locates the consequent state of an event relative to a reference time. To account for these generalizations, I argued that it is necessary to split the notion of a reference time into two distinct parameters (cf. [5]; see also [23] for independent evidence). I proposed a birelational analysis in which aspectual meaning involves both temporal information and information about discourse connectivity. In particular, aspect requires two inputs relative to which a described eventuality is located-(i) a time that is specified by a temporal location adverbial (or some other grammatical expression) and (ii) a state that is specified by the discourse context. Events are required to hold throughout the two inputs, while states hold throughout them.

In what follows, I assume a birelational analysis of aspect without further comment. As shown in §4, this assumption allows us to give an adequate semantics for now. I end this section by providing birelational meanings of two English expressions: an eventive and a stative aspectual phrase in (8) and (9) respectively. In the next section, I provide details about how the inputs to these phrases are supplied.

$$
\begin{gather*}
\text { AspP [Anna laugh }] \text { ma }  \tag{8}\\
\lambda s \lambda t \exists e[\tau(e) \subseteq t \wedge \tau(e) \subseteq \tau(s) \wedge \operatorname{laugh}(\text { anna }, e)] \\
\text { AspP }[\text { Anna be.sick }] \text { mu }  \tag{9}\\
\lambda s^{\prime} \lambda t \exists s\left[t \subseteq \tau(s) \wedge \tau\left(s^{\prime}\right) \subseteq \tau(s) \wedge \text { be.sick }(\text { anna }, s)\right]
\end{gather*}
$$

## 3 Meaning of temporal location adverbs

I assume the syntactic architecture in Fig. 2, where aspectual phrases combine with a tense operator and the resulting denotation combines with an adverbial.


Fig. 2. Assumed syntactic architecture.
I treat tense operators as relations between the speech event $e_{0}$ and a time argument $t$. For example, the past tense operator PST in (10) requires that a time argument precede the run time of the speech event and the present tense operator PRS in (11) requires that the two be identified.

$$
\begin{gather*}
\mathrm{T}[\mathrm{PST}] \text { m }  \tag{10}\\
\lambda \mathrm{Q} \lambda s \lambda t\left[t<\tau\left(e_{0}\right) \wedge \mathrm{Q}(s, t)\right] \\
\mathrm{T}[\mathrm{PRS}] \text { ~ }  \tag{11}\\
\lambda \mathrm{Q} \lambda s \lambda t\left[t=\tau\left(e_{0}\right) \wedge \mathrm{Q}(s, t)\right]
\end{gather*}
$$

With regard to temporal location adverbs like yesterday, the day before, at 5, and February 15, 1981, I propose that they combine with TP and have two functions. They supply a time input-which serves as the location time for a described eventuality (cf. [5])—and specify its duration as well as its relation to a perspectival event-i.e. the speech event or a previously mentioned discourse event (cf. Kamp and Reyle's notion of a temporal perspective point in [5]). ${ }^{3}$ Moreover, they supply a state input, which does not play a significant role in locating the described eventuality.

As an example of the analysis, consider the denotations of yesterday and the day before in (12) and (13):

> Adv [yesterday] $\mu \rightarrow$
> $\lambda \mathrm{Q} \exists t \exists s\left[\operatorname{day}(t) \wedge t<_{\text {day }} \tau\left(e_{0}\right) \wedge \mathrm{Q}(s, t)\right]$

Adv [the day before ${ }_{n}$ ] $\rightarrow$
$\lambda \mathrm{Q} \exists t \exists s\left[\operatorname{day}(t) \wedge t<_{d a y} \tau\left(e_{n}\right) \wedge \mathrm{Q}(s, t)\right]$

[^50]Both adverbs specify that the location time $t$ is a 24 -hour interval of time denoted by day that precedes the perspectival event by a day. Being an indexical, yesterday requires that the perspectival event be the speech event $e_{0}$. On the other hand, the anaphoric adverb the week before requires that the perspectival event be a previously mentioned discourse event $e_{n}$. This explains why yesterday can be used discourse initially, but the day before cannot (cf. Kamp and Reyle's discussion of last Sunday vs. the preceding Sunday in [5], pp. 622-625).

A question that arises is: Where does TP get its two inputs if there is no adverbial present? Following work by Carlota Smith ([25], [26]), I assume that semantically, there is always an adverb present (even if it not there syntactically). In particular, I assume that episodic sentences in the past tense that do not have an overt adverbial combine with a silent then (cf. Bäuerle's silent 'once' in [27]). Like other temporal location adverbs, then has two functions. As illustrated in (14), it supplies a time input, which does not play a significant role in locating the described eventuality (cf. [5], pp. 528-529). Moreover, it supplies a state input $s_{n}$ that requires a salient state antecedent that I will refer to as the topic state.

$$
\begin{gather*}
\operatorname{Adv}\left[<\text { then }_{n}>\right] \quad \begin{array}{c}
\text { Q } \exists t\left[\mathrm{Q}\left(s_{n}, t\right)\right]
\end{array}, ~ \tag{14}
\end{gather*}
$$

The meaning above explains why the sentences in (15) are infelicitous out-of-theblue: there is no topic state provided by the discourse context. ${ }^{4}$
\#Avital came in.
\#Then Avital came in.

Moreover, it explains the understood event ordering in the discourses below in (16): then (in its covert or overt manifestation) requires that the sitting down event be contained within the topic state. Assuming this state is the consequent state of the coming in event, it is correctly predicted that the sitting follows the coming in.

Yesterday, Avital came in. She sat down.
Yesterday, Avital came in. Then she sat down.
In sum, temporal location adverbs supply both temporal information and information about discourse connectivity. In particular, they supply two inputs that are required by aspectual phrases - a time and a state. Adverbs like yesterday and the day before are similar insofar as the supplied time input plays a greater role in fixing the temporal location of the described eventuality; the two adverbs differ solely in whether the perspectival event is the speech event or a previously mentioned discourse event. On the other hand, the state input supplied by the adverb then (in its overt or covert manifestation) plays a greater role in fixing the temporal location of the described eventuality. This explains why we often see this adverb in narrative progression contexts, but never discourse initially. In the next section, I propose that both the state and time inputs supplied by now play a significant role in fixing the temporal location of the described eventuality.

[^51]
## 4 Meaning of 'now'

In the introduction, we saw that now has two key properties: it is an anaphor that seeks a salient event antecedent and it has an affinity for stative sentences. The basic idea of my analysis is as follows. Now encodes the following directions: (i) search for a topical event that serves as the "current perspective" and (ii) describe what took place throughout this topical event. The latter direction is consistent with the aspectual requirements imposed on stative predicates, but not eventive ones, thereby explaining the contrast in (17). Moreover, the contrast in (18) is explained in the following way. Without now, the states of being old and sick are required to hold throughout the topic state, namely the consequent state of the winning event (cf. discussion of (16)). With now, however, the states of being old and sick are required to hold throughout a topical event that serves as the "current perspective." The topical event must be the event of going to the plastic surgeon assuming that the past perfective clause "had won the beauty contest" makes the consequent state of the winning event salient (and not the winning event itself). ${ }^{5}$

Yesterday, Anna went to her plastic surgeon. She had won the beauty contest 30 years ago. Now she \{wanted to replace/*replaced\} her nose and upper lip.
Yesterday, Anna went to her plastic surgeon. She had won the beauty contest 30 years ago. \{Now she was old and sick/\#she was old and sick\}.

In order to make sense of this proposal within the theory outlined in the previous two sections, consider the meaning for now below, in (19):

$$
\begin{gather*}
\operatorname{Adv}\left[\mathrm{now}_{n}\right] \quad \text { m }  \tag{19}\\
\lambda \mathrm{Q} \exists t \exists s\left[t=\tau\left(e_{n}\right) \wedge \operatorname{CoNS}\left(e_{n}\right)=s \wedge \mathrm{Q}(s, t)\right]
\end{gather*}
$$

According to the formula above, now has the same semantic type and uses the same ingredients as other temporal location adverbs. In particular, it supplies a time input that is related to a salient event $e_{n}$ that serves as the perspectival event. In this way, now is on a par with the day before viz. (13). It differs, however, in that it requires the supplied time input to be identified with (rather than precede) the run time of the perspectival event (viz. the condition $t=\tau\left(e_{n}\right)$ ). As will be shown below, this difference is what makes now compatible with both the present and the past tense.

Like all other location adverbs, now also supplies a state input. However, unlike other adverbs, it relates this state to the perspectival event. In particular, it requires the supplied state input to be a consequent state of the perspectival event (viz. the condition $\left.\operatorname{CONS}\left(e_{m}\right)=s\right)$.

The relations $t=\tau\left(e_{n}\right)$ and $\operatorname{CoNS}\left(e_{n}\right)=s$ encoded by now entail that an eventuality described by AspP holds throughout the perspectival event as desired. Such is the case because-given the analysis sketched out in the previous section - $t$ and $s$ are the inputs relative to which an eventuality described by AspP is located. In particular, events described by AspP are required to hold within these inputs, while states are required to hold throughout them. This leads to contradiction with eventive sentences,

[^52]but not with stative sentences. That is, it follows from (19), (20) and (22) that the nose replacing event is contained within two non-overlapping eventualities-i.e. the perspectival event and its consequent state-thereby explaining the ungrammaticality of (17) with replaced. On the other hand, it follows from (19), (20) and (23) that a state of being sick held throughout the perspectival event, thereby explaining now's affinity for stative sentences.
\[

$$
\begin{gather*}
\mathrm{T}[\mathrm{PST}] \text { mu }  \tag{20}\\
\lambda \mathrm{Q} \lambda s \lambda t\left[t<\tau\left(e_{0}\right) \wedge \mathrm{Q}(s, t)\right] \\
\mathrm{T}[\mathrm{PRS}] \text { ~n }  \tag{21}\\
\lambda \mathrm{Q} \lambda s \lambda t\left[t=\tau\left(e_{0}\right) \wedge \mathrm{Q}(s, t)\right] \\
\mathrm{AspP}[\text { she replace her nose }] \text { mu }  \tag{22}\\
\lambda s \lambda t \exists e[\tau(e) \subseteq t \wedge \tau(e) \subseteq \tau(s) \wedge \text { replace.her.nose }(\text { she }, e)] \\
\mathrm{AspP}[\mathrm{Anna} \text { be sick }] \text { mu }  \tag{23}\\
\lambda s^{\prime} \lambda t \exists s\left[t \subseteq \tau(s) \wedge \tau\left(s^{\prime}\right) \subseteq \tau(s) \wedge \text { be.sick }(\text { anna }, s)\right]
\end{gather*}
$$
\]

The proposed analysis not only accounts for now in contexts where it co-occurs with the past tense, but it also accounts for the so-called indexical use of now in examples like (24). Here we see now appearing discourse initially and co-occurring with the present tense; it makes reference to the time at which it is uttered.

> Anna is sick now.

This is just one way in which now is used in a discourse; its seeming indexical behavior in (24) comes from the present tense, which identifies the run time of the speech event with the time introduced by now, which in turn is identified with the perspectival event. For this reason it follows from (19), (21) and (23) that the state of being sick described in (24) holds throughout the speech event as desired.

## 5 Conclusion

I end this paper by mentioning two challenges for the proposed analysis. The first comes from Hans Kamp's example in (25), which entails that an earthquake is taking place at the speech event. What is interesting about (25) is that there is no present tense in the sentence and the aforementioned entailment disappears without now.

I learned last week that there would now be an earthquake ([10], pp. 299).

Given the analysis proposed here, one could say that the perspectival event in (25) must be the speech event because it is compatible with the semantics of would and there is no other possible antecedent; the learning event described by the matrix clause is presumably ruled out because would requires the earthquake to follow this event. In other words, the idea is that now is compatible with a present or a past perspectival event and-if no grammatical elements (viz. the present tense) indicate otherwise-independent rules of anaphora resolution determine which one is chosen.


#### Abstract

Another challenge for the proposed analysis concerns the behavior of other temporal location adverbs that appear to 'lose' their indexicality in FID analogous to now. For example, consider tomorrow in (26), where it does not refer to a day after the speech event (see [29] for examples involving other adverbs).


Tomorrow was Monday, Monday, the beginning of another school week! ([1])

Given the proposed analysis, there are two avenues to pursue: (i) like now, tomorrow is an anaphor or (ii) an FID operator is responsible for shifting tomorrow's coordinates in (26). In its extreme, (i) leads to the perhaps undesirable claim that many (if not all) adverbial expressions that are typically thought to be indexical are really anaphoric. The less radical view in (ii), on the other hand, suggests that an FID operator is also at play when now occurs in FID. If that's right, then the effects of this operator are truth-conditionally undetectable given now's semantics.

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# Logical Consequence Inside Out 

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Tarski's definition of logical consequence for an interpreted language rests on the distinction between extra-logical symbols, whose interpretation is allowed to vary across models, and logical symbols, aka logical constants, whose interpretation remains fixed. In this perspective, logicality come first, and consequence is a byproduct of the division between logical and extra-logical symbols. Our aim here is to lay the basis for a shift in perspective: let consequence come first, so that the demarcation of a set of constants can be viewed as the by-product of the analysis of a relation of logical consequence. The idea for extracting logical constants from a consequence relation is the following: they are the symbols which are essential to the validity of at least one inference, in the sense that replacing them or varying their interpretation would destroy the validity of that inference. Conversely, definitions of logical consequence can be construed as providing us with mappings from sets of symbols (the ones selected as logical constants) to consequence relations. ${ }^{3}$ Extraction of constants is expected to be an 'inverse' to generation of consequence relations.

In Sections 1 and 2, we introduce a general substitutional framework for the abstract study of consequence relations. Extraction of constants is presented in Section 3. It is shown that extraction thus defined does not straightforwardly provide an inverse to generation of consequence relations. To circumvent this limitation, we consider in Section 4 'richness' properties of languages that make things better. In Section 5, we prove that extraction and generation constitute a Galois connection, considering families of expansions of a language, instead of a single language at a time. This gives us the correspondence for non-substitutional Tarskian consequence as a limit case.

## 1 Preliminaries

### 1.1 Languages

In the Bolzano setting, languages are interpreted; in particular every sentence is either true or false. We shall need very few assumptions about what sentences look like or how they are structured. For definiteness, a language $L$ has a set Sent $L_{L}$ of sentences, which are finite strings of signs, some of which, called symbols, belong to a set $S_{y m b}^{L}$. Let $u, v, u^{\prime}, \ldots$ vary over $\operatorname{Symb}_{L}, \varphi, \psi, \ldots$ over $\operatorname{Sent}_{L}$, and $\Gamma, \Delta, \ldots$ over finite subsets sets of $\operatorname{Sent}_{L} . V_{\varphi}$ is the set of symbols occurring in $\varphi$; likewise $V_{\Gamma}=\cup\left\{V_{\varphi}: \varphi \in \Gamma\right\}$. $\operatorname{Tr}_{L} \subseteq \operatorname{Sent}_{L}$ is the set of true sentences in $L$.

[^53]
### 1.2 Replacement

We need a notion of 'appropriate' replacement of symbols by other symbols. To this end, think of $S y m b_{L}$ as partitioned into a set of categories. Then, a replacement is a partial function $\rho$ from $\operatorname{Symb}_{L}$ to $S y m b_{L}$ such that for $u \in$ $\operatorname{dom}(\rho), u$ and $\rho(u)$ belong to the same category. $\varphi[\rho]$ is the result of replacing each occurrence of $u$ in $\varphi$ by $\rho(u)$. It is convenient to assume that $V_{\varphi} \subseteq \operatorname{dom}(\rho)$ - in words, $\rho$ is a replacement for $\varphi$ - so that $\rho$ is the identity on symbols that don't get replaced. We may then assume that the following conditions hold: ${ }^{4}$
(1) a. If $\rho$ is a replacement for $\varphi, \varphi[\rho] \in \operatorname{Sent}$ and $V_{\varphi[\rho]}=\operatorname{range}\left(\rho \upharpoonright V_{\varphi}\right)$
b. $\quad \varphi\left[i d_{V_{\varphi}}\right]=\varphi$
c. If $\rho, \sigma$ agree on $V_{\varphi}$, then $\varphi[\rho]=\varphi[\sigma]$.
d. $\quad \varphi[\rho][\sigma]=\varphi[\sigma \rho]$, when $\sigma$ is a replacement for $\varphi[\rho]$

### 1.3 Consequence relations

Definition 1. A relation $R \subseteq \wp\left(S e n t_{L}\right) \times \operatorname{Sent}_{L}$ is

1. reflexive iff for all $\varphi \in \operatorname{Sent}_{L}, \varphi R \varphi ;{ }^{5}$
2. transitive iff whenever $\Delta R \varphi$ and $\Gamma R \psi$ for all $\psi \in \Delta$, we have $\Gamma R \varphi$;
3. monotone iff $\Delta R \varphi$ and $\Delta \subseteq \Gamma$ implies $\Gamma R \varphi$;
4. truth-preserving iff whenever $\Gamma R \varphi$ and (every sentence in) $\Gamma$ is true, $\varphi$ is also true.

Definition 2. A consequence relation in $L$ is a reflexive, transitive, monotone, and truth-preserving relation between finite sets of $L$-sentences and $L$-sentences. ${ }^{6}$

Let $\Rightarrow, \Rightarrow^{\prime}, \ldots$ vary over the set $C O N S_{L}$ of consequence relations in $L$. Define:
(2) a. $\quad \Gamma \Rightarrow \Rightarrow^{\max } \varphi$ iff it is not the case that $\Gamma$ is true and $\varphi$ is false.
b. $\quad \Gamma \Rightarrow{ }^{\min } \varphi$ iff $\varphi \in \Gamma$.
$\Rightarrow{ }^{\max }$ is essentially material implication.
Proposition 1. $\Rightarrow^{\max }, \Rightarrow^{\min } \in C O N S_{L}$, and $\left(C O N S_{L}, \subseteq\right)$ is partial order with $\Rightarrow{ }^{\text {min }}$ as its smallest and $\Rightarrow{ }^{\text {max }}$ as its largest element.

## 2 Bolzano Consequence

### 2.1 Definition of $\Rightarrow$ _

The following definition should be familiar, except that (a) it is substitutional rather than model-theoretic; (b) it allows any set of symbols to be treated as logical.

[^54]Definition 3. For any $X \subseteq S y m b_{L}$, define the relation $\Rightarrow_{X}$ by
$\Gamma \Rightarrow_{X} \varphi$ iff for every replacement $\rho$ (for $\Gamma$ and $\varphi$ ) which is the identity on $X$, if $\Gamma[\rho]$ is true, so is $\varphi[\rho]$.

A relation of the form $\Rightarrow_{X}$ is called a Bolzano consequence (relation); $B C O N S_{L}$ is the set of Bolzano consequences. ${ }^{7}$

Proposition 2. (a) $B C O N S_{L} \subseteq C O N S_{L}$
(b) In addition, Bolzano consequence is base monotone:
$X \subseteq Y$ implies $\Rightarrow_{X} \subseteq \Rightarrow_{Y}$
(c) $\left(B C O N S_{L}, \subseteq\right)$ is a partial order with $\Rightarrow_{\emptyset}$ as its smallest and $\Rightarrow_{\text {Symb }}$ as its largest element.
$\left(B C O N S_{L}, \subseteq\right)$ is a sub-order of $\left(C O N S_{L}, \subseteq\right)$, and $\Rightarrow^{\max }=\Rightarrow_{S y m b}$, although usually $\Rightarrow^{\text {min }} \subsetneq \Rightarrow \emptyset$. The following two lemmas are trivial but fundamental:

Lemma 1. (Replacement Lemma) If $\Gamma \Rightarrow_{X} \varphi$ and $\rho$ doesn't move any symbols in $X$, then $\Gamma[\rho] \Rightarrow_{X} \varphi[\rho]$.

Lemma 2. (Occurrence Lemma) $\Gamma \Rightarrow_{X} \varphi$ if and only if $\Gamma \Rightarrow_{X \cap V_{\Gamma \cup\{\varphi\}}} \varphi$.

### 2.2 Examples

Propositional logic A standard language of propositional logic has symbols in a set $X_{0}$ of connectives, say, $X_{0}=\{\neg, \wedge, \vee\}$, and an infinite supply $p_{0}, p_{1}, \ldots$ of propositional letters. The usual definition of logical consequence, $\models_{P L}$, is modeltheoretic, but we can 'simulate' it in the present substitutional setting, where $p_{0}, p_{1}, \ldots$ are sentences with fixed truth values. Assuming that the sequence of truth values of $p_{0}, p_{1}, \ldots$ is not eventually constant, one easily verifies that

$$
\begin{equation*}
\Gamma \models_{P L} \varphi \text { iff } \Gamma \Rightarrow_{X_{0}} \varphi \tag{3}
\end{equation*}
$$

First-order logic For first-order logic the symbols are, say, $X_{1}=X_{0} \cup\{\exists, \forall,=\}$, and a supply of predicate symbols and individual constants. Now there is a difference between model-theoretic and substitutional definitions: in general we have

$$
\begin{equation*}
\models_{F O} \subsetneq \models_{F O_{\text {subst }}} \subsetneq \Rightarrow_{X_{1}} \tag{4}
\end{equation*}
$$

where $\models_{F O_{\text {subst }}}$, i.e. the consequence relation you get with a standard substitutional interpretation of the quantifiers, as in [3]. So $\Vdash_{F O}$ is a consequence relation, but not a Bolzano consequence.

[^55]
### 2.3 Minimal sets of symbols

Different sets may generate the same Bolzano consequence, so one expect sets that are minimal in this respect to be particularly well behaved.

Definition 4. $X$ is minimal iff for all $u \in X, \Rightarrow_{X} \neq \Rightarrow_{X-\{u\}}$.
Proposition 3. $X$ is minimal iff no proper subset of $X$ generates the same consequence relation.

The next result shows that it is sufficient to look at consequence relations generated by minimal sets.

Proposition 4. Every $X \subseteq S y m b_{L}$ has a subset which is minimal among those generating $\Rightarrow_{X}$.

A stricter notion of minimality is the following:
Definition 5. $X$ is strongly minimal iff for all $u \in X$ there are $\Gamma, \varphi$, and $u^{\prime}$ such that $\Gamma \Rightarrow_{X} \varphi, \Gamma\left[u / u^{\prime}\right]$ is true, but $\varphi\left[u / u^{\prime}\right]$ is false. ${ }^{8}$

The following is practically immediate.
(5) If $X$ is strongly minimal, it is minimal.

Let $M I N_{L}\left(S M I N_{L}\right)$ be the set of (strongly) minimal subsets of Symb ${ }_{L}$. Strong minimality says that $\Rightarrow_{X} \subseteq \Rightarrow_{X-\{u\}}$ fails in a particular way: a counterexample exists which involves replacing only $u$. One can show that, unless extra assumptions are made about the language (Section 4 below), not all Bolzano consequences are of the form $\Rightarrow_{X}$ for strongly minimal $X$. But those of this form are particularly well behaved:

Proposition 5. If $X$ is strongly minimal then, for all $Y \subseteq S y m b_{L}, X \subseteq Y$ iff $\Rightarrow_{X} \subseteq \Rightarrow_{Y}$.

Corollary 1. The mapping ${\underset{ـ}{ـ}}$ is one-one on strongly minimal sets.

## 3 Extracting constants from consequence relations

### 3.1 Defining extraction

We now introduce an operation corresponding to the extraction of logical constants from a consequence relation. When a particular consequence relation is given, certain symbols are to be considered as logical constants because the consequence relation makes them play a special role with respect to validity. Our guiding intuition is that a symbol is constant if replacing it can destroy at least one inference. ${ }^{9}$

[^56]Definition 6. The function $C_{-}: \operatorname{CONS}_{L} \rightarrow \wp\left(\right.$ Symb $\left._{L}\right)$ is defined for $\Rightarrow \in$ $\operatorname{CONS}_{L}$ and $u \in \operatorname{Symb}_{L}$ by $u \in C_{\Rightarrow}$ iff there are $\Gamma, \varphi$ and $u^{\prime}$ such that $\Gamma \Rightarrow \varphi$ but $\Gamma\left[u / u^{\prime}\right] \nRightarrow \varphi\left[u / u^{\prime}\right]$.

Logical consequence can be construed as a function from sets of symbols to consequence relations. Extraction goes in the opposite direction. Moreover, the domains of both functions are naturally ordered by inclusion, so the situation is as shown in Figure 3.1. Proposition 2(b) said that $\Rightarrow_{-}$is an order-preserving mapping from $\left(\wp\left(S y m b_{L}\right), \subseteq\right)$ to $\left(C O N S_{L}, \subseteq\right)$. We would like $C_{\text {_ }}$ to provide some sort of inverse order-preserving mapping. Before looking into this and other properties of $C_{-}$, let us see some examples of how $C_{-}$works.


Fig. 1. Logical consequence and constant extraction

### 3.2 Examples

The function $C_{\text {_ }}$ might fail to yield the intended result because of its substitutional character. In particular, if a symbol $u$ is unique in its category, there is no other symbol to replace $u$ with, and trivially it will not count as a logical constant, no matter what inferential role it plays. This situation arises with negation, which is usually the only unary connective in the language. To sidestep this difficulty, let us assume, when considering propositional logic or first-order logic, that they come equipped with another unary connective, say $\dagger$, interpreted by the constant unary truth-function 'equal to false'. Then we get :

Proposition 6. $C_{\models_{P L}}$ is the standard set of logical constants of $P L$.
Let us see why in two examples. $p \models_{P L} p \vee q$ but $p \not \vDash_{P L} p \wedge q$. Replacing $\vee$ by $\wedge$ destroys the validity of the first inference, so $\vee \in C_{\models_{P L}}$. Similarly, $\neg \neg p \models_{P L} p$ but $\dagger \dagger p \not \vDash_{P L} p$, therefore $\neg \in C_{\models_{P L}}$. Similarly for quantifiers in first-order logic.

Proposition 7. $C_{\models_{F O}}=C_{\models_{F O_{\text {subst }}}}$ is the standard set of logical constants of first-order logic.

### 3.3 Facts about $C_{-}$in the Bolzano setting

As a direct consequence of the Replacement Lemma, $C_{-}$will never pick out non-logical constants when it is applied to a Bolzano consequence.

## General Program

Proposition 8. For all $X \in \wp\left(\right.$ Symb $\left._{L}\right), C_{\Rightarrow_{x}} \subseteq X$.
Something stronger holds for strongly minimal $X$ :
Proposition 9. For all $X \in \operatorname{SMIN}_{L}, C_{\Rightarrow_{X}}=X$.
From this and Proposition 5, we get:
Proposition 10. $\Rightarrow_{\text {_ }}$ restricted to $S M I N_{L}$ is an isomorphism with inverse $C_{\text {_ }}$.
This tells us that $C_{\text {_ }}$ plays its role as an order-preserving inverse mapping on some proper subset of $C O N S_{L}$, namely the Bolzano consequences generated from strongly minimal sets of constants. These are of course severe limitations to the scope of the result, and the remainder of this paper will be devoted to providing an understanding of the global picture. But in the present framework, $C_{-}$is simply not an order-preserving inverse on all of $C O N S_{L}$.

Proposition 11. There are languages $L$ and consequence relations $\Rightarrow$ and $\Rightarrow^{\prime}$ in $\mathrm{CONS}_{L}$ such that:
(a) $\Rightarrow \subseteq \Rightarrow^{\prime}$ but $C_{\Rightarrow} \nsubseteq C_{\Rightarrow^{\prime}}$
(b) $\Rightarrow \nsubseteq \Rightarrow_{C}$

The failure of (a) in particular is no surprise given that there are both a positive and a negative condition in the definition of $C_{-}$. The witness to a non-valid inference might disappear by shifting to a bigger consequence relation. More surprisingly, the situation is no better for Bolzano consequences.

Proposition 12. There are languages $L$ and sets $X, Y \subseteq \operatorname{Symb}_{L}$ such that:
(a) $\Rightarrow_{X} \subseteq \Rightarrow_{Y}$ but $C_{\Rightarrow_{X}} \nsubseteq C_{\Rightarrow_{Y}}$
(b) $\Rightarrow_{X} \nsubseteq \Rightarrow_{C_{A_{X}}}$

## 4 Extra symbols

The following example vividly illustrates the importance of having extra symbols available in a language. Let $S y m b_{L}=\{a, b\}$, Sent $_{L}=\left\{R x y: x, y \in S y m b_{L}\right\}$, and $\operatorname{Tr}_{L}=\{R a a, R b b, R a b\}$. For example,

$$
\Rightarrow_{\emptyset} R a a,,^{10} \not \not_{\emptyset} R a b, \quad \Rightarrow_{\{a\}} R a b
$$

Here, you must move two symbols in order to turn a true sentence into a false one. As a result, $C_{-}$picks no constants at all: for all $X \subseteq S y m b_{L}, C_{\Rightarrow_{x}}=\emptyset$. However, expand $L$ conservatively to $L^{\prime}$ by adding at least one new symbol $c$, while $\operatorname{Tr}_{L}=\operatorname{Tr}_{L^{\prime}} \cap \operatorname{Sent} t_{L}$. Then, regardless of the truth values of new sentences in $L^{\prime}$ :
(6) In $L^{\prime}$, for all $X \subseteq \operatorname{Symb}_{L}, C_{\Rightarrow_{x}}=X$.

For example, we now have $\Rightarrow_{\{a\}} R a b$ in $L^{\prime}$ (by conservativity), but $\not \not_{\{a\}} R c b$, (by the replacement $\rho(c)=b, \rho(b)=a$ ). Thus, in $L^{\prime}, a \in C_{\Rightarrow_{\{a\}}}$.

[^57]
### 4.1 Richness and abundance

One way of making extra symbols available is to simply assume that there are infinitely many symbols of each category in L. Call such languages rich. Note that nothing prevents most of these symbols from meaning the same.

Proposition 13. If $L$ is rich, then $\Rightarrow_{X} \subseteq \Rightarrow_{Y}$ implies $\Rightarrow_{X}=\Rightarrow_{X \cap Y}$. In particular, for any $X$, the set $\left\{Z: \Rightarrow_{Z}=\Rightarrow_{X}\right\}$ is closed under finite intersections, so if $X$ is finite, this set has a smallest element.

Proposition 14. If $L$ is rich, and $X$ is minimal and finite, then $C_{\Rightarrow_{x}}=X$.
Using a variant of the earlier example, one can show that the assumption of finiteness in this proposition is essential.

Corollary 2. If $L$ is rich, then for finite $X, \Rightarrow_{X}=\Rightarrow_{C \Rightarrow_{X}}$.
Corollary 3. If $L$ is rich, then every finite $X \subseteq S y m b_{L}$ has a unique smallest subset, namely $C_{\Rightarrow_{X}}$, that generates $\Rightarrow_{X}$.

Here is an even stronger requirement on $L . u$ and $u^{\prime}$ (of the same category) are synonymous,

$$
u \equiv_{L} u^{\prime}
$$

iff replacing (some) occurrences of $u$ by $u^{\prime}$ or vice versa does not change the truth value of $L$-sentences. We say that $L$ is abundant iff there are infinitely many synonyms of each symbol. So all the results above hold for abundant $L$, but in addition we have

Proposition 15. If $L$ is abundant, minimality and strong minimality coincide.
Another variant of our example shows that this can fail when only richness is assumed.

Corollary 4. If $L$ is abundant, the results of Proposition 14 and Corollaries 2 and 3 hold for infinite $X$ as well.

### 4.2 Expansions

Richness and abundance may seem a bit extravagant assumptions. What one really needs, however, is the ability to add new symbols to $L$, in particular symbols with the same meaning as old ones, i.e. synonyms or copies. We now slightly revise our Bolzano set-up to make this possible.

Recall that an interpreted language $L$, as we defined it, comes with sets $\operatorname{Symb}_{L}, \operatorname{Sent}_{L}$, and $\operatorname{Tr}_{L}$; in fact, we may set $L=\left\langle\operatorname{Symb}_{L}, \operatorname{Sent}_{L}, \operatorname{Tr}_{L}\right\rangle$. We say that $L^{\prime}$ is an expansion of $L, L \leq L^{\prime}$, iff $\operatorname{Symb}_{L} \subseteq \operatorname{Symb}_{L^{\prime}}$, Sent ${ }_{L}=\left\{\varphi \in \operatorname{Sent}_{L^{\prime}}\right.$ : $\left.V_{\varphi} \subseteq \operatorname{Symb}_{L}\right\}$, and $\operatorname{Tr}_{L}=\operatorname{Tr}_{L^{\prime}} \cap$ Sent $_{L} . L^{\prime}$ is an expansion with copies, $L \leq_{c} L^{\prime}$, iff in addition every new symbol is synonymous, in $L^{\prime}$, with some $L$-symbol.

Proposition 16. $\leq$ is a partial order (reflexive, antisymmetric, and transitive), and $\leq_{c}$ is a sub-order.

A partially ordered set $Z$ is directed iff it is upward closed: if $a, b \in Z$ there is $c \in Z$ such that $a \leq c$ and $b \leq c$. Now, our idea is to replace the fixed language $L$ with a directed family $\mathcal{L}$ of expansions of $L$. This requires a slight reformulation of what we have done so far. In what follows, $\mathcal{L}$ is any directed family of expansions of $L$. To start with Bolzano consequence, suppose $\Gamma \cup\{\varphi\} \subseteq$ $S_{e n t}^{L}$ and $X \subseteq S y m b_{L}$.

Definition 7. $\Gamma \Rightarrow_{X, L} \varphi$ iff for every $L^{\prime} \in \mathcal{L}$ and every replacement $\rho$ in $L^{\prime}$ (for $\Gamma$ and $\varphi$ ) which is the identity on $X$, if $\Gamma[\rho] \subseteq \operatorname{Tr}_{L^{\prime}}$, then $\varphi[\rho] \in \operatorname{Tr}_{L^{\prime}}$.

The family $\mathcal{L}$ is suppressed in this notation, and has to be made clear in context. If $\mathcal{L}=\{L\}$, we have our previous notion of Bolzano consequence: $\Rightarrow_{X, L}=\Rightarrow_{X}$. Normally, the sentences we talk about will belong to several languages in $\mathcal{L}$.. That this is not a problem follows from

Lemma 3. If $\Gamma \cup\{\varphi\} \subseteq \operatorname{Sent}_{L}, X \subseteq \operatorname{Symb}_{L}$, and $L^{\prime} \in \mathcal{L}$, then

$$
\Gamma \Rightarrow_{X, L} \varphi \text { iff } \Gamma \Rightarrow_{X, L^{\prime}} \varphi,
$$

where the right-hand side is relative to the subclass $\mathcal{L}^{\prime}=\left\{L^{\prime \prime} \in \mathcal{L}: L^{\prime} \leq L^{\prime \prime}\right\}$.
In what follows, when $\mathcal{L}$ is given and $L^{\prime} \in \mathcal{L}$, we always understand $\Rightarrow_{X, L^{\prime}}$ to be relative to the corresponding subfamily generated by $L^{\prime}$.

Next, we extend the notion of (strong) minimality to the new set-up: $X$ is minimal iff for each $u \in X$ there is $L^{\prime} \in \mathcal{L}$ such that $\Rightarrow_{X, L^{\prime}} \neq \Rightarrow_{X-\{u\}, L^{\prime}}$, and analogously for strong minimality. Finally, we extend the definition of $C_{-}$to the case of consequence relations of the form $\Rightarrow \Rightarrow_{X, L}$. Let $u \in S y m b_{L}$.

Definition 8. $u \in C_{\Rightarrow x, L}$ iff there are $L^{\prime} \in \mathcal{L}, \Gamma \cup\{\varphi\} \subseteq$ Sent $_{L^{\prime}}$, and $u^{\prime} \in$ Symb $_{L^{\prime}}$ such that $\Gamma \nRightarrow_{X, L^{\prime}} \varphi$ but $\Gamma\left[u / u^{\prime}\right] \nRightarrow_{X, L^{\prime}} \varphi\left[u / u^{\prime}\right]$.

Call a family $\mathcal{L}$ is copy-closed iff for every $L^{\prime} \in \mathcal{L}$ and every $A \subseteq \operatorname{Symb}_{L^{\prime}}$ there are $L^{\prime \prime} \in \mathcal{L}$ and $B \subseteq \operatorname{Symb}_{L^{\prime \prime}}$ such that $B \cap \operatorname{Symb}_{L^{\prime}}=\emptyset$ and there is a copy $b \in B$ of every $a \in A$. A simple case of a copy-closed family is $\operatorname{copies}(L)=$ $\left\{L^{\prime}: L \leq_{c} L^{\prime}\right\}$. This is essentially the interpreted language $L$ with the possibility of adding (arbitrarily many) new names of already named things. Thus, it is a very mild extension of the original Bolzano set-up. Now all results assuming richness or abundance from the previous subsection hold automatically relative to copy-closed families, without any further assumptions:

Proposition 17. Relative to a copy-closed directed family of expansions of $L$ :
(a) Minimality and strong minimality coincide.
(b) For all $X \subseteq \operatorname{Symb}_{L}$, $\Rightarrow{ }_{X, L}=\Rightarrow_{C_{\exists} \exists_{X, L}}$.
(c) Each $X \subseteq$ Symb $_{L}$ has a unique smallest subset, $C_{\Rightarrow_{X, L}}$, generating $\Rightarrow_{X, L}$.

## 5 Galois connections

### 5.1 General consequence relations

We generalized our initial framework by working with directed families of expansions of $L$. In terms of Figure 3.1, the sets of symbols we are interested in are still subsets $S_{y m b}$. But such sets generate consequence relations for $L$ as well as for the expansions of $L$. In particular, the extended Definition 8 of $C_{-}$appeals not only to the consequence relation of $L$ but also to those of the expansions. As a result, we need to extend our notion of a consequence relation.

Definition 9. A general consequence relation for a family of languages $\mathcal{L}$ is a family of consequence relations $\Rightarrow=\left\{\Rightarrow_{L^{\prime}}\right\}_{L^{\prime} \in \mathcal{L}}$ such that for all $L^{\prime}, L^{\prime \prime} \in \mathcal{L}$ with $L^{\prime} \leq L^{\prime \prime}, \Rightarrow_{L^{\prime}} \subseteq \Rightarrow_{L^{\prime \prime}}$.

For $X \subseteq \operatorname{Symb}_{L}$, let $\Rightarrow_{X}$ be the family $\left\{\Rightarrow_{X, L^{\prime}}\right\}_{L^{\prime} \in \mathcal{L}} . \Rightarrow_{X}$ is a general consequence relation. Note that the extended Definition 8 of $C_{-}$applies not just to $\Rightarrow_{X, L}$ but to any general consequence relation. Given a directed family $\mathcal{L}$ of expansions of $L$, we let $G C O N S_{L}$ be the class of general consequence relations for $\mathcal{L}$ and $B G C O N S_{L}$ the class of general consequence relations of the form $\Rightarrow_{X}$.

### 5.2 Galois connection for copies

What kind of correspondence do we get between $\Rightarrow_{X}$ and $C_{-}$in this setting? We want something as close as possible to an isomorphism, with as few assumptions as possible on $\mathcal{L}$. A relevant notion of correspondence in that context is the notion of Galois connection. A Galois connection between two ordered sets $A$ and $B$ is a pair $(f, g)$ of functions, with $f: A \rightarrow B$ and $g: B \rightarrow A$, such that the following four conditions hold: (1) $f$ is monotone, (2) $g \circ f$ is decreasing, (3) $g$ is monotone, (4) $f \circ g$ is increasing. $f$ is then an isomorphism with inverse $g$ from $g(B)$ to $f(A)$. Intuitively, $f$ and $g$, even though they do not constitute a full-blown isomorphism, give rise to one between the sufficiently well-behaved subsets $g(B)$ and $f(A)$.

Proposition 18. Relative to a copy-closed family, the following hold:
(a) $\Rightarrow_{X} \subseteq \Rightarrow_{Y}$ implies $C_{\Rightarrow_{X}} \subseteq C_{\Rightarrow_{Y}}$
(b) $\Rightarrow_{X} \subseteq \Rightarrow_{C} \Rightarrow_{X}$

Considering $\left(\Rightarrow_{-}, C_{-}\right)$as a tentative Galois connection between $\wp\left(S y m b_{L}\right)$ and $G C O N S_{L}$, conditions (1) and (2) are always satisfied. (a) and (b) in Proposition 18 are (3) and (4), when the class of general consequence relations is restricted to $B G C O N S_{L}$. We have shown:

Theorem 1. ( $\left.\Rightarrow_{-}, C_{-}\right)$is a Galois connection between $\wp\left(\right.$ Symb $\left._{L}\right)$ and $B G C O N S_{L}$ for copy-closed families of languages.

The set $C_{B G C O N S_{L}}$ of sets of symbols which are the image of some $\Rightarrow_{X}$ in $B G C O N S_{L}$ under $C_{-}$is of special interest, since it is the restriction of $\wp\left(\right.$ Symb $\left._{L}\right)$ for which $\Rightarrow{ }_{-}$is an isomorphism.
Proposition 19. Relative to a copy-closed family of expansions of $L, C_{B G C O N S_{L}}$ is the set of minimal sets in $\wp\left(S_{y m b}^{L}\right)$.

On the left-hand side of our picture, the well-behaved objects in $\wp\left(S y m b_{L}\right)$ are the minimal sets. On the right-hand side, our Galois connection has the nontypical property that $\Rightarrow$ _ is onto. If we were to extend the picture to include not only $\mathrm{BGCONS}_{L}$ but all of $G C O N S_{L}$, we would get that the part of $\mathrm{GCONS}_{L}$ for which we have the isomorphism is precisely $\operatorname{BGCONS}_{L}$, but the properties stated in Proposition 18 for relations in $B G C O N S_{L}$ do not hold for all relations in $\mathrm{GCONS}_{L}$.
Question: Is there a natural class $G C O N S_{L}^{*} \supseteq B G C O N S_{L}$ for which they hold?

### 5.3 Tarskian consequence

$\operatorname{copies}(L)$ is the simplest case of a copy-closed family of languages. A maximal case is the family of all expansions of a base-language $L$. Instead of just fixing a set of true sentences, consider interpreted languages $L$ for which truth is defined as truth with respect to a fixed intended interpretation $I$ of symbols of $L$. Let ' $J \vDash \varphi$ ' abbreviate ' $\varphi$ is true according to interpretation $J$ '. Tarskian consequence (with a fixed domain of interpretation) can then be defined:

Definition 10. $\Gamma \not \vDash_{X} \varphi$ iff for all $J$ such that $J \approx_{X} I$, if $J \vDash \Gamma$, then $J \vDash \varphi$.
( $J \approx_{X} I$ means that $J$ and $I$ agree on $X \subseteq$ Symb $_{L}$.) Tarskian consequence is equivalent to Bolzano consequence with respect to the family of all expansions:
Proposition 20. $\Gamma \vDash_{X} \varphi$ iff for every $L^{\prime} \geq L$ and every replacement $\rho$ that keeps all elements in $X$ fixed, if $I^{\prime} \vDash \Gamma[\rho]$, then $I^{\prime} \vDash \varphi[\rho]$.
(Here $I^{\prime}$ is an interpretation extending $I$ to the new symbols in Symb $_{L^{\prime}}$.) Together with Proposition 18 and the fact that the family of all expansions is copy-closed, this implies that there is a Galois connection between $\wp\left(S y m b_{L}\right)$ and the class of Tarskian consequence relations.

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# Modified Numerals as Post-suppositions 

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#### Abstract

The paper provides a compositional account of cumulative readings with non-increasing modified numerals (aka van Benthem's puzzle), e.g., Exactly three boys saw exactly five movies. The main proposal is that modified numerals make two kinds of semantic contributions. Their asserted/at-issue contribution is a maximization operator that introduces the maximal set of entities that satisfies their restrictor and nuclear scope. The second contribution is a post-supposition, i.e., a cardinality constraint that needs to be satisfied relative to the context that results after the at-issue meaning is evaluated. We take contexts to be sets of variable assignments relative to which quantificational expressions are interpreted and which are updated as a result of their interpretation.


## 1 Cumulativity and Modified Numerals

The goal of the paper is to provide a compositional account of cumulative readings with non-increasing modified numerals (aka van Benthem's puzzle, van Benthem 1986), exemplified in (1) below. We discuss mainly exactly $n$ numerals, but the same problem arises with other non-increasing numerals, e.g., at most $n$.
(1) Exactly three ${ }^{x}$ boys saw exactly five ${ }^{y}$ movies.

The most salient reading of sentence (1) is the surface-scope distributive one, namely: there are exactly three boys such that each of them saw exactly five movies (possibly different from boy to boy). We are not interested in this reading (although we discuss it briefly later on), but in the cumulative reading, namely: consider the maximal number of boys that saw a movie and the maximal number of movies seen by a boy; there are three such boys and five such movies. This reading of sentence (1) is true in Figure 2 below and false in Figure 1. Note that Figure 1 is exactly like Figure 2, with the addition of boy $\mathbf{b}_{\mathbf{1}}$, movie $\mathbf{m}_{\mathbf{1}}$ and the arrow between them symbolizing the seeing relation at the very top of Figure 1.

Importantly, the cumulative reading is different from: the maximal number of boys that (between them) saw exactly five movies is three. ${ }^{1}$ This is actually

[^58]not a reading of sentence (1), although it bears some resemblance to its distributive reading. In fact, the situations in Figures 1 and 2 above distinguish between them: the cumulative reading is intuitively false in Figure 1 (4 boys and 6 movies) and true in Figure 2, while the other 'reading' just mentioned is true in both situations. The distinction between the cumulative reading and this other 'reading' is important for theoretical reasons: many formal systems derive something like it when they attempt to capture the cumulative reading.


Figure 2
boys movies


Our proposal is that modified numerals make two kinds of contributions to the meaning of sentences like (1): $(i)$ their asserted/at-issue contribution is a maximization operator that introduces the maximal set of entities that satisfies their restrictor and nuclear scope; (ii) they also contribute a post-supposition, i.e., a cardinality constraint (e.g., exactly five) that needs to be satisfied relative to the context that results after the at-issue meaning is evaluated. For our purposes, contexts are sets of total variable assignments relative to which quantificational expressions are interpreted and which are updated as a result of the interpretation of such expressions. That is, we work with a simplified version of Dynamic Plural Logic (DPlL, van den Berg 1996).

The main difference between the present account and Krifka (1999) is conceptual: we take modified numerals to constrain quantificational - not focus alternatives, where a quantificational alternative is one of the assignments satisfying a quantificational expression. Thus, we reconceptualize DPlL as the logic of quantificational alternatives in natural language interpretation.

## 2 Modified Numerals as Post-suppositions

We work with the usual models for classical first-order logic (FOL) $\mathfrak{M}=\langle\mathfrak{D}, \mathfrak{I}\rangle$ : $\mathfrak{D}$ is the domain of individuals and $\mathfrak{I}$ is the basic interpretation function such that $\mathfrak{I}(R) \subseteq \mathfrak{D}^{n}$ for any $n$-ary relation $R$. An $\mathfrak{M}$-assignment $g$ is a total function
from the set of variables $\mathcal{V}$ to $\mathfrak{D}$. The essence of quantification in FOL is pointwise/variablewise manipulation of variable assignments, abbreviated $h[x] g$. We generalize this to sets of assignments $H[x] G$ cumulative-quantification style.
(3) $h[x] g:=h$ differs from $g$ at most with respect to the value assigned to $x$

$$
H[x] G:=\left\{\begin{array}{l}
\text { for all } h \in H, \text { there is a } g \in G \text { such that } h[x] g  \tag{4}\\
\text { for all } g \in G, \text { there is a } h \in H \text { such that } h[x] g
\end{array}\right.
$$

This is not a way of sneaking cumulativity into the system. Formally, $H[x] G$ is a natural generalization of $h[x] g$ : it is an equivalence relation over sets of total assignments, just as $h[x] g$ is an equivalence relation over total assignments.

Atomic formulas are tests, i.e., they check that the input context $G$ satisfies them and pass this context on. Cardinality constraints on the values of variables are also tests; the cardinality of the set of individuals $X$ is symbolized as $|X|$. Dynamic conjunction and random assignment are interpreted DPL-style.
(5) $\llbracket R\left(x_{1}, \ldots, x_{n}\right) \rrbracket^{\langle G, H\rangle}=\mathbb{T}$ iff

$$
G=H \text { and for all } h \in H,\left\langle h\left(x_{1}\right), \ldots, h\left(x_{n}\right)\right\rangle \in \Im(R)
$$

(6) $G(x):=\{g(x): g \in G\}$
(7) $\llbracket x=n \rrbracket^{\langle G, H\rangle}=\mathbb{T}$ iff $G=H$ and $|H(x)|=n$
(8) $\llbracket x \leq n \rrbracket^{\langle G, H\rangle}=\mathbb{T}$ iff $G=H$ and $|H(x)| \leq n$
(9) $\llbracket x \geq n \rrbracket^{\langle G, H\rangle}=\mathbb{T}$ iff $G=H$ and $|H(x)| \geq n$
(10) $\llbracket \phi \wedge \psi \rrbracket^{\langle G, H\rangle}=\mathbb{T}$ iff there is a $K$ s.t. $\llbracket \phi \rrbracket^{\langle G, K\rangle}=\mathbb{T}$ and $\llbracket \psi \rrbracket^{\langle K, H\rangle}=\mathbb{T}$
(11) $\llbracket[x] \rrbracket^{\langle G, H\rangle}=\mathbb{T}$ iff $H[x] G$

The translation of singular indefinite articles and bare numerals has the form given in (12) below. Square brackets [] indicate restrictor formulas and round brackets () indicate nuclear scope formulas. As (13) and (14) show, $n$ is 1 for singular indefinite articles, $n$ is 2 for the bare numeral two etc. This translation schema is just an abbreviation, provided in (15). Proper names are interpreted like indefinites; their restrictor requires the variable to have the same value as a non-logical constant, e.g., JASPER in (16) below (where JASPER denotes the individual Jasper). Pronouns are indexed with the variable introduced by their antecedent and their translation is that variable itself; we ignore differences between singular and plural pronouns. For example, (17) is translated as in (18).
(12) $\exists x[x=n \wedge \phi](\psi) \quad$ intuitively: $n \phi$-individuals are $\psi$
(13) $\quad \mathrm{A}^{x}$ wolf came in. $\rightsquigarrow \exists x[x=1 \wedge \operatorname{wOLF}(x)](\operatorname{COME-IN}(x))$
(14) Two ${ }^{x}$ wolves came in. $\rightsquigarrow \exists x[x=2 \wedge \operatorname{wolf}(x)](\operatorname{COME}-\operatorname{IN}(x))$
(15) $\exists x[x=n \wedge \phi](\psi):=[x] \wedge x=n \wedge \phi \wedge \psi$
(16) $\exists x[x=\mathrm{JASPER}](\phi):=[x] \wedge x=\mathrm{JASPER} \wedge \phi$
(17) $\mathrm{A}^{x}$ wolf came in. $\mathrm{It}_{x}$ bit Jasper ${ }^{y}$.
(18) a. $\exists x[x=1 \wedge \operatorname{wOLF}(x)](\operatorname{COME-IN}(x)) \wedge \exists y[y=\operatorname{JASPER}](\operatorname{BitE}(x, y))$
b. $[x] \wedge x=1 \wedge \operatorname{wolf}(x) \wedge \operatorname{COME-IN}(x) \wedge[y] \wedge y=\operatorname{JASPER} \wedge \operatorname{BITE}(x, y)$

The definition of truth below says that a formula $\phi$ is true if there is at least one successful way to update the input context of evaluation $G$ with $\phi$. Except

## General Program

for the fact that we work with sets of assignments instead of single assignments, our interpretation function and truth definition are not different from the corresponding FOL or DRT/FCS notions (only their packaging is different).
(19) Truth: a formula $\phi$ is true relative to an input set of assignments $G$ iff there is an output set of assignments $H$ such that $\llbracket \phi \rrbracket^{\langle G, H\rangle}=\mathbb{T}$.

### 2.1 Modified Numerals

We capture the meaning of modified numerals by means of a maximization operator $\mathbf{M}$ that enables us to introduce the set of all individuals satisfying their restrictor and nuclear scope. For example, $\mathbf{M}([x] \wedge \operatorname{BOY}(x))$ introduces the variable $x$ and requires it to store all and only the individuals satisfying $\operatorname{BOY}(x)$ : $[x] \wedge \operatorname{BOY}(x)$ ensures that we store in $x$ only individuals that satisfy $\operatorname{BOY}(x)$ and $\mathbf{M}$ ensures that we cannot store more individuals in $x$ and still satisfy $\operatorname{BOY}(x)$. We can now provide a preliminary translation for modified numerals, which has the form in (21). For example, Exactly three ${ }^{x}$ boys left is translated as in (22): we store in $x$ all the boys that left and test that there are 3 such entities.

$$
\begin{align*}
& \llbracket \mathbf{M}(\phi) \rrbracket^{\langle G, H\rangle}=\mathbb{T} \text { iff }  \tag{20}\\
& \llbracket \phi \rrbracket^{\langle G, H\rangle}=\mathbb{T} \text { and there is no } H^{\prime} \text { s.t. } H \subsetneq H^{\prime} \text { and } \llbracket \phi \rrbracket^{\left\langle G, H^{\prime}\right\rangle}=\mathbb{T} \\
& \text { exactly } n \quad \exists x=n[\phi](\psi):=\mathbf{M}([x] \wedge \phi \wedge \psi) \wedge x=n \\
& \exists x=3[\operatorname{BOY}(x)](\operatorname{LEAVE}(x)):=\mathbf{M}([x] \wedge \operatorname{BOY}(x) \wedge \operatorname{LEAVE}(x)) \wedge x=3
\end{align*}
$$

We can further elaborate on the above sentence with They were hungry and derive the intuitively-correct truth conditions for the resulting discourse. But we derive incorrect truth conditions for sentence (1):
a. $\exists x=3[\operatorname{Boy}(x)](\exists y=5[\operatorname{MOvie}(y)](\operatorname{seE}(x, y)))$
b. $\mathbf{M}([x] \wedge \operatorname{BOY}(x) \wedge \mathbf{M}([y] \wedge \operatorname{MOVIE}(y) \wedge \operatorname{SEE}(x, y)) \wedge y=5) \wedge x=3$

We do not derive the cumulative reading, true only in Figure 2, but the 'reading' true in both Figure 1 and Figure 2: the maximal number of boys that (between them) saw exactly 5 movies is 3 . What we want is a translation that places the cardinality requirement $y=5$ contributed by the direct object outside the scope of the operator $\mathbf{M}([x] \wedge \ldots)$ contributed by the subject, as shown in (24a) or, equivalently, (24b) below. These formulas capture the cumulative reading of (1): we introduce the maximal set $x$ of boys that saw a movie and the maximal set $y$ of movies seen by a boy and test that there are 5 such movies and 3 such boys.
a. $\mathbf{M}([x] \wedge \operatorname{BOY}(x) \wedge \mathbf{M}([y] \wedge \operatorname{MOVIE}(y) \wedge \operatorname{SEE}(x, y))) \wedge y=5 \wedge x=3$
b. $\mathbf{M}([x] \wedge \operatorname{Boy}(x) \wedge[y] \wedge \operatorname{MOVie}(y) \wedge \operatorname{SeE}(x, y)) \wedge y=5 \wedge x=3$

### 2.2 Post-suppositions

To compositionally derive such a representation, we will take cardinality requirements to be part of a dimension of meaning separate from the asserted/at-issue
meaning (but closely integrated with it). We take them to be post-suppositions, i.e., tests on output contexts, as opposed to presuppositions, which are tests on input contexts. See Lauer (2009) for another use of this notion and Farkas (2002) and Constant (2006) for related post-assertion constraints on output contexts.

Post-suppositions are formulas introduced at certain points in the interpretation that are passed on from local context to local context and that need to be satisfied only globally, relative to the final output context. Our notion of context is now a set of assignments $G$ indexed with a set of tests $\zeta$, represented as $G[\zeta]$. All the above formulas are interpreted in the same way, except that we accumulate post-suppositions as we incrementally update our input context. Thus, our interpretation function is of the form $\llbracket \llbracket \rrbracket^{\left\langle G[\zeta], H\left[\zeta^{\prime}\right]\right\rangle}$, where $\zeta \subseteq \zeta^{\prime}$.

We mark a test $\phi$ as a post-supposition by superscripting it, as shown in (25) below; semantically, we completely ignore the input set of assignments $G$ and simply add $\phi$ to the set of tests $\zeta$. Such superscripted tests are post-suppositional in the sense that they are required to be true relative to the final output context. This is formalized by the new definition of truth in (26) below, which treats the formulas $\psi_{1}, \ldots, \psi_{m}$ as post-suppositions because they are tests performed on the final output set of assignments $H$ (again: contrast this with presuppositions).
(25) $\llbracket \phi \rrbracket^{\left\langle G[\zeta], H\left[\zeta^{\prime}\right]\right\rangle}=\mathbb{T}$ iff $\phi$ is a test, $G=H$ and $\zeta^{\prime}=\zeta \cup\{\phi\}$
(26) Truth: a formula $\phi$ is true relative to an input context $G[\emptyset]$, where $\emptyset$ is the empty set of tests, iff there is an output set of assignments $H$ and a (possibly empty) set of tests $\left\{\psi_{1}, \ldots, \psi_{m}\right\}$ s.t. $\llbracket \phi \rrbracket^{\left\langle G[\emptyset], H\left[\left\{\psi_{1}, \ldots, \psi_{m}\right\}\right]\right\rangle}=\mathbb{T}$ and $\llbracket \psi_{1} \wedge \ldots \wedge \psi_{m} \rrbracket^{\langle H[\emptyset], H[\emptyset]\rangle}=\mathbb{T}$.
Modified numerals are interpreted as before, except that the cardinality requirement is a post-supposition. Numeral modifiers exactly, at most, at least etc. are functions taking a bare numeral as their argument and introducing ( $i$ ) a maximization operator $\mathbf{M}$ scoping over the random assignment and the restrictor and nuclear scope formulas and (ii) a post-supposition consisting of the cardinality requirement ordinarily contributed by the bare numeral. The resulting translation of sentence (1) in (28) below derives the correct cumulative truth conditions. Note that the four formulas in (28a,b,c,d) are truth-conditionally equivalent.
exactly $n \quad \exists^{x=n}[\phi](\psi):=\mathbf{M}([x] \wedge \phi \wedge \psi) \wedge x=n$
a. $\exists^{x=3}[\operatorname{BOY}(x)]\left(\exists^{y=5}[\operatorname{MOVIE}(y)](\operatorname{SEE}(x, y))\right)$
b. $\mathbf{M}\left([x] \wedge \operatorname{BOY}(x) \wedge \mathbf{M}([y] \wedge \operatorname{MOVIE}(y) \wedge \operatorname{SEE}(x, y)) \wedge^{y=5}\right) \wedge^{x=3}$
c. $\mathbf{M}([x] \wedge \operatorname{BOY}(x) \wedge \mathbf{M}([y] \wedge \operatorname{MOVIE}(y) \wedge \operatorname{SEE}(x, y))) \wedge^{y=5} \wedge^{x=3}$
d. $\mathbf{M}([x] \wedge \operatorname{BOY}(x) \wedge[y] \wedge \operatorname{MOVie}(y) \wedge \operatorname{SeE}(x, y)) \wedge y=5 \wedge x=3$

Just as before, if we elaborate on (1) with They liked them $_{y}$, we derive the correct interpretation for the entire discourse: every one of the three boys liked every movie he saw (and not the movies some other boy saw).

The proposed analysis of modified numerals involves three crucial ingredients: ( $i$ ) evaluation pluralities (sets of assignments), (ii) maximization operators over such pluralities and (iii) post-suppositions and their unusual scoping behavior. The following three sections provide independent evidence each for them.

## 3 Universal Quantifiers

The fact that we use evaluation pluralities enables us to also account for cumulative readings of universals (Schein 1993, Kratzer 2000, Champollion 2009). ${ }^{2}$

Consider the sentence in (29) below (from Kratzer 2000). Its cumulative reading is: there are three editors such that each of them caught at least one mistake and every mistake was caught by at least one of the three editors. We translate distributive universal quantification as shown in (30): we introduce the set of all individuals $x$ that satisfy the restrictor $\phi$ by means of the maximization operator $\mathbf{M} x$ and we check that each of these individuals also satisfies the nuclear scope $\psi$ by means of the distributivity operator $\delta$.
(29) Three ${ }^{x}$ copy editors (between them) caught every ${ }^{y}$ mistake in the manuscript.
(30) $\quad \forall x[\phi] \delta(\psi):=\mathbf{M} x(\phi) \wedge \delta(\psi)$
$\mathbf{M} x$ is the selective counterpart of the unselective, adverbial $\mathbf{M}$ : unselective $\mathbf{M}$ maximizes over sets of assignments $H$, while selective $\mathbf{M} x$ maximizes over sets of individuals $H(x)$ ('selective' and 'unselective' in the sense of Lewis 1975). Using unselective maximization for modified numerals is justified by the fact that their modifier can be non-adjacent/adverbial, as shown by the examples below.
(31)
$\llbracket \mathbf{M} x(\phi) \rrbracket^{\left\langle G[\zeta], H\left[\zeta^{\prime}\right]\right\rangle}=\mathbb{T}$ iff $\llbracket[x] \wedge \phi \rrbracket^{\left\langle G[\zeta], H\left[\zeta^{\prime}\right]\right\rangle}=\mathbb{T}$ and there is no $H^{\prime}$ s.t. $H(x) \subsetneq H^{\prime}(x)$ and $\llbracket[x] \wedge \phi \rrbracket^{\left\langle G[\zeta], H^{\prime}\left[\zeta^{\prime}\right]\right\rangle}=\mathbb{T}$.
(32) Three boys saw five movies, exactly/precisely/at (the) most.
(33) The league limits teams to playing two games in a row - or, at the most, four games in five days, NBA spokesman Tim Frank says. ${ }^{3}$

The distributivity operator $\delta$ in (34) (based on Brasoveanu 2008) says that we distributively update a set of assignments $G$ with a formula $\phi$ by updating each singleton set $\{g\} \subseteq G$ with $\phi$ and taking the union of the resulting output sets of assignments $K$. In addition, $\delta$ discharges all post-suppositions contributed by the formula in its scope. Thus, just like presuppositions, post-suppositions are not always satisfied globally, but can be satisfied/discharged at intermediate points in the semantic composition, i.e., in more local output contexts.
$\llbracket \delta(\phi) \rrbracket\left\langle G[\zeta], H\left[\zeta^{\prime}\right]\right\rangle=\mathbb{T}$ iff $\zeta=\zeta^{\prime}$ and there exists a relation $\mathcal{R}$ between
assignments and sets of assignments, i.e., of the form $\mathcal{R}(g, K)$, s.t. $(i)$
$G=\operatorname{Dom}(\mathcal{R})$ and $H=\bigcup \operatorname{Ran}(\mathcal{R})$ and $(i i)$ for all $g$ and all $K$ such that
$\mathcal{R}(g, K)$, there is a $($ possibly empty $)$ set of formulas $\left\{\psi_{1}, \ldots, \psi_{m}\right\}$ s.t.
$\llbracket \phi \rrbracket\left\{\{g\}[\zeta], K\left\lceil\zeta \cup\left\{\psi_{1}, \ldots, \psi_{m}\right\}\right]\right\rangle=\mathbb{T}$ and $\llbracket \psi_{1} \wedge \ldots \wedge \psi_{m} \rrbracket\langle K[\zeta], K[\zeta]\rangle=\mathbb{T}$

The translation of sentence (29) above is provided below: we introduce a set $x$ of three editors and the set $y$ of all mistakes and check that, for every assignment $h$ in the resulting output state $H$, the editor $h(x)$ caught the mistake $h(y)$.

[^59]a. $\exists x[x=3 \wedge \operatorname{EDitor}(x)](\forall y[\operatorname{mistakE}(y)] \delta(\operatorname{Catch}(x, y)))$
b. $[x] \wedge x=3 \wedge \operatorname{Editor}(x) \wedge \operatorname{M} y(\operatorname{MistakE}(y)) \wedge \delta(\operatorname{CATCH}(x, y))$

The distributivity operator $\delta$ is semantically vacuous in (35) - but not always. Consider the example below, from Kratzer (2000). This sentence does not have a cumulative reading to the effect that, between them, the editors caught a total of 500 mistakes. Its only reading is the distributive one: every editor is such that s/he caught 500 mistakes. We derive the distributive reading if the universal takes scope over the numeral every $\gg 500$. That is, cumulative readings are possible with universals only if they have narrow scope relative to the numerals they 'cumulate' with. As long as the non-surface scope $500 \gg$ every is blocked for sentence (36), we correctly derive the unavailability of the cumulative reading.
(36) Every ${ }^{x}$ copy editor caught $500^{y}$ mistakes in the manuscript.

$$
\begin{equation*}
\forall x[\operatorname{Editor}(x)] \delta(\exists y[y=500 \wedge \operatorname{MiStake}(y)](\operatorname{CATCh}(x, y))) \tag{37}
\end{equation*}
$$

We also account for mixed cumulative-distributive sentences, e.g., Three video games taught every quarterback two new plays (Schein 1993): every quarterback is related cumulatively to three video games (a total of three video games taught all the quarterbacks), but distributes in the usual way over two new plays (every quarterback learned two possibly different plays). This automatically follows in our system if we preserve the surface-scope relations three $\gg$ every $\gg$ two.

Finally, we capture the distributive reading of (1) by means of the operator $\delta$ : distributive modified numerals have a $\delta$ operator over their nuclear scope.
(38) $\exists^{x=n}[\phi] \delta(\psi):=\mathbf{M}([x] \wedge \phi \wedge \delta(\psi)) \wedge{ }^{x=n}$
(39) $\quad \exists^{x=3}[\operatorname{BOY}(x)] \delta\left(\exists^{y=5}[\operatorname{MOVIE}(y)] \delta(\operatorname{SeE}(x, y))\right)$

## 4 Implicatures

Analyzing modified numerals by means of a maximization operator over evaluation pluralities enables us to account for the independent observation that modified numerals do not trigger scalar implicatures, unlike bare numerals/indefinites. This is because the operator $\mathbf{M}$ contribute by modified numerals effectively eliminates referential uncertainty. In any given world, the variable introduced by a modified numeral can be associated with only one set of values: the set of all entities satisfying the restrictor and nuclear scope of the modified numeral. This is shown by the contrast below (from Umbach 2006).
(40) \{Two/\#At least two $\}$ boys were selling coke. They were wearing black jackets. Perhaps there were others also selling coke, but I didn't notice.

If there are more than two boys selling coke, the variable introduced by the bare numeral two can take different sets of two boys as values, i.e., the output contexts obtained after the update with a bare numeral may assign different sets of values to the variable contributed by the bare numeral. In contrast, the variable introduced by at least two has only one possible value: the set of all boys
selling coke. In any given world, all output contexts obtained after the update with a modified numeral assign the same value to the variable it contributes.

Thus, scalar implicatures are triggered by items that allow for referential indeterminacy/uncertainty. It is this semantic uncertainty that kicks off the pragmatic inferential process resulting in the addition of scalar implicatures.

But referential certainty is distinct from epistemic certainty. Suppose that our contexts are not simply sets of assignments $G, H, \ldots$, but pairs of a world and a set of assignments $\langle w, G\rangle,\left\langle w^{\prime}, H\right\rangle, \ldots$ (in the spirit of Heim 1982). The information state at any point in discourse consists of all the pairs that are still live options, i.e., that are compatible with all the previous updates. Referential uncertainty is encoded by the second member of such pairs. Epistemic uncertainty is encoded by the first member of the pairs, i.e., by the set of worlds in the current information state - aka the current Context Set (Stalnaker 1978).

Modified numerals are referentially determined, but epistemically uncertain. If we fix the world, the variable contributed by the modified numeral has only one value, but this value may vary from world to world. Hence, we can use them (as opposed to their bare counterparts) only if we are epistemically uncertain about the cardinality of the maximal set of entities introduced by them.

This is the reason for the modal readings of indicative sentences with modified numerals (no need for insertion of covert modals, as in Nouwen 2009 and references therein). Jasper invited maximally 50 people to his party (from Nouwen 2009) is felicitous only if the speaker is uncertain with respect to the cardinality of the set of invited people (hence the 'range of values' interpretation). So, if the speaker does not know how many people Jasper invited, it is unacceptable to continue with: 43 , to be precise. The same pragmatic infelicity can arise intrasententially: \#A hexagon has at most/maximally/up to 11 sides (Nouwen 2009) is infelicitous if we know what the word hexagon means.

Finally, given their epistemic uncertainty, modified numerals trigger epistemic implicatures of the kind proposed in Büring (2008) for at least.

## 5 Modals and Modified Numerals

This section provides independent evidence for the analysis of modified numerals in terms of post-suppositions. The unusual scoping behavior of post-suppositions and their interaction with distributivity enables us to capture the scopal interactions between modified numerals and modals. This is a novel result that solves an outstanding problem for the current analyses based on standard assumptions about the semantics of minimizers/maximizers and necessity/possibility modals (see Nouwen 2009 and references therein for more discussion). We provide the representations for two typical sentences (from Nouwen 2009) instantiating this problem and leave a more detailed discussion for another occasion.

Necessity modals are analyzed as distributive universal quantifiers in the modal domain; in (42) below, $R$ is a contextually-provided accessibility relation and $R_{w^{*}}(w)$ is interpreted as: $w$ is an $R$-accessible world from the actual world $w^{*}$. The reading of sentence (41) we are after is: the minimum number of books
that Jasper is allowed to read is 10 . The update in (43) captures this reading: each world $w$ that is $R$-accessible from the actual world $w^{*}$ is such that, if we store in $y$ all the books Jasper read, the cardinality of the set of books is at least 10. That is: Jasper reads at least 10 books in every deontically-ideal world $w$.
(41) Jasper $^{x}$ should $^{w}$ read at least ten ${ }^{y}$ books (to please his mother).
(42) $\quad \operatorname{NEC} w(\phi):=\mathbf{M}\left([w] \wedge R_{w^{*}}(w)\right) \wedge \delta(\phi)$
(43) a. NEC $w\left(\exists x[x=\mathrm{JASPER}]\left(\exists \exists^{y}{ }_{w} 10\left[\operatorname{BOOK}_{w}(y)\right]\left(\operatorname{READ}_{w}(x, y)\right)\right)\right)$
b. $\mathbf{M}\left([w] \wedge R_{w^{*}}(w)\right) \wedge$

$$
\delta\left([x] \wedge x=\operatorname{JASPER} \wedge \mathbf{M}\left([y] \wedge \operatorname{BOOK}_{w}(y) \wedge \operatorname{READ}_{w}(x, y)\right) \wedge y \geq w 10\right)
$$

We also account for maximal permissions like (44) below, interpreted as: the maximum number of people Jasper is allowed to invite is 10 . We take possibility modals to be the counterparts of a modified numeral in the modal domain that contributes a non-singleton cardinality requirement. The maximization operator $\mathbf{M}$ over worlds is independently justified by modal subordination (Roberts 1989), e.g., A wolf might come in. It would eat Jasper first is interpreted as: for any epistemic possibility of a wolf coming in, the wolf eats Jasper first. The update in (46) introduces all the worlds $w$ that are $R$-accessible from the actual world $w^{*}$ and such that Jasper invites some people in $w$. For each such world $w, y$ stores all the people invited by Jasper. Finally, we check that there is more than one world $w$ and that the cardinality of the set $y$ in each world $w$ is at most 10 .
(44) $\mathrm{Jasper}^{x}$ is allowed ${ }^{w}$ to invite at most ten ${ }^{y}$ people.
(45) $\operatorname{POS} w(\phi):=\exists^{w>1}\left[R_{w^{*}}(w)\right](\phi)=\mathbf{M}\left([w] \wedge R_{w^{*}}(w) \wedge \phi\right) \wedge w>1$

$$
\begin{align*}
& \text { a. } \operatorname{POS} w\left(\exists x[x=\operatorname{JASPER}]\left(\exists y \leq_{w} 10\left[\operatorname{PERSON}_{w}(y)\right]\left(\operatorname{INVITE}_{w}(x, y)\right)\right)\right)  \tag{46}\\
& \text { b. } \\
& \mathbf{M}\left([w] \wedge R_{w^{*}}(w) \wedge[x] \wedge x=\operatorname{JASPER} \wedge[y] \wedge \operatorname{PERSON}_{w}(y) \wedge \operatorname{INVITE}_{w}(x, y)\right) \wedge
\end{align*}
$$

## 6 Conclusion

We introduced a framework that distinguishes evaluation plurality (sets of assignments) from domain plurality (non-atomic individuals). The maximization operator $\mathbf{M}$ and the distributivity operator $\delta$ are to evaluation pluralities what the familiar Link-style sum and distributivity operators are to domain pluralities. Cumulativity is just non-distributivity with respect to evaluation pluralities, while collectivity is just non-distributivity with respect to domain pluralities.

Modified numerals are maximal and introduce cardinality post-suppositions, which are constraints on output contexts - in contrast to presuppositions, which constrain input contexts. Just as presuppositions, post-suppositions can be satisfied/discharged non-globally, e.g., in the scope of distributivity operators. Postsuppositions are distinct from regular at-issue meaning with respect to their evaluation order: they can constrain the final, global output context. The exceptional scoping behavior of post-suppositions enables us to account for cumulative readings of non-increasing modified numerals and for their interaction with modal verbs. The referential maximality of modified numerals accounts for the fact that they do not trigger scalar implicatures, but only epistemic implicatures.

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# Cumulative readings of every do not provide evidence for events and thematic roles 

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#### Abstract

An argument by Schein $(1986,1993)$ and Kratzer (2000) does not conclusively show that events and thematic roles are necessary ingredients of the logical representation of natural language sentences. The argument claims that cumulative readings of every can be represented only if at least agents are related to verbs via events and thematic relations. But scope-splitting accounts, which are needed anyway for noun phrases headed by every and other quantifiers, make it possible to represent cumulative readings in an eventless framework. While Kratzer regards the limited distribution of cumulative every as evidence for asymmetries in the logical representation of thematic roles, the empirical generalization on which she bases her reasoning is not the only plausible one. It looks more likely that every must be c-commanded by another quantifier in order to cumulate with it, no matter what its thematic role is.


## 1 Introduction

The question whether events and thematic roles are part of the logical representation of natural language sentences has been debated for over forty years. Early formal semantic work, as well as some modern authors, simply represents the meaning of verbs with $n$ syntactic arguments as $n$-ary relations. A transitive verb, for example, is assumed to denote a two-place relation. Against this, Davidson (1967) argued that verbs denote relations between events and their arguments, so that a transitive verb denotes a three-place relation. Once events have been introduced, it becomes possible to see verbs as predicates over events, and to express the relationship between events and their arguments by separate predicates, i.e., thematic roles. This is the Neo-Davidsonian position (e.g. Parsons, 1990; Schein, 1993). Finally, Kratzer (2000) argues for an asymmetric position, according to which only agents are represented as thematic roles. The positions are illustrated in Table 1.

[^60]| Position | Verbal denotation | Example: Brutus stabbed Caesar |
| :--- | :--- | :--- |
| Traditional | $\lambda y \lambda x[\operatorname{stab}(x, y)]$ | $\operatorname{stab}(b, c)$ |
| Classical Davidsonian | $\lambda y \lambda x \lambda e[\operatorname{stab}(e, x, y)]$ | $\exists e[\operatorname{stab}(e, b, c)]$ |
| Neo-Davidsonian | $\lambda e[\operatorname{stab}(e)]$ | $\exists e[\operatorname{stab}(e) \wedge \operatorname{agent}(e, b) \wedge$ theme $(e, c)]$ |
| Asymmetric | $\lambda y \lambda e[\operatorname{stab}(e, y)]$ | $\exists e[\operatorname{agent}(e, b) \wedge \operatorname{stab}(e, c)]$ |

Table 1. A summary of the positions in event semantics

Over the course of the years, events and thematic roles have grown to be much more than mere notations. ${ }^{1}$ For example, many theories that resort to the thematic role agent make specific claims about the semantic content of agenthood. But the choice between the representations in Table 1 has a more basic consequence. Because they use a larger number of relations, Neo-Davidsonian and asymmetric representations offer additional degrees of freedom. They make it possible to codify meanings in which one argument modifies a different event variable than the verb does. Such configurations are impossible to write down without the help of thematic roles, regardless of their precise semantics. Schein (1993) calls the property of such sentences essential separation.

The argument presented in Schein (1993) and - in reformulated and extended form - in Kratzer (2000) holds that cumulative readings of every involve essential separation. My goal is to refute this specific argument by showing how these readings can, in fact, be adequately captured using an eventless representation that does not use explicit roles. The crux of the argument bears on how the meaning of every is adequately represented. There are many ways to adapt eventless frameworks to the task at hand; see Brasoveanu (this volume) for a dynamic framework. I will stay close to the framework used in Kratzer (2000) in order to make the comparison as easy as possible. I will focus on the parallels with existing approaches to quantification, rather than on technical aspects.

Following Kratzer, I use the algebraic semantic framework of plurals introduced in Link (1983). ${ }^{2}$ Since Schein not only argues for events and thematic roles

[^61]but also, separately, against Link's framework, let me briefly justify my choice. As Schein points out, his two arguments are logically independent of each other, so his argument for events and roles can be recast in mereological terms, and this is in fact what Kratzer (2000) does. ${ }^{3}$ I have two reasons for following her example. First, this makes it easier to compare my approach to Kratzer's. Second, I will argue that cumulative readings of every can be modeled using standard accounts of cumulative readings such as Krifka (1986) and Sternefeld (1998), and these accounts happen to be formulated in Link's algebraic framework. That said, choosing Link's framework is not essential for my purposes as long as the domain of individuals is grounded in atoms or individuals that have no parts. Under this standard assumption, join semilattices are isomorphic to an appropriate kind of set-theoretic lattice; see Schwarzschild (1996) for an example. So everything I say about individuals can be reformulated without the use of a mereological framework.

## 2 Schein and Kratzer's Argument

Schein's original argument is very intricate and relies on complicated sentences involving three quantifiers. I will discuss these sentences later. Here, I summarize and address Kratzer's simplified exposition of his argument. It is based on the following sentence:

Example 1. Three copy editors caught every mistake in the manuscript.
Kratzer claims that (1) has a reading that can be paraphrased as "Three copy editors, between them, caught every mistake in the manuscript." In this reading, there are three copy editors, each of them caught at least one mistake, and every mistake was caught by at least one copy editor. ${ }^{4}$ If the subject DP is understood distributively, neither the surface scope reading ("Each of three copy editors caught every mistake") nor the inverse scope reading ("each mistake is such that it was caught by each of three copy editors") is equal to Kratzer's reading, because unlike it, they both entail that each mistake was caught by more than one copy editor. One possible line of analysis would be to claim that in Kratzer's reading, the subject DP is understood collectively, so that any mistake that is caught by one of the editors counts as being caught by all three of them collectively (a "team credit" analysis). But, she argues, sentence (1) is true even if the editors worked independently of each other, which is incompatible with

[^62]
## General Program

the usual understanding of the collectivity notion. In particular, (1) entails that every copy editor found at least one mistake, while collective readings do not always license this entailment. For additional arguments against a team-credit analysis, see Bayer (1997). For these reasons, I will not rely on team credit.

My strategy consists in analyzing Kratzer's reading as a cumulative reading, the kind of reading which occurs in 600 Dutch firms own 5000 American computers (Scha, 1981). It expresses that there are 600 firms and 5000 computers, each firm owns at least one computer, and each computer is owned by at least one firm. Following Krifka (1986) and Sternefeld (1998), this reading can be represented as follows, without events or thematic roles:
Example 2. $\exists X$. [600-firms $(X) \wedge \exists Y$. [5000-computers $(Y) \wedge{ }^{* *}$ own $\left.\left.(X, Y)\right]\right]$.
This representation makes use of the following ingredients and conventions. Uppercase letters are used for variables and constants that denote either atoms or sums, and lowercase letters for those that denote atoms. I use shorthands for the noun phrase denotations: for example, the predicate 600 -firms is true of any sum of firms whose cardinality is 600 . The cumulation operator ${ }^{* *}$, a generalization of the pluralization operator from footnote 2 , has been defined in various ways in the literature (see e.g. Beck and Sauerland, 2000). The definition I use is from Sternefeld (1998): Given a complete join semilattice $\langle S, \sqsubseteq\rangle$ and a binary relation $R \subseteq S \times S,{ }^{* *} R$ is the smallest relation such that (i) if $R(X, Y)$ then ${ }^{* *} R(X, Y)$; (ii) if ${ }^{* *} R\left(X_{1}, Y_{1}\right)$ and ${ }^{* *} R\left(X_{2}, Y_{2}\right)$ then ${ }^{* *} R\left(X_{1} \oplus X_{2}, Y_{1} \oplus Y_{2}\right)$.

Cumulative readings express information about the cardinalities of the minimal witness sets associated with the quantifiers involved (Szabolcsi, 1997). Standard representations of every have problems with this kind of configuration (Roberts, 1987). For example, interpreting "every mistake" in situ as $\lambda P . \forall x$.mistake $(\mathrm{x}) \rightarrow P(x)$ leads to the interpretation in (3). But this is just the surface scope reading. The problem arises because "every mistake" does not provide a handle on its witness set, i.e. the set containing every mistake. ${ }^{5}$

## Example 3. $\exists Y$.[three-copy-editors $(Y) \wedge \forall x$.[mistake $\left.\left.(x) \rightarrow{ }^{* *} \operatorname{catch}(Y, x)\right]\right]$

As Schein and Kratzer observe, if we adopt a Neo-Davidsonian position, the cumulative reading can nonetheless be represented adequately. Their idea is that once we have the agent role at our disposal, we can represent (1) roughly as "There is a sum of mistake-catching events $E$, the agents of these events amount to a sum $X$ of three editors, and every mistake was caught in at least one of these events", as in (4):
Example 4. $\exists E \exists X\left[\right.$ three-copy-editors $(X) \wedge^{* *} \operatorname{agent}(E, X)$
$\wedge \forall y[\operatorname{mistake}(y) \rightarrow \exists e[e \sqsubseteq E \wedge \operatorname{catch}(e, y)]]$
$\left.\wedge \exists Y\left[{ }^{*} \operatorname{mistake}(Y) \wedge{ }^{* *} \operatorname{catch}(E, Y)\right]\right]$
Following Schein, Kratzer takes this fact to show that we need to have at least the relation agent at our disposal in our logical representation.

[^63]
## 3 Modeling Cumulative every Without Events

Schein and Kratzer's argument is based on the assumption that the adequate translation of every mistake is in terms of a universal quantifier. The difficulty arises from the fact that the cumulative reading of (1) expresses something about the set or sum of all mistakes. But the universal quantifier does not give us a handle on this object, because it holds of any set that contains every mistake and possibly some non-mistakes.

The first step towards a solution was taken in Landman (2000), who claimed that every mistake can shift to a referential interpretation, one that denotes the sum or group of all mistakes, written $\sigma x$.mistake $(x) .{ }^{6}$ On this view, every mistake is synonymous with the mistakes, if we disregard the fact that the latter sometimes allows nonmaximal interpretations (Krifka, 1996; Malamud, 2006). At first sight, this suggestion faces an obvious problem: The distribution of every mistake is more restricted than the one of the mistakes. As is well known, every forces distributivity over its argument position:

Example 5. a. \#Every soldier surrounded the castle. (only distributive) b. The soldiers surrounded the castle. (distributive or collective)

This problem can be overcome by assuming that the restrictor of every is interpreted both in its base position as a restriction on the values of its argument position, and above the cumulation operator, where it is the input to sum formation. ${ }^{7}$ Evidence that supports this assumption comes from two strands of research. A growing body of literature suggests that the syntax of every $N$, and of quantified nominals in general, breaks down into two components; in the case of every $N$, one component expressing exhaustivity and one expressing distributivity. ${ }^{8}$ For example, according to Szabolcsi (1997), noun phrases headed by every consist of an exhaustive and a distributive component, which can take scope separately under limited conditions. That the restrictor of quantifiers should be interpreted both in situ and in the scopal position fits well within the general picture suggested by reconstruction effects, i.e. effects in which part of the lexical content of moved phrases is semantically interpreted in its base position. Reconstruction effects involving both every and other A'-moved items are well

[^64]documented in various constructions. Examples are binding theory (Chomsky, 1993; Fox, 1999) and antecedent-contained deletion (Sauerland, 2004).

Abstracting away from details, the insight I take from this work is that the exhaustive component of every (the one that refers to the sum entity) corresponds to its higher scopal position, and the component that corresponds to its restrictor is interpreted both in its higher and lower scopal position.

Technically, the concept that restrictors of quantifiers are interpreted in several places can be expressed in any number of ways: syntactically, for example, by creating multiple copies of phrases (Engdahl, 1986; Chomsky, 1993) or multiply dominated phrases (Johnson, 2007); or semantically, by encapsulating the contribution of the restrictor into objects that the interpretation function makes accessible in several places, such as choice functions (Sauerland, 2004) or sets of assignments (Brasoveanu, this volume). Rather than comparing all these approaches, I simply choose the proposal with the lowest types and the least departure from ordinary syntactic assumptions, both for lack of space and because this makes the interaction with the cumulation operator easier to grasp. I adopt the proposal by Fox $(1999,2002)$, according to which in situ copies are interpreted by a special semantic rule, shown here in simplified form:
Example 6. Trace Conversion Rule: $\llbracket[(\mathrm{Det}) \mathrm{N}]_{x} \rrbracket=\iota y .[\llbracket \mathrm{N} \rrbracket(y) \wedge y=x]$
With Trace Conversion, the lower copy of a DP every $N$ which bears the index $x$ is interpreted as "the N which is $x$ ". The contribution of the determiner in the lower copy is ignored. The distributivity of the quantifier is modeled by a star operator. I also assume that all quantifiers (even those in subject position) move before they are interpreted, so that trace conversion always applies. On three copy editors, the effect of trace conversion is vacuous, so I don't show it. ${ }^{9}$

As an example, "Every dog barks" is interpreted as in (7). Here and below, the parts contributed by "every N" are underlined.
Example 7. $\sigma x \cdot \operatorname{dog}(x) \in^{*} \lambda X\left[\operatorname{barks}\left(\underline{\iota x^{\prime}} \cdot \operatorname{dog}\left(x^{\prime}\right) \wedge x^{\prime}=X\right)\right]$
The cumulative reading of (1) can be represented as follows:
Example 8. $\exists X[$ three-copy-editors $(X) \wedge$
$\left.\langle X, \underline{\sigma y} . \operatorname{mistake}(y)\rangle \in{ }^{* *} \lambda X^{\prime} \lambda Y\left[{ }^{* *} \operatorname{catch}\left(X^{\prime}, \underline{\iota y^{\prime}} . \operatorname{mistake}\left(y^{\prime}\right) \wedge y^{\prime}=Y\right)\right]\right]$.
This is provably equivalent to Kratzer's representation in (4), provided that $\operatorname{catch}(x, y)$ holds whenever $\exists e[\operatorname{agent}(e, x) \wedge \operatorname{catch}(e, y)]$ and that (at least) the second argument of catch is always atomic. ${ }^{10}$ Note that the requirement that $Y$ range over singular mistakes effectively restricts it to atomic values.

[^65]
## 4 Mixed Cumulative-Distributive Readings

The sentences originally discussed by Schein (1993) are more complicated than Kratzer's in two respects. First, they involve nonincreasing numeral quantifiers such as exactly two. When these quantifiers occur in cumulative readings, the formulation of their maximality conditions requires special attention, but this is true no matter whether events and thematic roles are used (von Benthem, 1986; Krifka, 1999; Landman, 2000; Robaldo, 2009; Brasoveanu, this volume). Second, the sentences exhibit mixed distributive-cumulative configurations, such as in the following example:


The relevant reading of this sentence is the one in which there is a given set of three videos which between them were responsible for the fact that every quarterback learned two new plays. The solution from the previous section works here as well. We can represent the reading as in an eventless framework as follows:

Example 10. $\exists X[$ three-video-games $(X)$
$\wedge\langle X, \sigma y$. quarterback $(y)\rangle \in{ }^{* *} \lambda X^{\prime} \lambda Y[\exists Z$ two-new-plays $(Z)$
$\wedge^{* * *} \operatorname{taught}\left(X^{\prime}, \underline{\left.\left.\left.\iota y^{\prime} . \text { quarterback }\left(y^{\prime}\right) \wedge y^{\prime}=Y, Z\right)\right]\right]}\right.$
In this formula, the exhaustive component of "every quarterback" stands in a cumulative relation with "three video games", while its distributive component makes sure that teach relates individual quarterbacks to sums of two plays each. ${ }^{* * *}$ is the ternary equivalent of ${ }^{* *}$. Two instances of cumulation are needed: the higher one to give every quarterback scope over two new plays, and the lower one to reflect the lack of scopal dependency between the three video games and any given set of two plays. This is because sentence (9) does not express for any set of two plays how many of the three video games taught that set.

## 5 Structural Asymmetries in Cumulative Readings

Recall that Kratzer's larger goal is to argue for a representation in which only the agent role, but not the theme role, is expressed as a separate relation. Kratzer is aware that the relevant reading of (1) can be described as a cumulative reading, but she prefers not to model it as such, observing that cumulative readings are less readily available with every in general.

Example 11. a. Every copy editor caught 500 mistakes in the manuscript. b. 500 mistakes in the manuscript were caught by every copy editor.

Cumulative readings are absent from both examples in (11). In these examples, every is in agent position. Based on this, she generalizes that every can
take part in cumulative readings only when it is not in agent position, cf. (1). This is indeed predicted by the asymmetry in her representation.

I doubt that Kratzer's generalization is the right one. Data cited in Zweig (2008) suggests that even when every-phrases do not denote the agent, they cannot always take part in cumulative readings. Zweig considers a scenario where "an international chess tournament is held between three teams from three countries: Estonia, Fiji, and the Peru. The tournament consists of a series of games, with no game played by two players from the same team. No draws or stalemates are allowed; the game is replayed until there is a winner. At the end of the day, it turns out that the Estonian team did very poorly: no Estonian won any games."

According to Zweig, it is true in this scenario to say (12a), while its passivized variant (12b) is judged as false. Native speakers uniformly judge that (12b), unlike (12a), implies that each game was won by both teams, an impossibility.
Example 12. a. The Fijians and the Peruvians won every game.
b. Every game was won by the Fijians and the Peruvians.

This minimal pair suggests that what blocks the cumulative reading of cer-tainevery-phrases is not their thematic role but the fact that they c-command the other quantifier. The following example from Bayer (1997) supports this.

Example 13. a. Every screenwriter in Hollywood wrote Gone with the Wind. b. Gone with the Wind was written by every screenwriter in Hollywood.

For Bayer, (13a) is "clearly bizarre", which is compatible with Kratzer's prediction, as well as with the c-command constraint proposed here. But he reports that (13b) has a possible reading where every screenwriter in Hollywood contributed to the writing of the movie. Since every is in agent position in both cases, the asymmetry is unexpected on Kratzer's hypothesis.

## 6 Conclusion

Cumulative readings of "every" do not pose a special problem for eventless representations, contra Schein (1993) and Kratzer (2000). They do not constitute an argument that the logical representations of natural language sentences must make use of events or of thematic roles. The restriction on cumulative readings of "every" is more accurately stated in terms of c-command than in terms of thematic roles, so it is not an argument for the asymmetric account in Kratzer (2000). Of course, this does not exclude the possibility that events and thematic roles might be present in the linguistic system for other reasons. The claim here is simply that cumulative readings of every do not bear on their status.

Further work is needed to explore and derive the c-command generalization. One option is to restrict the ${ }^{* *}$ operator so that, outside of the lexicon, it only appears on syntactically plural verb phrases. This would be similar to the constraint proposed in Kratzer (2007), but it would not cover (13). The dynamic system in Brasoveanu (this volume) also derives the generalization, provided that cumulative every cannot take inverse scope. It remains to be seen whether this constraint can be maintained while permitting inverse scope of every in general.

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# Restricting and Embedding Imperatives 

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#### Abstract

We use imperatives to refute a naïve analysis of update potentials (force-operators attaching to sentences), arguing for a dynamic analysis of imperative force as restrictable, directed, and embeddable. We propose a dynamic, non-modal analysis of conditional imperatives, as a counterpoint to static, modal analyses (e.g., Schwager [2006]). Our analysis retains Kratzer's [1981] analysis of $i f$-clauses as restrictors of some operator (with Schwager), but avoids typing it as a generalized quantifier over worlds (against her), instead as a dynamic force operator (cf. Portner [2004, 2008]; Potts [2003]). Arguments for a restrictor treatment (but against a quantificational treatment) are mustered, and we propose a novel analysis of update on conditional imperatives (and an independently motivated revision of the standard ordering-semantics for root modals that makes use of it). Finally, we argue that imperative force is embeddable under an operation much like dynamic conjunction.


## 1 Plan

Sentences of the imperative clause-type (hereafter 'imperatives') are conventionally associated with a distinctive kind of force (what I will call 'imperative force') that is both performative and directive (see esp. Portner [2004]). It is performative in the sense that the conventional discourse function of imperatives is not to describe facts about the world, but rather to introduce new facts (about obligations or commitments) into a discourse. It is directive in the sense that imperatives function primarily to shape the intentions (indirectly, by directly shaping things that, in turn, directly shape the intentions) of their addressees.

There is widespread agreement that a semantico-pragmatic analysis of imperatives should have something to say about this dimension (call it the 'force dimension') of the conventional meaning of imperatives. ${ }^{1}$ What, exactly, needs to be said, beyond the fact that imperatives conventionally receive performative and directive interpretations, is often unclear. In this paper, I articulate

[^66]substantive conditions of adequacy on an account of the force dimension of imperative meaning. My principal focus is on the performative effects of conditional imperatives (cis; see 1 ) and unconditional imperatives (Uis; see 2 ).

1. If the temperature drops, shut the window! $\approx($ if $\phi)(!\psi)$
2. Shut the window! $\approx!\phi$

Schwager's [2006] account, which treats imperatives as a species of modal clause (hence, imperative operators as Kratzer-ian restrictable modal operators), is designed to handle CIs, but ultimately handles neither. Portner's [2008] account makes implicit use of directed speech-act (force) operators (à la Potts [2003]), so that the force of an imperative is to add the content of the imperative (what's commanded, i.e., the complement of the force operator) to the addressee's To-Do List. It does well with UCIs, but falters with cIs.

We strictly improve on these proposals by reconceptualizing force operators. The ordinary treatment (classic references are Stenius [1967]; Lewis [1970]) views speech-acts on the model of propositional attitudes: as an agent may believe $\phi$, she may assert $\phi$, command $\phi$, question whether $\phi$, etc. ${ }^{2}$ Handling CIs requires a new approach: speech-acts are less like propositional attitudes, more like literal actions whose force (contextual effect) can be modulated, via linguistic and extra-linguistic mechanisms, and whose functional potential can be formally modeled in a familiar logic of programs. Conditional imperatives, we'll see, illustrate a syntactic mechanism of force-modulation, which we model as force-restriction (in a sense to be precisified). (Making use of this analysis requires modifying the standard Kratzer [1981] semantics for modals. There are, we'll see, independent reasons for doing this.)

Our stance here is roughly the same as Krifka [2001, 2004], which emphasizes natural language devices (generally corresponding to regular operations on programs) for building complex speech-acts out of component speech-acts. The question naturally arises: which such operations are expressible in natural language? The essay closes with some tentative remarks on this question.

## 2 Menu

The conventional discourse function of an imperative is, I will suppose, to introduce some sort of obligation or commitment on its addressee, via modification of parameters of the context to which the interpretation of obligation- or commitment-describing modalities is sensitive (cf. Han [1999], Portner [2004, 2008]). Imperative force is performative because it generally yields a context in which certain obligation-descriptions are true (where previously they were

[^67]false), directive because its target is the indirect regulation of the behavior of its addressee. Adequate accounts of imperative force will predict that CIs tend to introduce corresponding conditional obligations (cos), UIs tend to introduce corresponding unconditional obligations (UOS). Concretely, (1) and (2) should tend to make it the case that if the temperature drops, you must shut the window, and that you must shut the window, respectively. Should an account fail to predict this in a given context, there should be a plausible explanation (for instance, the prior context enforcing a conflicting obligation).

### 2.1 Modal Analyses

The paradigm example of the modal analysis of imperatives is Schwager's [2006] (although see also Aloni [2007]). Schwager assigns a CI (if $\phi$ )(! $\psi$ ) (read: if $\phi, I$ hereby command that $\psi$ ) the logical form $O(\psi / \phi)$ (read: if $\phi, \psi$ must be realized) with the standard Kratzer [1981] restrictor semantics. ${ }^{3}$ With $c$ a context, $f_{c}$ is the modal base (a body of information), $g_{c}$ the ordering source (for Schwager a set of contextually given preferences, usually, but not always, supplied by the speaker). Both map worlds to sets of propositions. ${ }^{4}$
Definition 1. $\llbracket O(\psi / \phi) \rrbracket^{c, w}=1 \Leftrightarrow \min \left(f_{c}(w) \cup \llbracket \phi \rrbracket^{c}, \preceq_{g_{c}(w)}\right) \subseteq \llbracket \psi \rrbracket^{c}$, where:

- $\min \left(\Phi, \preceq_{\Psi}\right):=\left\{w \in \bigcap \Phi: \forall v \in \bigcap \Phi: v \preceq_{\Psi} w \Rightarrow w \preceq_{\Psi} v\right\}$
- $w \preceq_{\Psi} v \Leftrightarrow\{P \in \Psi: v \in P\} \subseteq\{P \in \Psi: w \in P\}$

The analysis assigns imperatives truth-conditions - the same as their modalized LFs. As such, the analysis would appear to offer no account of imperative forceappear, indeed, to predict that imperative force as a subtype of assertoric force.

Schwager tries to avoid the worry by introducing contextual constraints on the felicitous utterance of an imperative. Imperative utterances are infelicitous at $c$ unless the speaker of $c$ :

- Has exhaustive knowledge, à la Groenendijk \& Stokhof (1984), about $f_{c}$ and $g_{c}$, so that he 'utters a necessity proposition he cannot be mistaken about.'
- Affirms the relevant preference for $\phi$ a good 'maxim for acting.'

When these conditions are met, an imperative utterance generally receives the performative and directive interpretation adverted to above.

There are problems. First, if the speaker of $c$ isn't mistaken, then $O(\psi / \phi)$ is already true at $c$. Performative effect, which paradigmatically consists in updating $c$ so that $O(\psi / \phi)$ goes from false to true, is therefore erased. Second, affirmation that $\phi$ is a good 'maxim for acting' is exactly the type of speech-act we should like to analyze. We would like to model how such affirmation is generally associated with the introduction of new obligations on the addressee. Saying that imperatives receive a performative and directive interpretation when certain presuppositions are met is no replacement for an account of what, precisely, such an interpretation consists in.

[^68]
### 2.2 Dynamic Analyses

Portner [2004, 2008] (cf. Han [1999]; Potts [2003]) analyzes imperative performative effect as addition to an addressee-indexed ordering source, her 'To-Do List' (TDL). Imperatives are associated directly with a type of 'sentential force,' rather than indirectly (via analysis as a species of necessity modal with an exclusively performative interpretation). With [•] a dynamic interpretation function, mapping formulas to update potentials, $c$ a context, $T_{c}$ a function from individuals to their TDLs, $a_{c}$ the addressee, the idea is this:
Definition 2. $c[!\phi]=c^{\prime}$ is just like $c$, except $\llbracket \phi \rrbracket^{c}$ is on $T_{c^{\prime}}\left(a_{c}\right)$
This analysis meets the criteria of adequacy on accounts of unconditional imperative force. Making use of the Kratzer semantics for modals, we can see that even where some of the $T_{c}\left(a_{c}\right)$-best worlds compatible with the $c$-relevant information do not satisfy $\phi$, it will tend to be the case that $O(\phi / T)$ is true at $c^{\prime}$, since it will tend to be the case that all of the $T_{c^{\prime}}\left(a_{c}\right)$-best worlds compatible with the same information do satisfy $\phi$, in virtue of the presence of $\llbracket \phi \rrbracket^{c}$ on $T_{c^{\prime}}\left(a_{c}\right)$. In cases where this does not reliably hold at $c^{\prime}$ (e.g., cases where updating $c$ with ! $\phi$ introduces a logical incompatibility into the TDL), it's not clear that we really do want to predict that new obligations are imposed. Such cases will tend to coincide with cases where the prior context enforces a conflicting obligation.

The analysis does not, however, meet the criteria of adequacy on accounts of conditional imperative force. In a footnote, Portner [2004] moots an analysis in terms of conditional update: informally, he suggests, [(if $\phi)(!\psi)]$ adds $\llbracket \phi \rrbracket^{c}$ to $a_{c}$ 's TDL, once $\phi$ is true. But this fails to explain the conventional discourse effect of CIs: the imposition of cos. Even when $\phi$ is false at both $c$ and the result of updating $c$ with (if $\phi)(!\psi)$, this sort of update will typically introduce a CO of the form $O(\psi / \phi)$. Concretely: given an utterance of (1) at $c$, the associated co (if the temperature drops, you must shut the window) will tend to be in force at the updated context, regardless of the truth of the temperature drops at either $c$ or $c$ updated with the CI.

A preliminary diagnosis of the problem: for cis, we require an update on TDLs that is performed regardless of the antecedent's truth then. The failure seems to stem from deferring update to the ordering source until the antecedent of the imperative is true. An immediate thought, then, is to treat conditional imperative force as a kind of unconditional imperative force:
Definition 3. $c[(\operatorname{if} \phi)(!\psi)]=c^{\prime}$ is just like $c$, except $\llbracket \phi \supset \psi \rrbracket^{c}$ is on $T_{c^{\prime}}\left(a_{c}\right)$
Call this the Wide-Scoping Proposal for CIS (WSPCI), so named because, according to the wSPCI, $[($ if $\phi)(!\psi)]=[!(\phi \supset \psi)] .{ }^{5}$ The WSPCI runs into empirical

[^69]problems. Consider the following case (from Kolodny \& MacFarlane [2009]): ten miners are all trapped in a shaft-A or B, although we do not know which-and threatened by rising waters. We can block one shaft or neither, but not both. If we block the shaft they are in, all are saved. If we guess wrong, all die. Now consider the following set of imperatives.
3. If they're in A, block A! $\approx$ (if in_A) (!block_ $A$ )
4. If they're in B, block B! $\approx\left(\right.$ if in_ $\left._{-} B\right)(!$ block_ $B)$
5. Don’t block either shaft! $\approx!\neg\left(\right.$ block_ $_{-} A \vee$ block_ $\left.B\right)$

The imperatives in (3-5) seem like sound advice. But if the WSPCI is right, they add the following to the addressee's TDL: $\llbracket i n_{-} A \supset b l o c k \_A \rrbracket^{c}, \llbracket i n_{-} B \supset b l o c k \_B \rrbracket^{c}$, and $\llbracket \neg\left(b l o c k_{-} A \vee b_{l o c k}-B\right) \rrbracket^{c}$. The only way to satisfy all of these demands is to make sure the miners are in neither A nor B. But this is presupposed impossible at $c$. This does not square with intuitions: a speaker issuing these imperatives at $c$ is not demanding something presupposed to be impossible. ${ }^{6}$

## 3 Restricting Force

The dynamic account, as it stands, seems to lack the resources to predict the relevant phenomena regardling cos. There are only two sorts of update to perform on a TDL: deferred and non-deferred (immediate) addition. Deferred addition does not account for the conventional discourse effect of cIs. Immediate addition implies that there is some proposition that a CI adds to the addressee's TDLthat conditional commanding is a species of unconditional commanding. There are no obvious candidates for the identity of this proposition.

Each tack assumes that imperative force comes in a single variety: imperative force involves a speaker demanding that some proposition be true (with the deferred update proposal making this demand contingent on some further condition). I see no way of preserving this assumption while being able to predict the desired facts about the relationship between Cis and cos. So I suggest we jettison it. The guiding idea here will be a familiar one: unconditional commanding is a species of conditional commanding. The former corresponds to a kind of unrestricted imperative force, the latter to a kind of restricted imperative force.

### 3.1 First Pass

How to formalize this idea? The first thought is to explicitly type tDLS as Kratzer-ian conversational backgrounds: functions from worlds to a set of propositions. Doing this allows us to think of tDLs as something like a set of contingency plans: they furnish different practical 'recommendations' depending on the situation the agent finds herself in. Formally, we index TdLs to both agents and worlds, and treat (if $\phi)(!\psi)$ as adding $\llbracket \psi \rrbracket^{c}$ to $a_{c}$ 's TDL at the $\phi$-worlds (or some contextually selected subset thereof; cf. Mastop [2005]: 103).

[^70]Definition 4. $c[($ if $\phi)(!\psi)]=c^{\prime}$ is like $c$, except $\forall w \in \llbracket \phi \rrbracket^{c}: \llbracket \psi \rrbracket^{c} \in T_{c^{\prime}}\left(a_{c}\right)(w)$
This is a natural and elegant extension of Kratzer's restrictor analysis of conditional antecedents. Rather than restricting the domain of a generalized quantifier, however, CI antecedents function to restrict the scope of dynamic update. Update with UIs is thus understood in terms of update with cIs, rather than vice versa. UIs issue a demand on the addressee that holds in all possible contingencies, while genuine cIs issue a demand on the addressee that holds in some non-trivial restriction of the set of possible contingencies.

Elegant though it is, this proposal does no better at predicting the desired relationship between CIs and COs. We do get unconditional obligations (UOs) of the form $O(\psi / \top)$ when evaluating these formulas at $\phi$-worlds. But we get nothing at $\neg \phi$-worlds. The CI updates the addressee's TDL only at the $\phi$-worlds, and does nothing otherwise. This means we have only a metalinguistic analogue of the desired prediction: given that (if $\phi)(!\psi)$ is issued at $c$, if $\phi$ is true at $w$, then typically $\psi$ is required at $w$ (i.e., typically, $\llbracket O(\psi / \top) \rrbracket^{c^{\prime}, w}=1$, where $c^{\prime}$ is $c$ updated with $($ if $\phi)(\psi)$ ). This isn't good enough: we'd like to predict the object-language CO if the temperature drops, you must shut the window true at the updated context, regardless of whether the temperature drops is true then. ${ }^{7}$

### 3.2 Second Pass

Something is very intuitive about the contingency plan understanding of the tDL. The problem is that, on the standard Kratzer semantics for modals, the world of evaluation fixes the ordering source at a context: contingencies cease to be relevant (in the sense that they are ignored by the semantics) once the world of evaluation is fixed. So, TDLs should be indexed to some semantic parameter other than the world of evaluation.

Our analysis indexes tdLs to bodies of information (modal bases, whether construed as sets of worlds or propositions), rather than worlds. On this picture, the contingencies relevant to planning are informational, rather than 'factual,' in character: the TDL furnishes different practical 'recommendations' for an agent depending on the information available to her at the context. Formally, we treat (if $\phi)(!\psi)$ as adding $\llbracket \psi \rrbracket^{c}$ to $a_{c}$ 's TDL at every body of information $\Phi \supseteq f_{c}(w) \cup$ $\llbracket \phi \rrbracket^{c}$, for each $w$ (i.e., every $\phi$-containing expansion of the information at $c$ ).

Definition 5. $c[($ if $\phi)(!\psi)]=c^{\prime}$ is like $c$, except: $\forall w: \forall \Phi \supseteq f_{c}(w) \cup \llbracket \phi \rrbracket^{c}: \llbracket \psi \rrbracket^{c} \in T_{c^{\prime}}\left(a_{c}\right)(\Phi)$
As before, a UI ! $\phi$ is a vacuously restricted CI: $[!\phi]:=[($ if $\top)(!\phi)]$; unconditional commanding is still a species of conditional commanding. The difference is that UIS add their consequents to every expansion of the information sans phrase.

This is the analysis of imperative force which I will be endorsing in this paper. It is a restrictor analysis of CI antecedents: CI antecedents restrict the

[^71]set of contingencies to which a command pertains, thereby modulating the force of the associated speech-act. It is fundamentally opposed to the 'propositional attitude' model of speech acts described in this essay's introduction.

### 3.3 Information-Sensitive Ordering Semantics

Allowing the ordering source at a context $c$ to be determined by the information at $c$, rather than the world of evaluation, does not, by itself, secure the desired relationship between CIs and cos. Getting this right requires modifying the semantics to make use of the information-sensitive ordering source. ${ }^{8}$ The relevant change is having conditional antecedents function as both domain restrictors and ordering source shifters.

Definition 6. $\llbracket O(\psi / \phi) \rrbracket^{c, w}=1 \Leftrightarrow \min \left(f_{c}(w) \cup \llbracket \phi \rrbracket^{c}, \preceq_{T_{c}(a)\left(f_{c}(w) \cup \llbracket \phi \rrbracket^{c}\right)}\right) \subseteq \llbracket \psi \rrbracket^{c}$
Informally, the formula $O(\psi / \phi)$ says the best-on-the supposition-that- $\phi \phi$-worlds are $\psi$-worlds. This secures the right result in the if the temperature drops... case. The relevant CI adds the proposition that the addressee shuts the window to her TDL at every body of information $\Phi$ such that $\Phi$ entails that the temperature is dropping. The information-sensitive semantics (ISS) evaluates the relevant Co by looking at the addressee's TDL with respect to such a body of information.

This is a major revision of the Kratzer [1981] semantics, which allows contingency in ordering sources only via variation in the world coordinate, not via variation in the domain of quantification. So there is reason to worry that it is ad hoc. It can, in fact, be independently motivated. Consider, once again, Kolodny \& MacFarlane's [2009] miner case, and the obligation-descriptions in (6-8).
6. If they're in A , we gotta block $\mathrm{A} \approx O($ block_A/in_A $)$
7. If they're in B , we gotta block $\mathrm{B} \approx O\left(\right.$ block_ $_{-} B /$ in_ $\left._{-} B\right)$
8. We may leave both shafts open $\approx \neg O\left(\left(\right.\right.$ block_ $_{-} A \vee$ block_ $\left.\left._{-} B\right) / T\right)$

Given the case, informants reliably hear each of these obligation-descriptions as true (so, a fortiori, consistent). But, using the information-insensitive Kratzer semantics, whenever the modal base entails (i.e., it is known) that the miners are either all in A or all in B, these sentences are provably inconsistent.

Proof. Suppose (6-8) are true at $w$ and $\bigcap f_{c}(w) \subseteq \llbracket i n_{-} A \vee i n_{-} B \rrbracket^{c}$.

- Let $g_{c}$ be an ordering source. Choose any $v \in \min \left(f_{c}(w), \preceq_{g_{c}(w)}\right)$.
- Since $\bigcap f_{c}(w) \subseteq \llbracket i n_{-} A \vee i n_{-} B \rrbracket^{c}, v \in \min \left(f_{c}(w) \cup \llbracket i n_{-} A \rrbracket^{c}, \preceq_{g_{c}(w)}\right)$ or $v \in$ $\min \left(f_{c}(w) \cup \llbracket i n \_B \rrbracket^{c}, \preceq_{g_{c}(w)}\right) .{ }^{9}$
- By Kratzer's semantics (Defn. 1), since (6) and (7) are true at $w, \min \left(f_{c}(w) \cup\right.$ $\left.\llbracket i n_{-} A \rrbracket^{c}, \preceq_{g_{c}(w)}\right) \subseteq \llbracket b l o c k \_A \rrbracket^{c}$ and $\min \left(f_{c}(w) \cup \llbracket i n_{-} B \rrbracket^{c}, \preceq_{g_{c}(w)}\right) \subseteq \llbracket b l o c k \_B \rrbracket^{c}$.

[^72]- So $v \in \llbracket b l o c k \_A \rrbracket^{c} \cup \llbracket b l o c k \_B \rrbracket^{c}$.
- So $\min \left(f_{c}(w), \preceq_{a_{c}(w)}\right) \subseteq \llbracket b l o c k \_A \rrbracket^{c} \cup \llbracket b l o c k \_B \rrbracket^{c}$.
- So $\llbracket O(($ block_ $A \vee$ block_B $) / T) \rrbracket^{c, w}=1$. Contradiction.

Space prevents me from discussing in detail the substance of the the proof or our proposal for cos (but see my [2009b]). Briefly, the iss blocks the proof by varying the ordering sources that are relevant for evaluating the co-descriptions in (6-8): (6) uses an ordering source indexed to a body of information that entails that the miners are in shaft A, (7) uses an ordering source indexed to a body of information that entails that the miners are in shaft B, while (8) uses an ordering source indexed to a body of information that does not settle the miners' location. The upshot: the ISS seems to be independently motivated, not ad hoc.

## 4 Postscript: Embedded Force

It is useful to think of imperative force as a complex update on TDLs, constructed out of a set of basic updates on TDL components, together with a regular operation. In this case, the operation is ; (sequencing). Sequencing is function composition: if $\alpha$ and $\beta$ are context change potentials, then:

$$
\alpha ; \beta=\lambda c . c \alpha \beta
$$

A TDL is a set of contingency plans: a set of information-plan pairs. Basic updates are additions to contingency plans. Complex or composite update is understood as a series of additions to an addressee's contingency plans (which plans being a function of how the speaker chooses to modulate the force of her command). The update associated with a CI (if $\phi)(!\psi)$ at $c$ is a (possibly infinite) sequencing of the following basic update program:

$$
\lambda\langle\Phi, \Psi\rangle \cdot\left\{\begin{array}{l}
\left\langle\Phi, \Psi \cup\left\{\llbracket \psi \rrbracket^{c}\right\}\right\rangle \text { if } f_{c}(w) \cup \llbracket \phi \rrbracket^{c} \subseteq \Phi \\
\langle\Phi, \Psi\rangle \text { otherwise }
\end{array}\right.
$$

There is, then, a sense in which utterances of CIs conventionally involve the performance of a composite speech-act: a 'conjunction' of instructions about updating individual contingency plans. ${ }^{10}$ Standard treatments of force do not provide for complex updates built with regular operations: force is computed by applying a force-operator to a content, and doesn't embed. We disagree: force seems to embed under an operation reminiscent of dynamic conjunction.

We also see speech-act sequencing, of a rather different sort, in the various ways a speaker may direct imperative force. So far we have (implicitly) construed imperatives as taking direction arguments: a context in which an imperative utterance occurs will tend to select someone at whom imperative force is targeted, i.e., an addressee. This orientation is, we see, sufficiently flexible to distinguish singular-addressee imperatives like (9) from group-addressee imperatives like (10). But it founders with plural-addressee imperatives like (11) and (12).

[^73]9. Have the orchestra play Beethoven's $5^{\text {th }} \approx!\left[\right.$ make-play $\left.(\mathbf{5 t h})(\mathbf{o r c h})\left(a_{c}\right)\right]$
10. Play Beethoven's $5^{\text {th }}$ (together) $\approx!\left[\operatorname{play}(5 \mathbf{t h})\left(a_{c}\right)\right]\left(a_{c}=\right.$ the orchestra)
11. Everyone play her part $\approx$ ???
12. (Conductor addressing orchestra members:) Play your part $\approx$ ???

In (11) and (12) no single individual or group of individuals is targeted by the imperative. Rather, each individual in a set of addressees is targeted, separately. Their force is, for each addressee $a$, to instruct that $a$ play $a$ 's part.

Plural addressee imperatives thus seem to demand that we allow some sort of quantification to outscope the imperative operator-seem to demand, that is to say, a representation something like the following: ${ }^{11}$

$$
\forall x![\operatorname{play}(\text { the }- \text { part }-\mathbf{o f}-x)(x)]
$$

In the absence of a vocative (as with, e.g., 12), the default approach is to bind free variables by $\forall$-closure. The intended interpretation of such formulas has them denoting sequences of updates: the result of sequencing the following set of updates, for all $a \in \mathcal{A}_{c}$, where $\mathcal{A}_{c}$ is the set of addressees determined by $c$ :

$$
\left\{\beta \mid \exists a \in \mathcal{A}_{c}: \beta=[\mathbf{p l a y}(\text { the }-\mathbf{p a r t}-\mathbf{o f}-a)(a)]\right\}
$$

In the general case, formulas of the form $\forall x:($ if $\phi)(!\psi)$ are interpreted as in Defn. 7. (Note: here we assume, tentatively, that quantification into an imperative operator must bind variables in the direction argument-position.)
Definition 7. $c[\forall x:($ if $\phi)(!\psi)]=c^{\prime}$ is like $c$, except: $\forall a \in \mathcal{A}_{c}: \forall w: \forall \Phi \supseteq f_{c}(w) \cup \llbracket \phi \rrbracket^{c}: \llbracket \psi \rrbracket^{c[x / a]} \in T_{c^{\prime}}(a)(\Phi)$
Formulas of the form $\forall x$ : (if $\phi)(!\psi)$ can thus be viewed as expressing sequences of speech-acts along two dimensions. We have a 'conjunction' of instructions for each addressee, and each such instruction for a given addressee $a$ is comprised of a 'conjunction' of instructions about updating $a$ 's contingency plans.

The general orientation of this approach raises further questions. I can only gesture at their answers here. For instance: is embedding of speech-act-operators under an $\exists$-like operation (or of update potentials under a $\vee$-like operation) permitted (cf. Krifka [2004], who suggests that it may be)? My tentative answer is: probably not. The purported linguistic evidence for the expressibility of such speech-acts in natural language is weak (as I argue in Charlow [2009a]). There is, moreover, arguably no reasonable thing for such an operation to mean. Suppose basic update potentials are functions defined for contexts. Interpreting $\vee$ in terms of $\cup$ will tend to yield update potentials that are not functions from input contexts to output contexts, but rather relations between input contexts and several possible output contexts. Complex update potentials formed with

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such operations will tend, in other words, to be indeterministic programs. Indeterminism in update potentials is prima facie objectionable: basic conversational platitudes plausibly require that a cooperative speaker know how her utterance will update the context. ${ }^{12}$

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[^75]
# A First-Order Inquisitive Semantics 

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#### Abstract

This paper discusses the extension of propositional inquisitive semantics (Ciardelli and Roelofsen, 2009b; Groenendijk and Roelofsen, 2009) to the first order setting. We show that such an extension requires essential changes in some of the core notions of inquisitive semantics, and we propose and motivate a semantics which retains the essential features of the propositional system.


## 1 Introduction

The starting point of this paper is the propositional system of inquisitive semantics (Ciardelli, 2009; Ciardelli and Roelofsen, 2009a,b; Groenendijk and Roelofsen, 2009). Whereas traditionally the meaning of a sentence is identified with its informative content, in inquisitive semantics -originally conceived by Groenendijk (2009b) and Mascarenhas (2009)- meaning is taken to encompass inquisitive content, consisting in the potential to raise issues.

More specifically, the main feature of this system is that a disjunction $p \vee q$ is not only informative, but also inquisitive: it proposes two possibilities, as depicted in figure $1(\mathrm{~b})$, and invites other participants to provide information in order to establish at least one of them.

The main feature of a first-order extension can be expected to be that existential quantification also has inquisitive effects. A simplified version, assuming finite domains, was used in Balogh (2009) in an analysis of focus phenomena in natural language. However, as was shown in Ciardelli (2009), defining a first order system that can deal with infinite domains is not a trivial affair. While there I proposed to enrich the propositional system in order to make the predicate extension possible, what I outline here is a conservative extension of the original framework, which retains most of its essential features, in particular the decomposition of meanings into a purely informative and a purely inquisitive component.

## 2 Propositional inquisitive semantics

We start by recalling briefly the propositional implementation of inquisitive semantics. We assume a set $\mathcal{P}$ of propositional letters. Our language will consist

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Fig. 1. Examples of propositional inquisitive meanings.
of propositional formulas built up from letters in $\mathcal{P}$ and $\perp$ using the connectives $\wedge, \vee$ and $\rightarrow$. We write $\neg \varphi$ as an abbreviation for $\varphi \rightarrow \perp$.

Our semantics is based on information states, modeled as sets of valuations. Intuitively, a valuation describes a possible state of affairs, and a state $s$ is interpreted as the information that the actual state of affairs is described by one of the valuations in $s$. In inquisitive semantics, information states are always used to represent the state of the common ground of a conversation, not the information state of any individual participant.

Definition 1 (States). A state is a set of valuations for $\mathcal{P}$. We denote by $\omega$ the state of ignorance, i.e. the state containing all valuations. We use $s, t, \ldots$ as meta-variables ranging over states.
We get to inquisitive meanings passing through the definition of a relation called support between states and propositional formulas.

Definition 2 (Support).

```
\(s \neq p \quad \Longleftrightarrow \forall w \in s: w(p)=1\)
\(s \vDash \perp \quad \Longleftrightarrow s=\emptyset\)
\(s=\varphi \wedge \psi \Longleftrightarrow s=\varphi\) and \(s=\psi\)
\(s \models \varphi \vee \psi \Longleftrightarrow s \vDash \varphi\) or \(s \vDash \psi\)
\(s \models \varphi \rightarrow \psi \Longleftrightarrow \forall t \subseteq s\) : if \(t \models \varphi\) then \(t \models \psi\)
```

Support is used to define inquisitive meanings as follows.
Definition 3 (Truth-sets, possibilities, meanings).

1. The truth-set $|\varphi|$ of $\varphi$ is the set of valuations which make $\varphi$ true.
2. A possibility for $\varphi$ is a maximal state supporting $\varphi$.
3. The inquisitive meaning $[\varphi]$ of $\varphi$ is the set of possibilities for $\varphi$.

Informativeness The meaning $[\varphi]$ represents the proposal expressed by $\varphi$. One effect of the utterance of $\varphi$ is to inform that the actual world lies in one of the specified possibilities, i.e. to propose to eliminate all indices which are not included in any element of $[\varphi]$ : thus, the union $\bigcup[\varphi]$ expresses the informative content of $\varphi$. A formula which proposes to eliminate indices is called informative. It is easy to see that the equality $\bigcup[\varphi]=|\varphi|$ holds, insuring that inquisitive semantics preserves the classical treatment of information.

Inquisitiveness What distinguishes inquisitive semantics from classical update semantics is that now the truth-set $|\varphi|$ of a formula comes subdivided in a certain way, which specifies the possible resolutions of the issue raised by the formula. If resolving a formula $\varphi$ requires more information than provided by $\varphi$ itself, which happens iff $|\varphi| \notin[\varphi]$, then $\varphi$ requests information from the other participants, and thus we say it is inquisitive. In the present system (but not in the unrestricted system mentioned below) a formula is inquisitive precisely in case it proposes more than one possibility.

Assertions and questions Notice that formulas which are neither informative nor inquisitive make the trivial proposal $\{\omega\}$ (namely, they propose to stay in the given state). Thus, inquisitive meanings can be seen as consisting of an informative dimension and an inquisitive dimension. Purely informative (i.e., non-inquisitive) formulas are called assertions; purely inquisitive (i.e., non-informative) formulas are called questions. In other words, assertions are formulas which propose only one possibility (namely their truth-set), while questions are formulas whose possibilities cover the whole logical space $\omega$.

It is easy to see that disjunction is the only source of inquisitiveness in the language, in the sense that any disjunction-free formula is an assertion. Moreover, a negation is always an assertion: in particular, for any formula $\varphi$, its double negation $\neg \neg \varphi$, abbreviated by $!\varphi$, is an assertion expressing the informative content of $\varphi$.

An example of a question is the formula $p \vee \neg p$ depicted in 1 (c), which expresses the polar question 'whether $p$ '. In general, the disjunction $\varphi \vee \neg \varphi$ is a question which we abbreviate by ? $\varphi$.

We say that two formulas $\varphi$ and $\psi$ are equivalent, in symbols $\varphi \equiv \psi$, in case they have the same meaning. The following proposition, stating that any formula is equivalent with the conjunction of an assertion with a question, simply reflects the fact that inquisitive meanings consist of an informative and an inquisitive component.

Proposition 1 (Pure components decomposition). $\varphi \equiv!\varphi \wedge ? \varphi$
Obviously, the notions and the results discussed in this section may be relativized to arbitrary common grounds. For more details on the propositional system and its logic, the reader is referred to Groenendijk (2009a) and Ciardelli and Roelofsen (2009b).

## 3 The maximality problem

In this section I will discuss the main difficulty one encounters when trying to reproduce the above framework in a predicate setting; our analysis will lead to considerations which motivate the solution proposed in the next section.

Fix a first-order language $\mathcal{L}$. A state will now consist of a set of first-order models for the language $\mathcal{L}$ : not to complicate things beyond necessity, we shall make the simplifying assumption that all models share the same domain and the same interpretation of constants and function symbols. Thus, let $\mathbb{D}$ be a fixed structure consisting of a domain $D$ and an interpretation of all (constants and) function symbols in $\mathcal{L}$; a first-order model for $\mathcal{L}$ based on the structure $\mathbb{D}$ is called a $\mathbb{D}$-model.

Definition 4 (States). $A$ state is a set of $\mathbb{D}$-models.
If $g$ is an assignment into $D$, we denote by $|\varphi|_{g}$ the state consisting of those models $M$ such that $M, g \models \varphi$ in the classical sense. The extension of the definition of support is unproblematic. Just like disjunction, an existential will only be supported in those states where a specific witness for the existential is known.

Definition 5 (First-order support). Let $s$ be a state and let $g$ be an assignment into $D$.

$$
\begin{array}{ll}
s, g \models \varphi & \Longleftrightarrow \forall M \in s: M, g \models \varphi \text { for } \varphi \text { atomic } \\
\text { Boolean connectives } & \Longleftrightarrow \text { as in the propositional case } \\
s, g \models \exists x \varphi & \Longleftrightarrow s, g[x \mapsto d] \models \varphi \text { for some } d \in D \\
s, g \models \forall x \varphi & \Longleftrightarrow s, g[x \mapsto d] \models \varphi \text { for all } d \in D
\end{array}
$$

Based on support, we may define the informative content of a formula and prove that the treatment of information is classical. We may also define when a formula is inquisitive. However, there is a crucial thing that we cannot do: we cannot get a satisfactory notion of meaning by taking maximal supporting states, and indeed in any way which involves support alone. This is what the following examples show.

Example 1. Let our language consist of a binary function symbol + and a unary predicate symbol $P$; let our domain be the set $\mathbb{N}$ of natural numbers and let + be interpreted as addition. Moreover, let $x \leq y$ abbreviate $\exists z(x+z=y)$.

Let $B(x)$ denote the formula $\forall y(P(y) \rightarrow y \leq x)$. It is easy to check that a state $s$ supports $B(n)$ for a certain number $n$ if and only if $B(n)$ is true in all models in $s$, that is, if and only if $n$ is an upper bound for $P^{M}$ for any model $M \in s$, where $P^{M}$ denotes the extension of the predicate $P$ in $M$.

We claim that the formula $\exists x B(x)$-which expresses the existence of an upper bound for $P$ - does not have any maximal supporting state. For, consider an arbitrary state $s$ supporting $\exists x B(x)$ : this means that there is a number $n$ which is an upper bound for $P^{M}$ for any $M \in s$.

Now let $M^{*}$ be the model defined by $P^{M^{*}}=\{n+1\}$. $M^{*}$ does not belong to $s$, since we just said that the extension of $P$ in any model in $s$ is bounded


Fig. 2. The intended possibilities $|B(n)|$ for the boundedness formula and its truth set $|\exists x B(x)|$, which is not itself a possibility.
by $n$; hence $s \cup\left\{M^{*}\right\}$ is a proper superset of $s$. It is obvious that for any model $M \in s \cup\left\{M^{*}\right\}$ we have $P^{M} \subseteq\{0, \ldots, n+1\}$ and thus $M \models B(n+1)$. Hence, $s \cup\left\{M^{*}\right\} \models B(n+1)$ and therefore $s \cup\left\{M^{*}\right\} \models \exists x B(x)$. So, $s \cup\left\{M^{*}\right\}$ is a proper extension of $s$ which still supports $\exists x B(x)$.

This shows that any state that supports $\exists x B(x)$ can be extended to a larger state which still supports the same formula, and therefore no state supporting $\exists x B(x)$ can be maximal.

Let us meditate briefly on this example. What possibilities did we expect to come out of the boundedness example? Now, $B(x)$ is simply supported whenever it is known to be true, so it has a classical behaviour. The existential quantifier in front of it, on the other hand, is designed to be satisfied only by the knowledge of a concrete bound, just like in the propositional case a disjunction (of assertions) is designed to be satisfied only by the knowledge of a disjunct.

Therefore, what we would expect from the boundedness formula is a hybrid behaviour: of course, it should inform that there is an upper bound to $P$; but it should also raise the issue of what number is an upper bound of $P$. The possible resolutions ${ }^{1}$ of this issue are $B(0), B(1), B(2)$, etc., so the possibilities for the formula should be $|B(0)|,|B(1)|,|B(2)|$, etc.

Now, the definition of possibilities through maximalization has the effect of selecting alternative ways to resolve the issue raised by a formula, i.e. ways which are incomparable relative to entailment. The problem is that obviously, if 0 is a bound for $P$, then so are 1,2 , etc.; if 1 is a bound, then so are 2,3 , etc. So, the ways in which the issue raised by the boundedness formula may be resolved cannot be regarded as alternatives. Still, $B(0), B(1)$, etc. are genuine solutions to the meaningful issue raised by the existential, and our semantics should be able to capture this.

This indicates that we need to come up with another way of associating a proposal to a formula; and if we are to be able to deal with the boundedness example, we need our notion to encompass proposals containing non-alternative possibilities. Notice that we cannot hope for a definition of such possibilities in terms of support: this is witnessed by the following example.

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Example 2. Consider the following variant of the boundedness formula: $\exists x(x \neq$ $0 \wedge B(x))$. Possibilities for this formula should correspond to the possible witnesses for the existential, and since 0 is not a witness, we expect $|B(0)|$ not to be a possibility.

Thus, a system that represents the inquisitive behaviour of the existential quantifier in a satisfactory way should associate different possibilities to the formulas $\exists x B(x)$ and $\exists x(x \neq 0 \wedge B(x))$. Capturing this distinction is quite important; for, intuitively, "Yes, zero!" would be a compliant response to "There exists an upper bound for $P$ ", but not to "There exists a positive upper bound to $P "$, and being able to analyze compliance in dialogue is one of the principal aims of inquisitive semantics. However, the formulas $\exists x B(x)$ and $\exists x(x \neq 0 \wedge B(x))$ are equivalent in terms of support.

The point here is that, as argued in Ciardelli (2009), support describes the knowledge conditions in which the issue raised by a formula is resolved, but is not sufficiently fine-grained to determine what the resolutions of a formula are.

## 4 A first-order inquisitive semantics

The discussion in the previous section indicates that we need to devise a non support-based notion of meaning which allows for non-alternative possibilities, i.e. possibilities which may be included in one another. In order to do so, we start from the observation that propositional inquisitive meanings may also be defined recursively, by means of an operator Max which, given a set $\Pi$ of states, returns the set $\operatorname{Max}(\Pi)$ of maximal elements of $\Pi$.

## Definition 6.

1. $[p]=\{|p|\}$ if $p \in \mathcal{P}$
2. $[\perp]=\{\emptyset\}$
3. $[\varphi \vee \psi]=\operatorname{Max}([\varphi] \cup[\psi])$
4. $[\varphi \wedge \psi]=\operatorname{Max}\{s \cap t \mid s \in[\varphi]$ and $t \in[\psi]\}$
5. $[\varphi \rightarrow \psi]=\operatorname{Max}\left\{\Pi_{f} \mid f:[\varphi] \rightarrow[\psi]\right\}$,

$$
\text { where } \Pi_{f}=\{w \in \omega \mid \text { for all } s \in[\varphi] \text {, if } w \in s \text { then } w \in f(s)\}
$$

Restricting the clauses of this definition to indices belonging to a certain state $s$ we obtain the proposal $[\varphi]_{s}$ made by $\varphi$ relative to the common ground $s$.

Now, the most obvious way to allow for non-maximal possibilities is to simply remove the operator Max from the clauses. This strategy, pursued in my thesis (Ciardelli, 2009), changes the notion of meaning right from the propositional case.

In the resulting system, which we refer to as unrestricted inquisitive semantics, informativeness and inquisitiveness no longer exhaust the meaning of a formula. For, formulas such as $p \vee \top$ are neither informative nor inquisitive, but they still make a non-trivial proposal. Ciardelli et al. (2009) suggest that
such formulas may be understood in terms of attentive potential and shows how the enriched notion of inquisitive meaning provides simple tools for an analysis of might. In this respect, the unrestricted system is a simple but powerful refinement of the standard system.

However, this solution has also drawbacks. For, in some cases the interpretation of possibilities included in maximal ones in terms of attentive potential does not seem convincing. For instance, consider a common ground $s$ in which a concrete upper bound $n$ for $P$ is known, that is, such that $s \models B(n)$ : intuitively, the boundedness formula should be redundant relative to such a common ground, that is, we should have $[\exists x B(x)]_{s}=\{s\}$. However, in the unrestricted system, the boundedness formula still proposes the range of possibilities $B(0), \ldots, B(n)$, that is, we have $[\exists x B(x)]=\{|B(0)| \cap s, \ldots,|B(n)| \cap s, \emptyset\}$.

The behaviour of the propositional connectives is sometimes also puzzling: for instance, $(p \vee q) \wedge(p \vee q)$ also proposes the possibility that $p \wedge q$ (but $p \vee q$ does not), while the implication $p \rightarrow$ ? $p$ turns out equivalent with $\neg p \vee \top$.

My aim in the present paper is to outline a different road, to describe a way to extend propositional inquisitive semantics as it is to obtain a more "orthodox" predicate inquisitive semantics in which meaning still consists of informative and inquisitive potential.

Definition 7. If $\Pi$ is a set of states, say that an element $s \in \Pi$ is optimally dominated in case there is a maximal state $t \in \Pi$ with $t \supsetneq s$.

In the unrestricted propositional semantics, due to the finitary character of propositional meanings, non-maximal possibilities are always properly included in some maximal one. Therefore, taking the maximal elements or filtering out optimally dominated ones are operations which yield the same result.

On the other hand, the example of the boundedness formula shows that the meanings we want to obtain in the first-order case may consist of an infinite chain of possibilities, none of which is maximal. Here, as we have seen, extracting maximal states in definition 6 leaves us with nothing at all; filtering out optimally dominated states, on the other hand, has no effect in this case and yields the intended meaning of the boundedness formula.

These observations lead to the idea of expanding definition 6 with the natural clauses for quantifiers (where the behaviour of $\exists$ and $\forall$ is analogous to that of $\vee$ and $\wedge$ respectively), while substituting the operator MAX with a more sensitive filter NoD which, given a set of states $\Pi$, returns the set of states in $\Pi$ which are not optimally dominated. The result is the following definition.

Definition 8 (First-order inquisitive meanings). The inquisitive meaning of a formula $\varphi$ relative to an assignment $g$ is defined inductively as follows.

1. $[\varphi]_{g}=\left\{|\varphi|_{g}\right\}$ if $\varphi$ is atomic
2. $[\perp]_{g}=\{\emptyset\}$
3. $[\varphi \vee \psi]_{g}=\operatorname{NOD}\left([\varphi]_{g} \cup[\psi]_{g}\right)$
4. $[\varphi \wedge \psi]_{g}=\operatorname{NOD}\left\{s \cap t \mid s \in[\varphi]_{g}\right.$ and $\left.t \in[\psi]_{g}\right\}$
5. $[\varphi \rightarrow \psi]_{g}=\operatorname{NoD}\left\{\Pi_{f} \mid f:[\varphi]_{g} \rightarrow[\psi]_{g}\right\}$

## General Program

$$
\begin{aligned}
\text { 6. }[\exists x \varphi]_{g} & =\operatorname{NoD}\left(\bigcup_{d \in D}[\varphi]_{g[x \mapsto d]}\right) \\
\text { 7. }[\forall x \varphi]_{g} & =\operatorname{NoD}\left\{\bigcap_{d \in D} s_{d} \mid s_{d} \in[\varphi]_{g[x \mapsto d]}\right\}
\end{aligned}
$$

Again, the proposal $[\varphi]_{s, g}$ made by $\varphi$ relative to the common ground $s$ and the assignment $g$ is obtained by restricting the clauses to indices in $s$. Obviously, if $\varphi$ is a sentence, the assignment $g$ is irrelevant and we may therefore omit reference to it.

There is, however, a subtlety we must take into account. While in the propositional case a formula may propose the empty state only if it is inconsistent, with the given definition the empty state would pop up in totally unexpected circumstances, with unpleasant consequences in terms of entailment and equivalence; for instance, we would have $[\exists x(x=0 \wedge B(x))]=\{|B(0)|, \emptyset\} \neq\{|B(0)|\}=[B(0)]$. To fix this problem, we modify slightly our definitions, stipulating that the empty state is optimally dominated in a set of states $\Pi$ as soon as $\Pi$ contains a nonempty possibility. For the rest, we can keep the definition of the system unchanged.

Notice that by definition of the operator NoD, we can never end up in an absurd situation like the one discussed in example 1 , in which $[\varphi]=\emptyset$ (in which, that is, a formula would propose nothing!) Moreover, it is easy to establish inductively the following fact, which shows that we have indeed defined a conservative extension of propositional inquisitive semantics.

Proposition 2. If $\varphi$ is a quantifier-free formula, then the meaning [ $\varphi$ ] given by definition 8 coincides with the meaning of $\varphi$ considered as a propositional formula, as given by definition 3.

The system we defined can cope with the subtleties highlighted by example 2 : formulas which are equivalent in terms of support may be assigned different meanings, and may even have no common possibility at all, thus differing dramatically in terms of the compliant responses they allow.

Example 3. In the context of example 1, let $E(x)=\exists y(y+y=x)$ and $O(x)=$ $\neg E(x)$; clearly, $E(x)$ and $O(x)$ are assertions stating, respectively, that $x$ is even and that $x$ is odd. We have:

1. $[\exists x B(x)]=\{|B(n)|, n \in \mathbb{N}\}$
2. $[\exists x(x \neq 0 \wedge B(x))]=\{|B(n)|, n \neq 0\}$
3. $[\exists x(E(x) \wedge B(x))]=\{|B(n)|, n$ even $\}$
4. $[\exists x(O(x) \wedge B(x))]=\{|B(n)|, n$ odd $\}$

On the one hand, one knows an even upper bound for $P$ iff one knows an odd upper bound, so the formulas $\exists x(E(x) \wedge B(x))$ and $\exists x(O(x) \wedge B(x))$ are resolved in exactly the same information states, which is what support captures. On the other hand, the sentences "there is an even upper bound to $P$ " and "there is an odd upper bound to $P$ " invite different responses, and the system rightly predicts this by assigning them distinct possibilities.

Moreover, unlike the unrestricted system, the proposed semantics correctly predicts that the boundedness formula is redundant in any information state in which an upper bound for $P$ is known: if $s=B(x)$, then $[\exists x B(x)]_{s}=\{s\}$.

Many features of the propositional system carry over to this first-order implementation. Crucially, meaning is still articulated in two components, informativeness and inquisitiveness. For, consider a $\varphi$ which is neither informative nor inquisitive: since $\varphi$ is not inquisitive, $|\varphi| \in[\varphi]$; and since $\varphi$ is not informative, $|\varphi|=\omega$; finally, since the presence of the filter NoD explicitly rules out possibilities included in maximal ones, $\omega$ must be the unique possibility for $\varphi$, that is, $\varphi$ must be an inquisitive tautology.

Assertions and questions may be defined as usual, and it is still the case that for any formula $\varphi,!\varphi$ is an assertion, ? $\varphi$ is a question, and the decomposition $\varphi \equiv!\varphi \wedge$ ? $\varphi$ holds, where equivalence amounts to having the same meaning.

Obviously, the classical treatment of information is preserved, i.e. we have $\bigcup[\varphi]=|\varphi|$. Finally, the sources of inquisitiveness in the system are disjunction and the existential quantifier, in the sense that any formula not containing disjunction or the existential quantifier is an assertion.

## 5 Conclusions

In this paper we proposed a conservative extension of propositional inquisitive semantics to the first order setting, focussing on the essential changes that this move required. These were (i) to state the semantics in terms of a recursive specification of the possibilities for a sentence, rather than in terms of support; and (ii) to switch from the requirement of maximality to that of not being optimally dominated. These changes have no effect on the propositional case.

The proposed system was motivated here by the attempt to obtain correct predictions while retaining as much as possible of the propositional system: a very important thing which remains to be done is to provide a more conceptual justification for the given definitions.

Moreover, a task for future work is the investigation of both the logical features of the proposed semantics and its application to natural language, in particular to the semantics of interrogative sentences.

With regard to this latter aspect, notice that our logical semantics as such does not embody a specific theory on the semantic analysis of interrogatives. Instead, it offers a general logical framework in which also opposing empirical analyses may be formulated and studied. This is most obviously so for the Hamblin analysis of questions Hamblin (1973), which is covered by inquisitive existential quantification $(\exists x P x)$, and the partition approach of Groenendijk and Stokhof (1984), which is covered by universal quantification over polar questions $(\forall x ? P x)$. The treatment of which-questions in Velissaratou (2000), which analyzes such questions in terms of exhaustive answers, but not as partitions, may also be represented (by $\forall x(P x \rightarrow ? Q x)$ ).

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# There is Something about Might 

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#### Abstract

In this paper we present an alternative interpretation of statements of epistemic possibility, which does not induce a consistency test on a common ground, as in (Veltman 1996), but which tests whether the possibility is supported by some update of the common ground, as in (Veltman 1984). The information space relative to which such claims are evaluated are taken to consist in the possible developements of a discourse in action. It is shown that this notion of Might not only behaves better logically and pragmatically speaking, but that it also allows for non-trivial attitude reports and questions about epistemic possibilities. These epistemic modal statements can also be understood to guide or focus the inquisitive actions of the discourse participants.


## 1 Epistemic Modalities

Epistemic modal operators like Might and Must in English, and semantically related verbs, adverbs and markers, express a kind of possibility or necessity relative to some body of knowledge, evidence, or other constraints. A sentence formalized as $\operatorname{Might}(\phi)$ (or: $\stackrel{\diamond}{ }$ ) is used to express that $\phi$ is not excluded relative to some source of evidence. In the standard semantic approach (Kratzer 1977) such a body of knowledge or evidence is conceived of as a set of possibilities (situations, worlds, ...), relative to which $\diamond \phi$ is true iff $\phi$ is true with respect to some possibilities in $K$.

In the literature, this basic interpretation of the modalities has been challenged and modified in two respects. Firstly, epistemic modals are seen to be inherently contextual, or indexical. The relevant body of knowledge against which to evaluate epistemic modals has to be found relative to the discourse situation in which these modal sentences are uttered. Secondly, the relevant bodies of information have been argued to be those of the interlocutors in an actually unfolding discourse. Building on Stalnaker's idea of establishing common grounds, an utterance of $\diamond \phi$ has been taken to express consistency of $\phi$ with the current information state of the interlocutors in a discourse. This idea has been formally developed in (Veltman 1996) and subsequent work.

Notoriously, such a consistency interpretation of $\varsigma \phi$ can be deemed rather vacuous. While Veltman's update semantics is motivated in part by (Stalnaker 1978)'s idea that assertions, or utterances, are put to use to substantially contribute to a common ground for the participants in a discourse, the epistemic
test associated with $\diamond \phi$ appears to do nothing of the kind. In response to a claim that it might be the case that $\phi$, one can simply agree that it is consistent with the common ground that $\phi$, or just disagree that it is not. Upon the interpretation proposed, there is no other option available. Worse, assuming, as one would ideally do, that the common ground contains common knowledge, and that participants have the gift of introspection, a use of $\diamond \phi$ is utterly pointless, and would at best remedy possibly misconceptions of the common ground - while the remedies or required revisions typically remain beyond the scope of current systems of update or inquisitive semantics.

It has been suggested every here and there that epistemic modal statements additionally serve to "raise" possibilities, that they are used to bring us to "attend to" or "focus on" possibilities. (Hulstijn 1997; Groenendijk 2007; Yalcin 2008; Roussarie 2009; Brumwell 2009; Groenendijk \& Roelofsen 2009). However, it has sofar remained unclear what exactly it means to raise a possibility, or for there to be one. As before, in response to a claim that $\uparrow \phi$, one might agree that, "Yes, there is the possibility that $\phi$. " or that "No, there is not." but this will not all by itself serve to make $\diamond \phi$ any less pointless. Surely, $\diamond \phi$ can be taken to effectuate something like the presence or actuality of the possibility that $\phi$ in the common ground. The question then, however, becomes what these actually present possibilities are? One may ask, what is the difference between a state of information with, or the same one without the possibility that $\phi$. So far I have seen no answer but that the first does not, and the second does support that $\stackrel{\wedge}{ }$. Not very informative yet. Nevertheless, it seems hardly anybody would deny that such possibility statements serve a non-trivial purpose. For instance, because they have substance. In this paper I will polemically argue for this point by associating them with ordinary truth-conditions. As will come clear once we go along, nothing really hinges on the issue on whether to call these truth-conditions, or acceptability-conditions, or whatever conditions of your ilk.

The main idea pursued in this paper is that the epistemic Might-operator can be made more sense of if we revive an original interpretation of $\rangle$, as an ordinary modal operator defined over a space, not of simple possibilities, but of information states, as proposed in the so-called data semantics from (Veltman 1984; Landman 1986). Roughly, $\diamond \phi$ is taken to state $\phi$ holds in an update of the current information state. Like the $\diamond$-operator from modal logic, which deems $\diamond \phi$ true in a situation (world, ...) iff there is an accessible situation (world, $\ldots$ ) in which $\phi$ is true, epistemic Might ( $\diamond \phi$ would be rendered true if there is an update, or extension, of the current information state in which $\phi$ holds. As we will see below, this interpretation is practically sufficiently close to the interpretation of $\diamond \phi$ as a consistency test on information states; however, it also allows us to make more substantial sense of statements of epistemic possibility.

Veltman and Landman have originally focused on the logical aspects of their modal operators and related conditional sentences, but they have remained by and large silent about the set up of the space of information states in which the modal operators get defined. There, it has been relatively classically assumed to be a fixed space, with a set of information states assumed given, together with
a primitive and fixed extension or update relation. With all the work that has been done on the formal semantics and pragmatics of discourse, however, such spaces of information states and their updates have been and can be investigated and formalized in lots of further detail in the meantime. In this paper I want to show that indeed a neat formulation of $\diamond \phi$ can be given, drawing from the data semantics insights on Might, fleshing it out relative to a notion of a common ground, which is indexically linked to an actually occurring discourse. The space of updates or extensions of the relevant information states can be taken to consist in the future developments of the common ground in a discourse in action. And $\diamond \phi$ can be taken to state the speaker's opinion that $\phi$ holds in a possible, maybe partial, resolution of the discourse.

## 2 Optimal Inquisitive Discourse

In order to implement the above ideas one can in principle take any classical or non-classical framework of interpretation, which deals with the raising and resolving of issues in discourse, like that of (Ginzburg 1995; Roberts 1996; Hulstijn 1997; Groenendijk 2007; Groenendijk \& Roelofsen 2009), to name a few. For the present purposes it seems appropriate to build on my own (Dekker 2004; Dekker 2007), since the framework proposed there is framed in classical semantic and pragmatic terms, and arguably consistent with the others.

In (Dekker 2004; Dekker 2007) a notion of an optimal inquisitive discourse is defined that relates a set of agents whose epistemic states carry information and are troubled by questions. Let me first clarify what I mean with questions. There are questions which people have and questions people pose. Questions people have is what they wonder about, out of curiosity, but normally in relation to the Big Question, "What to do?" Questions people pose may and may not be questions people have, but normally they are, and they serve to make questions they have into issues which they share with others.

An appropriate way to model states with information and questions is given in (Groenendijk 2007) (originally from 1999) in which states are modeled by a symmetric and transitive relation on a set of possibilities. The idea is that possibilities that stand in that relation are considered possible ways the actual world or situation might be, and that the difference between connected possibilities is considered immaterial. Formally, a possibility $i$ is considered to be a way the world might be in state $\sigma$, iff there is an $i^{\prime}$, typically $i$ itself, such that $\left\langle i, i^{\prime}\right\rangle \in \sigma$. In such a case we say $i \in D(\sigma)$, with $D(\sigma)$ representing the data in $\sigma$. If $\langle i, j\rangle \in \sigma$, it is considered no question whether the actual world is like $i$ or $j$. However, if $i, j \in D(\sigma)$, and $\langle i, j\rangle \notin \sigma$, then the difference between the two does count. In that case the information state models the issue whether the actual world is an $i$ - or a $j$-kind world. The relevant 'kinds' here are very much defined by the given information state. Like I said, states are modeled by means of a symmetric and transitive relation $\sigma$, so they induce an partition of a subset of the whole
set of possibilities, viz., of the data set $D(\sigma)$ of $\sigma .{ }^{1}$ The real question modeled is then, in which block of connected possibilities the actual world resides-not which particular possibility it is in such a block.

The notion of an optimal inquisitive discourse in (Dekker 2004; Dekker 2007) is based on the simple assumption that agents involved in a communication aim to get their questions resolved in a reliable and respectable manner. In, indeed, the very simple cases, they have to do with the questions they have and with the information which is there, the joint information of the interlocuting participants. By the end of the day, the interlocutors want to get their questions resolved, so that they know what to do. Having no other information available than the information one has oneself, and what the others may provide, and, if necessary, the information from an oracle, the information which is exchanged and ends up in the common ground is ideally supported by the joint information of the interlocutors. Formally, a discourse situation involves a number of agents $a_{1}, \ldots, a_{n} \in A$, each with their own (private) information and (private) questions, modeled by information states $\sigma_{1}, \ldots, \sigma_{n}$, respectively. We also assume an oracle $\mathcal{O}=\sigma_{0}$ to model the possibility of solicited and unsolicited information.

Definition 1 (Optimal Inquiry) An inquisitive discourse $\Phi$ among a set of agents $a_{1}, \ldots, a_{n} \in A$ with information states $\sigma_{1}, \ldots, \sigma_{n}$, together with an oracle $\mathcal{O}=\sigma_{0}$, is optimal iff:

$$
\begin{array}{rr}
- & \forall i(1 \leq i \leq n): D(\llbracket \Phi \rrbracket) \cap D\left(\sigma_{i}\right) \models \sigma_{i} \\
& \left(s \models \sigma, s \text { answers } \sigma, \text { iff } s^{2} \subseteq \sigma\right. \text { ) } \\
& \left(\bigcap_{0 \leq i \leq n}\left(\sigma_{i}\right)\right) \subseteq D(\llbracket \Phi \rrbracket) \\
\Phi \text { is minimal and } \text { well-behaved } & \text { (quantity and manner) }
\end{array}
$$

Assuming $\llbracket \Phi \rrbracket$, the interpretation of the discourse $\Phi$, to convey information and raise issues, it can be rendered as an information state in its own right. The first requirement says that $\Phi$ answers the questions of any participant. ${ }^{2}$ In the second requirement $\bigcap_{0<i<n}\left(\sigma_{i}\right)$ presents the joint information and questions of the participants. The data provided by $\Phi$ are required to be supported by the joint information of the participants. The minimality requirement obviously relates to Grice's maxim of quantity and is motivated by the insight that the Big Question is never "What is the world exactly like?", but, rather, "What to do?" with limited resources of information, reasoning, and time. A Gricean manner maxim is motivated by the observation that the exchange of information inherently involves engaging in a social practice.

The above definition indicates the way in which a discourse might ideally proceed. The participants each ask the questions they have, and the others give the required answers. Of course, it may be the case that the participants fail

[^78]the answer, so that one may try to consult the oracle, but this one may fail the answer as well. The main goals can be achieved differently, though. The required information may be there in a discourse situation, but distributed over the agents, or interlocutors. Thus, an optimal inquiry might run as follows then.
(1) $A$ : Will Bernd be at the reception?
(2) $B$ : I don't know. He will be if he finished his grading.
(3) $C$ : Oh, but he just finished his grading.

This is an example where $B$ provides unsolicited information, which nevertheless makes the exchange run smooth. More interesting may be a case where it serves to ask a question one doesn't have, as is elaborated in some detail in (Dekker 2004; Dekker 2007). Someone may simply wonder whether or not to attend to the reception, the answer to which may depend on the configuration of lecturers attending it. Instead of spelling out the favorable and unfavorable configurations it may be worthwhile to simply ask which lecturers attend. A few sample answers of lecturers attending and those not attending may already suffice to get the original question answered. So-called conditional questions may also turn out to be very useful, potentially. I may ask "If Carla goes to the reception, will you go there as well?", and a positive reply to this question may sufficiently answer my own question in the sense that I then know I will not be going there. The main point about these examples is that they are reasonable in that they may contribute to establishing an optimal exchange, even though they are not guaranteed to do so. The reason is that, while the global goal is clear, an optimal exchange of information, after all, the agents have to act, and inquire, under uncertainty. It is against this general background that epistemic modality statements can be seen to make sense. By employing $\diamond \phi$ we claim one points at a possible resolution of the current discourse, and this may serve to point at a possibility which deserves further investigation. This, notwithstanding the fact that, of course, the ensuing investigation may turn out negative after all.

## 3 Epistemic Modality in Discourse

The little discourse (1-3) above might have proceeded differently, for instance, as follows
(4) A: Will Bernd be at the reception?
(5) $B$ : He might have finished grading.
(6) $A$ : So, what?
(7) $B$ : If he has, he will definitely be there.

Upon this way of proceeding, the interlocutors have an incentive to go and find out whether John has indeed finished grading, that is, a new question has emerged from the possibility statement. Similarly, if I wonder whether or not to go to the reception, and ask who will be there, the assertion that Bernd might be there would elicit a possibility that would directly decide my original question: if Bernd goes I wouldn't hesitate to go as well. Again it incites to investigate or query whether Bernd indeed will come. Finally, if we are looking for the bicycle
keys, with the major issue being where the keys are, we are possibly facing a whole lot of questions, viz., for any possible location $l$ the question whether the keys are at $l$. The statement that they might be in the basement would turn the main question into a more feasible one, viz, whether they are in the basement, and we may find reason to try and find evidence for that possibility, among the interlocutors, by consulting the oracle, or, what may amount to the same thing, go down the basement and look for the keys.

In each of the above cases, of course, there is no guarantee that the stated possibility will turn out true, or supported, and, hence, may help answer our question. Still, it does incite a specific investigative action, which may lead us to do at least something to achieve the required goal. By pointing at a possible resolution of the current discourse situation, one in which $\phi$ holds, this automatically raises the question whether we can reach that state. This, naturally, provides the incentive to go and find out.

Before turning to the definition of the possibility statements themselves, we have to be more specific about possible resolutions of a discourse situation.

Definition 2 (Resolutions) If $D_{j}$ is a discourse situation after a discourse $\Phi$ established a common ground $\gamma_{j} \subseteq \llbracket \Phi \rrbracket$, then a possible resolution of $D_{j}$ is a common ground $\gamma_{r}$ that answers a reaonable update $D_{r-1}$ of $D_{j}$, with common ground $\gamma_{r-1} \subseteq \gamma_{j}$ (i.e., $Q\left(\gamma_{r}\right) \subset Q\left(\sigma_{r-1}\right)$ ).

This definition is quite weak indeed, because it allows for very partial resolutions of a discourse situation. ${ }^{3}$

Definition 3 (Epistemic Possibilities) $\diamond \phi$ is true at $D_{j}$ iff $\phi$ holds in a possible resolution $\gamma_{r}$ of $D_{j}$ (i.e., iff $D\left(\gamma_{r}\right) \subseteq D(\llbracket \phi \rrbracket)$ ).

The present definiton of epistemic Might directly accounts for a number of typical features of its use. In the first place $\diamond \phi$ doesn't make sense in situations where $\phi$ is an issue already, or where the issue whether $\phi$ has been resolved. In the second place it is fully indexical. The truth of $\stackrel{\delta}{ }$ totally depends on the situation in the discourse where it is used, and on the information available there. In the third place it is non-persistent. Once new relevant information enters the common ground, the possibility that $\phi$, once acknowledged, may eventually have to be given up. By the same token, in the fourth, and final, place, the stated possibility or resolution should not be any theoretically possible update of the common ground: it should be a reasonably possible update, not one which is loaded with unsolicited details orthogonal to the issues which are raised in the common ground. The present definition thus suits some quite common opinions about epistemic Might.

By way of illustration, consider the following statement.
(8) Bernd might not go to the reception.

[^79]Out of the blue, this would appear to be a vacuous statement, to be rendered false indeed. However, in a context where one addresses Bernd's ex Denise, who wants to go to the reception, but who has plenty of reasons to not see Bernd, it makes sense. Suppose, that we are conversing about the reception and Ann knows that Pete goes to the reception, and Ben is sure that Pete will not go without his new friend Bernd. Denise makes the above statement. In the delicate circumstances, the statement seems true. However, in the same circumstances, delicate as they are, Ann and Ben may conjoin their information, and decide that, oops, Pete is going to the reception with Bernd. If Denise states that Bernd might not go to the reception, they will have to correct her. Notice that the sample statement changes from practically false, to deemed true, to eventually false again.

For a full account of possibility statements, and their use in discourse, we need of course to specify the notion of a reasonably possible update in much more detail. In part this will be framed against the background consisting of the interlocutors' understanding of an optimal inquisitive discourse, as defined above, but it will also have to take into account the actual discourse situation itself, the information the interlocutors have, about the (current stage of the) situation, and about each other's (lack of) information. We leave a specification of these details for the full version of the paper.

Although our understanding of epistemic modality is rather different, logically speaking, from Veltman's consistency Might, pragmatically speaking it makes quite similar predictions. For notice that, on the one hand, in run of the mill cases consistency of $\phi$ with the common ground corelates with the theoretical possibility of an update with $\phi$. Moreover, on the second hand, the very fact that the update with $\phi$ is suggested by any use of $\diamond \phi$ may automatically raise it as an issue in the current discourse, and, hence, as something true in a possible resolution of the ensuing discoruse. Notice, though, that these systematic similarities are purely pragmatic, and, hence, very defeasible.

For, $\diamond \phi$ can be rejected not just because of inconsistence of $\phi$ with the common ground, but because an update with $\phi$ is ruled out for other reasons. For instance, if $\phi$ is refused as an issue. For instance, philosophically minded persons may at any moment bring up the possibility that there might be cockroach in your coffee, that aliens from space may rule the world tomorrow, or that we are brains in a vat. Upon our understanding of might we need not believe these propositions to be false, in order to, still reject the accompanying statements of epistemic possibility. To accept these statements, it would normally require a reason to even consider the stated possibilities, while one may even also reject the possibility without further argument. Moreover, $\diamond \phi$ can be true and accepted even if $\phi$ is inconsistent with our current implicit or explicit information. It may open up our eyes, for possibilities thoughtlessly excluded. Possibility statements may in principle announce or require an act of true belief revision. So while we may have not been truly believing that the keys are somewhere in the basement, but have been looking for them on the silent assumption that they are there, the announcement that we might have left them in the garage provides the incentive for another potentially very sucessful inquisitive action.

## 4 Questions and Beliefs About Modality

As defined, a possibility statement has truth-conditions, but its truth is very much context-dependent, unstable, and, hence, quite a bit negotiable. Nevertheless, with this little bit of truth-conditions $\vee \phi$ may non-trivially figure in attitude reports and questions. As (Gillies \& von Fintel 2008; Brumwell 2009; Roussarie 2009) have observed, the following sentences do not just report or question (in)consistencies, but true worries, beliefs and questions:
(9) Benjamin wonders whether he might go to the reception.
(10) Sybille believes that he might stay home.
(11) What do you think. Might Ben go somewhere else?

The present account can neatly account for this, but first observe that the interpretation of Might as just a consistency test appears to be quite inappropriate. When Ben is wondering whether he might go to reception, he is not just reflecting on his information. He is not inspecting his knowledge, with the question, "Well, is my information state consistent with this possibility?" Also, saying that Sybille believes that Ben might stay home does not just require that her information state be consistent with that possibility. The fact that her information does not exclude such a possibility is not sufficient for such an attribution to be true. (For, otherwise she could be attributed all kinds of epistemic possibilities about the whereabouts of my cousins whom she has never heard of.) Also, a question with might in it, as in (11) would really be no question. Assuming the common ground is public, we are all supposed to know whether it does or does not exclude the possibility that Ben goes somewhere else. Neither does it seem to ask for our beliefs about the common ground. (Like, "We are having a common ground together, but we don't know what it is.")

On the account presented in the previous section these statements gain full weight. Example (9) can be taken to state that Nicholas indeed wonders whether there is a reaonably possible update of his current state into one in which he comes - or if there is no such update. This does not require deciding yet, it is more like deciding if it is still conceivable to possibly decide positive. (Of course, if the outcome is negative, he would consistently decide he will not go, we hope.) Likewise, example (10) can be taken to state that Sybille believes that there is a reasonably possible update of her state to one in which Nicholas stays home. And finally, example (11) may be taken as a genuine question whether there is a reasonably possible update of the common ground in which $\phi$ holds.

Surely, much more needs to be done to formally elaborate these proposals. As above, we need to take into account indexical beliefs about the actual discourse situation, the way the interlocutors think it may or may not develop, and so on. Page limitations, however, again prohibit us to go into details.

## 5 Conclusion

In this paper I have presented a more or less classical interpretation of statements of epistemic possibility, according to which $\diamond \phi$ states that $\phi$ holds in an
update, or resolution, of the common ground. These statements are have content, which make them suitable for use in non-trivial attitude reports and questions about epistemic possibilities. These epistemic modal statements can also be understood to guide or focus the inquisitive actions of the discourse participants. By staging and explaining Might utterances within a context of investigative discourse, Might can be seen to guide and focus our inquisitive actions.

For substantial parts of the present proposal, intuitive motivation has been given. Modeling data or information in terms of non-excluded possibilities has been given the required philosophical motivation in the work of Frege, Wittgenstein, and Tarski. Modeling questions has been independently motivated using the tools and ideas of decision theory, as it has been most perspiciuously formulated in the proposals from (van Rooy 2003). By understanding discourse acts as moves towards the goal of an optimal inquisitive discourse, we may now also gain understanding the use of possibilities 'attended to'.

The perspective on the use of modality statements in discourse, which I have offered in this paper, can be taken motivate the idea of attending to possibilities, stipulated in(Yalcin 2008; Roussarie 2009; Brumwell 2009; Groenendijk \& Roelofsen 2009). Nevertheless, approaches like those mentioned do not seem to elicit explanations like those given here. The reason is that they tend to understand or explain reasonable discourses in terms of the structural properties of each individual utterance relative to those of the local situation. They rely on notions of 'congruence', 'answerhood' or 'compliance', which are entirely local properties of utterances, in given discourse situations. These notions, however, will not serve to explain why and when it makes sense to ask questions which one doesn't have, or to provide information not asked for.

The present proposal seeks to understand the discourse contributions as more or less reasonable attempts to engage in the larger project of achieving an optimal inquisitive discourse. It is only relative to the wider goal of effective and reliable communication, of situated agents, that we can understand what the individual contributions can be taken to try or mean. In such a setting, it appears to be very reasonable indeed to sometimes raise questions and provide data which have been unsolicited, and, typically, to raise possibilities to attention, like we do with epistemic modality statements. A global perspective on discourse, and I think this is the one Grice originally must have had in mind, seems to automatically make sense of these contributions.

I would like to conclude the paper with a final observation, in line with the present discussion. First, maybe Goldbach's second conjecture is true, while it is false to say that it might be true. We simply don't know. Second, it is not so that we might be all wrong about everything. Surely, this is not to say that we are right about anything.

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# Incommensurability 

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#### Abstract

This paper discusses subcomparatives with 'incommensurable' adjectives (e.g. beautiful and intelligent), which have received little attention in the literature so far. This is surprising, as the topic is of great importance for the current discussion with respect to the choice between a vague predicate analysis and degree-based approaches to gradability. This paper studies the properties of comparisons involving 'incommensurable' adjectives on the basis of a new collection of (mostly attested) data. A confrontation of the data with both degree-based and non degree-based theories offers evidence for the latter, and more in particular for a more constrained version of Klein's analysis ([11],[12]) as presented in Doetjes, Constantinescu \& Součková [6].


Keywords: subcomparatives, vague predicate analysis, degrees, comparison of deviation, relative comparison

## 1 Introduction

In the literature, different judgments can be found for adjectival subcomparatives with so-called 'incommensurable' adjectives. Adjectival subcomparatives are comparatives which contain an overt adjective both in the main clause and in the than-clause. These two adjectives usually differ from one another. An example is given in (1):
(1) The table is longer than the desk is wide

The adjectives long and wide correspond to the dimensions of length and width respectively, and these dimensions can be measured by the same measurement system. According to Kennedy [9], the number of adjectives that may occur in subcomparatives is limited by the fact that adjectives in these structures need to be commensurable. In case they are incommensurable, as the adjectives in (2), the sentence is not felicitous. Thus he concludes that incommensurability constitutes an argument against the vague predicate analysis of adjectives as developed by Klein ([11],[12]) and recently defended by Van Rooij [16].
(2) \#My copy of The brothers Karamazow is heavier than my copy of The Idiot is old

Even though this example is convincing, and indeed seems to be rather odd, Bartsch \& Vennemann ([1]:91) discuss another case of a comparative with supposedly incommensurable adjectives, and claim that the sentence is fine:

## (3) Marilyn is more beautiful than she is intelligent

As Bartsch \& Vennemann indicate, the important reading is not the metalinguistic one (where more could be replaced by rather), but the reading in which a comparison is made between Marilyn's beauty and her intelligence. Surprisingly, the relevant reading of (3) is mostly ignored in the literature (with the exception of [1], [8], [2], [3]), and if addressed, relatively few examples are taken into account. Some of Bale's
[2] examples are given in (4):
(4) a. Seymour is as intelligent as Esme is beautiful
b. If Esme chooses to marry funny but poor Ben over rich but boring Steve, [...] Ben must be funnier than Steve is rich.
c. Although Seymour was both happy and angry, he was still happier than he was angry.

The properties of subcomparatives with so-called incommensurable adjectives are important for the way gradability is represented. The only way to handle this type of phenomenon in a degree based approach is to assume some sort of a mapping mechanism that turns the incommensurable degrees, that is, degrees on different scales, into objects that may be compared (cf. [1], [8], [2], [3]). On the other hand, sentences such as (3) and (4) can be seen as an argument in favor of the vague predicate analysis.

The first part of this paper examines a collection of (mostly attested) examples of subcomparatives containing 'incommensurable' adjectives in English and Dutch. I will argue that sentences such as (3) and (4) have to be seen as a subcase of what I will call Relative Comparison or RC (following [6]), and that Comparison of Deviation ([9],[10]) should also be seen as an instance of RC. I will also discuss conditions on RC that can make sense of the contrast between (2) on the one hand, and well-formed cases of RC on the other. In the second part of the paper, the data will be confronted to both the vague predicate analysis and theories of gradable expressions that make use of degrees. I will argue that RC should be seen as evidence for a constrained version of the vague predicate analysis, as proposed by Doetjes, Constantinescu \& Součková [6]

## 2 What is relative comparison?

The sentences in (3) and (4) raise to two different questions. In the first place, one needs to know whether the phenomenon exemplified in (3) and (4) is limited to subcomparatives with incommensurable adjectives, or that there are also sentences with commensurable adjectives that exhibit a similar behavior and should be analyzed in the same way. In the second place, given the contrast between the judgments given in the literature for (2) and (3)-(4), one wants to know under what conditions this type of sentences can be used

Before addressing this second question, I will first discuss some properties of these structures. More in particular, I will argue that RC is a rather broad phenomenon, which covers all subcomparatives with a relative interpretation, excluding only
subcomparatives with an absolute interpretation such as (1) above, in which the absolute width of the table is compared to the absolute length of the desk (cf. [6]).

According to Bale [2], relative comparison (in his terms 'indirect comparison') is not restricted to subcomparatives with incommensurable adjectives. It also occurs in elliptical comparatives with two different norms, as in (5):
(5) Ella is heavier for a baby than Denis is for a three year old.

As Bale notes, an ordinary degree based theory would expect this type of sentences to be impossible, as we are certainly not comparing the weight of the baby to the weight of the three year old in absolute terms. What we do compare here is the relative weight of the baby (as compared to other babies) and the relative weight of the three year old (as compared to other three year olds).

The sentence in (5) is actually very similar to subcomparatives with two polar opposites and a comparison of deviation interpretation, as in (6a) below. Kennedy ([9],[10]), who discusses this type of sentences in detail, argues that direct comparison of the degrees corresponding to polar opposites is not possible, as these form different objects. In order to derive this, he postulates that the degree corresponding to a positive adjective constitutes a positive extent (ranging from zero to some point on the scale), while degrees introduced by negative adjectives correspond to negative extents (ranging form some point on a scale to infinity). As a result, the positive adjective tall conveys information about the height an object has, while the negative adjective short conveys information about the height an object does not have'([9]:193). As comparison of two degrees is based on the inclusion relation, this way of modeling positive and negative degrees excludes comparison of a positive and a negative degree even if they are defined as degrees on the same scale. However, in this latter scenario there is a way out. Comparatives and equatives with two polar opposites that make use of the same scale may be interpreted as instances of Comparison of Deviation (COD). Kennedy derives the example in (6a) as in (6b), which results in a comparison of the two differential extents, measuring the difference between the actual degree and the standard. The ZERO function maps the two differential extents onto two extents that both start at the zero point of the same scale, and as such can be compared.
(6) a. The Cubs are as old as the White Sox are young
b. $\quad \operatorname{ZERO}\left(\right.$ old $\left.(C u b s)-d_{\text {s.oldness }}\right) \succcurlyeq \operatorname{ZERO}\left(\right.$ young $($ White Sox $\left.)-d_{\text {s.youngness }}\right)$

Kennedy's analysis predicts that COD is restricted to adjectives that project degrees on the same scale (antonyms and dimensional adjectives that are compatible with the same measurement system, such as long and tall). As such, he excludes the possibility of COD in subcomparatives with incommensurable adjectives (cf. (2)), but he can handle Bale's example in (5). The analysis of sentences such as (6a) as involving a comparison of the deviation from the standard implies that the degrees are at least equivalent to the standard value, and as such these sentences presuppose the positive form of the adjectives they contain, as the positive also introduces the standard [5].

For Bartsch \& Vennemann [1] there is no fundamental difference between sentences such as (6) (Kennedy's COD) and cases such as (2) and (3) (comparisons with incommensurable adjectives). In both cases, the comparison concerns the difference between the actual degree and the norm, and as such they are all analyzed
in terms of a comparison of the deviations from the respective standards introduced by the two adjectives. In the case of dimensional adjectives, this comparison makes use of a conventional measure. In the case of sentences such as (3), they introduce a scale on which specific and average beauty/intelligence values can be assigned numbers on a single scale (specific and average BQs and IQs, as they call them). As such, the differences between the specific and the average values may be compared. Hamann, Nerbonne \& Pietsch [8] arrive at a similar result by forcing the standard values corresponding to the two adjectives to be mapped onto the same point of the derived scale.

However, Bale [3] argues that (2) and (3) cannot be analyzed in a similar way to COD, as this type of sentence does not imply the positive, as illustrated in (7).
(7) Unfortunately, Mary is more intelligent than Medusa is beautiful.

Bale concludes that the neutralization effect we find in normal comparatives (cf. [4]) is also present in this type of comparison Bale and that the analysis of (2) and (3) should not introduce the standard. This implies that there are two different phenomena: COD on the one hand, and relative comparison (his indirect comparison) on the other

According to Bale, the difference between the two phenomena is correlated with the use of the analytic versus the synthetic form of the comparative. In COD the synthetic form is used, and this is in his view responsible for the effect that we find. However, there are two facts that complicate the picture. In the first place, the use of an analytic comparative as opposed to a synthetic form may introduce an evaluative interpretation of the adjective (see [6], [15]), and as such the lack of a neutral interpretation may well be directly due to the use of the analytic comparative, which would make it independent from the use of a subcomparative with two polar opposites. On the other hand, it is questionable whether the effect neutralization effect Bale talks about is always available, even for sentences with an analytic comparative In this regard it is interesting to look at COD sentences in German, where only the synthetic form used. Yet, these sentences have a comparison of deviation type of interpretation, which corresponds to a non neutral interpretation [4]. The positive form of the adjectives in (8) is presupposed, contrary to what we find in (7).
(8) ?Hans is kleiner als Eva groß ist
'Hans is shorter than Eva is tall'
At this point the picture seems to be rather complicated: on the one hand, people do not agree on whether we are dealing with one phenomenon or with two. On the other hand, even though neutralization effects can be found, as shown by Bale's data, they do not always occur. Obviously one could say that (7) is a case of relative comparison while (8) is a case of COD, but this does not explain why this would be so. More in particular, there does not seem to be any reason not to apply Bale's analysis to cases such as (8), and this raises the question why the effect found in (7) is necessarily absent in (8).

When looking at the sentences Bale uses in order to show that the neutral interpretation exists, it turns out that they have two things in common. In the first place, they contain positive adjectives (beautiful, intelligent, pretty), and in the second
place, they all have a strong ironical flavor. This is also clear in the example in (9), which is an attested Dutch sentence (internet).
(9) Gelukkig was [de hond] veel slimmer dan hij mooi was.
'Luckily the dog was much smarter than he was good-looking.'
The sentence in (9) does not only lack the presupposition that the dog is goodlooking, it strongly suggests that the dog is ugly, and in this respect the interpretation differs form a neutral or non evaluative interpretation. As such the sentence can be seen as a case of what Leech [13] calls 'criticism under the guise of praise': even though the dog is claimed to be pretty, the person who uses this sentence wants to convey that the dog is ugly. Given that praise usually involves positive adjectives, one expects this effect to arise only when positive adjectives are used. Interestingly, when one tries to formulate a negative counterpart of (9), one does not succeed. There is no way to interpret (10) without presupposing that the dog is ugly.
(10) Jammer genoeg was [de hond] veel dommer dan hij lelijk was
'Unfortunately the dog was much more stupid than he was ugly'
The effect in (9) might be analyzed as resulting from an 'ironic standard': the normal standard corresponding to the adjective mooi has been be replaced by an ironic standard, which stretches up the domain and as such permits to even include the ugly dog in the set of good-looking individuals.

Given that it is possible to force a non presupposed reading of the first adjective, as in (7), it should be possible to stretch up the domain of both adjectives. A closer look at the data shows that this seems to be the default case. Evidence for this comes from the fact that it is very hard to get the ironic reading of the sentence in (9) when the first adjective slim 'smart' is replaced by its negative counterpart dom 'stupid', as in (11a). Moreover, in equatives with two positive adjectives, it is not possible to interpret only one of the two adjectives ironically. In (11b), either both adjectives are ironical, or both are not. If one assumes that the ironic reading forces an 'ironic standard' for both adjectives, these restrictions can be understood.
(11) a. Jammer genoeg was [de hond] veel dommer dan hij mooi was
'Unfortunately the dog was much more stupid than he was good-looking'
b. De hond was even slim als hij mooi was
'The dog was as smart as it was good-looking'
An analysis of cases such as (7) and (9) in terms of an ironic 'standard' has an important advantage for the interpretation of the data. It makes it possible to assume that even (7) and (9) involve a comparison of deviation in the sense that they presuppose the positive. However, in this case, this positive has an ironic interpretation. The apparent lack of this type of effect in the traditional COD environments, and in particular in (8), follows from the fact that the domain of both adjectives needs to be stretched up, while this is only possible when a positive adjective is used. As such the effect is not expected to occur in sentences such as (8), wich contain both a positive and a negative adjective.

A further argument for treating RC and the traditional COD cases with polar opposites as one single phenomenon has been offered in [6]. We claim that in both types of sentences a similar interpretation is obtained, which is not the interpretation
in (6b) above. We argue that standard cases of COD do not involve a comparison of differential extents in an absolute sense, as predicted by Kennedy's analysis, but rather in a relative sense: if the two standards introduced by the two adjectives are clearly different, the same deviation (in absolute terms) counts as a smaller deviation from the higher standard than from the lower one. This can be illustrated by the example in (12a), which is arguably true under the COD interpretation in (12b) [10]
(12) a. The Sears Tower is as tall as the San Francisco Bay Bridge is long.
b. The degree to which the Sears Tower exceeds a standard of tallness (for buildings) is at least as great as the degree to which the San Francisco Bay Bridge exceeds a standard of length (for bridges)

If one compares the differential extents, one cannot do so in an absolute way, given that the total length of Sears Tower ( 527 meters) might well be less than the difference between the length of San Francisco Bay Bridge ( 5,920 meters) and the standard length for bridges. Such a scenario could still make the sentence true, as long as the two differential extents are comparable to one another in a relative way, given the size of the standard. The deviations are rather measured as a percentage of the standard than as an absolute value.

To conclude the first part of the section, there are good reasons to treat the original COD cases (involving polar oppositions) and subcomparatives with incommensurable adjectives as manifestations of one single phenomenon. In the first place, these sentences presuppose the positive (even though this fact may be obscured by the effect of irony). Moreover, all of these cases involve a relative, strongly context dependent interpretation, which makes them very different from subcomparatives that involve an absolute comparison such as the one in (1).

The next question to address is what constraints are placed on relative comparison. As observed at the beginning of this paper, not all combinations of adjectives seem to lead to a felicitous result (cf. (2)). However, a well chosen example in the right type of context can be fully felicitous and there is no reason to assume that the structure as such is ungrammatical. In the remainder of this section, I will argue that RC requires the two adjectives to be semantically or contextually associated to one another

A closer look the difference between the infelicitous example in (2) and for instance the fully felicitous attested example in (9) is that it is not easy to find some sort of a connection or relation between the two adjectives used in (2) (heavy and old). On the other hand, the two adjectives used in (9) (mooi 'pretty, good-looking' and slim 'smart') are conventionally associated to one another ("the looks and the brains"). It is not by accident that both Bartsch \& Vennemann and Bale use many examples with similar adjectives (see (3) and (4a)); this type is also very easy to find on internet in all sorts of contexts

When looking at other examples and at the contexts in which they are used, one can find further evidence for the idea that there needs to be some kind of an association between the two properties in order to make the sentence felicitous. This association can be of various kinds. In the original COD-cases, for instance, antonymy seems to play a role in licensing the use of the RC structure, as illustrated by (13) (note that in this example the analytic form of the comparative is used).
(13) Do you see a rectangle, that is taller than it is narrow? That's what I see and that's what other people see when you are wearing a long dress.

In many cases context plays a crucial role. The examples in (14) illustrate some felicitous uses of the adjective zwaar 'heavy' which contrast with its infelicitous use in (2). In (14a) (source: internet), the adjectives (zwaar 'heavy' in the main clause and sappig en aromatisch 'juicy and aromatic' in the than-clause) are all used to characterize peaches as being delicious. In (14b) (source: internet), the adjectives smakelijk 'tasty' and zwaar 'heavy' are both typical characterizations of a meal.
(14) a. [We hebben de] laatste Hongaarse perzikken (sic) gekocht, 4 in 800 gram (en even sappig en aromatisch als ze zwaar zijn).
'We bought the last the last Hungarian peaches, 4 in 800 grams (and as juicy and aromatic as they are heavy).'
b. Gelukkig was het [eten] even smakelijk als het zwaar was.
'Luckily the meal was as tasty as it was heavy.'
The example in (14b) is interesting for an other reason as well. It falls in a class of examples in which the two adjectives give a positive and a negative qualification, and as such suggest that the positive property compensates for the negative one. Some more examples of this kind are given in (15) (source: internet):
(15) a. Exercise is far more invigorating than it is tiring.
b. [Een tweeling hebben] is minder zwaar dan het leuk is.
'Having twins is less difficult than it is fun.'
Besides these cases and the ones with antonyms, the two adjectives usually have the same connotation and polarity. In many cases, both properties could explain a certain situation, and the sentence evaluates the respective contribution of each property (see also Bale's example in (4b)):
(16) "Als de graaf een schelm en een schurk is, zou hij het Geschrift nooit aan zijn neef gegeven hebben!" zei Frans. "Of hij moet nog dommer zijn dan hij schurkachtig is." (Tonke Dragt, De zevensprong) "'If the count is a scoundrel and a villain [as you were saying], he would never give the Manuscript to his nephew!" said Frans. "Or he has to be even more stupid than he is villainous.""
Finally, there are some rare cases in which the adjective in the than-clause expresses a particularly salient property of its subject, as in (17), taken from a poem by Gaston Burssens. The use of the RC structure insists on the silence of the willows by comparing it to a contextually salient property that is known to hold to a high degree.
(17) De wilgen zijn nog stiller dan ze krom zijn
'The willows are even more silent than they are bent'
To conclude, subcomparatives with so called incommensurable adjectives fall into a much larger class of subcomparatives with a non absolute interpretation, which also includes the traditional cases of comparison of deviation. In some cases the non neutral reading these sentences have, may be obscured by a stylistic use of the structure, involving an ironic interpretation of the adjectives. These comparisons may contain all sorts of adjectives, but in order to have a felicitous result, the two adjectives need to be associated to one another. As the examples above show, there are various ways in which this association can be obtained.

## 3 Theoretical consequences

At this point it is clear that subcomparatives with 'incommensurable' adjectives are not excluded and thus a complete theory of comparatives has to be able to derive them. As indicated in the introduction, these sentences cannot be handled by a standard degree based approach, because these adjectives do not project comparable degrees on a single scale. Various authors [1], [8], [2], [3]) solve this problem by mapping the degrees to different objects that can be compared, as indicated above. On the other hand, one might want to say that this type of sentence offers evidence in favor of the vague predicate analysis, in which such a mapping is not necessary. In what follows I will discuss a number of possible accounts in the light of the empirical generalizations made in the previous section.

Bartsch and Vennemann [1] argue in their account of sentences such as (2) that these have to be treated on a par with COD cases. For them, a sentence such as (2) involves a scale on which specific and average values for beauty and intelligence ("specific and average BQ's and IQ's as they call them) can be assigned in such a way that these numerical values can be compared. The interpretation of the sentence amounts to a comparison of the deviations between the specific and the average values for beauty and intelligence respectively. For COD sentences involving dimensional adjectives, they make the same assumption. However, in this case the grammar can make use of measures, such as feet or centimeters, depending on where the speakers come from. Interestingly, this is the point at which their proposal makes a false prediction. As shown above, COD makes a comparison between the relative lengths of two differential extents and not between their absolute lengths. This is not expected in their proposal, as their analysis of the incommensurable cases is modeled on the existence of measurement systems.

Bale [2],[3] offers a detailed analysis of the mapping between degrees on ordinary scales to degrees on a universal scale. In his view, the only difference between cases such as (1) (absolute comparison, where two measures are compared in an absolute way) and (3) (relative comparison) is that the domain of individuals that has to be taken into account for sentences such as (1) contains measures (which he considers to be a special type of individuals). Given that sentences such as (1) normally have neutral interpretations (see [7] for discussion), Bale predicts RC sentences to have a neutral interpretation as well. As such he fails to account for the limited nature and the ironic effect of this type of interpretation that has been illustrated in (9)-(11) above. A further problem of the type of mapping Bale proposes (which I will not describe in detail here for reasons of space) is that he predicts a fine-graininess that is not justified by the data. Bale reconstructs the precise position of every degree on the universal scale from the relative position the individual occupies on the primary scale with respect to other values on that scale. He assumes that a value on the primary scale is mapped onto a fraction on the universal scale. This fraction corresponds to the position of the value (where the lowest value equals one and the highest value equals the total number of values) divided by the total number of values on the scale. This is problematic in two respects. On the one hand, RC does not require the amount of information about the domain that Bale's system needs, and on the other hand, the meaning of these sentences is not as clear-cut as he predicts. RC is a coarse-grained phenomenon. Take the interpretation of the equative in (24a). The sentence implies
that the peaches are both very juicy and aromatic and very heavy, and the use of a comparative rather than an equative would only be possible if for instance the peaches were extremely juicy and aromatic while being only slightly bigger than average. In this respect, a less constrained mapping, as proposed by Hamann, Nerbonne \& Pietsch [8] is to be preferred. However, as shown below, the coarse-grained nature of RC follows directly from an account of comparatives that takes the vague predicate analysis as a starting point.

In approaches to comparatives based on the vague predicate analysis, the meaning of RC cases (that is, including the original cases of COD) involves the use of degree functions such as quite, very and extremely (cf. [12]:130, [14]). A sentence such as (4c) would be analyzed as in (18), where $d$ could be quite, very or extremely.
(18) $\exists d[(d($ funny $))($ Ben $) \wedge \neg(d($ rich $))($ Steve $)]$

This captures the coarse-grained nature of RC , as these modifiers are vague themselves and only allow for a rough division of the domain. This is an advantage over degree based approaches, as these necessarily involve a mapping, and this mapping may be done in a very precise way. Also, the fact that we are (necessarily) dealing with a rough type of comparison seems to be at least part of the reason why the two adjectives in this structure need to be associated to one another. Consider again the equative in (24a). The only information the comparative conveys is that the peaches are very juicy and aromatic. The fact that they are heavy is already present in the context. However, by using the RC structure, the fact that all these properties add to the satisfaction of the person who bought the peaches is focused on. A further advantage of this type of approach is that it predicts the relative interpretation of COD-cases involving a dimensional adjective to be the only possible one, as the interpretation of expressions such as very and extremely varies with the standard. Finally, given that John is quite/ very/ extremely tall cannot be followed by the sequence \#but he is not tall, the use of these modifiers makes it in principle possible to derive the COD-type interpretation of RC.

This last point is more complex, however. When looking in more detail at the standard formalization of the comparative under the vague predicate analysis, as formulated by Klein, it turns out that this approach does not account for the COD-type of interpretation. Rather, Klein predicts the effect in (9) to apply across the board. The formalization in (19) only implies that the dog should be smart. As such, Klein fails to account for the asymmetry between positive and negative adjectives noted above.

## (19) $\exists d[(d($ smart $))($ the $\operatorname{dog}) \wedge \neg(d($ good-looking $))($ the dog $)]$

This problem is solved in a more constrained version of Klein's analysis as we proposed in [6] and [7]. In our view, Klein's analysis has to be restated in terms of a comparison between degree functions. The than-clause introduces in this case the maximally informative degree function $\delta$ that, if applied to the adjective in the thanclause results in a set including the subject of this adjective (this is the formalization used in [7]). The analysis of (4b) is given in (20), where $\delta 1>_{A} \delta 2$ iff $\delta 1(\mathrm{~A}) \subset \delta 2(\mathrm{~A})$.
(20) $\exists \delta 1\left[(\delta 1(\right.$ funny $))($ Ben $) \& \delta 1>_{A} \operatorname{MAX}_{\text {good-looking }}(\lambda \delta 2(\delta 2($ rich $))($ Steve $\left.))\right]$

In this analysis, the functions that can be used must be inherently ordered with respect to one another (which is a consequence of Klein's Consistency Principle), and we
assume that quite, very and extremely fulfill this requirement as well. As such, the sentence in (4b) states that if Steve is quite rich, Ben has to be very funny, or, alternatively, if Steve is very rich and Ben has to be extremely funny. This seems to be exactly what the sentence means. The analysis differs from Klein's original formalization by putting a much stronger constraint on the semantic contribution of the than-clause. As for the example in (9), the than-clause introduces the most restrictive set $\delta$ (mooi) containing the dog. As a consequence, the ironic reading of the sentence can be attributed to a stylistic effect that stretches up the domain for mooi 'good-looking' as to even include the ugly dog.

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# Distributivity in reciprocal sentences 

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#### Abstract

In virtually every semantic account of reciprocity it is assumed that reciprocal sentences are distributive. However, it turns out that the distributivity must be of very local nature since it shows no effect on the predicate or other arguments in reciprocal sentences. I present a semantic analysis of reciprocals that treats reciprocal sentences as distributive but captures the local nature of distributivity.


## 1 Introduction

Two meaning components are present in reciprocals. First, reciprocals express anaphoricity to a plural argument. Second, they specify that the causal relation holds between distinct parts of the plural argument. I call the first meaning component of reciprocal anaphoric condition, and the second component distinctness condition. In (1) the anaphoric condition ensures that the object has the same reference as the subject. The distinctness condition specifies how the relation of hating is satisfied. More concretely, (1) is only true if Morris hated Philip and Philip hated Morris.
(1) Morris and Philip hated each other.

It seems that in order to capture the distinctness condition of reciprocals we have to interpret the relation in reciprocal sentences distributively. That is, the relation hate in (1) does not hold of the plurality Morris and Philip itself, rather, it holds of distinct individuals forming this plurality. To account for the distinctness condition we thus need some way of ensuring distributive quantification in reciprocal sentences.

In this paper I am going to argue that the distributive quantification necessary for capturing the distinctness condition of reciprocals must have a very limited scope. In fact, it should scope only over the reciprocal itself, and exclude other arguments, as well as the verb. The observation is not new. It has already been made in Williams' response to Heim et al. (1991a). However, Williams himself notes this as a problem but does not propose a semantic analysis. Subsequent analyses of each other either ignored this problem, admitted that their account cannot deal with it or claimed that the problem is not real. I am going to argue against the last solution and propose a semantic analysis of reciprocals with a limited scope of distributivity. The analysis is possible if we combine the theory of reciprocity with Landman's analysis of distributivity limited to thematic roles (Landman, 2000).

The paper is organized as follows. In the next section I list three arguments that point to the very limited nature of distributive quantification in reciprocal sentences. In Section 3 I show that parallel arguments exist in case of cumulative quantification, which led Landman (2000) to postulate a novel type of distributivity. Building on his idea (albeit not his actual implementation) I show how the same approach can account for the behavior of reciprocals. Section 4 is the conclusion.

## 2 Data

At least three arguments point to the conclusion that distributivity in reciprocal sentences is very limited in its scope.

The first argument comes from reciprocal sentences of type DP-V-each other(P) D, that is, where another argument is present. Consider (2a). As noted in Williams (1991), Moltmann (1992), to get the interpretation 'each child giving a different present', the plural DP is preferred over the singular one, cf. the difference between (2a) and (2b) in this interpretation.
a. Two children gave each other a Christmas present.
?? under the reading 'each child giving a different present'
b. Two children gave each other Christmas presents. OK under the reading 'each child giving a different present'

There are two strategies how one builds distributivity into reciprocal sentences. One option (Dalrymple et al. 1998, Sabato and Winter 2005 among others) is to build distributivity into the meaning of reciprocals. The second option makes use of distributivity postulated independently of reciprocals (Heim et al. 1991b, Beck 2001, among others). I focus here on the first option and come to the second option at the end of this section.

In the first approach one assumes that reciprocals scope over relations and require, in its basic reading, that the extension of relation includes all pairs of non-identical individuals. In example (2a), the relation is ' $\lambda x \lambda y$. $x$ gave $y$ a Christmas present'. Since $x$ and $y$ are distinct individuals (2a) can mean that the first child gave one present to the second child and the second child gave another present to the first child. Thus, we derive as the default reading the reading which is dispreferred in (2a). Obviously, the problem would disappear if we ensured that a Christmas present is outside the scope of the reciprocal, hence each other would not distribute over it. However, it is unclear why indefinites should by default scope over reciprocals given that normally the inverse scope is a dispreferred option.

This is Williams' and Moltmann's argument why distributivity should be very local or absent in reciprocal sentences. Dalrymple et al. (1998) and Beck (2001) respond to this by claiming that the reading marked as '??' in (2a) is possible so there is nothing bad after all if we derive it. I think that this cannot be the end of story, though. Williams' point was not that the reading (2a) is
impossible, only that it is marked, roughly equally as the distributive reading of (3) is marked.

## (3) Two children gave Mary a Christmas present.

The distributive reading of (3) improves if we, for instance, substitute two children by both children, and the same holds for (2a). This intuition has also been confirmed in a questionnaire studies, see Dotlačil (2009). Suppose we derive the marked status of the distributive reading in (3) by assuming that numeral noun phrases do not distribute, unlike quantifiers. However, this solution would fail to extend to (2a) since here there is an independent source of distributivity, namely, the reciprocal itself, which gives rise to the dispreferred reading by default. Thus, contrary to Dalrymple et al. (1998) and Beck (2001) I believe that even if one accepts (2a) under the relevant reading, one still needs to explain why the reading seems somewhat marked, in a parallel fashion to (3), and accounts in which reciprocals freely distributes over a Christmas present lack the explanation. Notice that if each other distributed only very locally, we might be able to say that the marked status of (2a) has the same reason as the marked status of (3).

The second argument for the very local scope of distributivity comes from a cumulative quantification, studied by Scha (1981) and Krifka (1989), among many others. Its connection to reciprocity has been discussed in Sauerland (1998) and Sternefeld (1998). The problem can be shown on (2b) but since this involves complications due to the presence of bare plurals, I use two different examples. The first one is a variation on (2b), the second one is from the Corpus of Contemporary American English.
(4) a. Two children gave five presents to each other (in total).
b. Critics and defenders of the Catholic Church have been aligned against each other in two conflicting camps.

A possible reading of (4a) is that two children gave each other some presents, such that in total five presents were given. (4b) can mean that critics have been aligned against defenders and defenders against critics and in total there were two competing camps. Consider (4b) in more detail. No matter whether the reciprocal scopes below or above two conflicting camps we only get the reading that critics were aligned in two conflicting camps, and so were defenders, which is not the reading we want. In a nutshell the problem is as follows. (4a) and (4b) are cases of a cumulative quantification. Normally, we can derive the cumulative reading as a lack of distributive quantification if we assume that none of the arguments distributes over the others and all arguments are interpreted in their thematic positions (in line of Krifka 1989 and others since). However, this is incompatible with the account of each other which requires distributivity. The problem could be avoided if we had a system where each other does require distributivity, but distributivity is only very local, not affecting the interpretation of other arguments.

The third argument comes from the fact that reciprocal sentences can combine with collective predicates. This is shown in (5a), from Dimitriadis (2000), and (5b), from the Corpus of Contemporary American English.
(5) a. Bill and Peter, together, carried the piano across each others lawns.
b. Cooper and friends gather at each other's homes to perform tunes and ballads.

The problem is that in Dalrymple et al. (1998) and others, (5a) ends up meaning that Bill together carried the piano and so did Peter, which is nonsense. However, (5a) and (5b) can be interpreted. The problem would again be avoided if we ensured that the distributivity associated with each other does not scope over the adverb together in (5a) or the collective verb gather in (5b).

These are problems for Dalrymple et al. (1998) and Sabato and Winter (2005) but they are similarly problematic for accounts in which reciprocals make use of independently postulated distributivity. To see how these accounts work consider (6).
(6) Morris and Philip hated each other.

There is a long tradition of analyzing referring expressions (like coordinations of proper names in (6)) as possibly distributing over the predicate. Various alternative analyses of how to achieve this exist. Regardless of the option we choose we build the distinctness condition of each other upon the capability of the subject to distribute over the predicate (Roberts 1991, Heim et al. 1991b, Beck 2001, among others). In particular, we might interpret each other as follows (see Beck 2001):
(7) $\quad$ each other $\rrbracket=$ the other one(s) among $x$ different from $y$

Now, we let $x$ to be bound by the plural argument, antecedening the reciprocal, and $y$ to be bound by the distributive quantifier. In (6) we thus derive the reading which could be (somewhat clumsily) paraphrased as 'each of Morris and Philip hated the other one among Morris and Philip different from himself', that is, Morris hated Philip and Philip Morris. Since it is necessary that the antecedent of reciprocals distribute, we run again into the problem why (2a) is degraded under the indicated interpretation. We also cannot explain why (5a) and (5b) are possible. Finally, (4a) and (4b) are problematic. Since the subject has to distribute in these readings, we derive that, for instance, (4b) is interpreted as 'critics were aligned in two competing camps, and so were defenders' which is not the correct interpretation. ${ }^{1}$

To sum up, three arguments point to the conclusion that distributivity, necessary to capture the distinctness condition of reciprocals, applies only very locally. In the next section, I propose an analysis of these data.

[^80]
## 3 Distributivity and reciprocals

### 3.1 Background assumptions

I assume that the interpretive model includes $D_{e}$, the domain of individuals, and $D_{v}$, the domain of events. Both $D_{e}$ and $D_{v}$ are structures ordered by 'sum', $\oplus$ in such a way that $\left\langle D_{e}, \oplus\right\rangle$ is isomorphic to $\left\langle\wp\left(D_{e}\right)-\{\emptyset\}, \cup\right\rangle$, similarly for $D_{v}$. For more details, see Landman (1991). I furthermore assume that sentences are interpreted in neo-Davidsonian fashion. Verbs are predicates of events, and arguments are introduced through separate thematic roles. For example, ((8a)) is interpreted as (8b).
a. Burt and Greg kissed Clara and Lisa
b. $\quad(\exists e)(* \operatorname{kiss}(e) \wedge * A g(\operatorname{BURT} \oplus \operatorname{GREG})(e) \wedge * T h(\operatorname{ClARA} \oplus \operatorname{LISA})(e))$

Notice that, as is standard in event semantics (see Krifka 1989, Landman 2000, Kratzer 2003, among others), predicates and thematic roles are pluralized by $*$. * is defined below. It should be straightforward to see how we could extend $*$ to cumulate on relations of higher arity than 2 .

$$
\begin{array}{ll}
\text { a. } & * P x=1 \text { iff } P x=1 \text { or } x_{1} \oplus x_{2}=x \text { and } * P x_{1} \text { and } * P x_{2}  \tag{9}\\
\text { b. } & * R(x)(y)=\text { iff } R(x)(y)=1 \text { or } x_{1} \oplus x_{2}=x \text { and } y_{1} \oplus y_{2}=y \text { and } \\
& * R\left(x_{1}\right)\left(y_{1}\right) \text { and } * R\left(x_{2}\right)\left(y_{2}\right)
\end{array}
$$

Thus, the event $e$ is possibly a plural event that has subevents in which parts of the plurality Burt $\oplus$ Greg kissed parts of the plurality Clara $\oplus$ Lisa. This would be true, if, for example, $e$ consisted of subevents $e_{1}$ and $e_{2}$, where Burt kissed Clara in $e_{1}$ and Greg kissed Lisa in $e_{2}$. This is the so-called cumulative reading.

To arrive at (8b) compositionally, I make the following assumptions. First, thematic roles are introduced separately in the syntax. Since each thematic role is of type $\langle e,\langle v, t\rangle\rangle$ to combine them together we either need to assume some lift operator which lifts one thematic role so it can apply to the other or we can assume a special mode of composition, event identification (Kratzer, 2003). I am going to assume the latter here. For now it suffices to have the event identification combine type $\langle e,\langle v, t\rangle\rangle$ with $\langle v, t\rangle$. It should be easy to see how we can generalize event identification to arbitrary types that end in $\langle v, t\rangle$, which I do not do here for space reasons.

$$
\begin{equation*}
\text { Event identification: } \lambda x_{e} \lambda e_{v} \cdot R(x)(e)+\lambda e_{v} \cdot P(e)=\lambda x \lambda e . R(x)(e) \wedge P(e) \tag{10}
\end{equation*}
$$

Finally, we want generalized quantifiers to be interpretable in their thematic positions (see Krifka 1989). For that we assume LIFT:

$$
\begin{equation*}
\text { LIFT: } \lambda R_{\langle e,\langle v, t\rangle\rangle} \lambda Q_{\langle\langle e, t\rangle, t\rangle} \lambda e . Q(\lambda x . R(x)(e)) \tag{11}
\end{equation*}
$$

Now, it should be clear how we can derive the resulting meaning (8b) from the syntactic structure (12) in a stepwise fashion. To make this more visible, I notate denotations of non-terminal nodes.


In the next section, I want to discuss more complicated cases in which cumulative readings intertwine with distributive readings, which will form the key insight for understanding what is going on in reciprocal sentences.

### 3.2 Distributivity in cumulative readings

Consider the following sentence, from Landman (2000).
Three boys gave six girls two flowers.
I am going to assume exactly-interpretation of each numeral argument, so the sentence could be paraphrased as 'exactly three boys gave exactly six girls exactly two flowers'.

It turns out that (13) can be true if there are three boys and six girls and each boy gave flowers to some of the six girls and each girl received flowers from some of the three boys, and six girls in total received two flowers each. The problem with this reading is that six girls distributes over two flowers (so, each girls ends up having two flowers) but three boys and six girls are interpreted cumulatively, that is, neither of these arguments distributes over the other argument. For more discussion and more examples showing the same point, see Roberts (1990), Schein (1993), Landman (2000) and Kratzer (2003). To account for this reading, we need to allow the object to distribute. However, we need to allow it to distribute only very locally, over the theme argument, and excluding the subject. The analysis of this is proposed in Landman (2000). However, I am going to differ from his approach because it is not clear how it could be extended to reciprocals.

The basic idea is that we let some thematic roles be related not to the event $e$ but to some subevent $e^{\prime}$. Thus, we assume a null operator which optionally applies to a thematic role and requires it to relate to $e^{\prime}$, a subevent of $e$ :

$$
\begin{equation*}
\text { The operator making a thematic role related to the subevent } e^{\prime} \tag{14}
\end{equation*}
$$ $\lambda R_{\langle e,\langle v, t\rangle\rangle} \lambda x \lambda e^{\prime} \lambda e . R(x)\left(e^{\prime}\right) \wedge e^{\prime} \leq e$

We can then distribute only over $e^{\prime}$ and exclude distribution over the whole event $e$. For instance, in (13) we require that the theme and goal arguments are not related to $e$ but to $e^{\prime}$, a subevent of $e$. Thus, when the goal and theme thematic roles combine we have the following function:

$$
\begin{equation*}
\lambda x \lambda e^{\prime} \lambda e . * G o(x)\left(e^{\prime}\right) \wedge * T h(2 \text { flowers })\left(e^{\prime}\right) \wedge e^{\prime} \leq e \tag{15}
\end{equation*}
$$

To let the goal argument distribute over the theme argument it suffices to allow cumulation of (=the application of $*$ to) the first two arguments of this function. I notate the distributive operator which enables this as $D$. The $D$ is defined as:

$$
\begin{equation*}
D\left(Q_{\langle e,\langle v,\langle v, t\rangle\rangle\rangle}\right)=\lambda x \lambda e . *\left(\lambda y \lambda e^{\prime} . Q(y)\left(e^{\prime}\right)(e)\right)(x)(e) \tag{16}
\end{equation*}
$$

We cumulate on the first two arguments of $Q$. Thus, $x$ and $e$ can be split into parts, for instance, $x_{1}, x_{2}$ and $e_{1}, e_{2}$ and $x_{1}, e_{1}$ satisfies $\lambda y \lambda e^{\prime} . Q(y)\left(e^{\prime}\right)(e)$, and the same for $x_{2}, e_{2}$. To see what $D$ is doing consider the example above. $D$ applies to (15) which derives the following:

$$
\begin{equation*}
\lambda x \lambda e . *\left(\lambda y \lambda e^{\prime} . * G o(y)\left(e^{\prime}\right) \wedge * T h(2 \text { flowers })\left(e^{\prime}\right) \wedge e^{\prime} \leq e\right)(x)(e) \tag{17}
\end{equation*}
$$

If six girls applies to (17) (by LIFT) we derive that six girls and $e$ can be split into parts, and we can pair up the parts of the nominal argument with the parts of the event such that each pair satisfies the following function:

$$
\begin{equation*}
\lambda y \lambda e^{\prime} . * G o(y)\left(e^{\prime}\right) \wedge * T h(2 \text { flowers })\left(e^{\prime}\right) \wedge e^{\prime} \leq e \tag{18}
\end{equation*}
$$

This is true if, for instance, there are six subevents of $e$ and every girl is the goal argument of one of the subevents and for each of the subevents there are two flowers that are the theme argument. Since the theme argument is in scope of $D$ the goal argument distributes over it. However, the goal argument does not distribute over the subject since we make the distribution apply only very locally, over thematic roles that are related to subevents. For more details on the compositional analysis and more discussion, see Dotlačil (2009).

### 3.3 Reciprocal sentences

We have seen that distributivity in reciprocal sentences should be limited in scope. Thus, the same strategy which allows us to combine distributive and cumulative readings in one clause should be used for reciprocals. Consider the sentence Morris and Philip hated each other. We let the agent and theme be related to the subevent $e^{\prime}$. The two thematic roles combine and give us (19). (19) is parallel to previous cases where thematic roles were related to subevents, the only difference is that now we abstract over the theme argument.

$$
\begin{equation*}
\lambda x \lambda y \lambda e^{\prime} \lambda e . * A g(x)\left(e^{\prime}\right) \wedge * T h(y)\left(e^{\prime}\right) \wedge * \operatorname{hate}(e) \tag{19}
\end{equation*}
$$

We need to let each other apply to this function and express that it holds for distinct parts of a plural argument. We assume the following interpretation:

$$
\begin{align*}
& \llbracket \text { each other } \rrbracket=\lambda Q \lambda x \lambda e . *\left(\lambda y \lambda z \lambda e^{\prime} \cdot Q(y)(z)\left(e^{\prime}\right)(e) \wedge\right.  \tag{20}\\
& \wedge \operatorname{distinct}(y)(z))(x)(x)(e)
\end{align*}
$$

In standard accounts like Dalrymple et al. (1998), reciprocals take a relation as its argument and require that $y, z$, parts of the plural argument $x$, which apply to the relation are distinct. The account here is somewhat similar but instead of letting each other apply to the relation it applies to $Q$, the relation of arity 4: this relates two individual arguments and two events. $Q$ can be built up by letting thematic roles relate to the subevent $e^{\prime}$ and abstracting over the object argument of the relation. Thus, each other can apply to (19). Notice that I leave it open how the distinctness itself should be understood. For the purposes of this paper, assume that it is equivalent to non-overlap.

Letting each other apply to (19) and to the subject Morris and Philip we get the representation which is true if the plurality Morris and Philip can be split into parts, such that one part hates the other part and the parts are distinct. This is what we want. The resulting interpretation is shown in (21)

$$
\begin{equation*}
\lambda e . *\binom{\lambda y \lambda z \lambda e^{\prime} . * \operatorname{Ag}(y)\left(e^{\prime}\right) \wedge * T h(z)\left(e^{\prime}\right) \wedge}{\wedge * \operatorname{hate}(e) \wedge \operatorname{distinct}(y)(z)}(\mathrm{m} \oplus \mathrm{p})(\mathrm{m} \oplus \mathrm{p})(e) \tag{21}
\end{equation*}
$$

Consider now (22), repeated from above. As we have discussed in Section 2, the indefinite is preferably not interpreted distributively.
(22) Two children gave each other a Christmas present.
?? under the reading 'each child giving a different present'
We let the agent and goal be related to subevents, which gives us:

$$
\begin{equation*}
\lambda x \lambda y \lambda e^{\prime} \lambda e . * \operatorname{Ag}(x)\left(e^{\prime}\right) \wedge * G o(y)\left(e^{\prime}\right) \wedge * \operatorname{give}(e) \wedge * T h(\text { a present })(e) \tag{23}
\end{equation*}
$$

If we let each other apply to (23) and to the subject two children we get:

$$
\begin{equation*}
\lambda e . *\binom{\lambda y \lambda z \lambda e^{\prime} . * \operatorname{Ag}(y)\left(e^{\prime}\right) \wedge * G o(z)\left(e^{\prime}\right) \wedge * \operatorname{give}(e) \wedge}{\wedge * \operatorname{Th}(\text { a present })(e) \wedge \operatorname{distinct}(y)(z)}(2 \text { kids })(2 \text { kids })(e) \tag{24}
\end{equation*}
$$

Notice that even though a present is in scope of $*$ and thus, one might think, could be interpreted as varying with respect to each child, it does not. The reason is that unlike the agent and goal argument, the theme argument is related to the event $e$. Therefore, (24) is true if one child gave another child a present, and the other child gave the first child a present, and in total one present was exchanged. Thus, unlike every single analysis of reciprocals I know of (with the exception of Moltmann 1992) we do not derive the distributive reading as the default one. We can still derive the distributive reading if we assume that the theme argument is also related to the subevent $e^{\prime}$. However, notice that this requires an extra operation, namely modification of the theme thematic role. It is likely that this extra operation makes the particular reading less likely. As we have seen above, it is also dispreferred to interpret two children gave Mary a Christmas present with Christmas presents varying for each kid. Here again, the dispreferred interpretation only follows if we let the theme argument be related to the subevent and the subject distribute over it. If these optional operations
are dispreferred in this case we expect them to be dispreferred in (22) as well. Thus, unlike previous accounts, we correctly capture the parallelism between distributivity in reciprocal and non-reciprocal sentences.

It should be clear that we can also derive the reading of Two children gave five presents to each other (in total) in which two children gave each other some presents, such that in total five presents were given. This reading is in fact captured in the representation (24), the only difference is that 'a present' is substituted by 'five presents'. Finally, let me come back to reciprocal sentences with collective predicates, like (25), repeated from above:

Cooper and friends gather at each other's homes to perform tunes and ballads.

What we derive as the interpretation of (25), disregarding the infinitival clause, is the following:

$$
\begin{equation*}
\lambda e . *\binom{\lambda y \lambda z \lambda e^{\prime} . * A g(y)\left(e^{\prime}\right) \wedge * T h(\text { house of } z)\left(e^{\prime}\right) \wedge}{\wedge * \operatorname{gather}(e) \wedge \operatorname{distinct}(y)(z)}(\mathrm{C} \oplus \mathrm{fr} .)(\mathrm{C} \oplus \mathrm{fr} .)(e) \tag{26}
\end{equation*}
$$

(26) is true if, for instance, each friend is the agent of gathering at his friends' homes. One might find this a non-sensical interpretation since it seems strange that a single person could be the agent of gathering. However, it has been argued in the work of Dowty and Brisson (see Brisson 2003 and references therein) that the agent of collective predicates like gather needs to satisfy only some general requirements that gathering might impose (getting to some particular place, for instance) and does not need to "undergo gathering" himself. This enables (26) to have a possible interpretation. We furthermore expect that collective predicates which do not have such unspecific requirements on their agents should not combine with reciprocals. One test to distinguish the two types of collective predicates is using the quantifier headed by all, see the difference in (27):
a. All the boys gathered in the hall.
b. * All the boys outnumbered the girls.

It turns out that collective predicates of the latter type cannot appear in reciprocal sentences either. For example, The boys in our class outnumber each other's families is uninterpretable. We expect this since reciprocals should only combine with collective predicates whose agents can be atomic individuals.

## 4 Conclusion

In order to accommodate the distinctness condition of each other we need to assume that reciprocal sentences include some sort of distributivity. I have shown that this distributivity is very local and has no effect on the predicate or other arguments in reciprocal sentences. This can be accommodated by using a very local version of distributivity which operates only between thematic roles hosting the reciprocal and its antecedent. The analysis gives an independent support to distributivity which does not scope over the whole clause but only over selected arguments.

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# A Logic for Easy Linking Semantics 

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#### Abstract

Most semantic frameworks assume that the denotations of verbs expect their arguments in a certain specific order. In fixed word order languages, hence, we could say that order codes case marking. Moreover, all syntax-semantic mappings have to provide a solution for the fact that DPs can denote individual concepts of (extensional) type $e$ as well as generalized quantifiers ( $\langle\langle e, t\rangle, t\rangle$ ). The paper presents a new variant of type logic which offers a lean syntax-semantics interface for semantic representation in a Montagovian format. Specifically, the syntax-semantics mapping does not require obligatory quantifier raising (as Heim+Kratzer, 1998) and does not force the semanticist to make claims about a fixed underlying order of arguments of the verb. The latter feature will facilitate semantic research on free word order languages and semantic research on languages where no syntactic analysis in a Minimalist framework is as yet available.


## 1 Linking: Troubles and a Vision

Which syntax feeds semantics? In the present paper, I want to address the syntax-semantics interface from the back end, so to speak, and propose a new logical backbone for semantics, one that is better suited to host syntax. I should stress that this is a service article. I will not criticize, defend or propose any linguistic analysis but want to present a linking formalism that is easy to handle and can be adapted for a wide range of potential semantic analyses. Nevertheless, my work was inspired by linguistic questions which I will briefly review.

Type mismatch problem: It is a common assumption that verbs denote relations between entities. We can use names, indexicals or definite NPs to refer to entities. Moreover, we can use DPs that denote quantifiers over entities. In that case, a type mismatch between verb argument and DP denotation has to be resolved. While some theories endorse the assumption that verbs denote relations between generalized quantifiers, most people prefer to retain the original logical type of verbs. For these, Heim + Kratzer (1998) develop the by now standard way to resolve the type mismatch between verb and quantifiers. They propose an analysis where quantifier raising, coindexing and the interpretation of traces as variables serves, not only to settle matters of scope, but also as the standard way to enable semantic composition of verb projection and quantificational DP. Hence, the type mismatch problem is considered as solved by many semanticists. However, the semantic composition of even a simple sentence like John likes most Fellini movies requires quantifier raising, interpreted traces, coindexing, and lambda abstraction.

Order codes argument structure: Standard semantic treatments of English and other languages assume a fixed (underlying) order of arguments of the verb. Word order, rather than case marking, is the factor that ensures that each DP or PP instantiates the correct argument place of the verb. According to this standard analysis, free word order languages where argument structure is exclusively determined by case marking should not exist. If a language is suspected to be of that type (see Haug, 2009 on Ancient Greek), or if a language is not as yet sufficiently well understood to make claims about word order, semantic analysis requires to stipulate a basic order of verbal arguments. This common feature of truth conditional semantics in the Montagovian format can even lead scholars to adopt other semantic frameworks which allow for

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a more direct impact of case marking in semantic interpretation. Hence, Montagovian semantics with interpreted case marking should be an attractive generalization of the standard framework.

The tacit argument problem: Many analyses propose that the verb has arguments that are not instantiated by overt phrases in the sentence. One example is provided in recent papers on tense by von Stechow (von Stechow et al., 2009). His analysis rests on a tense argument of the verb. In order to instantiate this argument in matrix clauses, he has to assume that there is a tacit temporal PRO, used as a dummy syntactic object that figures in quantifier raising. PRO leaves a trace which is interpreted as a time variable and instantiates the temporal argument of verbs. PRO is not a generalized quantifier, so it can not initiate lambda abstraction. In nonembedded sentences, von Stechow has to assume that PRO passes its index to an independent lambda operator and gets deleted afterwards. While Minimalist syntax allows to delete noninterpretable material, the entire process looks like an artifact of a specific kind of theory rather than an insight about the logical structure of language.

The event problem: In a standard Davidsonian analysis, event modifiers can apply to the event argument of the verb at many levels in syntax. In the standard fixed word order paradigm, we have to make a claim whether the event argument should be the first, or the second, etc. or the last argument of the verb. There is no agreed answer to this question and authors tend to avoid any principled position. I will discuss two possible options here.

Solution 1: We could claim that the event is an early argument of the verb such that, for instance, love denotes $\lambda e \lambda y \lambda x \operatorname{LOVE}(x, y, e)$. $\lambda e$ gets instantiated by the trace $x_{e}$ of an uninterpretable dummy E-PRO. E-PRO is co-indexed with $x_{e}$ and has to be raised to all positions immediately below an event modifier MOD. In that position, it has to pass its index to an independent lambda operator that makes $x_{e}$ accessible. After combination of MOD and verb projection, another trace of PRO instantiates the event argument of the verb, thereby making the argument inert until needed the next time. (Note: if there is more than one event modifier in a sentence, we will need a chain of traces of PRO).

Solution 2: We could alternatively claim that the event is a late argument of the verb, and our example verb love denotes $\lambda y \lambda x \lambda e \operatorname{LOVE}(x, y, e)$. If an event modifier wants to combine with the verb before the verb has met all its DP arguments, the modifier has to use some standard procedure to instantiate the innermost argument of an n-place relation and to reopen all other arguments after modification. Such modes of combination can certainly be defined. Still, the resulting analysis again carries the flavor of repairing theory-internal problems rather than offering insights about the logical structure of language.

It should be pointed out that Kratzer (2002/unpublished) might offer a solution: She assumes that each quantificational DP binds the (currently open) event argument with an existential quantifier, and at the same time introduces a new, plural event argument that remains accessible and consists of the sum of all smaller events. Following this proposal, a sentence like Sally fed all chicken in one hour then means $\exists E \forall x(\operatorname{Chicken}(x) \rightarrow \exists e F e e d(\operatorname{Sally}, x, e) \wedge e \subset E) \wedge \tau(E)=$ 1 hour) (ignoring further minimality requirements on events). Her analysis is motivated by the observation that different event modifiers can take scope below and above nominal quantifiers in one and the same sentence. Yet, the event problem originally is not a scope problem. If we want to generalize Kratzer's solution to a mechanism where the event parameter is accessible at each syntactic level, we'd have to claim that any DP (including definite noun phrases, proper names and other non-scope-taking DPs) existentially binds the event argument of the verb, combines with the verb, and afterwards introduces a new plural event that has the existentially bound first event as its part. Hence, a sentence like Sally fed Prillan will receive the following interpretation (again, leaving minimality conditions on E aside): $\exists E(\exists e(F e e d(S a l l y$, Prillan,$e) \wedge e \subset E))$ Even though this may not be wrong in a strictly logical sense, it is at least redundant. Event semantics
would loose much of its original appeal: Events should make semantic representations elegant and perspicuous, and not redundant and unperspicuous.

In this paper, I will define Linking Logic, a type logic on finite variable assignments, and Easy Linking Logic which endorses variables that are indexed with abstract case labels. This will allow us to design Easy Linking Semantics, a format for semantic analysis and composition that is independent of any specific grammatical framework and yet draws on earlier Montagovian semantics in a maximally conservative manner.

## 2 Linking Logic

In this section, I want to define a type logic which operates on partial variable assignments. ${ }^{1}$ All terms $t$ and formula $\phi$ are interpreted relative to models $M$ and variable assignments $g$. Unlike normal logics, however, the interpretation will only be defined for variable assignment functions which have the free variables of $t$ or $\phi$ as their domain. No formula can be evaluated relative to an assignment which is too "rich". As a consequence, variable binding will not always lead to interpretable formula. E.g. $\exists x \phi$ will only be interpretable if $x$ occurs free in $\phi$. These properties are not desired or desirable in logics for mathematics and philosophy in general, perhaps. However, they reflect deep insights about natural language interpretation. For example, the ban on vacuous quantification has been proposed as a principle at LF. My analysis implements this ban at an even deeper level in the logical backbone of semantic analysis.

Following standard semantic practice, I will use the atomic types $e, s, t$ in the sample system. Simpler and richer systems are possible.

## Types:

- $e, s, t$ are atomic types.
- If $\sigma$ and $\tau$ are types, then $\langle\sigma, \tau\rangle$ is a type.
- Nothing else is a type.

A type logical syntax: A type logic language $L$ on basis of these types consists of a set of constants for each type $\tau$, and a set of variables for each type $\tau$. In parallel, I will define the function $f r$ that maps any term to the set of free variables that occur in that term. The terms in $L$ are defined as follows:

- For each type $\tau$, any constant $c$ of type $\tau$ is a term of type $\tau$. The set of free variables fr $(c):=\emptyset$.
- For each type $\tau$, any variable $v_{i}$ of type $\tau$ is a term of type $\tau$. The set of free variables $f r\left(v_{i}\right):=\left\{v_{i}\right\}$.
- If $A$ is a term of type $\langle\sigma, \tau\rangle$ and $B$ is a term of type $\sigma$, then $A(B)$ is a term of type $\tau$. The set of free variables $f r(A(B)):=f r(A) \cup f r(B)$.
- Logical connectives on type $t$ : If $\phi$ and $\psi$ are of type $t$, then $\phi \wedge \psi, \phi \vee \psi, \phi \rightarrow \psi$ and $\neg \phi$ are terms of type $t$. The free variables are defined as follows: $\operatorname{fr}(\neg \phi):=\operatorname{fr}(\phi)$, and $f r(\phi \wedge \psi)=f r(\phi \vee \psi)=f r(\phi \rightarrow \psi)=f r(\phi) \cup f r(\psi)$ -
- If $\phi$ is a term of type $\tau$, and if $f r(\phi)$ contains variable $v_{i}$ of type $\sigma$ then $\lambda v_{i} \cdot \phi$ is a term of type $\langle\sigma, \tau\rangle$. The set of free variables $\operatorname{fr}\left(\lambda v_{i} \cdot \phi\right):=\operatorname{fr}(\phi)-\left\{v_{i}\right\}$.

[^81]
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The present system does not introduce syncategorematic quantification as an operation on type $t$ terms. Quantificational expressions can enter the system at the usual places: Determiners relate two sets and denote entities of type $\langle\langle e, t\rangle,\langle\langle e, t\rangle, t\rangle$; the denotations of determiner phrases have the type of generalized quantifiers $\langle\langle e, t\rangle, t\rangle$ and the normal universal and existential quantifiers $\forall, \exists$ will be defined as specific generalized quantifiers below. We will now turn to interpretation. In the following, I will use the notation $\left.g\right|_{A}$ for the partial function $g *$ which arises by restricting $g$ to domain $A$. Hence, $\left.g\right|_{f r(\phi)}$ stands for $g$, restricted to the free variables in term $\phi$.

Interpretation: Let $D_{e}, D_{s}$ be domains of entities and worlds, and let $D_{t}:=\{0,1\}$ as usual. Let $D_{\langle\sigma, \tau\rangle}:=\left\{f \mid f: D_{\sigma} \rightarrow D_{\tau}\right\}$ the respective functional domains, and use $\mathbf{D}$ to refer to this hierarchy of sets. Let moreover $I$ be a function which maps all constants of type $\tau$ into $D_{\tau}$. The type logical language $L$ is interpreted relative to the model $M=\langle\mathbf{D}, \mathbf{I}\rangle$ and partial variable assignments $g$ from Var into $\mathbf{D}$. Specifically, the interpretation of any term $\phi$ will only be defined for assignments $g$ such that $\operatorname{dom}(g)=f r(\phi)$. As before, $\emptyset$ is used for the empty variable assignment.

- Let $c$ be a constant of type $\tau .\|c\|^{M, \emptyset}:=I(c)$.
- Let $v_{i}$ be a variable of type $\tau$. Let $g$ be an assignment which is defined on $f r\left(v_{i}\right):=\left\{v_{i}\right\}$. Then $\left\|v_{i}\right\|^{M, g}:=g\left(v_{i}\right)$.
- Let $A$ be term of type $\langle\sigma, \tau\rangle$ and $B$ a term of type $\sigma$. Let $g$ be a variable assigment with $\operatorname{dom}(g)=f r(A(B))=f r(A) \cup f r(B)$. Then $\|A(B)\|^{M, g}:=\|A\|^{M, g_{1}}\left(\|B\|^{M, g_{2}}\right)$ where $g_{1}:=$ $g$ restricted to $f r(A)$ and $g_{2}=g$ restricted to $f r(B)$.
- Logical connectives on type $t$ : Let $\phi$ and $\psi$ be of type $t$. Let moreover $g$ any assignment with $\operatorname{dom}(g)=f r(\phi) \cup f r(\psi)$.
$\|\phi \wedge \psi\|^{M, g}=1$ iff $\|\phi\|^{M, g_{1}}=1$ and $\|\psi\|^{M, g_{2}}=1$.
$\|\phi \vee \psi\|^{M, g}=1$ iff $\|\phi\|^{M, g_{1}}=1$ or $\|\psi\|^{M, g_{2}}=1$.
$\|\phi \rightarrow \psi\|^{M, g}=1$ iff $\|\phi\|^{M, g_{1}}=0$ or $\|\psi\|^{M, g_{2}}=1$.
$\|\neg \phi\|^{M, g_{1}}=1$ iff $\|\phi\|^{M, g_{1}}=0$
In all cases, $g_{1}:=\left.g\right|_{f r(\phi)}$ and $g_{2}:=\left.g\right|_{f r(\psi)}$.
- If $\phi$ is a term of type $\tau$, and if $f r(\phi)$ contains variable $v_{i}$ of type $\sigma$ then $\lambda v_{i} . \phi$ is a term of type $\langle\sigma, \tau\rangle$. Let $g$ be an assignment with $\operatorname{dom}(g)=\operatorname{fr}(\phi)-\left\{v_{i}\right\}$. Then $\left\|\lambda v_{i} \cdot \phi\right\|^{M, g}:=$ the function which maps all $m \in D_{\sigma}$ to $\|\phi\|^{M, g^{\prime}}$ where $g^{\prime}:=g \cup\left\{\left\langle v_{i}, m\right\rangle\right\}$.

This concludes the definition of a type logical language with sparse assignments. Any term in $L$ can exclusively be interpreted with respect to variable assignments that run exactly on the free variables of the term. While this may look like a restriction at first sight, the system covers all and exactly the functions served by variable assignments elsewhere. The mayor difference between sparse assignment logics and classical logics arises already in the definitions of well-formed terms. Whereas classical logics allow for vacuous binding, the use of $\lambda$-abstraction is restricted to terms where the bound variable actually occurs free in the term. Let $\phi$ be a term of type $t$ and let the variable $v_{i}$ be in $f r(\phi)$. Then we will use the following abbreviations:

$$
\begin{aligned}
& \exists v_{i} \phi:=\neg\left(\lambda v_{i} \cdot \phi=\lambda v \cdot \neg(v=v)\right) \\
& \forall v_{i} \phi:=\lambda v_{i} \phi=\lambda v \cdot v=v
\end{aligned}
$$

The two quantifiers inherit the ban on vacuous binding from $\lambda$-abstraction. Apart from that, they have the usual truth conditions. Let us check this for the existential quantifier $\exists v_{i} \phi$. We know that $v_{i} \in f r(\phi)$ and $f r\left(\exists v_{i} \phi\right)=f r(\phi)-\left\{v_{i}\right\}$. Given a model $M$ and assignment $g$ which is defined on $\operatorname{fr}(\phi)-\left\{v_{i}\right\},\left\|\exists v_{i} \phi\right\|^{M, g}=1$ iff there is an extension $g *=g \cup\left\{\left\langle v_{i}, m\right\rangle\right\}$ such that
$\|\phi\|^{M, g *}=1$. Note that $\phi$ is defined for assignment $g *$ because we assumed that $v_{i}$ is free in $\phi$.
Another operator that will be used later is the subset relation $\subset$ of type $\langle\langle e, t\rangle,\langle\langle e, t\rangle, t\rangle\rangle$. If $A, B$ are terms of type $\langle e, t\rangle$, then $\|A \subset B\|^{M, g}$ is defined for all $g$ with $\operatorname{dom}(g)=\operatorname{fr}(A) \cup \operatorname{fr}(B)$.
$\|A \subset B\|^{M, g}=1$ iff $\|A\|^{M,\left.g\right|_{f r(A)}}$ is the characteristic function of a set $A^{\prime}$ in $M,\|B\|^{M,\left.g\right|_{f r(B)}}$ is the characteristic function of a set $B^{\prime}$ in $M$ and $A^{\prime} \subset B^{\prime}$.
This might be a good place to illustrate that bound variables do not have any influence on the meaning of terms. Consider the terms $\lambda v_{2} \cdot M A N\left(v_{2}\right)$ and $\lambda v_{g} . W A L K\left(v_{g}\right)$.

$$
\left\|\lambda v_{\mathcal{Z}} \cdot M A N\left(v_{2}\right) \subset \lambda v_{g} \cdot W A L K\left(v_{g}\right)\right\|^{M, g}=1 \mathrm{iff}
$$

$\left\|\lambda v_{2} \cdot M A N\left(v_{2}\right)\right\|^{M, g} \subset\left\|\lambda v_{g} . W A L K\left(v_{g}\right)\right\|^{M, g}$, that is iff
the set $M A N$ with the characteristic function $\left\|\lambda v_{2} \cdot M A N\left(v_{2}\right)\right\|^{M, g}$ is a subset of the set $W A L K$ with the characteristic function $\left\|\lambda v_{g} . W A L K\left(v_{g}\right)\right\|^{M, g}$.

Although the computation of the two latter characteristic functions operates via $v_{2}$ and $v_{g}$, the same functions would result if we execute the computation via any other variable. Generally, bound variables can be renamed like in classical logics (i.e. taking care that the new variable isn't one bound by an operator inside the scope of the original binding operator). We can hence freely use renaming of variables, for instance in order to graphically distinguish saturated arguments from open arguments of the verb.

## 3 Easy Linking Semantics

In what follows, I will use an Easy Linking Logic $L_{\text {link }}$ which deviates from the systems above in its variables of type $e$. Apart from ordinary variables, we will use variables with abstract case labels like nom, acc, dat, gen. These include labels for prepositional cases like by, for, to, with. We will also assume that if the same preposition can be used with different thematic roles, and combines with the same verb twice, it will count as two different labels. Hence, with ${ }_{1}$ in with great care counts as a different abstract prepositional case than the with ${ }_{2}$ in with a hammer in the following sentence.

## (1) With great care, Joan opened the box with a hammer.

Finally, I propose to use the labels $t$, $p l$, $e$ for times, place and events. Hence, Var $=$ $\left\{v_{n o m}, v_{a c c}, v_{d a t}, \ldots, e, t, p l, v_{1}, v_{2}, v_{3}, \ldots\right\}$. The exact choice of labels can be adapted if necessary. Likewise, we can assume that the linking logic $L_{\text {link }}$ has more abstract case indices than we actually want to use of some specific semantic analysis. As before, formulae in $L_{\text {link }}$ will be interpreted in suitable models $M$ relative to finite assignments $g$.

What is the meaning of a verb in Easy Linking Semantics? I assume that the "conceptual" content of verbs in English should be captured in a variable-independent way as an $n$-place relation between objects, events, and worlds as usual. Hence, we will use conceptual denotations of verbs like the following:

```
\([[s t a b]]^{c}=\|\lambda x \lambda y \lambda e \lambda w \cdot \operatorname{STAB}(x, y, e, w)\|^{M}\)
\([[b u y]]^{c}=\|\lambda x \lambda y \lambda z \lambda e \lambda w \cdot B U Y(x, y, z, e, w)\|^{M}\)
\([[\text { sell }]]^{c}=\|\lambda x \lambda y \lambda z \lambda e \lambda w \cdot \operatorname{SELL}(x, y, z, e, w)\|^{M}\)
\([[k i s s]]^{c}=\|\lambda x \lambda y \lambda e \lambda w \cdot \operatorname{KISS}(x, y, e, w)\|^{M}\)
\([[\text { rain }]]^{c}=\|\lambda e \lambda w \cdot R A I N(e, w)\|^{M}\)
```


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These denotations can be viewed as conceptual values of English as well as German, Dutch, Russian or Japanese verbs, and they are not committed to any syntax-semantics interface. For the sake of illustration, I decided to use the Davidsonian format with an event argument for the verb. This is not what Beaver \& Condoravdi propose, but Easy Linking Semantics is particularly attractive if you want to use events.

When verbs enter into the composition of a sentence, they change to their linking semantics. Each verbal argument is instantiated with a variable which carries the abstract case label that corresponds to the phrase that realizes this argument in sentences. Event and world argument will likewise be instantiated by specific event- and world variables. The following examples illustrate the step. I use [[...]] for the linking semantics of words in English, whereas \|...\| evaluates terms in $L_{\text {link }}$ in a model $M$.

$$
\begin{aligned}
& {[[\text { stab }]] \longrightarrow\left\|S T A B\left(v_{n o m}, v_{a c c}, e, w\right)\right\|^{M}} \\
& {[[\text { buy }]] \longrightarrow\left\|B U Y\left(v_{n o m}, v_{a c c}, v_{\text {from }}, e, w\right)\right\|^{M}} \\
& {[[\text { sell }]] \longrightarrow\left\|S E L L\left(v_{n o m}, v_{a c c}, v_{t o}, e, w\right)\right\|^{M}} \\
& {[[\text { kiss }]] \longrightarrow\left\|K I S S\left(v_{n o m}, v_{a c c}, e, w\right)\right\|^{M}} \\
& {[[\text { rain }]] \longrightarrow\|R A I N(e, w)\|^{M}}
\end{aligned}
$$

These $L_{\text {link }}$ terms each denote a set of partial assignments from variables with case labels into the model domain $M$. In using variables, I make the syntax look as similar to traditional logic as possible. In using variables with case indices, I endorse Beaver \& Condoravdi's proposal that linking should be part of the semantic value of verbs rather than part of a trace mechanism at the syntax-semantics interface.

### 3.1 Saturation of arguments

We will assume that DPs carry their abstract case as a syntactic feature. These cases will enter the semantic composition; hence the denotation of $D P_{\text {case }}$ is a tuple which consists of generalized quantifier (the same as in classical semantics) and its case label. In a sentence like the following, the subject DP Ann hence is interpreted as $\langle\lambda P . P(A N N)$, nom $\rangle$.

## (2) Ann coughed

Generally, a DP combines with a sister constituent XP as follows:

$$
\begin{aligned}
& {\left[\left[\mathrm{DP}_{\text {case }} \mathrm{XP}\right]\right]=\langle[[\mathrm{DP}]], \text { case }\rangle \oplus[[\mathrm{XP}]]} \\
& =[[\mathrm{DP}]]\left(\lambda v_{\text {case }} \cdot \psi\right) \text { where } \psi \text { is an } L_{\text {link }} \text { term that codes the denotation of XP: }[[\text { XP }]]= \\
& \|\psi\|^{M} .
\end{aligned}
$$

Note that this definition does not depend on any specific term that is used to represent the meaning of XP. It can be shown that for any two terms $\Psi_{1}, \Psi_{2}$ which both code the meaning of XP, the result of the above lambda-abstraction is identical for both terms. The crucial insight is that all ways to code the meaning of XP must coincide in their free variables, and these always have to contain $v_{\text {case }}$. Equivalent codings will then yield the same logical object for the same variable assignments; which is all that is needed to ensure identical results of lambda-abstraction over $v_{\text {case }}$. Hence, the result of semantic composition is well-defined. Let me show an example.

$$
\begin{aligned}
& {[[\text { Ann }]]=\left\langle\| \lambda P \cdot P(\text { ANN }) \|^{M}, \text { nom }\right\rangle} \\
& {[[\text { coughed }]]=\left\|\operatorname{COUGH}\left(v_{\text {nom }}, e, w\right)\right\|^{M}}
\end{aligned}
$$

$$
\begin{aligned}
& {[[\text { Ann coughed }]]=\|\lambda P . P(A N N)\|^{M}\left(\left\|\lambda v_{n o m} . C O U G H\left(v_{n o m}, e, w\right)\right\|^{M}\right)} \\
& =\left\|\lambda v_{\text {nom }} \cdot \operatorname{COUGH}\left(v_{n o m}, e, w\right)(A N N)\right\|^{M} \\
& =\|\operatorname{COUGH}(A N N, e, w)\|^{M}
\end{aligned}
$$

The next example shows object quantification. The procedure is very similar to a HeimKratzer treatment though without any need to raise the object DP.
(3) Ann read every book.

$$
\begin{aligned}
& {[[r e a d]]=\left\|R E A D\left(v_{n o m}, v_{a c c}, e, t\right)\right\|^{M}} \\
& {[[\text { every book }]]=\left\langle\| \lambda Q_{<e, t>} \forall x\left(B O O K(x) \rightarrow Q(x) \|^{M}, a c c\right\rangle\right.} \\
& {[[\text { read every book }]]=\| \lambda Q_{<e, t>} \forall x\left(B O O K(x) \rightarrow Q(x) \|^{M}\left(\left\|\lambda v_{a c c} \cdot R E A D\left(v_{n o m}, v_{a c c}, e, t\right)\right\|^{M}\right)\right.} \\
& =\| \forall x\left(B O O K(x) \rightarrow \lambda v_{a c c} \cdot R E A D\left(v_{n o m}, v_{a c c}, e, t\right)(x) \|^{M}\right. \\
& =\| \forall x\left(B O O K(x) \rightarrow R E A D\left(v_{n o m}, x, e, t\right) \|^{M}\right. \\
& {[[\text { Ann read every book. }]]} \\
& =\left\langle\|\lambda P \cdot P(A N N)\|^{M}, \text { nom }\right\rangle \oplus \| \forall x\left(B O O K(x) \rightarrow R E A D\left(v_{n o m}, x, e, t\right) \|^{M}\right. \\
& =\|\lambda P . P(A N N)\|^{M}\left(\| \lambda v_{\text {nom }} . \forall x\left(B O O K(x) \rightarrow R E A D\left(v_{n o m}, x, e, t\right) \|^{M}\right)\right. \\
& =\| \lambda v_{\text {nom }} \cdot \forall x\left(B O O K(x) \rightarrow R E A D\left(v_{n o m}, x, e, t\right)(A N N) \|^{M}\right. \\
& =\| \forall x\left(B O O K(x) \rightarrow R E A D(A N N, x, e, t) \|^{M}\right.
\end{aligned}
$$

The derivation of subject quantifiers is exactly parallel. And, of course, two quantificational DPs can combine in one sentence. The order of application will determine scope relations; I leave it to the reader to compute more examples. ${ }^{2}$

So far, I have not specified how world and event variables should be bound. As for the world variable, I refer the reader to the treatment of intensionality as proposed in Fintel \& Heim (2007). Actually, their use of partial assignments as part of their metalanguage is the same as our use of partial assignments as part of the underlying logic. Hence, the present account is fully compatible with their intensional apparatus. Unlike the world index, the event parameter should be bound at some place. We can do so by making use of an existential closure operator ECL for the variable $e$ at any point. Let $\Phi$ be some $L_{\text {link }}$ term that represents the meaning of XP where $e$ occurs free in $\Phi$. [[ ECL XP ]] $=\|\lambda e . \Phi \neq \emptyset\|^{M}=\|\exists e \Phi\|^{M}$. As before, existential closure is only defined if $e$ occurs free in $\Phi$, and yields the same result for all equivalent terms that could represent the meaning of XP.

Unlike DP arguments, the Davidsonian event variable is often used in order to collect several event modifications before it undergoes existential closure. This can be implemented in the present system by assuming that event modifiers leave the event argument as an open variable. The event argument can be bound either by ECL or by an overt quantifying expression, but not by an event modifier.
(4) Ann read every book carefully

1. $[[$ read $]]=\left\|R E A D\left(v_{\text {nom }}, v_{a c c}, e, t\right)\right\|^{M}$
2. $[[$ carefully $]]=\left\langle\|\lambda P(C A R E F U L(e) \wedge P(e))\|^{M}, e\right\rangle$
[^82]
## General Program

3. $[[$ read carefully $]]=\|\lambda P(C A R E F U L(e) \wedge P(e))\|^{M}\left(\left\|\lambda e . R E A D\left(v_{\text {nom }}, v_{\text {acc }}, e, t\right)\right\|^{M}\right)$

$$
\left.=\left\|\left(C A R E F U L(e) \wedge \lambda e . R E A D\left(v_{n o m}, v_{a c c}, e, t\right)(e)\right)\right\|^{M}\right)
$$

$$
\left.=\left\|\left(C A R E F U L(e) \wedge R E A D\left(v_{\text {nom }}, v_{a c c}, e, t\right)\right)\right\|^{M}\right)
$$

4. $[[E C L$ read carefully $\left.]]=\left\|\exists e\left(C A R E F U L(e) \wedge R E A D\left(v_{n o m}, v_{a c c}, e, t\right)\right)\right\|^{M}\right)$
5. [[ every book ]] $=\left\langle\| \lambda Q_{<e, t\rangle} \forall x\left(\operatorname{BOOK}(x) \rightarrow Q(x) \|^{M}\right.\right.$,acc $\rangle$
6. [[ [ECL read carefully] every book $]]=$

$$
\| \lambda Q_{<e, t>} \forall x\left(\operatorname{BOOK}(x) \rightarrow Q(x) \|^{M}\left(\left\|\lambda v_{a c c} \cdot \exists e\left(C A R E F U L(e) \wedge R E A D\left(v_{n o m}, v_{a c c}, e, t\right)\right)\right\|^{M}\right)\right.
$$

$$
=\| \forall x\left(\operatorname{BOOK}(x) \rightarrow \exists e\left(C A R E F U L(e) \wedge R E A D\left(v_{n o m}, x, e, t\right)\right) \|^{M}\right.
$$

7. [[ Ann read every book carefully $]$ ] $=$

$$
\begin{aligned}
& \left\langle\|\lambda P . P(A N N)\|^{M}, \operatorname{nom}\right\rangle \oplus\left\|\forall x\left(B O O K(x) \rightarrow \exists e\left(C A R E F U L(e) \wedge R E A D\left(v_{n o m}, x, e, t\right)\right)\right)\right\|^{M} \\
& =\|\forall x(\operatorname{BOOK}(x) \rightarrow \exists e(\operatorname{CAREFUL}(e) \wedge \operatorname{READ}(A N N, x, e, t)))\|^{M}
\end{aligned}
$$

Alternatively, we can apply ECL after combining verb and object DP and get the following.

$$
\|\exists e(\forall x(B O O K(x) \rightarrow C A R E F U L(e) \wedge R E A D(A N N, x, e, t)))\|^{M}
$$

Finally, the following example can be treated similarly if we replace ECL by the event quantifier twice.
(5) Ann twice read every book carefully.

The quantifier twice contributes $\left\langle\left\|\lambda P \exists e_{1} \exists e_{2}\left(e_{1} \neq e_{2} \wedge P\left(e_{1}\right) \wedge P\left(e_{2}\right)\right)\right\|^{M}, e\right\rangle$. Combination with any XP proceeds by lambda-abstraction over the event argument in the semantics of XP, and functional application. We can derive the following two readings.

$$
\begin{array}{r}
\| \exists e_{1} \exists e_{2}\left(e_{1} \neq e_{2} \wedge \forall x\left(\operatorname{BOOK}(x) \rightarrow C A R E F U L\left(e_{1}\right) \wedge R E A D\left(A N N, x, e_{1}, t\right)\right) \wedge\right. \\
\forall x\left(\operatorname{BOOK}(x) \rightarrow C A R E F U L\left(e_{2}\right) \wedge R E A D\left(A N N, x, e_{2}, t\right)\right) \|^{M} \\
\| \forall x\left(\operatorname{BOOK}(x) \rightarrow \exists e_{1} \exists e_{2}\left(e_{1} \neq e_{2} \wedge \operatorname{CAREFUL}\left(e_{1}\right) \wedge R E A D\left(A N N, x, e_{1}, t\right)\right)\right. \\
\left.\left.\wedge C A R E F U L\left(e_{2}\right) \wedge R E A D\left(A N N, x, e_{2}, t\right)\right)\right) \|^{M}
\end{array}
$$

I will leave it at these illustrations of possible ways to use Linking Logic and Easy Linking Semantics in designing a semantics for fragments of English. The linking mechanism rests on the idea that clauses are closed domains in which every argument of the verb occurs only once. In this preliminary version, I will leave it open whether we will combine Easy Linking Semantics with indices in those cases where parts of a clause undergo long distance movement (or scope). Likewise, I will not detail the analysis of passives here. Passivation requires a different instantiation in linking semantics value of the verb which reflects the shifted grammatical roles. So far, I have demonstrated how Easy Linking Semantics can implement quantification, argument saturation and argument modification without binding the argument. Beaver \& Condoravdi propose that modification is particularly needed for the time argument of verbs, and develop a particular way of shifting the value of the time arguments, which is effected by temporal modifiers. I will not take a stand as to whether this is the best, the only, or just one way of treating temporal modification but I want to show that it can be implemented in Easy Linking Semantics, too.

### 3.2 Functional shifting of arguments

Beaver \& Condoravdi make repeated use of operations that shift the value of variable assignments. For instance, they use functions which map each set of points of time onto the maximal subset which entirely consists of time points in July, in order to test what happened in July). These functions serve a special purpose in their overall tense semantics which I will not recapitulate here. However, let us see how values of the time argument of verbs can be shifted by means of a simple function, e.g. the function which maps a time point $\tau$ to $\tau+1$. I will generally use $t$ for the time argument (variable) and greek letters for time points.

For the sake of simplicity, I will ommit the Davidsonian event argument in the present section. This is not to say that the technique is restricted to non-Davidsonian semantics. Consider the following formula in $L_{\text {link }}$ which states that Anne coughed in $w$ at $t$.
$\|C O U G H(A N N E, w, t)\|^{M, g}$
The formula is defined for all $g$ with the domain $\{t, w\}$ on times and worlds in $M$ which are such that their extension to $v_{\text {nom }}$ which map $v_{\text {nom }}$ to $A N N E$ is in [[cough]]. Assume that we want to modify this formula in a way that ensures that Anne coughed at the time point that follows on $g(t)$. If you need a linguistic counterpart of this modification, you could imagine that it is contributed by one moment later. We can achieve this modification by lambda-abstracting over $t$ and applying the resulting function to $(t+1)$. The computation proceeds as follows:

1. $\|\operatorname{COUGH}(A N N E, w, t)\|^{M, g}=1$ iff $\operatorname{dom}(g)=\{t, w\}$ and all extensions of $g$ to $v_{\text {nom }}$ which map $v_{\text {nom }}$ to $A N N E$ are in the denotation of cough.
2. $\|\lambda t . \operatorname{COUGH}(A N N E, w, t)\|^{M, g^{\prime}}$ is defined for all assignments where $\operatorname{dom}\left(g^{\prime}\right)=\{w\}$. It denotes that function $\mathbf{F}$ from time points $\tau$ to $\{0,1\}$ which maps $\tau$ to 1 exactly if the extension $g^{" \prime}:=g^{\prime}+\langle t, \tau\rangle$ is such that $\|\operatorname{COUGH}(A N N E, w, t)\|^{M, g^{\prime \prime}}=1$.

We will now apply this function to the term $t+1$.

1. $\| \lambda t$.COUGH $(A N N E, w, t)(t+1) \|^{M, g}$ is defined for our old assignments $g$ with $\operatorname{dom}(g)=$ $\{t, w\}$. (Note that $t$ is again free in the new formula, because it was free in the argument term.)
2. According to our definition of functional application in SALo, we get
$\|\lambda t . \operatorname{COUGH}(A N N E, w, t)(t+1)\|^{M, g}$
$=\|\lambda t . \operatorname{COUGH}(A N N E, w, t)\|^{M, g_{1}}\|(t+1)\|^{M, g_{2}}$
where $g_{1}=\left.g\right|_{\{w\}}$ and $g_{2}=\left.g\right|_{\{t\}}$. This latter combination is equal to:
3. $\mathbf{F}\left(g_{2}(t)+1\right)$, where $\mathbf{F}$ is $\|\lambda t . \operatorname{COUGH}(A N N E, w, t)\|^{M, g_{1}}$. Given that $g_{2}(t)=g(t)$, this application yields true exactly if $A N N E$ coughs at time $g(t)+1$. The application yields false else.

Generalizing this mechanism, we can apply a functional shift to the tense argument $t$ in a given formula. Like in all other cases, a modifier that involves the argument will first effect lambda abstraction over that argument. Next, this lambda term is applied to a term of the form $F(t)$. The argument place remains open; the formula is still defined for partial variable assignments $g$ which have the respective variable in their domain (the time variable $t$ in our example).

Functional shifts can be combined. We could decide to apply a function $G(t):=2 t$ in addition to $F(t)=t+1$ (whatever sense this may make on times). The order of semantic application determines the order in which F and G operate on the tense argument. Remember that, in the following formulae, $\lambda t$ binds only the open variable $t$ in $\phi$.

## General Program

$$
\begin{aligned}
& \|\lambda t \cdot \phi(t)(F(t))\|^{M}=\|\phi(t+1)\|^{M} \\
& \|\lambda t \cdot \phi(F(t))(G(t))\|^{M}=\|\lambda t . \phi(t+1)(G(t))\|^{M}=\|\phi(2 t+1)\|^{M} \\
& \|\lambda t \cdot \phi(t)(G(t))\|^{M}=\|\phi(2 t)\|^{M} \\
& \left.\|\lambda t \cdot \phi(G(t))(F(t))\|^{M}=\|\lambda t . \phi(2 t)(F(t))\|^{M}=\|\phi(2(t+1))\|^{M}=\| \phi(2 t+2)\right) \|^{M}
\end{aligned}
$$

Beaver \& Condoravdi (2007) use functional composition in order to model stacked temporal modifiers of the kind in the morning on Saturday for three weeks in 2008. They exploit the fact that the syntactic order of temporal modifiers determines the order of application in the semantic representation. In their framework, certain ungrammatical orders of modifiers can be explained by the fact that the respective composition of functions is undefined or yields empty results.

## 4 Summary

The present paper spells out a type logic on partial variable assignments which combines the expressive power of classical type logic with full control over the open variables of each term. Full control over free variables can be a convenient feature in many contexts in natural language semantics. In a next step, I proposed to use type logics that use variables which are indexed with abstract case labels. This type logic can serve as the backbone of semantic analysis, offering a convenient way to activate and inactivate parameters in the semantic computation. I proposed a specific example of Easy Linking Semantics to illustrate the potential of the linking mechanism. It allows to define semantic combination of argument and operator in much the same way as the QR-based mechanism proposed in Heim \& Kratzer (1998), but without quantifier raising at LF. This is particularly advantageous for verb arguments which do not meet their modifying or saturating phrase at a fixed place in the sentence. Such verb arguments include the time argument, space argument, but also the event argument, if you chose to operate in a traditional Davidsonian event semantics (Parsons, 1990). Easy Linking Semantics is likewise an attractive alternative framework in modeling the semantics of free word order languages. It is also suited to formulate the semantic component for grammars that do not make use of movement operations in the same way as GB and Minimalist grammars. Easy Linking Semantics, finally, is closely related to Linking Semantics as in Beaver \& Condoravdi (2007). It offers a near-type logic way to refer to denotations in their linking structures and can be generalized to accommodate their event-free semantic fragment of English (see extended version).

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# Rivalry between French -age and -ée: the role of grammatical aspect in nominalization ${ }^{*}$ 

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#### Abstract

This paper will provide an account for the existence of pairs of deverbal nominals with -age and -ée giving rise to event readings. We first study the argument structure of the bases and of the derived nominals, and establish the general tendencies. We further examine the Aktionsart of the nominalizations and of the verbal bases. We conclude that these levels of investigation are not sufficient to determine the proper contribution of the two nominalization patterns and further demonstrate that the relevant contribution they make is at the level of grammatical aspect. We therefore propose that -age introduces the imperfective viewpoint, whereas -ée introduces the perfective viewpoint.


Keywords: nominalizations, event and argument structure, grammatical aspect

## 1 Introduction

In this presentation we will study French deverbal nouns with the suffixes -age and -ée which are derived from the same verbal base-a case of nominalization rivalry ignored in the literature. Based on a corpus of event nominal pairs derived from 29 verbal bases (which we selected from the TLFi dictionary and completed with web occurrences), we will provide an account of the existence of such pairs in the language. Two questions immediately arise in light of such cases:

- Is there any linguistic reason for the existence of these pairs?
- Do these nominalizations have a distinctive contribution?

Looking at the interplay between event structure, Aktionsart and grammatical aspect, we will try to sketch an answer to these general questions, and propose that the nominalizations under consideration contribute different grammatical aspect values.

[^83]
## 2 Argument structure of the verbal bases

### 2.1 All verbal bases selected

We begin by examining two existing hypotheses: (a) the suffix -age selects transitive verbal bases (Dubois-Charlier (1999)), and (b) only unaccusative verbs allow -ée nominalization (Ruwet (1988)). Examination of the argument structure type of the bases leads us to conclude that there is no clear specialization of the two nominalizations: both can combine with transitive, unaccusative and unergative bases (cf. Legendre (1989) for unaccusativity tests in French). However, some trends and regularities are visible. The transitive base is the primary type selected by both processes that construct N -age and N -ée pairs:
(1) couler du bronze'to cast bronze', couler une cloche, 'to cast a bell'
$\rightarrow$ le coulage / la coulée du bronze/ d'une cloche 'the casting of bronze/a bell'
However, nominalizations with both -age and -ée also select unergative bases (2) and unaccusatives (3).
(2) CHEVAUCHER 'aller à cheval' 'to ride' $\rightarrow$ la chevauchée hebdomadaire 'the weekly ride' / le chevauchage sous un soleil éclatant 'the riding under a blazing sun'
(3) ARRIVER 'to arrive' $\rightarrow$ l'arrivage / l'arrivée de la marchandise, des ouvriers '"the arriving"/ the arrival of the merchandise, of the workers'

### 2.1 General preferences

When selected by only one of the two nominalizations, there is a general preference for certain bases: -age shows a tendency to select transitive bases (4) while unaccusatives are selected by -ée (5).
(4) tourner le film 'to shoot the film'
$\rightarrow$ le tournage du film / *la tournée du film 'the shooting of the film’
(5) le fascisme monte en Europe 'fascism grows in Europe'
$\rightarrow$ la montée du fascisme/*le montage du fascisme 'the growth of fascism'
On the one hand, the data confirm the arguments of Martin (2008) (that nominalization with -age is not limited to transitive bases) and of Legendre (1989) (that -ée nouns are not a valid test for unaccusativity). On the other hand, this result determines the argument structure of the verbal bases selected by the two affixes.

### 2.3 Proposal: highlighting of causation

### 2.3.1. Transitive bases

Nominalization with -age highlights the proto-agent property (cf. Dowty (1991)) of the external argument of the verb (cf. Kelling (2001) and Martin (2008) for an earlier analysis). Our analysis is supported by the different meanings associated with N -age and N -ée derived from the same transitive verb base (7a) and by neologisms (7b). Nominalization with -age underlines the causative sense while with -ée it highlights the resultative sense.
a. Le montage des briques / la montée des briques 'the lifting of bricks' (cause/result)
b. @...avec Sarko, on est entré dans l'ère de l'effrayage!
with Sarko, we entered the age of scaring (built on EFFRAYER 'scare' transitive-causative : x CAUSE y is scared)

### 2.3.2. Unaccusative bases

(i) Nominalization with -age seems to introduce a semantic participant into the event structure of the base verb which has the proto-agent property external causation.
For deverbal nouns built from some unaccusative bases, such as ARRIVAGE 'arrival', POUSSAGE 'growth', nominalization with -age seems to introduce causation which allows a verbal paraphrase with faire 'make'.
(8) a. l'arrivage des légumes 'the "arriving" = arrival of the vegetables'
$=$ 'faire arriver les légumes' 'make the vegetables arrive'
b. le poussage des poils sur le torse 'the growth of hair on the chest'
$=$ 'faire pousser les poils à l'aide d'une lotion' 'make the hair grow using a lotion'
c. le levage de la pâte = 'faire lever la pâte'
'the rising of the dough' = 'make the dough rise'
This is also true for other deverbal nouns with-age that have no morphological counterpart with -ée, like ATTERRISSAGE, which is derived from an unaccusative verb that has no transitive counterpart in French (unlike in English and German).
(9) a. l'avion a atterri 'the plane landed'
b. *le pilote a atterri l'avion 'the pilot landed the plane'
c. l'atterrissage de l'avion 'the landing of the plane'
(ii) Exceptions

But this pattern is not systematic. An -age nominal is ungrammatical when the unaccusative V selects an internal argument that cannot be affected by (agentive or instrumental) causation.
(10) a. la coulée / *le coulage de neige/ de lave 'the flow of snow / of lava'
b. la couchée / le couchage des réfugiés - la couchée / *le couchage du soleil
'the going-to-bed of refugees / the setting of the sun'
The contrasts in (10a-b) are explained by the fact that it is not possible to cause the sunset, or to take into account an external cause (other than natural) for the flowing of lava or of snow. Conversely, the examples in (11) are acceptable because it is possible to have an external initiator of the situation expressed by the verb COULER 'flow', and therefore the property 'causally affected' of the proto-patient is present:
(11) le coulage / la coulée d'eau 'the flowing of water'

We can therefore conclude that in the case of unaccusative verbs that select an internal argument which cannot be affected by causation, the internal argument cannot figure as a participant (y) in the complex event structure in (12).
(12) [ x CAUSE [BECOME y <STATE>]]

In addition, it also allows us to refine the 'agentivity' property of -age, proposed in Kelling (2001) and Martin (2008).

### 2.3.3 Refinement of our proposal

Martin (2008) proposed to extend the 'agentivity' property characterizing -age deverbals on transitive bases to account for two unaccusative verbs, ARRIVER 'arrive' and POUSSER 'grow', giving rise to -age nouns. However she neither mentions the
conditions in which this property is neutralized, nor whether these unaccusative verbs are the only ones that may involve "agentivity" when nominalized by -age.

Our study reveals several points.
(i) This 'agentivity' property cannot be extended to all the unaccusatives (even those without a transitive counterpart), as in (13).
(13) $\quad \operatorname{COULER}_{\text {[unacc] }}$ 'flow' $\rightarrow$ coulée / * coulage de la lave 'flow / *flowing of the lava'
(ii) An unaccusative verb can be nominalized by -age and yet not involve agentivity (14).
(14) PASSER 'pass' $\rightarrow$ le passage de l'ouragan 'the passing of the hurricane'
(iii) Unergatives (as in 15a) and some transitive verbs in the corpus (15b) are not causative, even if they allow nominalization by -age.
(15) a. SAUTER 'jump' $\rightarrow$ sautage 'jumping' (trampoline)
b. remonter l'escalier 'to climb back upstairs' $\rightarrow$ le remontage d'escalier 'the climbing back upstairs'
Causation is therefore highlighted by -age nominalization in a very particular way. We propose that causation is not directly introduced by -age (since certain -age nominalizations of unaccusative bases are not causative) but only highlighted when the verb inherently possesses this property. In other words the internal argument must have a proto-P property "be causally affected", which must be specified in the lexical entry of the verb. The proto-P property on the internal argument implies a proto-A property: "x causally affects $y$ ". It is conceivable, according to our study, that this lexical property of the verb is only activated through morphological derivation.

## 3 Aspectual properties

Since the rivalry between nominalizations with -age and -ée does not seem to be constrained by the argument structure of the verbal base, we continue our investigations by examining the lexical-aspectual properties of the verbs.

### 3.1 Aspectual properties of the verbal bases

Our corpus analysis shows that -age and -ée nominalizations are not sensitive to the lexical-aspectual class of their verbal bases, since they can select bases from all the aspectual classes except for pure states: activities (16), accomplishments (17), and achievements (18).

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POUSSER 'push' ACT \(\rightarrow\) deux heures de poussage / de poussée (naissance) two hours of pushing / of push (delivery)
PESER (tr) 'weigh' ACC \(\rightarrow\) pesage / pesée de l'enfant 'the weighing of the baby' ARRIVER 'arrive’ ACH \(\rightarrow\) l'arrivage du navire / l'arrivée du navire 'the "arriving" / the arrival of the ship'
```


### 3.2. Aspectual inheritance vs. aspectual shift

The application of the set of tests for French nominalizations elaborated by Haas et al. (2008) to the -age and -ée pairs allows us to conclude that the two constructions
have different lexical-aspectual values, which they generally inherit from the verbal bases, but which can also be the result of an aspectual shift induced by nominalization.

### 3.2.1. Aspectual inheritance

Activity verbs can give rise to activity nominals with -age and -ée, as shown by the fact that these nominals reject the structure un $N$ de $x$-temps 'a N of x-time' in (19a), excluded for ACT nominals (Haas et al. (2008)). Accomplishments give rise to Durative Culminative Occurrences (DCO, following terminology and tests from Haas et al 2008). This is indicated in (19b) by the fact that the corresponding nominals appear in ' x time of N '. There are also achievements that give rise to Punctual Occurences (PO, 19c). Contrary to ACT nominals, DCO and PO nominals appear in the subject of $a$ eu lieu 'happened'. DCO nominals, but not PO nominals, can be the subject of a duré 'lasted' and appear in en cours de 'in the process of' N.
(19) a. V ACT $\rightarrow$ N ACT

CRIER (unerg.) 'shout' :
Il a crié pendant une heure/ \#en une heure
He shouted for an hour / \#in an hour
$\rightarrow$ une heure de criage / \# un criage d'une heure
an hour of shouting / \#a shouting of an hour b. V ACC $\rightarrow \mathrm{N}$ DCO
plumer un volatile $\rightarrow$ pendant le plumage des oies/ entre deux plumées d'oies
'to pluck a bird' $\rightarrow$ 'during the plucking of geese / between two pluckings of geese'
c. V ACH $\rightarrow \mathrm{N} \mathrm{PO}$

ARRIVER 'arrive' (unacc.) :
le train est arrivé à $20 \mathrm{~h} 00 \rightarrow$ l'arrivée du train à 20 h 00
the train arrived at $8 \mathrm{p} . \mathrm{m} \rightarrow$ the arrival of the train at $8 \mathrm{p} . \mathrm{m}$.

### 3.2.2. Aspectual shift

Haas et al. (2008) added a new category of deverbal nouns: Durative nonCulminative Occurrences (DnCO). The DnCO manifestation 'demonstration' is derived from an activity verb MANIFESTER 'demonstrate' but successfully passes the test 'subject of a eu lieu 'happened' (which excludes activity nominals). DnCOs differ from other Occurrences ( $\mathrm{DCO}, \mathrm{PO}$ ) in not being culminative; that is, if the process denoted by the noun is interrupted, we can nonetheless assert that the denoted event took place (e.g., the manifestation has been interrupted $\rightarrow$ they manifested, vs. the delivery has been interrupted $\rightarrow$ \# she gave birth)

Consequently, there are cases in which the aspectual value of the base is shifted in the nominalization process. Such cases include (i) activity bases which derive DnCOs (20a-b), as shown by their ability to appear with pendant 'during'; (ii) achievement bases giving rise to DCO (instead of PO), which can take en cours de 'in the process of ${ }^{\prime}$ in (20c).
(20) a. V ACT $\rightarrow \mathrm{N}$ DnCO (for -age and -ée ): traîner la quille 'to drag the keel'
$\rightarrow$ pendant le traînage/ pendant la traînée 'during the dragging / during the "drag"' b. V ACT $\rightarrow \mathrm{N}$ DnCO (for -ée ):
chevaucher pendant deux heures (activity) 'to ride for two hours'
$\rightarrow$ le jour de la chevauchée ( DnCO ) 'the day of the ride'

$$
\begin{aligned}
& \text { c. V ACH } \rightarrow \text { N ODC (for -age) } \\
& \text { ARRIVER 'arrive' (ACH) } \\
& \rightarrow 5173 \text { tonnes (de céréales) étaient en cours d'arrivage par camions } \\
& \text { '5173 tones (of cereals) were in the process of arriving by trucks' }
\end{aligned}
$$

These results show that the two nominalizations -age and -ée are not tied to specific lexical-aspectual values. However, in the case of -age, we can remark that the shift goes in the direction of durativity (as in 20c), whereas in the case of -ée, the shift is associated with terminativity. Nonetheless, the Aktionsart of these nominals seems to be insufficient in distinguishing their properties. In the following section, we will show that the distinguishing factor is in fact their contribution on the level of grammatical aspect (viewpoint - Smith (1991)).

### 3.3. Grammatical aspect in nominalizations

Given the existence of these pairs of nouns, it is reasonable to hypothesize that the two nominalizations correspond to different ways of conceptualizing events: focusing on the event as a whole (closed) in the case of -ée, or, in the case of -age, focusing on the ongoing process or on an internal phase of the event denoted by the verbal base. Thus, -age introduces the imperfective aspect, while -ée introduces the perfective aspect. The difference should therefore be situated on the level of grammatical aspect (viewpoint). In this light, we propose the following account of the pairs:
(21) Proposal: With the same verbal base (tr., unacc. and unerg.) -age and -ée contribute grammatical aspect introducing an imperfective vs. perfective value

### 3.3.1. Series of arguments supporting this semantic difference

The first argument is provided by the semantic difference between the two nominalizations, which is highlighted by the following distributional tests.
(i) Event nominals with -age, but not with -ée, can appear with the preposition APRĖS 'after', which requires a perfective event as its complement, exactly as in the case of (finite and non-finite) complement clauses.
(22) a. ??après l'arrivage de la marchandise / après l'arrivée de la marchandise' 'after the arriving of the merchandise / after the arrival of the merchandise'
b. après être arrivée, la marchandise a été vendue 'after being arrived, the merchandise has been sold'
a. ??après le pesage du bébé / après la pesée du bébé 'after the weighing of the baby'
b. après avoir pesé le bébé 'after having weighed the baby'
(ii) Event nominals with -age, but not with -ée, can appear as object of INTERROMPRE 'interrupt' (24), or as subject of PROGRESSER 'progress' (25).
(24) L'arrivage / ??l'arrivée des ouvriers a été interrompu(e) par un convoi de police
'the arriving / the arrival of the workers has been interrupted by a police crew'
(25) Le perçage / ??la percée du tunnel a progressé.
'the drilling / the "drilling" of the tunnel progressed'
(iii) The two nominalizations have different meanings (namely 'process in development' with -age and 'whole process' with -ée), when they appear as objects of FILMER 'to film' (26) or SURVEILLER 'supervize' (27).
(26) a. J'ai filmé le pesage du bébé (le déroulement / une portion du procès) I filmed the weighing of the baby (the development / a phase of the process)
b. J'ai filmé la pesée du bébé (la globalité de l'event : début, milieu, fin)

I filmed the weighing of the baby (the whole event: start, development, end)
a. J'ai surveillé l'arrivage des marchandises (le déroulement du procès)
'I supervised the arriving of goods' ('supervise the process')
b. \#J'ai surveillé l'arrivée des marchandises (épier, guetter, attendre)
'I supervised the arrival of goods' ('look for, wait for the arrival')
(iv) pluractionality of -age as manifestation of its imperfectivity value Another argument for imperfectivity in the case of -age nominals is their pluractional meaning. Recall that in the literature on pluractionality, pluractional markers are defined as imperfective (iterative or habitual) aspectual operators (cf., Van Geenhoven (2004)). Nominalizations with -age involve a pluractional meaning which conflicts, in the case of achievement verbal bases, with the cardinality of the internal argument, thus explaining the contrasts in (29) and (30).
(29) *'arrivage d'un légume / OK des légumes, de la marchandise
'the arriving of a vegetable / of vegetables, of the merchandise'
(30) *le tuage d'une mouche / OK de mouches 'the killing of a fly / of flies'

Similar tests have been used crosslinguistically in the domain of verbal aspect for West Greenlandic in Van Geenhoven (2004) and aspectual periphrases with andar in Spanish by Laca (2006). Pluractionality has been also documented for Romanian Supine nominalizations by Iordăchioaia \& Soare (2008), Alexiadou \& al (2008). In (31), the supine derived from 'kill' is ruled out when combined with a singular argument:
(31) ucisul *unui jurnalist / jurnaliștilor de către mafia politică
'the killing *of a journalist / of journalists by the political mafia' [Romanian]

### 3.3.2. Extension to nominalizations with -age/ -ment

Our proposal, according to which -age/-ée introduce an opposition at the level of grammatical aspect, allows us to reconsider the treatment of nominalization with agel -ment put forward in Martin (2008). Martin (2008) explains the contrast in (32b) through the fact that a pedestrian is not an incremental Theme.
(32) a. Pierre a écrasé une banane/ un piéton
'Peter crushed a banana / ran over a pedestrian'
b. l'écrasage d'une banane / \# l'écrasage d'un piéton 'the crushing of a banana' / "the running over of a pedestrian"
c. l'écrasement d'un piéton "the running over of a pedestrian"

If our proposal for -age/ -ée pairs can be extended to -age/-ment, more precisely, if nominalization with -ment can be considered as highlighting the global event, then the contrast in (32b) - (32c) is predicted ${ }^{1}$. In pairs, -age nominals denote an ongoing event, so in (32b), écrasage cannot take a pedestrian as an argument, because run over a pedestrian denotes a punctual event (an achievement), and cannot be conceptualized in its development, but only as a global (closed) situation.

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## 4. Confirmation and extension of the proposal: transitive-unaccusative verbs; transitive verbs and unaccusative verbs

### 4.1. Selectional restrictions on the nominalization of transitive-unaccusative verbs

Our proposal is further confirmed by selectional restrictions on these nominalizations in the case of transitive-unaccusative verbs (see also Martin 2008 for -age/-ment). As shown in (33), -age selects the transitive base whereas the unaccusative base is selected by -ée.
(33) a. Marie a percé son abcès > le perçage de l'abcès.
'Mary burst her abscess / the bursting of the abscess'
b. Son abcès a percé > la percée de l'abcès /vs. \#le perçage de l'abcès
'Her abscess burst / the bursting of the abscess'
(i) Proposal: Given that -age conceptualizes the situation type denoted as ongoing, then it is expected that -age selects the event structure involving the initiator (or the volitional causer) of the ongoing process: the complex one (transitive pattern) where figures the initiator, x , whereas -ée will select the simple one (unaccusative pattern):
(34) PERCER 'to burst'
a. [x CAUSE [BECOME y <BURST>]] for (35a) $\rightarrow$ PERÇAGE
b. [BECOME y <BURST>] for (35b) $\rightarrow$ PERCÉE
(ii) Account of these selectional restrictions for -age vs. -ment deverbals of transitive-unaccusative verbs by Martin (2008). According to Martin (2008) [Property 1], for GONFLER ‘inflate, blow’ (transitive-unaccusative verb), -age deverbals are built on the long eventive chain of the verb (the transitive pattern) : gonflage du ballon par Pierre, while -ment deverbals are built on the short one (the unaccusative pattern) : gonflement du ballon 'the inflation of the balloon'. This distribution is correct, but, as noted by Martin (2008) herself, -ment deverbals can also be built on the long eventive chain of the alternating verbs (gonflement du ballon par Pierre 'the inflation of the balloon by Pierre'). This casts doubts on the exploitation of the notion of length eventive chain for explaining the selectional restrictions.

### 4.2. Transitive-unaccusative and transitive bases selected by both -age/-ée

If -age and -ée respectively introduce imperfective and perfective grammatical aspect, the selectional restrictions in the case of transitive-unaccusative verbs follows naturally: -age is predicted to select only the complex event structure because it contains the initiator of the denoted situation type (35a) - transitive pattern ; whereas -ée will select the simple event structure ((35b) - unaccusative pattern) :

## (35) <br> a. [x CAUSE [BECOME y <STATE>]] <br> b. [BECOME y <STATE>]] <br> ........ ///I/I/I/I/I/I/I/I/I/I/I//............. -age <br> 

Because -ée presents the situation as closed, we predict that -ée can also select a complex event structure including the initiator (35a) in case of transitive unaccusative verbs, then also accounting for le gonflement du ballon par Pierre 'the inflation of the balloon by Pierre' exactly as for transitive base verbs of our corpus selected by both nominalizations.
(36) rentrer les vaches 'to bring in the cows': [x CAUSE [BECOME y <PLACE>]]
a. La rentrée des vaches 'the bringing in of cows'
b. @ j'ai effectué la rentrée des bêtes 'I did the bringing in of the animals'
c. [x CAUSE [BECOME y <PLACE>]]

a. Le rentrage des vaches 'the bringing in of cows'
b. @ opération rentrage des vaches avec une voisine qui n'y connaît rien
'the operation of bringing in the cows with a neighbour who knows nothing about'
c. [x CAUSE [BECOME y < PLACE>]]
...//I/I/I/I/I/I/I/I........... -age

For transitive-unaccusative verbs, -ée can also select the complex event structure, but -age can only select the complex one, because of their respective grammatical aspect values.

### 4.3. Nominalization of unaccusative verbs without transitive counterparts

Our proposal makes the following prediction: because these unaccusative verbs have a simple event structure [without an external initiator (x)] they will only be selected by -ée (39). The prediction is borne out: (40c) vs. (40b) :
(39) PERCER 2 émerger 'to emerge': [BECOME y <émergé>]
(40) a. @les fleurs ont percé / l'entreprise a rapidement percé (PERCER 2 émerger) 'the flowers "broke through"' 'the enterprise broke through'
b. \# le perçage des fleurs/ \# le perçage de l'entreprise
'the "breaking-through" of the flowers' 'the breaking through of the enterprise'
c. @la percée des fleurs / la percée de l'entreprise
'the "break-through" of the flowers' 'the breaking through of the enterprise'
Our proposal then covers the distribution of patterns that Martin (2008) treats in terms of length of the eventive chain, but it goes further: (i) by proposing a principled reason for this distribution : because N -age denotes an ongoing process (so a portion of it) - imperfective view point - it highlights the initiator of the situation denoted by the verb, involved in the ongoing process; (ii) by accounting for the fact that the complex event structure is not only combinable with -age, but also with -ée (and also with -ment examples of Martin (2008)). The same proposal (i.e. (21)) allows us to account for the selectional restrictions in the case of transitive-unaccusative verbs (age selects the transitive one, -ée selects the unaccusative one) but also to predict the nominalization of 'pure' unaccusative verbs.

## 5. Conclusion

This corpus study allowed us to show:

- Nominalizations with -age and -ée can select all types of bases, but -age exhibit preference for transitive bases, whereas -ée for unaccusative ones.
- General inheritance of the lexical aspectual value of the base verb by these deverbal nouns, but also aspectual shift, reflecting durativity in the case of age and terminativity in the case of -ée.
- A common "core" property that underlies the properties exhibited by the nominalization - the introduction of a grammatical aspectual value (perfective/ imperfective) by the nominalization.
- These factors are hierarchically ordered such that the grammatical aspect introduced by the nominalization is correlated with operations on the argument structure in some nominalizations, probably by determining the inheritance or the "introduction"/ "activation" of causation in -age nominals.
- Consequently, the various properties associated with -age nominals in the literature (e.g., agentivity, incrementality, length of the eventive chain) follow from our general proposal that -age and -ée convey different grammatical aspectual values.


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# Free Choice from Iterated Best Response 

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#### Abstract

This paper summarizes the essence of a recent game theoretic explanation of free choice readings of disjunctions under existential modals (Franke, 2009). It introduces principles of game model construction to represent the context of utterance, and it spells out the basic mechanism of iterated best response reasoning in signaling games.


## 1 Free Choice Disjunctions \& Game Theory

Contrary to their logical semantics, disjunctions under modal operators as in (1a) may receive free-choice readings (FC-readings) as in (1b) (Kamp, 1973).
a. You may take an apple or a pear.
$\diamond(A \vee B)$
b. You may take an apple and you may take a pear.
$\diamond A \wedge \diamond B$

This inference is not guaranteed by the standard logical semantics which treats disjunction as truth-functional connective and the modal as an existential quantifier over accessible worlds. Of course, different semantics of disjunctions or modals are conceivable and have been proposed by, for instance, Kamp (1978), Zimmermann (2000) or Asher and Bonevac (2005). But, all else being equal, a pragmatic solution that retains the logical semantics and treats FC-readings as Gricean inferences seems preferable (cf. the arguments in Schulz, 2005).

Unfortunately, a naïve approach to Gricean scalar reasoning does not suffice. If we assume that the set of expression alternatives with which to compare an utterance of (1a) contains the simple expressions in (2), we run into a problem.
(2) a. You may take an apple. $\diamond A$
b. You may take a pear.
$\diamond B$

Standard scalar reasoning tells us that all semantically stronger alternatives are to be inferred not to be true. This yields that $\square \neg A$ and that $\square \neg B$, which together contradicts (1a) itself.

This particular problem has a simple solution. Kratzer and Shimoyama (2002) observe that the FC-reading follows from naïve scalar reasoning based on the alternatives in (2) if we use the already exhaustified readings of the alternatives as in (3).
(3) a. You may take an apple, but no pear.

$$
\diamond A \wedge \neg \diamond B
$$

b. You may take a pear, but no apple.
$\diamond B \wedge \neg \diamond A$
Truth of (1a) together with the falsity of both sentences in (3) entails the FCreading in (1b).

There is clearly a certain intuitive appeal to this idea: when reasoning about expression alternatives it is likely that potential pragmatic enrichments of these may at times be taken into account as well. But when and how exactly? Standard theories of scalar reasoning do not integrate such nested pragmatic reasoning. This has been taken as support for theories of local implicature computation in the syntax where exhaustifity operators can apply, if necessary, several times (Chierchia, 2004; Fox, 2007). But the proof that such nested or iterated reasoning is very much compatible with a systematic, global, and entirely Gricean approach amenable to intuitions about economic language use is still up in the air.

Enter game theory. Recent research in game-theoretic pragmatics has produced a number of related models of agents' step-by-step pragmatic reasoning about each others' hypothetical behavior (Stalnaker, 2006; Benz and van Rooij, 2007; Jäger, 2007). This is opposed to the more classical equilibrium-based solution concepts which merely focus on stable outcomes of, mostly, repeated play or evolutionary dynamics. The main argument of this paper is that such step-bystep reasoning, which is independently motivated, explains free-choice readings along the lines sketched above: early steps of such reasoning establish the exhaustive readings of alternative forms, while later steps of the same kind of global reasoning can pick on previously established readings.

In order to introduce and motivate this game theoretical approach, two sets of arguments are necessary. ${ }^{1}$ Firstly, we need to settle on what kind of game model is required in order to represent conversational moves and their interpretation. This is to be addressed in section 2. Secondly, we need to spell out a solution concept by means of which pragmatic language use can be explained in the chosen game models. This is the topic of section 3. Finally, section 4 reviews briefly how this approach generalizes.

## 2 Interpretation Games As Context Models

It is standard in game-theoretic pragmatics to assume that an informative assertion and its uptake can reasonably be modelled as a signaling game. More specifically then, the pragmatic interpretation of assertions can be modelled by a particular kind of signaling game, which I will call interpretation game. These latter games function as representations of the context of utterance (as conceived by the receiver) and are constructed from a given target expression whose interpretation we are interested in, together with its natural Neo-Gricean alternatives and their logical semantics. Let me introduce both signaling games and interpretation games one after the other.

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Signaling Games. A signaling game is a simple dynamic game between a sender and a receiver. The sender has some private information about the state of the world $t$ which the receiver lacks. The sender chooses a message $m$ from a given set of alternatives, all of which we assume to have a semantic meaning commonly known between players. The receiver observes the sent message and chooses an action based on this observation. An outcome of playing a signaling game for one round is given by the triple $t, m$ and $a$. Each player has his own preferences over such outcomes.

More formally speaking, a signaling game (with meaningful signals) is a tuple

$$
\left\langle\{S, R\}, T, \operatorname{Pr}, M, \llbracket \cdot \rrbracket, A, \mathrm{U}_{S}, \mathrm{U}_{R}\right\rangle
$$

where sender $S$ and receiver $R$ are the players of the game; $T$ is a set of states of the world; $\operatorname{Pr} \in \Delta(T)$ is a probability distribution over $T$, which represents the receiver's uncertainty which state in $T$ is actual; ${ }^{2} M$ is a set of messages that the sender can send; $\llbracket \cdot \rrbracket: M \rightarrow \mathcal{P}(T) \backslash \emptyset$ is a denotation function that gives the predefined semantic meaning of a message as the set of all states where that message is true; $A$ is the set of response actions available to the receiver; and $\mathrm{U}_{S, R}: T \times M \times A \rightarrow \mathbb{R}$ are utility functions for both sender and receiver.

Interpretation Games. For models of natural language interpretation a special class of signaling games is of particular relevance. To explain pragmatics inferences like implicatures we should look interpretation games. I assume here that these games can be constructed generically from a set of alternatives to the to-be-interpreted expression, together with their logical semantics. Here are the assumptions and the construction steps.

Firstly, the set of receiver actions is equated with the set of states $A=T$ and the receiver's utilities model merely his interest in getting to know the true state of affairs, i.e., getting the right interpretation of the observed message:

$$
\mathrm{U}_{R}(t, m, a)= \begin{cases}1 & \text { if } t=a \\ 0 & \text { otherwise }\end{cases}
$$

Moreover, in the vein of Grice (1989), we assume that conversation is a cooperative effort - at least on the level of such generic context models - so that the sender shares the receiver's interest in correct interpretation: ${ }^{3}$

$$
\mathrm{U}_{S}(t, m, a)=\mathrm{U}_{R}(t, m, a)
$$

For a set $M$ of messages given by some (normal, natural, Neo-Gricean) set of alternative forms to the target sentence whose implicatures we are interested

[^86]
## General Program

in, we can derive a set of state distinctions $T$. Clearly, not every possible way the world could be can be distinguished with any set $M$. So we should restrict ourselves to only those states that can feasibly be expressed with the linguistic means at hand. What are those distinctions? Suppose $M$ contains only logically independent alternatives. In that case, we could in principle distinguish $2^{M}$ possible states of the world, according to whether some subset of messages $X \subseteq M$ is such that all messages in $X$ are true, while all messages in its complement are false. (This is what happens in propositional logic, when we individuate possible worlds by all different valuations for a set of proposition letters.) But for normal pragmatic applications the expressions in $M$ will not all be logically independent. So in that case we should look at states which can be consistently described by a set of messages $X \subseteq M$ all being true while all expressions in its complement are false. Moreover, since at least the target message may be assumed true for pragmatic interpretation, we should formally define the set of states of the interpretation game as given by the set of all subsets $X \subseteq M$ containing the target message such that the formula

$$
\bigwedge X \wedge \neg \bigvee M \backslash X
$$

is consistent. With this, the semantic denotation function $\llbracket \rrbracket \rrbracket$ is then straightforwardly defined as:

$$
\llbracket m \rrbracket=\{t \in T \mid m \in t\} .
$$

Finally, since we are dealing with general models of utterance interpretation, we should not assume that the receiver has biased beliefs about which specific state obtains. This simply means that in interpretation games $\operatorname{Pr}(\cdot)$ is a flat probability distribution.

Example. To give a concrete example, here is how to construct an interpretation game for the target expression in (1a). Everything falls into place once a set of alternatives is fixed. To keep the exposition extremely simple, let us first only look at the set of messages in (4). (See section 4 for more discussion.)
(4) a. You may take an apple or a pear.

$$
\begin{array}{r}
m_{\diamond(\mathrm{A} \vee \mathrm{~B})} \\
m_{\diamond \mathrm{A}} \\
m_{\diamond \mathrm{B}}
\end{array}
$$

b. You may take an apple.
c. You may take a pear.

Based on these alternatives, there are three states we need to distinguish:

$$
\begin{aligned}
t_{\mathrm{A}} & =\left\{m_{\diamond \mathrm{A}}, m_{\diamond(\mathrm{A} \vee \mathrm{~B})}\right\} \\
t_{\mathrm{B}} & =\left\{m_{\diamond \mathrm{B}}, m_{\diamond(\mathrm{A} \vee \mathrm{~B})}\right\} \\
t_{\mathrm{AB}} & =\left\{m_{\diamond \mathrm{A}}, m_{\diamond \mathrm{B}}, m_{\diamond(\mathrm{A} \vee \mathrm{~B})}\right\} .
\end{aligned}
$$

Here, $t_{\mathrm{A}}$ is a state where the hearer may take an apple but no pear, and $t_{\mathrm{AB}}$ is a state where the hearer may take both an apple and a pear. These states yield the interpretation game in figure 1 . Notice that we consider only those states,

| $\operatorname{Pr}(t) a_{\mathrm{A}} a_{\mathrm{B}} a_{\mathrm{AB}} \mid m_{\diamond \mathrm{A}} m_{\diamond \mathrm{B}} m_{\diamond(\mathrm{AVB})}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $t_{\text {A }}$ | $1 / 3$ | 1,10,0 0,0 | $\sqrt{ }$ |  | $\checkmark$ |
| $t_{\text {B }}$ | 1/3 | 0,0 1, 10,0 | - |  | $\checkmark$ |
| $t_{\text {A }}$ | $1 / 3$ | 0,0 0,0 1, 1 | $\checkmark$ | $\checkmark$ | $\checkmark$ |

Fig. 1. Interpretation game constructed from (1a) and (4)
because these are the only distinctions we can make between worlds where the target message (1a) is true that can be expressed based on consistent valuations of all alternatives. Certainly, in the present case, this is nearly excessively simple, but it is not trivial and, most importantly, there is still room for pragmatic interpretation: there are still many ways in which sender and receiver could coordinate on language use in this game. What is needed is a solution concept that singles out uniquely the player behavior that explains the free choice inference.

## 3 Iterated Best Response Reasoning

Behavior of players is represented in terms of strategies. A pure sender strategy $s \in \mathrm{~S}=M^{T}$ is a function from states to messages and a pure receiver strategy $r \in \mathrm{R}=A^{M}$ is a function from messages to actions. A pure strategy profile $\langle s, r\rangle$ is then a characterization of the players' joint behavior in a given signaling game. For instance, the tuple:

$$
s=\left\{\begin{array}{l}
t_{\mathrm{A}} \mapsto m_{\diamond \mathrm{A}}  \tag{1}\\
t_{\mathrm{B}} \mapsto m_{\diamond \mathrm{B}} \\
t_{\mathrm{AB}} \mapsto m_{\diamond(\mathrm{AVB})}
\end{array}\right\} \quad r=\left\{\begin{array}{ll}
m_{\diamond \mathrm{A}} & \mapsto t_{\mathrm{A}} \\
m_{\diamond \mathrm{B}} & \mapsto t_{\mathrm{B}} \\
m_{\diamond(\mathrm{AVB})} \mapsto t_{\mathrm{AB}}
\end{array}\right\}
$$

is a strategy profile for the game in figure 1. And a special one, indeed. It corresponds to the intuitive way of using the corresponding natural language expressions: the interpretation of $m_{\diamond A}$, for instance, is the exhaustive reading that only $A$, but not $B$ is allowed; and the interpretation of $m_{\diamond(A \vee B)}$ is the free choice inference that both taking $A$ and taking $B$ are allowed. This is therefore what a solution concept is required to predict in order to explain FC-readings based on the game in figure 1.

But the strategy profile in (1) is not the only one there is. Also, the rather unintuitive pooling strategy profile

$$
s=\left\{\begin{array}{l}
t_{\mathrm{A}} \mapsto m_{\diamond(\mathrm{AVB})}  \tag{2}\\
t_{\mathrm{B}} \mapsto m_{\diamond(\mathrm{AVB})} \\
t_{\mathrm{AB}} \mapsto m_{\diamond(\mathrm{AVB})}
\end{array}\right\} \quad r=\left\{\begin{array}{ll}
m_{\diamond \mathrm{A}} & \mapsto t_{\mathrm{AB}} \\
m_{\diamond \mathrm{B}} & \mapsto t_{\mathrm{AB}} \\
m_{\diamond(\mathrm{AVB})} \mapsto t_{\mathrm{AB}}
\end{array}\right\}
$$

is conceivable. What is worse, both strategy profiles describe an equilibrium state: given the behavior of the opponent neither player has an incentive to deviate. But, clearly, to explain the FC-reading, the profile in (1) should be selected, while the profile in (2) should be ruled out. In other words, we need a mechanism with which to select one equilibrium and rule out others.

## General Program

IBR Models. One way of looking at an iterated best response model (IBR model) is exactly that: a plausible mechanism with which reasoners (or a population) may arrive at an equilibrium state (rather than another). An IBR model assumes that agents reason about each other's behavior in a step-by-step fashion. The model is anchored in naïve behavior of level-0 players that do not take opponent behavior into account, but that may be sensitive to other non-strategic, psychological factors, such as, in our case, the semantic meaning of messages. Players of level$(k+1)$ assume that their opponent shows level- $k$ behavior and play a best response to this belief. ${ }^{4}$

Here is a straightforward IBR sequence as a solution concept for signaling games. Naïve players of level-0 are defined as playing some arbitrary strategy that conforms to semantic meaning. For the sender, this yields:

$$
S_{0}=\{s \in \mathrm{~S} \mid \forall t \in T: t \in \llbracket s(t) \rrbracket\} .
$$

Level- 0 senders are characterized by the set of all pure strategies that send only true messages. For interpretation games, naïve receiver types receive a similarly straightforward characterization:

$$
R_{0}=\{r \in \mathrm{R} \mid \forall m \in M: r(m) \in \llbracket m \rrbracket\} .
$$

Level-0 receivers are characterized by the set of all pure strategies that interpret messages as true.

In order to define level- $(k+1)$ types, it is necessary to define the notion of a best response to a belief in level- $k$ behavior. There are several possibilities of defining beliefs in level- $k$ behavior. ${ }^{5}$ The most convenient approach is to assume that agents have unbiased beliefs about opponent behavior. Unbiased beliefs in level- $k$ behavior do not favor any one possible level- $k$ behavior, if there are several, over any other, and can therefore be equated simply with a flat probability distribution over the set of level- $k$ strategies.

Turning first to higher-level sender types, let us write $R_{k}(m, a)$ for the probability that a level- $k$ receiver who is believed to play a random strategy in $R_{k}$ will play $a$ after observing $m$. Then level- $(k+1)$ senders are defined by

$$
S_{k+1}=\left\{s \in \mathrm{~S} \mid s(t) \in \arg \max _{m \in M} \sum_{a \in A} R_{k}(m, a) \times \mathrm{U}_{S}(t, m, a)\right\}
$$

as the set of all best responses to that unbiased belief.
For higher-level receiver types the same standard definition applies once we have characterized the receiver's posterior beliefs, i.e., beliefs the receiver holds

[^87]about the state of the world after he observed a message. These need to be derived, again in entirely standard fashion, from the receiver's prior beliefs $\operatorname{Pr}(\cdot)$ and his beliefs in sender behavior as given by $S_{k}$. Let $S_{k}(t, m)$ be the probability that a level- $k$ sender who is believed to play a random strategy in $S_{k}$ will send $m$ in state $t$. A level- $(k+1)$ receiver has posterior beliefs $\mu_{k+1} \in(\Delta(T))^{M}$ calculated by Bayesian conditionalization, as usual:
$$
\mu_{k+1}(t \mid m)=\frac{\operatorname{Pr}(t) \times S_{k}(t, m)}{\sum_{t^{\prime} \in T} \operatorname{Pr}\left(t^{\prime}\right) \times S_{k}\left(t^{\prime}, m\right)}
$$

Level- $(k+1)$ receivers are then defined as best responding to this posterior belief:

$$
R_{k+1}=\left\{r \in \mathrm{R} \mid r(m) \in \arg \max _{a \in A} \sum_{t \in T} \mu_{k+1}(t \mid m) \times \mathrm{U}_{R}(t, m, a)\right\}
$$

This last definition is incomplete. Bayesian conditionalization is only defined for messages that are not surprise messages. A surprise message for a level- $(k+1)$ receiver is a message that is not used by any strategy in $S_{k}$ in any state. A lot can be said about the proper interpretation of surprise messages (see the discussion in Jäger and Ebert, 2009; Franke, 2009; Mühlenbernd, 2009). (This is the place where different belief revision strategies of the receiver could be implemented, if needed or wanted.) For the purposes of this paper it is sufficient to assume that whatever else the receiver may come to believe if he observes a surprise message, he will stick to the belief that it is true. So, if for some message $m$ we have $S_{k}(t, m)=0$ for all $t$, then define $\mu_{k+1}(t \mid m)=\operatorname{Pr}(t \mid \llbracket m \rrbracket)$.

Example. The simple IBR model sketched here does what we want it to: it uniquely singles out the intuitive equilibrium state in equation (1) for the game in figure 1 . To see how this works, and to see where IBR may rationalize the use of exhaustified alternatives in Gricean reasoning, let us calculate the sequence of reasoning starting with $R_{0}$ for the simple game in figure 1 (the case starting with $S_{0}$ is parallel): ${ }^{6}$

$$
\begin{array}{ll}
R_{0}=\left\{\begin{array}{ll}
m_{\diamond \mathrm{A}} & \mapsto t_{\mathrm{A}}, t_{\mathrm{AB}} \\
m_{\diamond \mathrm{B}} & \mapsto t_{\mathrm{B}}, t_{\mathrm{AB}} \\
m_{\diamond(\mathrm{AVB})} & \mapsto t_{\mathrm{A}}, t_{\mathrm{B}}, t_{\mathrm{AB}}
\end{array}\right\} & S_{1}=\left\{\begin{array}{ll}
t_{\mathrm{A}} & \mapsto m_{\diamond \mathrm{A}} \\
t_{\mathrm{B}} & \mapsto m_{\diamond \mathrm{B}} \\
t_{\mathrm{AB}} & \mapsto m_{\diamond \mathrm{A}}, m_{\diamond \mathrm{A}}
\end{array}\right\} \\
R_{2}=\left\{\begin{array}{ll}
m_{\diamond \mathrm{A}} & \mapsto t_{\mathrm{A}} \\
m_{\diamond \mathrm{B}} & \mapsto t_{\mathrm{B}} \\
m_{\diamond(\mathrm{AVB})} & \mapsto t_{\mathrm{A}}, t_{\mathrm{B}}, t_{\mathrm{AB}}
\end{array}\right\} \quad S_{3}=\left\{\begin{array}{ll}
t_{\mathrm{A}} & \mapsto m_{\diamond \mathrm{A}} \\
t_{\mathrm{B}} & \mapsto m_{\diamond \mathrm{B}} \\
t_{\mathrm{AB}} & \mapsto m_{\diamond \mathrm{AVB}}
\end{array}\right\} \\
R_{4}=\left\{\begin{array}{ll}
m_{\diamond \mathrm{A}} & \mapsto t_{\mathrm{A}} \\
m_{\diamond \mathrm{B}} & \mapsto t_{\mathrm{B}} \\
m_{\diamond(\mathrm{AVB})} & \mapsto t_{\mathrm{AB}}
\end{array}\right\} .
\end{array}
$$

[^88]Naïve receiver behavior only takes semantic meaning into account and this is what $S_{1}$ plays a best response to. Given $S_{1}$, messages $m_{\diamond A}$ and $m_{\diamond B}$ are interpreted exhaustively by $R_{2}$, as meaning "you may do $A$, but not $B$ ", while message $m_{\diamond(A \vee B)}$ is a surprise message, and will be interpreted merely as true. This makes $m_{\diamond(\mathrm{AVB)}}$ the only rational choice for $S_{3}$ to send in $t_{\mathrm{AB}}$, so that in one more round of iteration we reach a fixed point equilibrium state in which $R_{4}$ assigns to $m_{\diamond(A \vee B)}$ the FC-reading that he may do $A$ and that he may to $B$. In sum, the FC-reading of $m_{\diamond(A \vee B)}$ is derived in two steps of receiver reasoning by first establishing an exhaustive interpretation of the alternatives, and then reasoning with this exhaustive interpretation to arrive at the FC-reading.

## 4 IBR Reasoning: The Bigger Picture

The previous two sections have tried to give, as short and yet accessible as possible, the main mechanism of IBR reasoning and the demonstration that IBR reasoning can account for FC-readings of disjunctions. Many assumptions of this approach could not have possibly been spelled out sufficiently, and so the impression may arise that IBR reasoning, as outlined here, is really only arbitrarily designed to deal with a small problem of linguistic interest. This is, decidedly, not so. There are good and independent motivations for both game model construction and solution concept, and both in tandem do good explanatory work, both conceptually and empirically (see Benz and van Rooij, 2007; Jäger and Ebert, 2009; Franke, 2009).

Moreover, it should be stressed that the IBR approach also handles more complex cases than the easy example discussed above, of course. Most importantly, it predicts well also when other scalar contrasts, such as given by (5a) or (5b), are taken into account as well.

$$
\begin{array}{ll}
\text { a. You must take an apple or a pear. } & m_{\square(A \wedge B)}  \tag{5}\\
\text { b. You may take an apple and a pear. } & m_{\diamond(\mathrm{A} \wedge \mathrm{~B})}
\end{array}
$$

Including more alternative messages results in bigger context models that include more state distinctions. But still IBR reasoning gives intuitive results. For instance, Franke (2009) spells out the IBR reasoning based on a set of alternatives that includes (4) and the conjunctive alternative in (5b). Doing so, we derive that (1a) is taken to implicate that $\diamond(A \wedge B)$ is false. This is as it should be: in a context where the conjunctive alternative is salient, this inference should be predicted, but for the FC-reading alone only simple alternatives as in (4) should suffice. Similar considerations apply to the stronger modal alternative.

Generalizing the result further, it is possible to show that for any $n$-place case of the form $\diamond\left(A_{1} \vee \cdots \vee A_{n}\right)$ we derive the inference that $\diamond A_{i}$ under IBR logic. The argument that establishes this result is a so-called unravelling argument which I can only sketch here: in the first step (of receiver reasoning) all "singleton" messages of the form $\diamond A_{i}$ are associated with their exhaustive readings; in the second step all two-place disjunctions $\diamond\left(A_{i} \vee A_{j}\right)$ are associated with states in
which exactly two actions are allowed one of which must be $A_{i}$ or $A_{j} ;{ }^{7}$ continuing in this way, after $n$ rounds of reasoning the form $\diamond\left(A_{1} \vee \cdots \vee A_{n}\right)$ gets the right interpretation that all actions $A_{i}$ are allowed.

Interestingly, IBR does not need to assume conjunctive alternatives even for the general $n$-place case, while Kratzer and Shimoyama (2002)'s approach has to. ${ }^{8}$ To see this, look at the three-placed case $\diamond(A \vee B \vee C)$ with only alternatives $\diamond A, \diamond B$ and $\diamond C$. The exhaustive readings of these are given in (6).
(6) a. $\diamond A \wedge \neg \diamond B \wedge \neg \diamond C$
b. $\diamond B \wedge \neg \diamond A \wedge \neg \diamond C$
c. $\diamond C \wedge \neg \diamond A \wedge \neg \diamond B$

But truth of $\diamond(A \vee B \vee C)$ together with the falsity of all sentences in (6) does not yield the FC-reading that any of $A, B$ or $C$ are allowed. To establish the FC-reading, we also need the alternatives $\diamond(A \wedge B), \diamond(A \wedge C)$ and $\diamond(B \wedge C)$ with their exhaustive readings in (7).
a. $\diamond(A \wedge B) \wedge \neg \diamond C$
b. $\diamond(A \wedge C) \wedge \neg \diamond B$
c. $\diamond(B \wedge C) \wedge \neg \diamond A$

If we then want to account for the presence of the FC-reading in the absence of the scalar inference that $\forall(A \wedge B \wedge C)$ is false, we need to assume that all alternatives with two-placed conjunctions are given, but not the three-placed conjunctive alternative. This is not impossible, but also not very plausible.

Finally, let me also mention for the sake of completeness that the IBR approach also deals with free choice readings of disjunctions under universal modals in the exact same fashion as outlined here. A parallel account also deals with the structurally similar inference called simplification of disjunctive antecedents as exemplified in (8).
(8) a. If you take an apple or a pear, that's okay.
b. If you take an apple, that's okay. And if you take a pear, that's also okay.

The IBR model is also capable of dealing with epistemic ignorance readings such as forced by (9).
(9) You may take an apple or a pear, but I don't know which.

To capture these, however, the game models have to be adapted to include also possible sender uncertainty.

[^89]
## General Program

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# Goodness 

Bart Geurts

If it wasn't obvious that equivalent descriptions may cause differential evaluations, there is a considerable body of experimental evidence to prove the point. For instance, Levin (1987) asked participants to evaluate the hypothetical purchase of ground beef that was described as " $75 \%$ lean" for one group and " $25 \%$ fat" for another. Despite the fact that these descriptions are truth-conditionally equivalent ( $75 \%$ lean ground beef is $25 \%$ fat, and vice versa), Levin found that the first group produced higher ratings on several scales, including high/low quality and good/bad taste; these effects persisted, albeit at attenuated levels, even after the ground beef had been tasted (Levin and Gaeth 1988). Similarly, when medical treatments were alternatively described in terms of survival and mortality rates (McNeill et al. 1982, Levin et al. 1988) or when research and development teams were alternatively presented in terms of their success and failure rates (Duchon et al. 1989), positive descriptions prompted higher rates of positive responses. In this paper, I study a number of puzzles which were inspired by these experimental findings. I will argue that these puzzles, which are about the interpretation of evaluative statements, call for a novel kind of pragmatic treatment, which I will develop in some detail. Possible connections between this analysis and the experimental data are discussed in Geurts (2010).

Sad tidings. An airplane carrying 600 passengers has crashed in the Pyrenees. 400 people died in the accident; 200 survived. Hence, in this context, the propositions " 200 people survived" and " 400 people died" would seem to be equivalent. Now consider the following pair of statements:
(1) a. It's good that 200 people survived.
b. It's good that 400 people died.

According to my intuition, we would tend to read these statements as contradicting each other. It would be decidedly odd for someone who has just uttered (1a) to go on uttering (1b). And this is not just because (1b) is a peculiar statement in its own right, for someone who, depravedly,
stated (1b) with full conviction would not be expected to endorse (1a) as well. It is also relevant to note that (1a) and (1b) don't have to be construed as contradictories. For the true Panglossian, everything is equally right and good, and therefore one of that tribe could endorse both statements without fear of contradicting himself. There may be a strong preference for a contradictory construal, but it is not mandatory.

It will be obvious, I trust, what my first question is going to be: How is it possible for (1a) and (1b) to be interpreted as contradictories, given that, by hypothesis, their embedded clauses are truth-conditionally equivalent? The second puzzle is the obverse of the first one: How is it possible for (1a) and (1b) to be consistent with (2a) and (2b), respectively?
(2) a. It's bad that 400 people died.
b. It's bad that 200 people survived.

Again, it would be rather nasty for someone to say (2b), and in this sense the sentence is odd, but that is beside the point. The problem I'm interested in is how (2b) manages to be consistent with (1b). Ditto for (1a) and (2a).

It might be thought that both of these problems admit of a straightforward solution. For it is obvious that, out of context, the sentences "400 people died" and "200 people survived" express distinct propositions. However, these propositions come apart only in worlds in which the number of passengers does not equal 600, and it is hard to see why that should be relevant. Hence, I will stick to the assumption that, in our examples, these sentences are truth-conditionally equivalent.

Now change the scenario somewhat. The number of passengers remains the same, but the exact number of casualties is not yet known. All we have to go on is that more than 200 people survived the crash, or equivalently, that fewer than 400 died. Now consider:
(3) a. It's good that more than 200 people survived.
b. It's good that fewer than 400 people died.

Unlike (1a,b), this pair is clearly consistent. In fact, (3a) and (3b) would seem to be synonymous. How is this possible? That is my third and last puzzle.

Although I won't be able, on this occasion, to completely solve all three puzzles, I do believe I can offer the outlines of a plausible solution. To explain the guiding idea, let me show how (1a) and (1b) might come to contradict each other. On the one hand, if someone utters (1a), we tend to infer that, according to the speaker:
（4）It would have been better if more than 200 people had survived and worse if fewer than 200 people had survived．

On the other hand，if someone uttered（1b）with sufficient conviction，we would be inclined to infer that，according to the speaker：
（5）It would have been better if more than 400 people had died and worse if fewer than 400 people had died．

These inferences are incompatible，and that＇s why（1a）and（1b）are con－ tradictories on what I take to be their most natural readings．Hence，the key idea is that the speaker＇s evaluation of an actual state of affairs may carry information about how he would have evaluated alternative states of affairs．The main goal of this paper is to investigate the mechanism underlying such counterfactual implications，and to show in more detail how they will help to solve our three puzzles．

The inference in（4），for example，would be accounted for if we could assume that whatever quality is expressed by＂good＂is positively corre－ lated with the quantitative scale on which the embedded clause of（1a） is sitting．Let me explain．Since＂good＂is a gradable adjective，its inter－ pretation is relative to a comparison set．For example，if I say＂It＇s good that it＇s raining＂，the comparison set might simply be \｛［it＇s raining 】，【it＇s not raining $\rrbracket\}$ ，in which case my utterance implies that the first is better than the second，or more formally：$g\left(\llbracket i t^{\prime}\right.$ s raining $\left.\rrbracket\right)>g\left(\left[i t^{\prime}\right.\right.$ s not raining $\left.\rrbracket\right)$ ， where $g$ is a＂goodness function＂，which maps propositions onto qualita－ tive degrees．

When＂good＂combines with a quantifying proposition like 【200 people survived $\rrbracket$ ，the comparison set might be $\{\llbracket n$ people survived $\rrbracket 0 \leq n \leq$ $600\}$ ．Besides being ordered in qualitative terms，this set also comes with a quantitative ordering，which I will symbolise by＂$\preceq$＂：
（6）$\llbracket 0$ people survived $\rrbracket \prec \llbracket 1$ person survived $\rrbracket \prec \llbracket 2$ people survived $\rrbracket \ldots$
I assume that $\preceq$ may but not need not be an entailment ordering；in the current example it isn＇t．

Now，we can capture the inferences in（4）and（5）as follows：
（7）Co－optation（strong version）
$\forall \varphi, \psi$ ：if $\varphi \succ \psi$ ，then $g(\varphi)>g(\psi)$ ．
The label＂co－optation＂derives from the intuition that the quantitative ordering $\preceq$ is in a sense co－opted for fleshing out the qualitative ordering induced by $g$ ．I will have more to say about this presently．As defined in
(7), co-optation is a rather strong assumption to make, but it should be noted that the most obvious way of weakening it will render it too weak:
(8) Co-optation (weak version)
$\forall \varphi, \psi$ : if $\varphi \succeq \psi$, then $g(\varphi) \geq g(\psi)$.
While the strong version of co-optation says that more of a good thing is better (and more of bad thing is worse), the weak version merely entails that more of a good thing is not worse (and more of a bad thing is not better), which is too weak for deriving the inferences in (4) and (5).

The following version of co-optation is strictly weaker than (7), but slightly stronger than (8), and strong enough for our purposes:
(9) Co-optation (medium-strong version)
a. $\forall \varphi, \psi$ : if $\varphi \succeq \psi$, then $g(\varphi) \geq g(\psi)$, and
b. $\exists \varphi, \psi: \varphi \succ \psi$ and $g(\varphi)>g(\psi)$.

This says that, as you go down a series of propositions lined up by increasing strength, goodness never decreases and increases at least once. Let's apply this to our first puzzle:
(10) a. It's good that 200 people survived.
b. It's good that 400 people died.

According to (9a), it follows from (10a) that
(11) $\forall m \geq n: g(\llbracket m$ people survived $\rrbracket) \geq g(\llbracket n$ people survived $\rrbracket)$
(Here and in the following, $0 \leq m, n \leq 600$.) On the other hand, when applied to (10b), (9b) yields:
(12) $\exists m>n: g(\llbracket m$ people died $\rrbracket)>g(\llbracket n$ people died $\rrbracket)$
which is equivalent to:
(13) $\exists m>n: g(\llbracket m$ people survived $\rrbracket)<g(\llbracket n$ people survived $\rrbracket)$

It will be clear that (11) and (13) contradict each other.
The third puzzle (I leave the second one for last) was to explain how the following statements can be consistent, and even synonymous:
(14) a. It's good that more than 200 people survived.
b. It's good that fewer than 400 people died.

If co-optation applies, (14a) gives rise to the following inferences:

```
\(\forall m \geq n:\)
    \(g(\llbracket\) more than \(m\) people survived \(\rrbracket) \geq g(\llbracket\) more than \(n\) people survived \(\rrbracket)\)
\(\exists m>n\) :
    \(g(\llbracket\) more than \(m\) people survived \(\rrbracket)>g([\) more than \(n\) people survived \(\rrbracket)\)
```

As it turns out, co-optation yields exactly the same inferences for (14b). Hence, (14a) and (14b) are equivalent even on the assumption that cooptation applies. Of course, the reason why this outcome is so markedly different from the previous example is that "fewer than" reverses the quantitative ordering on the comparison set associated with "good".

The last remaining puzzle is to explain how (16a) and (16b) manage to be compatible:
(16) a. It's good that 200 people survived.
b. It's bad that 400 people died.

It is instructive to compare this pair to the following examples with nonevaluative gradables:
(17) a. ?Harry is short and tall.
b. Harry is tall for a pygmy but short for a volleyball player.

Whereas it is quite difficult to interpret (17a) as non-contradictory, a plausible construal is readily available for (17b), presumably because the speaker indicates that he is juxtaposing two different measures of height, which he achieves by introducing two different comparison sets. It would be appealing to suppose that a similar shift in perspective distinguishes (16a) from (16b): the same state of affairs is good under one aspect and bad under another. However, if the embedded clauses in (16a) and (16b) are truth-conditionally equivalent, it would seem that the same comparison set is involved in both cases. So how can there be a shift in perspective? The answer, I would like to suggest, is that co-optation makes the difference, for it will induce, in effect, two separate scales on a single set of propositions. (16a) and (16b) evaluate the same state of affairs, but with respect to different backgrounds: in the former case, the statement is relative to a scale of propositions that are ordered from least good to best; in the latter, the same propositions are ordered from least bad to worst.

Having shown how co-optation might help to explain the interpretation of evaluative predicates, it is time to ask ourselves what exactly the status of this principle might be. To begin with, let us consider the possibility that co-optation is somehow hardwired into the semantics of "good",
"bad", and related expressions. There are reasons for doubting that this is right. First, as noted at the outset, the construals we've been dealing with aren't always mandatory. In order to take this into account, we would probably have to assume that evaluative predicates are semantically ambiguous between a co-optative and a non-co-optative meaning, which is not an attractive prospect. Secondly, no matter which version of co-optation we adopt, if it was to apply across the board we would predict that evaluative predicates are downward entailing, which doesn't seem correct. To explain, suppose the semantics of "good" is such that "It's good that $\varphi$ " is true iff $g(\varphi)>s$, where $s$ is a given standard of goodness. Then even the weakest version of co-optation implies that "It's good that ..." is a downward-entailing environment:
(18) If $\varphi$ is entails $\psi$, then "It's good that $\psi$ " entails "It's good that $\varphi$ ".

This prediction is dubious, though I should like to note that we must be careful to reject it for the right reasons.
(19) It's good that Edna was found.
$\Rightarrow$ It's good that she was found with a bullet hole in her forehead.
Even if this inference is patently invalid, this doesn't prove that "good" isn't downward entailing. Assuming that the interpretation of "good" is dependent on the comparison set associated with its clausal complement, it is quite likely that the comparison set associated with "Edna was found" will be different from that associated with "Edna was found with a bullet hole in her forehead." Therefore, it is practically inevitable that there will be a shift in perspective when we proceed from the premiss in (19) to the conclusion. Besides, sequences like "It's good that $\varphi$, and therefore it's good that $\psi^{\prime \prime}$ will tend to be infelicitous in any case, simply because "good" is factive. In order to test for the monotonicity properties of "good", it is better to use a non-factive construction and clausal complements that differ from each other merely in quantity:
(20) It would be good if you ate more than 3 apples per week.
$\Rightarrow$ It would be good if you ate more than 5 apples per week.
Now, this looks plausible enough, but then one realises that:
(21) It would be good if you ate more than 3 apples per week. $\nRightarrow$ It would be good if you ate more than 300 apples per week.

That "good" is not downward entailing is confirmed by the observation
that it doesn't license negative polarity items:
(22) *It's good that there is any cauliflower left.

If "good" isn't downward entailing, maybe it is upward entailing? This, too, is doubtful:
(23) It would be good if you ate fewer than 300 apples per week.
$\nRightarrow$ It would be good if you ate fewer than 3 apples per week.
Hence, "good" appears to be non-monotonic. This conclusion is in line with the following thought experiment. Edna is a great fan of strawberries, but values them most when they come in multiples of 12 , and then she doesn't mind if she has $12,24,36$, etc. Hence, Edna's goodness function for strawberries (or rather, for having strawberries) might look like this:


Not that this is a particularly likely scenario, but that is as it may be, as long as we can agree that it is possible in principle. Now Edna says:
(24) It would be good if I had 24 strawberries.

Given Edna's peculiar predilection for multiples of 12, her statement does not entail that it would be even better if she had 25 strawberries, nor does it entail that it would be worse if she had 12 .

The moral of the foregoing discussion is that the lexical meaning of "good" doesn't seem to impose any hard constraints on possible goodness functions. However, even if there are no hard constraints, there may well be soft constrains. In fact, I would like to suggest that goodness functions have a default profile:
(25) Prototypical goodness functions

Let $\mathrm{P}=\varphi_{0} \ldots \varphi_{k}$ be a sequence of propositions aligned according to some quantitative ordering $\preceq$, and $0<i \leq j \leq k$ (so, possibly, $i=j$ and/or $j=k$ ). Then a prototypical goodness function for P consists of three subfunctions $g, g^{\prime}$, and $g^{\prime \prime}$, such that:

- $\operatorname{dom}(g)=\varphi_{0} \ldots \varphi_{i}$ and $g$ is increasing,
- $\operatorname{dom}\left(g^{\prime}\right)=\varphi_{i+1} \ldots \varphi_{j}$ and $g^{\prime}$ is constant,
- $\operatorname{dom}\left(g^{\prime \prime}\right)=\varphi_{j+1} \ldots \varphi_{k}$ and $g^{\prime \prime}$ is decreasing.

Hence, the initial segment of a prototypical goodness function goes up, and then it may level off (if $g^{\prime}$ is non-empty), and may even take a dive (if $g^{\prime \prime}$ is non-empty). A function meeting these specifications could have one of the following contours, for example:


It seems to me that this covers the range of possibilities that readily come to mind when one considers what a goodness function might look like and there isn't much in the way of specific information to go on. In short, this seems like a plausible default to me.

A further assumption that I believe is natural to make is that, by default, if a goodness function has a hanging tail, then the tail will be ignored. For instance, if a speaker says:
(26) It would be good if you ate more than 3 apples per week.
then the hearer is not normally expected to take into account the fact that there is an upper limit to the number of apples that is good for her, even if this is evidently true.

If this story is correct, it follows that, by default, the co-optation assumption holds (though perhaps only within limits), but it doesn't follow that "good" is monotonic. Which would seem to be just the right mix of properties.

To conclude, let me try to say a bit more about the rationale behind co-optation. It has often been remarked that our species has a penchant for establishing connections. If a kangaroo escapes from the local zoo and a few days later another kangaroo does the same, we will immediately wonder whether there might be a connection. Similarly, if a speaker places two events side by side, like this:
(27) Edna fell. Harry pushed her.
hearers will find it hard not to establish a connection. And so on and on.

Co-optation is plausibly seen, I believe, as resulting from the same drive towards coherence. If a speaker associates two orderings with the same set of objects, it is only natural to suppose that the orderings might be related somehow, especially since one of them (the qualitative one) is greatly underdetermined by literal meaning. This explains why a connection is made, not how it is made. The answer to that question, I would like to suggest, is that co-optation is rooted in world knowledge. Based on regular exposure to quantitative and qualitative scales, we arrive at the notion of a prototypical goodness function, and that is what underlies co-optation.

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# A Formal Semantics for Iconic Spatial Gestures* 

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#### Abstract

In this paper I describe a formal semantics for iconic spatial gestures. My claim is that the meaning of iconic gestures can be captured with an appropriate mathematical theory of space and the familiar notion of intersecting modification. I support this claim with the analysis of some examples extracted from an annotated corpus of natural humanhuman interaction.


## 1 Introduction

The study of gestural behaviour in human communication has recently seen a rapid development, partially increased by the possibility of incorporating this knowledge in the design of embodied artificial agents for human-machine interfaces. However, to this date, the number of attempts to specify a formal framework for the analysis of gesture has been limited, and to our knowledge the only extensive attempt in this direction is the one by Lascarides and Stone [4]. In this paper, I address the same question of Lascarides and Stone, namely what the criteria that determine the semantic "well-formedness" of a gesture are, but we take a different approach. Rather than considering gestures a discourse-bound phenomenon, I assume that they contribute to communication at the meaning level. I will employ a montagovian perspective and show how we can account for their contribution to meaning formation in a way not dissimilar to verbal language. My proposal is complementary to the one of Lascarides and Stone, providing a more precise description of the mechanism of gesture meaning determination, which is left mainly unspecified in their account.

To keep things manageable, I restrict my attention to those gestures categorized in the literature as iconic. These gestures do not have a conventionalized meaning, but their interpretation is possible in conjunction with the interpretation of the accompanying verbal sentence. They iconically represent spatial or physical properties of the entities or events under discussion, in the sense that their formal appearance is determined by the spatial properties of the individuals/events under discussion. Another property that distinguishes these gestures from other typologies is the fact that they are completely independent of the lexical items they accompany. Their distribution is not tied to specific lexical

[^90]items and similarly the lexical items they accompany are not dependent on the gestures, ruling out any deictic dimension of the gestures.

The semantics I propose is based on the notion of iconic equivalence and of intersecting modification. The former concept corresponds roughly to the relation holding between two spaces that are indistinguishable. My claim is that these two concepts are sufficient to explain a wide range of cases of gesture and speech interaction.

The paper is structured as follows: in Sect. 2 I will introduce first informally and then more precisely what I propose to be the meaning of iconic gestures; in Sect. 3 I will then outline a theory of space that capture most of the spatial information expressed in gestures and conclude in Sect. 4 by illustrating the semantics on the base of two examples extracted from an annotated corpus of spontaneous gestures.

## 2 Semantics

### 2.1 Informal Introduction

The meaning of purely iconic gestures can be analyzed in terms of two simple concepts: iconic equivalence and intersectivity. Iconic equivalence is the relation holding between two spaces that are indistinguishable when observed at a specific resolution. With resolution I mean a mathematical language that describe certain properties of a space and an associated notion of equivalence between spaces. The notion of equivalence determines the descriptive limits of the language, or equivalently the ability of the language of identifying differences in two spaces. An observation becomes then a description of a space in the mathematical language in question. For instance we can observe a space using Euclidean geometry and consider it iconically equivalent to another space if the two spaces are congruent up to rigid transformations. If we observe the same space using the language of topology we would consider it iconically equivalent to another space if there is an homeomorphism between the spaces.

The second component at the heart of the analysis of iconic gestures meaning is intersectivity. My claim is that iconic gestures can be analyzed as modifiers of the interpretation of the fragment of verbal language they accompany that contribute additional constraints to the interpretation. The constraints are expressed in terms of iconic equivalence between the space shaped by the gesture and the space occupied by the referents introduced by verbal language. The assumption is of course that a gesture combines only with semantically well-typed expressions, to which I will refer as semantic constituents.

The process of interpretation of a fragment of natural language accompanied by a gesture can then be visualized as in Fig. 1. The gesture (considered as a physical act) is interpreted as describing a spatial configuration, called an iconic space. This space is generated from the kinetic representation of the gesture by a procedure $\phi$. The exact nature of this procedure is beyond the scope of this paper as it depends mainly on contextual and pragmatic factors. The semantic constituent (a string of words) is interpreted through a standard arbitrary

## General Program

interpretation function that associates with each word an element of a montagovian frame of reference. Additionally the words of the verbal language are given an interpretation also in a spatial frame of reference. This frame is an abstract representation of the physical space in which the individuals of the discourse universe exist. The two frames are connected by a family of mappings Loc that assign to the objects of the montagovian frame the space they occupy.


Fig. 1: Combined interpretation of speech and gesture.

### 2.2 Formal Semantics

As already stated, we interpret natural language expressions and gestures with respect to two types of ontologies, or frames of reference. The first frame of reference is a classical montagovian individual-based ontology $\mathcal{F}$. This frame is defined inductively as follows:

1. $D_{\mathrm{e}} \in \mathcal{F}$, where $D_{\mathrm{e}}$ is a primitive set of individuals,
2. $D_{\mathrm{t}} \in \mathcal{F}$, where $D_{\mathrm{t}}=\{1,0\}$,
3. if $\Gamma \in \mathcal{F}$ and $\Delta \in \mathcal{F}$ then $\Gamma^{\Delta} \in \mathcal{F}$, where $\Gamma^{\Delta}$ is the set of all functions from $\Gamma$ to $\Delta$.

As it is the case in many semantic analyses of natural language I will assume that the domain $D_{\text {e }}$ presents an internal structure that identifies sub-kinds of individuals, in particular I assume a distinction between singular and plural individuals.

The second frame of reference is a spatial ontology called $\mathcal{S}$. The frame $\mathcal{S}$ is defined inductively as follows:

1. $D_{\mathrm{r}} \in \mathcal{S}$, where $D_{\mathrm{r}}$ is a primitive set of regions of a space ${ }^{1}$ equipped with some additional structure that characterizes this collection as a space (e.g.
${ }^{1}$ Equivalently we could use a point-based geometry. I choose here to use a regionbased geometry because the logical language I propose to describe iconic spaces uses regions as primitive objects.
a relation of inclusion among regions together with the property of being an open region to consider the set a mereotopology)
2. $D_{\mathrm{t}} \in \mathcal{S}$,
3. if $\Gamma \in \mathcal{F}$ and $\Delta \in \mathcal{F}$ then $\Gamma^{\Delta} \in \mathcal{F}$.

It is important to point out that in the definition of $D_{\mathrm{r}}$ the notion of space is used in a flexible way. In most cases $D_{\mathrm{r}}$ can be considered a physical space in the classical sense but, as we will see later, sometimes we need to extend this notion to include the additional dimension of time, when for example we are interpreting gestures involving actions or events.

In what follows, we will assume the usual convention of saying that elements of $D_{\mathrm{e}}, D_{\mathrm{t}}$, and $D_{\mathrm{r}}$ have respectively type $e, t$ and $r$ and that elements of any domain $\Gamma^{\Delta}$ have type $\delta \gamma$.

The two frames are connected by a family Loc of (possibly partial) injective mappings from elements of $\mathcal{F}$ to $\mathcal{S}$. The elements of Loc are indexed by their domain, so for instance we will write for the member of Loc that has $D_{\mathrm{e}}$ as its domain $l o c_{\mathrm{e}}$. This implies that for each element of $\mathcal{F}$ we will allow only one mapping. We restrict the possible members of Loc with the following conditions:

1. for all $x \in D_{\mathrm{e}}, l o c_{\mathrm{e}}(x)=r$, where $r$ is an arbitrary element of $D_{\mathrm{p}}{ }^{2}$,
2. for all $x \in D_{\mathrm{t}}, \operatorname{loc}_{\mathrm{t}}(x)=x$,
3. for all $f \in \Gamma^{\Delta}, \operatorname{loc}_{\delta \gamma}(f)=f^{\prime}$, such that $\forall x \in \Delta \cdot f^{\prime}\left(\operatorname{loc}_{\delta}(x)\right)=\operatorname{loc}_{\gamma}(f(x))$.

In this way the structure of the frame $\mathcal{F}$ is reflected in $\mathcal{S}$ through Loc, which is a homomorphism from $\mathcal{F}$ to $\mathcal{S}$. Also the types of $\mathcal{F}$ are reflected in the types of $\mathcal{S}$. These conditions have also the pleasant property of allowing us to define the family Loc by simply defining $l o c_{\mathrm{e}}$.

The meaning of an iconic gesture can then be expressed as a function that intersects an element of a domain in $\mathcal{F}$ with an element of the corresponding domain in $\mathcal{S}$ under the Loc mappings. We split the denotation of the gestures in two objects: a first object that inhabits a domain in $\mathcal{S}$ and that expresses the condition of iconic equivalence between the iconic space and the reference space, and a second object expressed in term of a combinator that intersects the gesture with the accompanying semantic constituent bridging in this way the interpretation of the two modes of communication.

The denotation of an iconic gestures is expressed as the characteristic function of a set of $n$-tuples, with $n \geq 1$, of regions such that the restriction of the space at the base of $\mathcal{S}$ to an element of this is set is iconically equivalent to the iconic space described by the gesture. Let $\rho(S, X)$ be the function that restrict the space $S$ to its sub-region $X$, let $\equiv$ be the iconic equivalence relation and let $\gamma$ be the iconic space associated with a gesture, we say that the denotation of a gesture $g$ is the following function of type $r^{n} t$ (where with $\tau^{n} \sigma$ we mean a function with $n \geq 1$ abstractions of type $\tau$ ):

$$
\begin{equation*}
\llbracket g \rrbracket=\lambda r_{1} \ldots \lambda r_{n} . \rho\left(D_{\mathrm{r}}, \bigcup_{i=1}^{n} r_{i}\right) \equiv \gamma \tag{1}
\end{equation*}
$$

[^91]The combinator on the other hand acts as a glue between the interpretation of the semantic constituent and the interpretation of the gesture. We define two combinators, the first one $C_{\mathrm{P}}$ intersecting gestures of type $r^{n} t$ with constituents of type $e^{n} t$ (predicates) and the second one $C_{\mathrm{M}}$ intersecting gestures of type $r^{n} t$ with constituents of type $\left(e^{n} t\right) e^{n} t$ (predicate modifiers). The combinators also ensure that the entities depicted in the gesture co-refer with the entities introduced by natural language

$$
\begin{gather*}
C_{\mathrm{P}}=\lambda G \cdot \lambda P \cdot \lambda x_{1} \ldots \lambda x_{n} \cdot P x_{1} \ldots x_{n} \wedge G l o c_{\mathrm{e}}\left(x_{1}\right) \ldots l o c_{\mathrm{e}}\left(x_{n}\right) .  \tag{2}\\
C_{\mathrm{M}}=\lambda G \cdot \lambda M \cdot \lambda P \cdot \lambda x_{1} \ldots \lambda x_{n} \cdot M P x_{1} \ldots x_{n} \wedge G \operatorname{loc}_{\mathrm{e}}\left(x_{1}\right) \ldots l o c_{\mathrm{e}}\left(x_{n}\right) . \tag{3}
\end{gather*}
$$

The application of $C_{\mathrm{P}}$ or $C_{\mathrm{M}}$ to a gesture results in an intersecting modifier in the sense of [2]. We can in fact prove the following two propositions:

Proposition 1. Let $G$ be the denotation of a gesture of type $r^{n} t$, then for every function $P$ of type e ${ }^{n} t$ we have that $C_{\mathrm{P}} G P=P \sqcap_{e^{n} t} C_{\mathrm{P}} G 1_{e^{n} t}$, where $\Pi_{e^{n} t}$ is the meet operation for objects of type $e^{n} t$ and $1_{e^{n} t}$ is the unit of $\square_{e^{n} t}$.

Proposition 2. Let $G$ be the denotation of a gesture of type $r^{n} t$, then for every function $M$ of type $\left(e^{n} t\right) e^{n} t$ we have that $C_{\mathrm{M}} G M=M \sqcap_{\left(e^{n} t\right) e^{n} t} C_{\mathrm{M}} G 1_{\left(e^{n} t\right) e t}$.

The fact that we require our combinators to correspond to the intersection (under the Loc mappings) of the meaning of the gesture and of the semantic constituent rules out the possibility of having combinators that combine iconic gestures with higher order constituent like generalized quantifiers. This restriction seems to be supported empirically by the fact that we were not capable of finding iconic gestures accompanying higher order quantifiers in a survey of a section of the Speech and Gesture Alignment (SAGA) corpus developed by the University of Bielefeld. ${ }^{3}$

## 3 A Logic for Iconic Spaces

In this short paper I will only sketch the spatial language that captures the spatial properties usually expressed with gestures. The language has been designed on the base of the analysis of the SAGA corpus. However it is probably impossible to give a general account of the spatial properties that we observe expressed in gestures, and for this reason the language has been designed to be flexible and allow the construction of different spatial theories for different applications. The language is inspired by various logical languages proposed in the literature, in particular the seminal analysis of Euclidean geometry by Tarski [7] and the logical interpretation of Mathematical Morphology, an image processing technique, proposed by Aiello and Ottens [1].

[^92]The language is a first order language whose intended domain is the set of sub-regions of an euclidean vector space and a set of scalars. The non-logical primitives of the language are the inclusion relation ( $\subseteq$ ) among regions, a distinguished region $\mathbf{n}$ corresponding to the points close to the origin (including the origin and) two binary operations $\oplus$ and $\odot$. The first operation $\oplus$ is defined with respect to two regions and corresponds to a generalized vector sum, known as Minkowski sum. It is defined as follows:

$$
\begin{equation*}
A \oplus B=\{a+b \mid a \in A, b \in B\} \tag{4}
\end{equation*}
$$

The second operation is defined between a scalar and a vector and is defined as follows:

$$
\begin{equation*}
s \odot A=\{s a \mid a \in A\} . \tag{5}
\end{equation*}
$$

The resulting language is capable of expressing a wide range of spatial properties. It can express mereotopological properties (inclusion, partial overlap, tangential contact, etc.). The language can express the relative position of two regions (in a categorical way) by simply adding to it a number of properly defined distinguished primitive regions. It can also express relative size and with the introduction of appropriate primitives more refined comparative relations like "taller than" or "larger than". Another type of spatial feature that the language can express and that we can observe often expressed in gestures is the orientation of the main axis of a region. More in general the language is capable of expressing many size and position independent spatial properties through the use of classes of prototypes expressed as primitive regions that are scaled and translated and then used to probe the space.

To express the notion of iconic equivalence I will adopt a weaker version of the standard relation of elementary equivalence between models. I will consider two models iconically equivalent if they satisfy the same iconic theory. An iconic theory is simply a conjunction of atomic formulae and negations of atomic formulae. In what follows I will assume that the iconic theory has been built by the following procedure. Given a space with $n$ distinguished regions (for instance the regions described by a gesture), we assign to each region a constant $\mathbf{r}_{\mathbf{i}}$ with $1 \leq i \leq n$ and we call the set of all region constants $R$. Let $D_{\mathrm{r}}$ be the set of regions in the space, and $\nu$ the interpretation function that maps every $\mathbf{r}_{\mathbf{i}}$ to the corresponding region of space, then for every $k$-ary predicate $P$ we take the Cartesian product $R^{k}$ and build the following conjunction:

$$
\bigwedge_{t \in R^{k}} \begin{cases}P(t) & \text { if } S, \nu \models P(t)  \tag{6}\\ \neg P(t) & \text { otherwise }\end{cases}
$$

The iconic theory is obtained by conjoining the resulting formulae.
Consequently the denotation of a gesture can be reformulated to incorporate this specific instance of iconic equivalence:

$$
\begin{equation*}
\llbracket g \rrbracket=\lambda r_{1} \ldots r_{n} . \rho\left(D_{\mathrm{r}}, \bigcup_{i=1}^{n} r_{i}\right), \nu\left[\mathbf{r}_{\mathbf{i}} \mapsto r_{i}\right] \models \Theta(\gamma) \tag{7}
\end{equation*}
$$

where $\Theta$ is the procedure described above for some fixed set of predicates.

## 4 Examples

I now analyze two examples extracted from the SAGA corpus. Beside illustrating the proposed semantics, the examples are meant to show the deep interaction between natural language semantics and gesture semantics. For this reason I selected two slightly involved cases that challenge our proposal in different ways. I will only outline the analysis of these examples: in particular I will only give an informal description of the iconic spaces associated with the gestures, as a complete formal characterization of these space would require the introduction of the complete spatial logic just sketched in Sect. 3

### 4.1 Interaction between Gestures and Plurals

The first example involves the interaction between plurality in natural language semantics and gestures. The example is taken from a dialogue between Router and Follower, the first describing the visible landmarks as seen during a bus ride. In the fragment we are interested in Router is describing a church with two towers. The speaker utters the sentence die [...] hat zwei Türme ("that [...] has two towers") with an accompanying iconic gesture roughly synchronized with the noun-phrase zwei Türme. The gesture is depicted in Fig. 2 together with the associated iconic space.


Fig. 2: Gesture accompanying the utterance die [...] hat zwei Türme and its associated iconic space

As a first step we need to define the semantics the constituent zwei Türme. To give a proper treatment of the plural Türme I assume the fairly standard

[^93]extension of the montagovian frame $\mathcal{F}$ discussed in Sec. 2 consisting in the introduction of sum individuals (see [5]). The sum individuals are members of the type $e_{+}$and we can know their cardinality with the function $|\cdot|$ and extract from them the individuals that compose them with a number of projection functions. I also assume a standard interpretation of a numeral like zwei as a function of type $\left(e_{+} t\right) e_{+} t$ that restrict a set of sum individuals to the subset composed by the elements with the correct cardinality (see [3]). The denotation of zwei Türme corresponds then to the set of sum individuals that have cardinality equal to 2 and that are the sum of individuals that are towers.

The proposed semantics seem inadequate to analyze this example because the number entities introduced in the verbal language does not match the number of regions depicted by the gesture ( 1 vs 2 ). However the gesture is combined in this case with a constituent referring to a plural individual and thus we can simply refine our semantics to take into account the refined individuals ontology. We extend the definition of Loc in such a way that the spatial projection of a sum individual is the tuple of the spatial projections of its composing atoms. So we say that for all $x \in D_{\mathrm{e}_{+}}, l o c_{\mathrm{e}_{+}}(x)=\left\langle r_{1}, \ldots, r_{n}\right\rangle$, where $n=|x|, x$ is the result of summing $x_{1}, \ldots, x_{n}$ and for $1 \leq i \leq n$ we have that $l o c_{\mathrm{e}}\left(x_{i}\right)=r_{i}$. We also need to introduce a combinator of type $\left(r^{n} t\right)\left(e_{+} t\right) e_{+} t$ to intersect the interpretation of a gesture with a plural predicate:

$$
\begin{equation*}
C_{\mathrm{P}_{+}}=\lambda G \cdot \lambda P \cdot \lambda x \cdot P x \wedge G \pi_{1}\left(l o c_{\mathrm{e}_{+}}(x)\right) \ldots \pi_{n}\left(l o c_{\mathrm{e}_{+}}(x)\right) . \tag{8}
\end{equation*}
$$

The resulting interpretation for the noun-phrase accompanied by the gesture is the following:

$$
\begin{equation*}
\lambda x .|x|=2 \wedge \text { towers } x \wedge \rho\left(D_{\mathrm{r}}, r_{1} \cup r_{2}\right), \nu\left[\mathbf{r}_{\mathbf{1}} \mapsto r_{1}, \mathbf{r}_{\mathbf{2}} \mapsto r_{2}\right] \models \Theta(\gamma) \tag{9}
\end{equation*}
$$

where the theory $\Theta(\gamma)$ could describe for instance a space with two disconnected, vertical regions, possibly with a certain shape (e.g. a prism-like shape rather than a cylindrical one).

### 4.2 Gestures in the Space-Time

Quite often gestures accompany description of actions, for example by exemplifying the trajectory of a movement. The following example is aimed at showing how we can treat time in iconic gestures. My claim is that for the purposes of determining the meaning of a gesture depicting an action or an event we can consider time as an additional dimension in our spatial ontology. A realistic spatio-temporal ontology would also require additional restrictions that rule out impossible situations like objects that move with infinite velocity or that cease to exist for a certain period of time, but for the goal of demonstrating how the semantics can cope with time related issues the simple addition of time as an unrestricted dimension will suffice.

The example is taken from the same portion of the SAGA corpus. In this case Router explains how the bus ride goes around a pond. Router utters the sentence du fährst um den Teich herum ("you drive around the pond") accompanied by the
gesture presented in Fig. 3. We represent the iconic space as a three dimensional space in which the vertical dimension represents time. The time dimension is "sliced" into instants to show that each instant is in itself a two dimensional space. The cylindrical region in the middle represents the constant position of the pond while the arch formed of squares represents the different positions occupied by the bus at different instants.


Fig. 3: Gesture accompanying du fährst um den Teich herum and corresponding iconic space

The analysis of this example is in all ways similar to the analysis of the previous one. In this case I assume that the gesture combines with the predicate fährst ... herum extended by the locative preposition um. ${ }^{5}$ The meaning of the gestures is represented as the characteristic function of a set of pairs of regions such that one represents a static circular bi-dimensional object and the other an object moving in time with and arc-like trajectory. The two regions moreover are located in the space in such a way that the circular one is roughly at the center of the trajectory followed by the other region. The set of regions satisfying these constraints is then intersected with the set of pairs of individuals corresponding to the denotation of the preposition um applied to the predicate fährst ... herum, i.e. the set of pairs of individuals such that the first one drives around the second one. In this way the referents introduced by the pronoun du and by the definite description den Teich are shared by the verb and the gesture resulting in the intuitive meaning that we would associate with this speech and gesture exchange.

[^94]
## 5 Conclusion

I presented a formal semantics for iconic gestures capable of capturing what is conceivably the meaning of iconic gestures. At the moment of writing I have implemented this semantics in a speech and gesture generation prototype that can produce simple descriptions of static and dynamic space configurations that are then rendered using an animated conversational agent. I have also started testing experimentally the assumption that gesture meaning is combined with the propositional meaning of verbal language. At the same time I am also extending the semantics to treat different types of gestures in order to provide a more uniform perspective on the way verbal language is augmented by non-verbal means.

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# On the scopal interaction of negation and deontic modals 

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#### Abstract

In this paper we argue that the different scopal relations that deontic modal auxiliaries cross-linguistically exhibit can be explained by assuming that (i) polarity effects arise in the domain of universal deontic modals and therefore not in the domain of existential deontic modals; and (ii) that all deontic modals must be interpreted VP in situ if their polarity requirements allow for that.


Keywords: Negation, Deontic Modality, Negative Polarity Items, Positive Polarty Items, Negative Quantifiers

## 1 Introduction

### 1.1 The data

Universal deontic modals come about in different kinds: English deontic must, ought and should scope over negation. On the other hand, have to, need to and need (without to) scope under negation. Need is a clear Negative Polarity Item (NPI) and may thus not appear in non-negative sentences.

| (1) | a. | John mustn't leave | $\square>\neg$ |
| :--- | :--- | :--- | :--- |
|  | b. | John oughtn't to leave | $\square>\neg$ |
|  | c. | John shouldn't leave | $\square>\neg$ |
| (2) | a. | John doesn't have to leave | $\neg>\square$ |
|  | b. | John doesn't need to leave | $\neg>\square$ |
|  | c. | John need'(n't) leave | $\neg>\square$ |

Unlike universal deontic modals, existential deontic modals may only appear under the scope of negation, as is shown below for may and can:
(3)
a. John cannot leave

$$
\neg>0
$$

b. John may not leave $\quad>0$

This pattern is not unique for English. In fact, to the best of our knowledge, this pattern (universal deontic modals can either scope over or under negation; existential ones can only scope under negation), applies to all languages that exhibit universal and existential modals. Spanish deber and tener for instance, behave on a par with English must and have to, in the sense that deber outscopes negation, whereas tener does not. Given that the Spanish negative marker no is always attached to the left of the finite verb, this shows even more that the observed pattern must reduce to properties of the modal verbs rather than their structural position with respect to negation at surface structure.

$$
\begin{array}{lll}
\text { a. } & \text { Juan no debe salir } & \square>\neg \\
\text { b. } & \text { Juan no tiene que salir } & \neg>\square \tag{4}
\end{array}
$$

In German, things are slightly different: sollen ('should') behaves like English should and outscopes negation; brauchen ('need to') is an NPI comparable to English need; and müssen ('must'), like English have to, scopes under negation. There is no modal verb with the meaning of English must/have to that can outscope negation. Existential deontic modals (e.g. dürfen ('may')), finally, always scope under negation

| a. | Hans soll nicht abfahren | $\square>\neg$ |
| :--- | :--- | :--- |
| b. | Hans braucht *(nicht) zu abfahren | $\neg>\square$ |
| c. | Hans muss nicht abfahren | $\neg>\square$ |
| d. | Hans darf nicht abfahren | $\neg>0$ |

In Dutch, things are also different, but still fall under the generalization that we formulated above. For most speakers the verb moeten ('must') outscopes negation and the NPI hoeven ('need') is under the scope of negation:

| a. | Jan moet niet vertrekken | $\square>\neg$ |
| :--- | :--- | :--- |
| b. | Jan hoeft *(niet) te vertrekken | $\neg>\square$ |

Finally some languages allow ambiguity with respect to the interpretation of universal deontics. Russian for example has two ways of combining negation with a universal deontic adjective (modal verbs are lacking in the language). Whereas the first reading (a) is one where negation unambiguously scopes over modality, the reading in b , where dolzhna ('obliged') has been fronted under focus is allows both scopal orders.

[^95]Although the cross-linguistic overview is far from complete, the picture that emerges is that languages are uniform in their scope-internal relation between existential deontic modals and negation, but that languages allow different scopal relations between negation and universal deontic modals depending on which modal element (verb/adjective) is taken.

### 1.1 Questions

The pattern above obviously calls for an explanation and therefore the two following questions need to be addressed:
a. What determines the scopal properties of universal deontic modals with respect to negation?
b. Why do existential deontic modals always appear under the scope of negation?

In the rest of this paper we will address these questions and argue that the scopal behaviour of deontic modals follows form independently motivated assumptions concerning (i) the status of polarity items and (ii) the possible positions of interpretation of lexical elements in the tree.

## 2 Previous proposals

The scopal relations between modals and negation has been observed and studied by a number of scholars, most notably [1], [2], [3], [4], [5] and [6]. In this section we will discuss and evaluate two proposals, which are quite similar in nature.

### 2.1 Cormack \& Smith (2002)

According to Cormack and Smith [4], there are two positions for modals, Modal1 and Modal2, and (sentential) negation scopes in between them.


Cormack and Smith adopt the following assumptions: (i) the scopal order between modal types is derived by semantic / conceptual necessity (though their formulation of this is not quite clear), i.e. the fact that epistemic modals scope over deontic does not follow from any syntactic principle; (ii) it is a property of syntax that there are
two possible positions for modals, one above and one below negation (the position that the negative marker occupies); and (iii) which specific modals go in Modall and which in Modal2 is lexically specified and therefore idiosyncratic in nature.

John doesn't have to leave
[John [NegP doesn't [Mod2P have to leave]]] $\quad \neg>\square$
(11) John mustn't leave
[John [ModiP must [NegP n't [vp leave]]] $\quad \square>\neg$
... dass Hans nicht abfahren muss
[CP dass Hans[NegP nicht [Mod2P [ ${ }_{\mathrm{vP}}$ abfahren] muss]]]

$$
\begin{equation*}
\neg>\square \tag{12}
\end{equation*}
$$

However, this analysis faces several problems. Although the assumption that the epistemic > deontic ordering is semantically / conceptually necessary, the necessity of the split between Modal1 and Modal 2 is less plausible. First in many languages there is no syntactic evidence for two different positions. This is illustrated for Spanish below. (Note that this may not be derived from movement of the negative marker no, as generally the surface position of the negative marker no always corresponds to its LF position.)
(13) a. Juan no debe salir $\quad>\neg$
b. Juan no tiene que salir $\quad \neg>\square$

Secondly, it remains unclear why only deontic universals modals allow for a lexical split. Why couldn't deontic existentials be analysed as Modal1? Cormack and Smith argue that children start out with a learning algorithm that takes all (deontic) universals to be Modal1 and all existentials to be Modal2 and that children may reanalyse some Modal1's as Modal2's if the language input forces them to so (e.g. need is reanalysed from Modal 1 to Modal2). But why couldn't a Modal2 be reanalysed as a Modal1?

### 2.2 Butler (2003)

Butler's analysis [5] is similar in spirit to [4]. He also derives the scopal properties from a universal syntactic template. For that he distinguishes between different functional projections for epistemic and root modals as well as different functional projections for existential and universal modals. Butler's analysis follows Cinque's/Rizzi's cartographic approach in the sense that all scopal properties reflect a universal basic structure. For negation and modality that is:

$$
\begin{align*}
& \text { EpistNecP }>(\text { NegP })>\text { EpistPosP }>\text { (strong) subject }>\text { RootNecP }>\text { NegP }>  \tag{14}\\
& \text { RootP }>\mathrm{vP}
\end{align*}
$$

Under Butler's proposal it follows immediately that all epistemic deontic modals take scope under negation, whereas a deontic universal like must outscopes negation.

However, it becomes unclear now why some deontic universals may not outscope negation, such as English have to or German müssen. Although Butler only briefly addresses this question, the only way to deal with such examples is to posit that the negative marker in those cases is in the higher NegP. However, such a solution introduces new problems as well. First, it becomes unclear again why other modals, such as must, may not be outscoped by such a high negation and secondly, it predicts that in all cases where negation outscopes have to (or any other deontic modal that scopes under negation), it also outscopes the subject. However, this predictions is too strong as it incorrectly rules out cases such as (15):

Many people don't have to work
'There are many people who are not required to work'

Finally it should be noted that this solution reduces the syntactic approach that Butler proposes into a lexical idiosyncratic approach as well: it needs somehow to be lexically encoded which position negation occupies when combined with a deontic universal. It is however unclear what kind of a mechanism could be responsible for that.

## 3 Analysis

In order to overcome the problem that approaches that are built on syntactic templates face, we argue instead that the scopal behaviour of deontic modals results from their lexical semantic properties, in casu their polarity properties. In accordance with two additional assumptions concerning the locus of interpretation of negative and deontic modal elements, we argue that all discussed facts follow directly.

### 3.1 Neutral and polar modals

As discussed before, the domain of (universal) deontic modals is one where NPI specifications hold.
(16) a. Sue need $*($ not $)$ leave.
$\begin{array}{ll} & \neg>\square \\ \text { Dutch } \quad \neg>\square\end{array}$
b. Je hoeft dat *(niet) te doen

German $\neg>\square$
c. Du brauchst dass *(nicht) zu tun

You need.NPI that (NEG) to do
'You don't need to do that'

Since NPIs surface in the domain of deontic modality, we should also expect there to be Positive Polarity Items (PPIs), as any domain that has one of these classes also exhibits the other class (quantifiers over individuals, adverbs, etc.). Adopting the presence of PPI's in the domain of deontic modals, the scopal properties of English
must, should, ought are already captured as these elements necessarily scope over negation. ${ }^{1}$

Finally, it should be noted that not all deontic modals are polarity items. English have to or German müssen can occur in positive sentences (hence they are not NPIs) and they appear under the scope of negation in negative sentences (hence they are not PPIs). This class of modals are referred to as 'neutral deontic modals'

At the same time, for reasons that we do not understand, no NPIs surface in the domain of deontic existential modals. On the basis of the same type of reasoning we applied above, no PPI deontic existential modal is expected to surface either, a prediction that to the best of our knowledge is borne out.

The landscape of deontic modals thus looks as follows:


### 3.2 Deontic modals and negation

However, this specification of deontic modals in terms of their polarity properties does not suffice to account for the scopal behaviour that deontic modals exhibit. It only explains the fixed scopal properties of NPI/PPI modals with respect to negation, but not the scopal relations between neutral deontic modals and negation. I.e. why does have to always scope under negation (and is that really always the case)?

Let us make the following two assumptions: (i) negation never lowers at LF: it is interpretated in its surface position and may only raise to a higher position at LF if it moves along with another, independently, raising element; (ii) deontic modals are base-generated VP-in situ. The first assumption is uncontroversial; the second, however, is not.

Received wisdom has it that in English these (and other) modals are base-generated in $\mathrm{I}^{0}$ (Dutch and German modals e,g, are generally assumed to be base-generated inside VP). If so, then there is no position for them to reconstruct to under negation. But is received wisdom correct in this case? The argument for generation in $I^{0}$ stems from the fact these modals always appear in $I^{0}$. Such modals are taken to differ in two ways from regular verbs: they only come in tensed forms and they are generated in $I^{0}$. However, only the first of these characterizations is needed, as it by itself derives the second one. We know that these deontic modal auxiliaries are moving verbs since they can make it up to $\mathrm{C}^{0}$ :

[^96]If these modals are movers, and if they are always tensed, then it follows that if they are generated in a VP, they will always move to at least $\mathrm{I}^{0}$. In short, this view is as consistent with the facts as the generation-in- $\mathrm{I}^{0}$ view is, and, as we will see, it is superior to the latter in getting the facts with one fewer special assumption about modals.

The only difference between deontic modals being base-generated in $\mathrm{I}^{\circ}$ and being base-generated inside VP is that in the latter case, these modals are taken to be lexical verbs and therefore they must be interpreted in their base position as well.

On the basis of these assumptions all facts follow naturally. Let's discuss first the examples in (1)-(3), repeated as (19)-(21) below:

| a. | John mustn't leave | $\square>\neg$ |
| :--- | :--- | :--- |
| b. | John oughtn't to leave | $\square>\neg$ |
| c. | John shouldn't leave | $\square>\neg$ |

Must, ought and should are base-generated VP in situ, and thus in a position lower than negation. However, since they are PPIs, their appearance under negation would make the sentences crash at LF and therefore, as a last resort option, these modals are interpreted in a higher head position to which they have moved in order to check their tense features and where they outscope negation.

| (20) | a. | John doesn't have to leave | $\neg>\square$ |
| :--- | :--- | :--- | :--- |
|  | b. | John doesn't need to leave | $\neg>\square$ |
| c. | John need*(n't) leave | $\neg>\square$ |  |

In (20) the same story applies, except for the facts that these modals, being neutral or even NPIs, do not render the sentence ungrammatical if they are interpreted in their base position, which is lower than negation. Therefore there is no proper trigger that could force them to raise across negation and the only reading these sentences receive is one where negation outscopes the modal.

| (21) | a. John cannot leave | $\neg>\diamond$ |
| :--- | :--- | :--- | :--- |
| b. | John may not leave | $\neg>\diamond$ |

Since there are no polar deontic existential modals all deontic existentials are neutral and remain to be interpreted at their base position, just like the cases in (20).

The Spanish facts are also covered, as the PPI modal deber will be forced to raise to a higher position at LF, whereas no such trigger exists for 'tener', which will therefore remain in its surface position at LF.

| (22) | a. | Juan no debe salir | $\square>\neg$ |
| :--- | :--- | :--- | :--- |
|  | b. | Juan no tiene que salir | $\neg>\square$ |

Now, let's consider the German cases:

| a. | Hans soll nicht abfahren | $\square>\neg$ |
| :--- | :--- | :--- |
| b. | Hans braucht *(nicht) zu abfahren | $\neg>\square$ |
| c. | Hans muss nicht abfahren | $\neg>\square$ |
| d. | Hans darf nicht abfahren | $\neg>0$ |

Note that German exhibits V2 in main clauses. However, V2 does not change the position where lexical verbs are interpreted in general. In this sense, V2 is to be considered a PF phenomenon. At LF, lexical verbs are still present at their base position. Sollen is a PPI and thus raises across negation at LF. Brauchen on the other hand is an NPI and will thus remain in situ (there is no trigger for raising; in fact the presence of such a trigger would violate its NPI licensing conditions). Müssen is neutral and won't raise at LF either. Dürfen, finally, is an existential and therefore neutral as well: hence $\neg>\square$.

Finally, the Russian examples need to be discussed. In the natural cases, negation outscopes the modal adjective dolzhna ('obliged'), so it cannot be analysed as a PPI modal. However, as an instance of constituent negation and being focussed it may outscope negation. This is the case in (24)b, which is ambiguous. Note that this is not a regular case of Russian sentential negation (as the auxiliary byla ('was') is not preceded by a negative marker). The question thus rises why this adjective may outscope negation. One possible solution is that it is an instance of metalinguistic negation, comparable to (25), but the exact analysis of (24)b is still subject of further study.
(24) a. Masha ne byla dolzhna chitat' knigu $\quad \neg>\square$

Masha neg was obliged read book
b. Masha ne DOLZHNA byla chitat' knigu $\quad \neg>\square ; \square>\neg$
Masha neg obliged was read book
(25) It's not that you don't NEED to read those books, you MUST not read those books!

### 3.3 Deontic modals and negative DPs

Another puzzle concerning the interaction between (deontic) modals and negation concerns the ambiguity of neutral modals with respect to Negative DPs, as has been observed by Iatridou \& Sichel [6]:
[6: 11]

| Type of Modal wrt sentential negation | Interpretive possibilities of (Negative component of) NegDP |
| :---: | :---: |
| Mod>Neg | Mod > Subject $_{\text {Neg }}$ |
|  | Mod $>$ Object $_{\text {Neg }}$ |
| Neg $>$ Mod | Subject $_{\text {Neg }}>$ Mod |
|  | Object $_{\text {Neg }}>$ Mod |
|  | Mod $>$ Object $_{\text {Neg }}$ |

While neutral and NPI modals behave similarly w.r.t. sentential negation, they behave differently with negation inside NegDPs. Iatridou \& Sichel show that neutral modals scope under a NegDP in subject position but are ambiguous with respect to a NegDP in object position:

## (27) a. Nobody has to/needs drive.

$$
\neg \rightarrow
$$

$\rightarrow>$
b. He has to/needs to do no homework tonight. $\quad \neg>\square$ (pref.)
c. In order to see how other people live, he
has to/needs to get no new toys for a while. $\quad \square>\neg$
However, an NPI modal will scope under negation no matter where that negation is. English NPI need is not sufficiently part of colloquial English for reliable judgments, but for German neutral DM müssen versus NPI brauchen, the facts are very clear: while müssen behaves exactly like English have to/need to in (27), brauchen is fine only in (28)a-b; in (28)c the intended reading is impossible to yield with brauchen:

| a. | Keiner muss/braucht (zu) fahren | $\neg>\square$ |
| :---: | :---: | :---: |
|  | Noone muss/braucht leave |  |
| b. | Er muss/braucht keine hausarbeiten (zu) machen | $\neg>\square$ |
|  | He muss/braucht no homework do |  |
| c. | Um zu sehen, wie andere leben, muss/*braucht er eine |  |
|  | Zeitlang keine neuen Geschenke (zu) bekommen | $\square>$ |
|  | In order to see how other people live, he muss/*bracht to get no new toys for a while |  |

These facts immediately follow from the presented analysis that takes modals such as English have to and German brauchen/muessen to be interpreted in their base position. Since objects are in the complement of the modal verb, they allow for an interpretation where the neutral modal outscopes them, but as these Negative DPs are able to undergo quantifier movement, the negation is able to outscope the modals as well. Subject Negative DPs, on the other hand, already at surface structure outscope the neutral modal, which therefore can never be put in a position where it outscopes the negation. Note that since NPI modals must be under the scope of negation, in these cases the narrow scope reading of the object is never available.

## 4. Conclusion and discussion

In the beginning of this paper we addressed two questions:
(30) a. What determines the scopal properties of universal deontic modals with respect to negation?
b. Why do existential deontic modals always appear under the scope of negation?

In this talk we argue that once it is adopted that (i) modals that always outscope negation are PPIs, (ii) only deontic universal modals exhibit polarity effects (there are no PPI/NPI deontic existentials), deontic modals are lexical verbs (sometimes in disguise), and (iv) negation does not lower at LF, all known facts concerning the scopal behaviour of deontic modals with respect to negation naturally follows.

In this talk we have applied this analysis to a small number of languages and we have shown how on the basis of these assumptions we could derive the attested facts.

However, a number of questions remain open. First, it remains unclear how polarity effects are acquired, i.e. how does the child know that must is a PPI and need an NPI? This is not a question that is specific for this analysis, but rather a general question for anyone trying to understand how any polarity items are acquired.

Second, why is it the case that only deontic modals exhibit polarity effects? In other words, why is the triangle in (17) a triangle?

Third, it is not really clear how to deal with the Russian cases of ambiguity. Note that since this analysis is based on PPI-hood as a trigger for LF movement, the proposal is generally not at ease with these kinds of ambiguities

Fourth, under this analysis it is assumed that that Negative DPs may undergo (some kind of) quantifier raising. It is a known fact, however, that Negative DPs do not outscope higher quantifiers (i.e. give rise to reverse readings). Take for instance CC.

$$
\begin{array}{ll}
\text { Everybody touched no desert } & \forall>\neg \exists ; * \neg \exists>  \tag{31}\\
\forall &
\end{array}
$$

However, what we assume (31) shows is that the relative scopal ordering of two quantifiers remains frozen. It does not show that no desert is forbidden to raise across the subject, as long as the is raises again across the object again. So (31) does not count as a proper counterargument against a QR analysis of negative DPs. The more general question as to what blocks the inverse reading in (31) remains an open question though.

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# Projective Meaning and Attachment 

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#### Abstract

This paper examines the possibility of providing a unified account of the projection properties of presuppositions, conventional and conversational implicatures. I discuss the solution offered in (Roberts et al. 2009) and show that the central notion we need to cover the spectrum of observations is that of attachment.


## 1 Introduction

The most basic observations about presuppositions concern what is called their projection behaviour. Roughly speaking, a presupposition can be characterised as an entailment which is able to project. A sentence $S$ presupposes a proposition $\phi$ whenever S entails $\phi$ and certain 'suitably modified' versions of S entail $\phi$ (projection). The 'suitably modified' qualification encompasses negation, interrogation and a variety of embeddings. For instance, Mary knows that Paul cheated on the exam and its modified versions Mary does not know / Does Mary know that Paul cheated on the exam preserve the presupposition that Paul cheated.

Projection is not automatic. It depends on context and on the properties of embedding. A less well-known property concerns the limitations on attachment. Ducrot (1972) had noted that it is difficult to attach a discourse constituent to a presupposition. For instance, the only possible meaning of (1) is that Paul does not cheat (asserted content) because he was behind in his work. The probably more natural interpretation that Paul was in the habit of cheating (presupposed content) because he was always behind cannot be construed.
(1) Paul has stopped cheating on exams because he was always behind in his work

The question naturally arises whether these two properties can be unified in some way and perhaps ultimately viewed as two sides of the same coin. In the next section, I describe in more detail the symmetry between projection and attachment constraints. In section 3, I present the approach of Roberts et al. (2009) and highlight the possibility of deriving from it attachment constraints, which are shown to have a clear experimental reflection in section 3.2. Finally, in section 4, I show that attachment is a more fundamental notion to analyse the interaction between discourse and projection.

## 2 Extending the Symmetry between projection and attachment

There is little doubt that presuppositions tend to project and do not provide a natural attachment site. Roberts et al. (2009) suggest that projection extends to conventional implicatures (CIs) and to certain conversational implicatures (cis). For instance, they borrow from Chierchia and McConnell-Ginet the observation that non-restrictive relative clauses project. (2) would be a case of CI projection because (i) it entails that Paul cheated on the exam and (ii) according to Potts (2005), such clauses trigger a CI.
(2) a. Paul, who has cheated on the exam, might be dismissed
b. Do you think that Paul, who has cheated on the exam, might be dismissed?

Cases of ci projection have been discussed in particular in (Simons 2005). Consider (3) (Simon's example 27). Answer B1 makes sense only if one assumes some sort of negative connection between rain and going on a picnic. This connection is preserved in B 2 variants.
(3) A - Are we going on a picnic?

B1 -It's raining
B2 -It's not raining / Is it raining?
Attachment limitations have also been investigated with a similar result. Ducrot's (1972) loi d'enchaînement ('linking law') targets presuppositions. In a nutshell, the linking law forbids any attachment to a presupposition, whether by way of a subordinating or coordinating conjunction, except for et ('and') and si ('if'), or by way of a 'logical relation'. In (Jayez 2005, Jayez and Tovena 2008), it is claimed that conventional implicatures are subject to the same limitations. For instance, in (4), the preferred interpretation is that John being unable to register for the next term is the cause of his failure. A more natural interpretation is that it is bad luck for him since he cannot register, but constructing this interpretation would involve recruiting the CI trigger unfortunately for the attachment (see Potts 2005 for evaluative adverbs and Jayez and Rossari 2004 for parentheticals).
(4) Unfortunately, Paul has failed his exam, because he cannot register for the next term

Finally, it has been noted in various works that CIs cannot provide natural targets for refutation, see (Jayez and Rossari 2004, Potts 2005). E.g. the refutations in (5) target only the asserted proposition that Paul has failed his exam, leaving aside the evaluative CI trigger unexpectedly.
(5) A - Paul has unexpectedly failed his exam

B - You lie / You are wrong / Impossible / Quite the contrary

I consider that refutation cases fall into the category of attachment limitations. In a refutation, the attempt by an addressee to attach a new constituent to a presupposition or to an implicature is bound to be perceived as artificial.

It is of course tempting to hypothesize that there is a common source behind the projection and the attachment observations, and that presuppositions, CIs and cis can be grouped into a natural class, whose members differ essentially by specific lexical profiles.

## 3 Accounting for the Symmetry: the QUD Approach

### 3.1 Basics

Recently, Roberts et al. (2009) have proposed that presuppositions, CIs and cis, which they group under the generic term of not-at-issue content, after Potts' term for CIs, share indeed a central property: they do not necessarily address the Question Under Discussion (QUD). Assuming that each discourse is organised around at least one common topic (the QUD), they offer the following principle.
(6) QUD principle All and only the not-at-issue content may project.

Two important points are to be mentioned at this stage. First, if we decide to see presuppositions and implicatures as members of a common family, it is no longer possible to attribute their common behaviour to properties that do not hold for the whole class. So, anaphoric or dynamic theories of presuppositions, whatever their merits, are not plausible candidates for unifying presuppositions, CIs and cis since, for instance, they do not make room for CIs (Potts 2005). Roberts et al. make the same point for common ground theories of presuppositions.

Second, if the QUD theory is correct, it should allow one to derive the attachment properties. Roberts et al. include the refutation test among those properties that characterise the projecting elements but they do not tackle the general question of attachments. Generalising from Potts, I assume that the semantic and pragmatic contribution of a discourse constituent can be seen as a $n$-tuple $\left\langle q, a_{1} \ldots a_{n}\right\rangle$, where the first element (at-issue content) addresses the QUD and the other ones are presupposed or implied material. Functions can extract the relevant material. If $C$ is a constituent, $A I(C)$ extracts the at-issue content of $C$, $\operatorname{pres}(C)$ the presuppositions, etc. Consider now a pair of adjacent constituents $\left(C_{1}, C_{2}\right)$ in a monologue, typically two successive sentences or clauses that convey a proposition. By using $C_{1}$, the speaker signals that she contributes to the QUD with $\operatorname{AI}\left(C_{1}\right)$. If the next constituent is connected to an element of $C_{1}$ different from $A I\left(C_{1}\right)$, the speaker abandons the QUD. In most contexts, this is an odd move because the speaker just addressed the QUD via $A I\left(C_{1}\right)$, hence the impression of a non sequitur. In dialogues, the situation is a little different since we cannot, in general, assign to participants a unique discourse strategy. It may be the case that participants disagree on certain issues. This accounts for the fact, noted by Jayez and Rossari and von Fintel (2004), that it is perfectly possible to interrupt the discourse trajectory ascribed to a participant, for instance by questioning a presupposition or a CI she endorses.

A - Unfortunately, Paul has failed his exam
B - Well, I wouldn't call that 'unfortunate' / It's not really unfortunate, you know, he's so lazy. He got what he deserves

In monologues, the price to pay for abandoning the QUD is higher since the speaker is supposed to have a coherent strategy. This is not quite impossible, however. A speaker may signal explicitly that she is abandoning the QUD with a special discourse marker such as by the way. In that case, the speaker may sound uncooperative, especially if she abruptly shifts the topic in the middle of a serious discussion, but she is not incoherent since she makes clear that she is not currently following a plan to tackle the QUD (8).
(8) Paul stopped smoking. By the way, Mary never took to smoking

There is also the (important) possibility that the non-at-issue content does address the QUD, a point to which I will return in section 4.2. In (9), B uses the double fact that Paul has been smoking and that he does not smoke as an argument in favour of her conclusion that Paul has a strong will.
(9) A - Does Paul have a strong will?

B - Generally speaking, yes. He has stopped smoking, for instance

### 3.2 Simple Experimental Evidence

One might argue that the QUD hypothesis, in its current stage, is only a clever guess. However, preliminary experimental evidence is clearly consonant with the hypothesis. If the QUD approach is right, competent speakers should process more easily an attachment to the at-issue content than to the non-at-issue content. In order to evaluate this prediction, I carried out a simple categorisation experiment.

46 French students were asked to classify 40 French two-sentence pairs as either banale (ordinary) or bizarre (weird). They were all native speakers, with an age range of 17-27 and an age mean of 20.1. The test was administered collectively (all the subjects rated the pairs together). Subjects had to read and rate pairs following the order on the test sheet and were not allowed to correct a previous choice. They were asked to run through the pair list as fast as possible. In each pair that was not a filler, the sentences were related by a consequence discourse marker (donc or alors $\approx$ 'so', 'therefore') or by a causal/justification subordinating conjunction (parce que $\approx$ 'because' or puisque $\approx$ 'since'). The pairs exploited either an at-issue or a non-at-issue linking and featured a presupposition or conventional implicature trigger in a $2 \times 2$ design. The following table shows the translations of the first five pairs with the expected answer in the last column.

| filler | trigger | connection mode | text | expected answer |
| :--- | :--- | :--- | :--- | :--- |
| yes |  |  | Max had the flu, so he stayed at home | OK |
| yes |  |  | Luc likes jam because the weather is fine | weird |
| no | almost | at-issue | Mary is almost late, so she hurries up | OK |
| no | stop | non at-issue | Paul stopped quivering, so he was cold | weird |
| no | unfortunately | non at-issue | The weather was fine, so, unfortunately, <br> Susan had work to do | weird |

The results can be analysed in several ways. In this paper, I describe only an exploration based on the Mac Nemar test for paired samples. This test is usually applied to temporal transitions of the same sample of subjects. For instance one wants to determine whether the proportion change in the value of some variable before and after a medical treatment is significant. The test can in fact be used whenever the proportions of binary responses of the same group are to be compared in two different conditions, namely two types of sentence pairs in our case. The sentence pairs (excluding fillers) were classified into different categories, according to their connection mode (at-issue or not at-issue) and the presupposition or CI triggers they contained. They were compared pairwise and the 496 resulting tests were themselves classified into different categories according (i) which mode of connection (at-issue, not at-issue with presupposition, not at-issue with CI) each pair exhibited and (ii) whether the trigger was identical in the two pairs.

The most salient observation is that, for identical triggers, there is more often a significant difference between the at-issue and non-at-issue cases and subjects preferentially reject the non-at-issue variant. There are 10 pairs (out of 13) that show a significant difference in the at-issue vs. (non-at-issue and presuppositional) comparison, and 15 pairs (out of 16) for the at-issue vs. (non-at-issue and CI) comparison. This is in agreement with the QUD approach and also with the extended version of Ducrot's loi d'enchaînement. However, individual results suggest that the difference in accessibility between at-issue and non-atissue content may vary across triggers. For instance, the seul ('only') and the $\grave{a}$ peine ('hardly') element do not fit well into this general picture. More work is needed to evaluate the import of specific properties of lexical items.

## 4 The attachment approach

In spite of its attractiveness, the QUD approach faces some problems and I will defend the view that the notion of attachment is a better candidate to address them.

### 4.1 When Contrast Steps in

The possibility of linking depends, among other things, on the discourse relation on which the linking is based. Ducrot's prohibition can be extended to conventional implicatures but concerns primarily what he called argumentative relations, that is, essentially, justification or explanation and consequence. The experimental findings reported above are based on those very same relations.

Contrast discourse markers do not give so clear-cut results. For instance, under at least one interpretation, B's answer in (10) means that, in contrast to Mary having smoked, Paul never smoked. Crucially, the at-issue content must be ignored in the contrast for it to make sense (see ??Mary does not smoke but Paul never smoked). Many analogous examples can be constructed: in (11) the linking associates the presupposition that Mary got three A's and the fact that she failed the French exam. In (12) the implicature that Mary is under twenty is involved (Jayez and Tovena 2008).
(10) $\quad \mathrm{A}$ - Do your friends smoke, in general?

B - It depends. Mary has stopped smoking but Paul never smoked
(11) A - How did Mary fare?

B - It depends. She was the only one to get three A's but she failed the French exam
(12) A - How old are they?

B - Mary is almost twenty but Paul is well over twenty
Following Umbach (2005), I assume that, in such cases, but triggers the accommodation of a quaestio, that is, an overt or abductively reconstructed question with respect to which the contrastive discourse constitutes a relevant answer. But dually connects two alternatives by asserting one and negating the other (the confirm + deny condition in Umbach's terms). A typical quaestio for $p$ but $p^{\prime}$ is 'are $p$ and $\neg p^{\prime}$ both true?'. Let us compare now (13), (14) and (15). B's answer in (13) is predictably odd since its at-issue content bypasses the QUD (whether Mary has been smoking in the past). In (14), the at-issue content of the first conjunct still bypasses the QUD, since the proposition that Mary does not smoke is hardly relevant to A's question. However, the combination of the presupposed part (Mary has been smoking) and the at-issue content of the second conjunct addresses the quaestio made explicit through A's question. (15) shows that the order of conjuncts matters. Why is it so?
(13) A - Did Mary smoke?
B - ??Mary has stopped smoking
(14) A - Did both Mary and Paul smoke?

B - Mary has stopped smoking, but Paul never smoked
(15) A - Did both Mary and Paul smoke?

B - ??Paul never smoked, but Mary still smokes
If the two conjuncts were conceived of as independent, as in an update sequence, the (14)-(15) contrast would be mysterious. I propose to represent the structures studied by Umbach as complex propositions, where the second conjunct 'maximally settles' the issue, from the speaker's point of view, that is, expresses the ultimate piece of information the speaker delivers on this particular issue at this stage. The asymmetry between the two conjuncts is captured by saying that (i) the second conjunct is attached to a new quaestio by a Question-Answer discourse relation in the most explicit cases or by a more abstract relation of

Resolution and (ii) the new quaestio takes into account the partial resolution of the initial quaestio by the first conjunct.
(16) Given a quaestio $Q$, an Umbach-structure $p$ but $p^{\prime}$ results in a Resolution type attachment of $p^{\prime}$ to the quaestio $Q^{\prime}$ obtained by eliminating the alternatives compatible with $Q$ but incompatible with $p$.
(16) captures the idea that the second conjunct is the salient resolver. If we accept that, whenever the quaestio remains implicit it is nonetheless a particular form of QUD, possibly one only the speaker is initially privy to (see Ginzburg 2009 for the epistemic treatment of QUDs), we see that the QUD intuition can be preserved in the above cases but that one has to introduce some additional attachment structure. The proposition that the speaker communicates to settle the issue raised by the QUD must depend on the at-issue content of the attached resolver. This requirement is violated in (15) because the second conjunct, that maximally settles the quaestio by selecting the alternative 'Mary smoked', does not address the new quaestio 'Granted that Paul did not smoke, did Mary smoke?' through its at-issue content.

### 4.2 The QUD Principle Revised

The problem discussed in this section is more serious. Consider (17).
(17) A - Is Paul a good partner?

B - He does not answer to mails very quickly
The preferred interpretation of B's answer is that Paul answers to mails, but not very quickly. Thus, the proposition that Paul answers to mails survives the negation and projects. However, it is difficult to say that it does not address the QUD, at least not if we consider what is relevant to the topic made salient by A's question. Similar observations hold for standard presuppositional cases. B's answer in (18) clearly presupposes that John has been smoking and this fact is strongly relevant to the main topic of John's temperament. It suggests for instance that John was unable to put a term to his addiction.
(18) A - Does Paul have a strong will?

B - Generally speaking, no. He didn't stop smoking, for instance
Note that neither with (17) nor with (18) do we base our understanding only on a general or circumstantial rule like [addiction $\leadsto$ no strong will]. It is necessary to make the fact that Paul answers to mails or that he has smoked enter the picture, in order to draw from B's answers various inferences relevant to the QUD. So, the situation cannot be reduced to the Simon's type of example we mentioned in section 2 .
(17) and (18) illustrate the possibility that information pieces which address the QUD project. Crucially, in both cases, one observes attachment limitations. E.g. it is impossible to interpret (19a) and (19b) as meaning that Paul answers to mails because he is professional and that he smoked because he liked smoking.
a. ...He does not answer to mails very quickly, because he is very professional
b. ...He didn't stop smoking, for instance, because he liked that

Such observations have two consequences. First, they show that material usually considered as implied or presupposed can address the QUD and be projected. Second, if attachment limitations were a reflection of not addressing the QUD, as I have proposed, they should disappear. In view of these problems, I propose to modify principle (6) as follows.
(20) Revised QUD principle In linguistic communication, whenever some content is conventionally marked as obligatorily interpretable with respect to the QUD, all and only the content that is not marked in this way projects.
(20) postulates that every piece of linguistic communication can come with conventionally QUD-relative content. The linguistic marking of at-issue content vs. presuppositions or CIs provides a typical case. I leave open the possibility that a linguistic item contains no conventionally QUD-relative content, as might be the case for interjections (Wharton 2003). Conventional QUD-relative content does not necessarily address the QUD, but is conventionally marked as obligatorily interpretable with respect to it. Thus, an uncooperative conventionally QUDrelative discourse constituent which abruptly 'drops' the current topic cannot be projected.

Conventionally QUD-relative content contains those elements which contribute to 'what is said' in the Gricean sense, that is, all the non-presupposed and non-conventionally implied formulae resulting from exploiting the linguistic code and assigning values to those indexical arguments that occur in the predicates of such formulae. This amounts to saying that the conventionally QUD-relative content comprises entailments and certain explicatures ${ }^{1}$ (Sperber and Wilson 1986). For instance, in (21a) the QUD relative content includes all the entailments of the proposition that it is raining at $t$, where $t$ is the value assigned to the time indexical associated with the sentence tense. In contrast, whereas the existence of a consequence relation between the rain and staying at home in (21b) is also considered as an explicature in some recent approaches (see Ariel 2008 for a survey), it is not integrated into the QUD-relative content under the present analysis. This choice is motivated in the next section, which considers the attachment problem.
a. It is raining
b. It is raining, so I prefer to stay at home

[^97]
### 4.3 Attachment Revisited

The reviewed data suggest that attachment is not uniquely context-sensitive. In fact, for at least certain discourse relations, including Explanation, Justification and Contrast, attachment may not target non QUD-relative content, even when this content happens to address the QUD, see (17), (18) and (19). This is not to be confused with a prohibition on binding. Lexical material such as pronouns or additive discourse markers (see Winterstein 2009 for too) can be bounded to non QUD-relative content. I propose that attachment limitations are related to the independence of QUD-relative and non QUD-relative content. Consider the well-known 'sister' example discussed by Stalnaker.

## (22) I have to pick up my sister at the airport

In a DRT-based treatment (Geurts 1999), (22) asserts that the speaker S has to pick up $x$ at the airport and presupposes that $x$ is a sister of the speaker. The net result is a set of literals $\left\{L_{1}=\operatorname{pick}-u p(x), L_{2}=\operatorname{sister}(x)\right\}$, whose elements sound unrelated. For instance, there is no obvious 'proposition' (literal) that would be a common consequence of $L_{1}$ and $L_{2}$ or would entail jointly $L_{1}$ and $L_{2}$. More generally, given the contribution of a discourse constituent, $\left\langle L_{1}, \ldots, L_{n}\right\rangle$, there is no guarantee that $L_{1} \ldots L_{n}$ can be jointly connected to a common literal through some discourse relation. If attachment was unconstrained, the general independence of the contribution members would make the construction of an interpretation in discourse even more difficult than it is. For instance, given simple two sentence dialogues of the form ( $\mathrm{A}: \mathrm{S} 1=\left\langle L_{1}, L_{2}\right\rangle-\mathrm{B}: \mathrm{S} 2=\left\langle L_{1}^{\prime}, L_{2}^{\prime}\right\rangle$ ), A would have to eliminate one of $L_{1}^{\prime}, L_{2}^{\prime}$ since both would be a priori equivalent candidates for providing a continuation to S1. Symmetrically, B would have to eliminate one of $L_{1}, L_{2}$ to determine which part of the contribution is intended by A to require a continuation. This would lead to massive ambiguity in the worst cases. A plausible conjecture is that languages have developed conventionalised preferences for attachment in order to streamline discourse management. We are now in a better position to understand the relation between the QUD and attachment. Only those elements that are marked for attachment are obligatorily interpreted as addressing the QUD because the constraints on attachment help keeping the thread in discourse evolution. Accordingly, when an element is marked for attachment, it is also marked as contributing to the discourse topic at the current point. Elements that are not so marked can project, since they are subtracted from the current discussion thread. As we saw in the previous section, this does not prevent something from addressing the QUD and projecting, if this element is not conventionally marked as attachable (and addressing the QUD).

## 5 Conclusion

The upshot of the previous discussion is that an element can address the QUD and nonetheless project. This is so because projection is (negatively) associated with conventionalised attachment preferences, that do not vary with the
context. Several important issues are still pending. I will mention two of them. First, additional experimental work is necessary to construct models of cognitive processing for non-at-issue content. In particular, recent work on anticipatory effects (Chambers and San Juan 2008) might complicate the debate over the role of common ground and, more generally, the dynamic character of presuppositions, questioned in various approaches (Abbott, Schlenker). Second, the status of non-conventional elements, so called 'conversational implicatures', is unclear. Since they do not necessarily correspond to a segment of linguistic code, their integration into a layered conventional system, as is proposed here, has to be reconsidered.

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# Adverbs of Comment and Disagreement ${ }^{\star}$ 

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#### Abstract

Adverbs of comment (AOCs) such as sadly, fortunately raise a question of subjective meaning, much like predicates of personal taste (fun, tasty), namely, to whom the speaker attributes the emotion or evaluation, when there is no overt for-PP. I extend Lasersohn's (2005) judge parameter to the analysis of AOCs and propose that disagreement on one and the same proposition only arises when the hearer correctly resolves the argument of judge despite its absence in overt syntax, i.e. $\operatorname{sad}(p, c)$ vs. $\neg \operatorname{sad}(p, c)$. Otherwise, only mis- or incomprehension occurs where the speaker and the hearer actually express two different propositions on the same issue, i.e. $\operatorname{sad}(p, c)$ vs. $\neg \operatorname{sad}(p, b)$.


## 1 Introduction

Adverbs of comment (henceforth, AOCs) such as sadly or fortunately raise a question of subjective meaning, much like predicates of personal taste (Lasersohn 2005) and epistemic modality (Stephenson 2007), namely, to whom the speaker attributes the emotion/evaluation when she uses an AOC, like sadly in e.g. (3-a). In the examples below, the lower-case $j$ indicates a judge parameter in the Lasersohnian sense.
(1) a. Roller coasters are fun.
b. Roller coasters are fun [for kids] ${ }_{j}$.
(2) a. The computer might be at risk.
b. In some world compatible with what [the technician $]_{j}$ knows in the actual world, the computer is at risk.
(3) a. Sadly, the Pink Panther is just one of those jokes that gets lost in translation.
b. Sadly [for Steve Martin] ${ }_{j}$, the Pink Panther is just one of those jokes that gets lost in translation.

In (3-b), the speaker makes it linguistically explicit that the state of affairs at issue is sad for Steve Martin, while it is left open in (3-a) for whom it is so. This kind of subjective meaning arises, as shown in $(1) /(2) /(3)$, due to the hidden

[^98]argument of judge at LF, and it disappears once $j$ is made explicit. Predicates of personal taste and AOCs are more similar to each other than to epistemic modal verbs in that syntactic evidence for the judge argument is in both cases provided by a for-PP.
I focus on the minimal pair in (3) in this paper. Following Bach (1999) and Potts (2005), I assume that a sentence with AOCs such as (3-b) is double-propositional, one proposition $p$ expressed by the sentence without the parenthetic sadly for Steve Martin and the other one $\operatorname{sad}(p, c), c$ being Steve Martin in this case. According to Potts (2005), the first proposition is at-issue while the second one is a conventional implicature (CI). In comparison to (3-b), the second proposition in (3-a) is incomplete. Because of this, disagreement on the second proposition (i.e. $\operatorname{sad}(p, c)$ ) demonstrates two different cases, one case I call real disagreement which only obtains when the hearer agrees with the speaker on the hidden argument of judge. That means that the speaker utters $\operatorname{sad}(p, c)$ with $c$ being a constant, e.g. Steve Martin (even though it is linguistically implicit), while the hearer by disagreement holds that $\neg \operatorname{sad}(p, c)$ with $c$ being the same constant, Steve Martin (as if it were linguistically explicit in the speaker's utterance). In the other case, which I call mis- or incomprehension, the speaker utters $\operatorname{sad}(p, c)$ while the hearer by disagreement actually expresses $\neg \operatorname{sad}(p, b), b$ being the individual(s) that the hearer has in mind that the state of affairs is sad for. In the first case, the disagreement is on one and the same proposition, namely, whether the state of affairs is sad for e.g. Steve Matin, while in the second case, the seeming disagreement is not on one and the same proposition, but on the propositional fragment (i.e. whether it is sad) and on the judge parameter at the same time: the speaker expresses that $\operatorname{sad}(p, c)$ whereas the hearer expresses $\neg \operatorname{sad}(p, b)$, which differ both in the polarity of the statements and in the argument of judge.
The paper is organized as follows. In Section 2, I elaborate on the idea of incomplete propositions by AOCs. In Section 3, I compare AOCs with predicates of personal taste in terms of subjective meaning and the consequences. Section 4 provides a formal analysis following Lasersohn (2005) and Stephenson (2007). The last section contains a concluding remark.

## 2 Incomplete Propositions

I assume that sentences sometimes do not express a complete proposition (Bach 1997, 2008, contra Cappelen and Lepore 2005). Incomplete propositions arise often due to a syntactically silent but semantically obligatory argument. Take the famous sentence about meteorological conditions for example, (4-b) is propositionally complete but (4-a) is not. This means we hold that (4-a) does not express one proposition but is used to express different propositions, depending on what the hidden argument - the location - is. Usually, the context of utterance makes the location explicit for such sentences. In comparison, (4-b) expresses one unambiguous proposition that it is raining in Amsterdam.
(4) a. It is raining.
b. It is raining in Amsterdam.

The role of the person(s) to a certain emotional state is not that different from that of the location to a certain meteorological condition. In the latter case, it is commonly assumed that a time argument - present in the tense morpheme and a place argument are needed for the sentence to make sense, while in the former case (putting tense aside for simplicity), we have a judge instead of a place argument. In a nutschell, I assume the incompleteness of It is raining and of Sadly, $p$ is due to a missing place/judge argument, which are needed to fill the necessary referential information to give (by the speaker) or get (by the hearer) a complete proposition. In the case of AOCs, sentences such as (3-a) express two propositions (Bach 1999, Potts 2005), one main, complete proposition that the Pink Panther is just one of those jokes that gets lost in translation and the other, secondary, incomplete proposition that this is sad. Nothing can be sad if no person is subject to this emotion. The exact group that the speaker has in mind can be made linguistically explicit as in (3-b).

Jackendoff (1972) proposes that such adverbs as sadly predicate over a sentence and a second argument SPEAKER. In the literature they are sometimes called speaker-oriented adverbs. With reference to the overt argument by the for-PP in (3-b), one can argue against the speaker-orientation of AOCs. Rather, they should be treated as two-place predicates (Liu 2009) taking a judge (in the Lasersohnian sense) as the second argument so that the evaluation can be attributed to the speaker, the addressees, the subject of the sentence, etc. Although this argument can be syntactically silent, a felicitous use of AOCs presupposes the existence of the judge. For example, in a war situation where the speaker informs his own party about the serious casualties of the opposite party, the literal use of unfortunately or tragically will be outrageous. This means that the argument of judge should be in the semantics of a sentence with AOCs, or in other words, with no judge, no complete proposition is expressed. The same holds for their adjective equivalents of e.g. It is sad (for Steve Martin) that the Pink Panther is just one of those jokes that gets lost in translation ${ }^{1}$. Without the PP, the sentence does not express a complete (CI) proposition, i.e. is not truth-evaluable.

The meaning I propose for AOCs such as sadly is $\lambda x \cdot \lambda p \cdot s a d(p, x)$. In the examples above, the for- PP instantiates the argument of judge. If there is no explicit PP, there are two ways to formalize that the existence of judge is presupposed, either $\exists x(\operatorname{sad}(p, x))$ or $\operatorname{sad}(p, \mathbf{c}), \mathbf{c}$ being a constant of type $e$ that is context-dependent. In the next section, I show that the meaning with the existential closure on the judge would lead to undesired results and that the hidden judge argument should be a constant in the LF.

[^99]
## 3 Disagreement and Subjective Meaning

### 3.1 Predicates of personal taste etc.

As Lasersohn (2005) claims, sentences like The chili is tasty is not truth-evaluable until the intended judge is resolved. In (5), what Mary does is comment on whether the chili is tasty (an incomplete proposition, Bach 2008) by her own judge (for a complete proposition). Although it seems that John and Mary disagree on the same proposition, they actually express different propositions on the same issue. When the domain of the intended judge is made linguistically explicit such as in (6), Mary can no longer felicitously disagree by simply taking a different judge.
(5) John: The chili is tasty. $\lambda x$. the chili is tasty for $x$ Mary: No, the chili is not tasty. $\lambda y$. the chili is not tasty for $y$
(6) John: This chili is tasty for Peter.

Mary: No, this chili is not tasty for Peter. / \# No, this chili is not tasty for Mark.

The same observation holds in connection with the domain restriction of quantifiers (von Fintel and Gillies 2008). Take only as an example, mis- or incomprehension can arise due to the implicit domain restriction, as (7) shows. The truth-value of the sentence obtains only if the domain restriction gets resolved. Accordingly, if the domain restriction of quantification is made linguistically explicit, no disagreement by taking a different domain restriction is felicitous, as shown in (8).
(7) A: Only Peter came to the party.

B: Really? I heard Sue was there too.
A: Yeah, but she was supposed to be there helping me.
(8) A: Among the people I invited, namely, Peter, Ben and Jane, only Peter came to the party.
B: \# Really? I heard Sue was there too.
Neutral and nonneutral modals, where "the kind of modality is linguistically specified in the former, but provided by the non-linguistic context in the latter" (Kratzer 1991: p.640), demonstrate similar effects of disagreement. Stephenson (2007) suggests that the judge dependency with epistemic modals is inherent, and I suspect that it is the same with quantifier domain restriction. In the following, I will not say more on them but concentrate mainly on predicates of personal taste and AOCs in parallelism.

### 3.2 AOCs

Concerning AOCs, it should first be mentioned that direct disagreement by beginning with No is not possible since AOCs contribute CI contents, while negation in Potts's (2005) two-dimensional system only applies to at-issue contents.

This explains the oddness of B's answer in (9). As disagreement on the CI content presupposes the agreement on the at-issue content, a No answer targets at-issue content just like sentential negation not, but disagreement on the atissue content invalidates the issue of the CI content. For more about the relation between these two contents, see Liu (2009).
(9) A: Sadly, the Pink Panther is just one of those jokes that gets lost in translation.
B: Ok, but this is not sad. (\# No, this is not sad.)
Second, this also explains why AOCs differ from predicates of personal taste or adjectives of comment when they are embedded. As Lasersohn (2005) and Stephenson (2007) point out, when predicates of personal taste are embedded for example in $(10-\mathrm{a})$, the sentence gets a salient reading that Mary is the judge. The same is true with adjectives of comment shown in (10-b), whereas it is not so with AOCs. The explanation is that AOCs are of CI type $\left\langle e^{a}, \ll s^{a}, t^{a}\right\rangle$ ,$\left\langle s^{a}, t^{c}\right\rangle \gg$ taking an individual ot type $\left\langle e^{a}\right\rangle$ and a proposition of type $\left\langle s^{a}, t^{a}\right\rangle$ as the two arguments, yielding a proposition of type $\left\langle s^{a}, t^{c}\right\rangle$. In comparison to the at-issue content, this CI content is not necessarily part of Mary's beliefs.
a. Mary $j_{j}$ thinks that the chili is tasty (for $j$ ).
b. Mary $j_{j}$ thinks that it is sad (for $j$ ) that the Pink Panther is ...
c. Mary thinks that sadly (for $j$ ), the Pink Panther is ...

Due to the for-PP, (3-a) and (3-b) have different effects in terms of disagreement. In (9), B agrees with A on the at-issue content of A's utterance but disagrees with her on the CI content. However, the disagreement of B can be attributed to two reasons:

- mis- or incomprehension: possibly because the context is not informative enough or because B fails somehow to comprehend even when it is. In this case, the issue is for whom it is sad, and A and B disagree in the sense that they take different judges for one of which it is sad and for the other it is not sad.
- real disagreement: this presupposes that B understands exactly what A means but disagrees with her, as if the argument of judge (e.g. for Steve Martin) were overt. In this case, the issue is whether this is sad for Steve Martin.

Only in the latter case is the disagreement on one and the same complete proposition, as shown in (11). In this case, B cannot simply take another judge, different from Steve Martin, whether explicitly or implicitly. The disagreement has to be on the same proposition, that this is sad for Steve Martin.
(11) A: Sadly for Steve Martin, the Pink Panther is just one of those jokes that gets lost in translation.
B: Ok, but this is not sad for Steve Martin.

Similarly, with two different overt arguments of judge, the same speaker can express propositional fragments differing in polarity, but this is not possible if the argument of judge is silent. In other words, with an explicit argument of judge, a new judge can be introduced to make up a new proposition of the same or opposite polarity ${ }^{2}$. With implicit judge, shifting between two different judges is ruled out. This is shown in (12), which provides evidence that with implicit judges, judge-shifting is only possible with context-shifting, for instance by speaker change or by change of the same speaker's mental state such as in (13). Compare this also with (14).
(12) a. Sadly for Steve Martin, the Pink Panther is just one of those jokes that gets lost in translation. But this is not sad for anybody else.
b. Sadly, the Pink Panther is just one of those jokes that gets lost in translation. \#But this is not sad.
(13) Sadly, (or maybe not sadly) the Pink Panther is just one of those jokes that gets lost in translation.
(14) a. It is raining in Amsterdam. It is not raining in Berlin.
b. \#It is raining. It is not raining. (Contradiction)
(15-a) provides an example where two propositions are expressed by two AOCs taking the same propositional argument, and (15-b) gives the same, but with their adjective counterparts as commentaries.
(15) a. Fortunately for them, unfortunately for us, it was a good choice.
b. It's fortunate for us, but unfortunate for the auto industry as a whole.

### 3.3 Judge as a Constant

The following is an argument why the judge is a contextually dependent constant.
a. Eva read.
b. It is raining.
c. Sadly, the Pink Panther is just one of those jokes that gets lost in translation.
a. $\quad \exists z(\operatorname{Thing}(z) \wedge \operatorname{Read}(e v a, z))$
b. ? $\exists z(\operatorname{Place}(z) \wedge \operatorname{Rain}(z))$
c. ? $\exists z(\operatorname{Judge}(z) \wedge \operatorname{sad}(p, z))$
a. $? \operatorname{Read}(e v a, c))$
b. Place $(c) \wedge \operatorname{Rain}(c)$
c. $\quad(\operatorname{Judge}(c) \wedge \operatorname{sad}(p, c))$

[^100]As (17) and(18) show, the interpretation with existential closure on places/judges is too weak while it is not for predicates like read/eat. Presumably, the reason is that what people read/eat is more difficult to individuate and it is also less necessary to do so. But places/people are by convention usually individuated by proper names. If we take (17-c) as the interpretation, the disagreement can go two ways: (19-a) is too strong and (19-b) is too weak. This favors the constant analysis for AOCs in LF.

$$
\begin{array}{ll}
\text { a. } & \neg \exists z(\operatorname{Judge}(z) \wedge \operatorname{sad}(p, z))  \tag{19}\\
\text { b. } & \exists z \neg(\operatorname{Judge}(z) \wedge \operatorname{sad}(p, z))
\end{array}
$$

### 3.4 Single/Multiple Truths

Imagine two scenarios: in one, $A$ just saw $B$ taste the chili. In this case, A means to ask whether the chili is tasty for $B$ and $B$ is supposed to answer whether the chili is tasty for her. Another scenario is where A has assigned B to find out whether the new chili product of their company is tasty for the customers. In this case, A means to ask whether the chili is tasty for the customers and B is supposed to give an answer - probably based on sampling statistics or sales simply. The dialogue in (20) can go with either scenario.

> A: Is the chili tasty?
> B: Yes, it is. / No, it isn't.

The first scenario is similar to (21) (Stephenson 2007). However, suppose Sam answers without having tried but based on the nice looks of the cake, the dialog in (21) sounds totally fine to me.
(21) Mary: How's the cake?

Sam: It's tasty.
Sue: No, it isn't, it tastes terrible.
Sam: \# Oh, then I guess I was wrong.
This point is crucial to the issue of subjective meaning with predicates of personal taste and AOCs (and possibly also epistemic modals but probably not quantifier domain restriction), namely, there might be no single truth about whether roller coasters are fun or whether the death of the boss is sad, as opposed to something like whether Petra is a doctor (Stephenson 2007). Or in other words, whether Petra is a doctor can be objectively true or false, but whether roller coasters are fun or whether the death of the boss is sad can only be subjectively true or false. In the absolute sense, the truth about whether roller coasters are fun or whether the death of the boss is sad consists of a set of (true) propositions, each of which takes a member of the relevant domain as the judge.
(22) A: Are roller coasters fun?

B: Roller coasters fun for $a$, not for $b$, for $c$, not for $d, \ldots$
(23) A: Is the death of the boss sad?

B: It is sad for $a$, not for $b$, for $c$, not for $d, \ldots$

A statement with such predicates is true as long as the speaker speaks truthfully. But this is only part of the truths about whether the death of the boss is sad, for example. Issues are more complicated when collective taste/emotion (like in the second scenario) rather than personal taste/emotion counts. I leave this for future work.

## 4 Analysis

In this section I will briefly introduce Lasersohn's (2005) and Stephenson's (2007) formal analyses for predicates of personal taste and then choose the latter analysis over the former for analyzing AOCs.
Kaplan (1989) proposes a two-step derivation for demonstratives, i.e. character as a function from context to content (proposition) and content as a function from world-time pairs $\langle w, t\rangle$ to truth values $\{0,1\}$. Following this, Lasersohn (2005) argues that a sentence with predicates of personal taste such as fun and tasty has a stable content but he claims that the truth value of this content is relativized to individuals. He therefore introduces a new judge index, the value of which is provided "in the derivation of truth values from content, not in the derivation of content from character" (Lasersohn 2005: p.643), that is, by the pragmatic context. To sum up, Lasersohn assumes that the content of e.g. (1-a) is semantically complete, i.e. it expresses a complete proposition, but its truth value is relativized to a world-time-judge triple $\langle w, t, j\rangle$. Take fun for example, the interpretation is below:
(24) Predicates of personal taste (Lasersohn 2005):
$\|f u n\|^{c ; w, t, j}=\left[\lambda x_{e} \cdot x\right.$ is fun for $j$ in $w$ at $\left.t\right]$
$\|$ fun for $D P\left\|^{c ; w, t, j}=\right\| f u n \|^{c ; w, t,\|D P\|^{c ; w, t, j}}$
In Stephenson (2007) ${ }^{3}$, a revised version of Lasersohn (2005), predicates of personal taste are two-place predicates, taking a PRO or a for-PP as the second argument, i.e. of judge. She treats the preposition for (semantically vacuous) as an identity function, that is, a function from individuals to individuals.

$$
\begin{align*}
& \text { Predicates of personal taste (Stephenson 2007): }  \tag{25}\\
& \|f u n\|^{c ; w, t, j}=\left[\lambda y_{e} \cdot\left[\lambda x_{e} \cdot x \text { is fun for } y \text { in } w \text { at } t\right]\right] \\
& \left\|P R O_{J}\right\|^{c ; w, t, j}=j \\
& \| \text { for } \|^{c ; w, t, j}=\left[\lambda y_{e} . y\right]
\end{align*}
$$

Stephenson (2007: p.500) claims that "The difference between epistemic modals and predicates of personal taste, then, is that epistemic modals are inherently judge-dependent, whereas predicates of personal taste become judge-dependent

[^101]only if they take $\mathrm{PRO}_{J}$ as an argument". Although I don't go into epistemic modals in the current paper, this point is crucial, as the same difference exists between epistemic modals and AOCs. In other words, Stephenson's analysis for predicates of personal taste can be extended to AOCs, since the subjective meaning results from the absence of an overt for-PP in both cases. The interpretation for the AOC sadly is provided below:
\[

$$
\begin{align*}
& \text { AOCs: }  \tag{26}\\
& \| \text { sadly }\left\langle_{<e^{a}, \ll s^{a}, t^{a}>,<s^{a}, t^{c} \ggg} \|^{c ; w, t, j}=\left[\lambda x_{e^{a}} .\left[\lambda p_{<s^{a}, t^{a}>} . p \text { is sad for } x\right. \text { in }\right.\right. \\
& w \text { at } t] \\
& \| \text { sadly for } D P\left\|^{c ; w, t, j}=\right\| \text { sadly } \|^{c ; w, t, j}\left(\|D P\|^{c ; w, t, j}\right)
\end{align*}
$$
\]

The same analysis can apply to their adjective counterparts.
(27) Adjectives of comment:
$\left\|s a d_{\left.<e^{a}, \ll s^{a}, t^{a}\right\rangle,\left\langle s^{a}, t^{a}\right\rangle \gg}\right\|^{c ; w, t, j}=\left[\lambda x_{e^{a}} .\left[\lambda p_{\left\langle s^{a}, t^{a}\right\rangle} . p\right.\right.$ is sad for $x$ in $w$ at $t$ ]]
$\|$ sad for $D P\left\|^{c ; w, t, j}=\right\| s a d \|^{c ; w, t, j}\left(\|D P\|^{c ; w, t, j}\right)$

### 4.1 When Judges Meet

Predicates of personal taste, epistemic modals and AOCs co-occur with one another. If we believe Stephenson (and I do) that epistemic modals are inherently judge-dependent, we can leave them aside first and concentrate on (28-a) to see how the two judges interact. The context is this: I talk with my boy friend about an author friend - Ali - who just published a book which got very bad reviews in the past month. What I say in (28-a) means in that context (28-b). My analysis of (28-a) is given in (29).
(28) a. The storyline was unfortunately boring.
b. Unfortunately for the author, the storyline was boring for the audience.
(29) The storyline was unfortunately $\mathrm{PRO}_{j_{2}}$ boring $\mathrm{PRO}_{j_{1}}$.
$\|$ boring $_{\left\langle e^{a},<e^{a},<s^{a}, t^{a} \gg\right.} \|^{c ; w, t, j}=\left[\left[\lambda y_{e^{a}} .\left[\lambda x_{e^{a} . x}\right.\right.\right.$ is boring for $y$ in $w$ at $t]]$
$\|\left[\text { boring } P R O_{j_{1}}\right]_{\left.<e^{a},<s^{a}, t^{a}\right\rangle} \|^{c ; w, t, j}=\left[\lambda x_{e^{a}} . x\right.$ is boring for $j_{1}$ in $w$ at $\left.t\right]$
$\|[\text { the storyline was boring }]_{\left\langle s^{a}, t\right\rangle} \|^{c ; w, t, j}=[$ the storyline is boring for $j_{1}$ in $w$ at $t$ ]
$\|$ unfortunatel $y_{\left.<e^{a}, \ll s^{a}, t^{a}\right\rangle,\left\langle s^{a}, t^{c}\right\rangle \gg} \|^{c ; w, t, j}=\left[\lambda x_{e^{a}} .\left[\lambda p_{\left.<s^{a}, t^{a}\right\rangle} . p\right.\right.$ is unfortunate for $x$ in $w$ at $t]$ ]
$\|\left[\text { unfortunately } P R O_{j_{2}}\right]_{\left.\left\langle<s^{a}, t^{a}\right\rangle,\left\langle s^{a}, t^{c}\right\rangle>\right\rangle} \|^{c ; w, t, j}=\left[\lambda p_{\left\langle s^{a}, t^{a}\right\rangle . p}\right.$ is unfortunate for $j_{2}$ in $w$ at $t$ ]
$\left\|(29)_{<s^{a}, t^{a}>\bullet<s^{a}, t^{c}>}\right\|^{c ; w, t, j}=<\exists t^{\prime}$ [the storyline is boring for $j_{1}$ in $w$ at $t^{\prime}<t$ ], it is unfortunate for $j_{2}$ that $\exists t^{\prime}$ [the storyline is boring for $j_{1}$ in $w$ at $\left.t^{\prime}<t\right]$ in $w$ at $t>$

## 5 Conclusion

To sum up, AOCs such as sadly, tragically, unfortunately are another example to be taken into consideration in the general phenomenon of subjective meaning, along with predicates of personal taste (and also quantifier domain restrictions / epistemic modality). A sentence with an AOC but with no overt argument of judge is propositionally incomplete and thus semantically vague. In this case, disagreement either involves the hearer's mis- or incomprehension of the intended judge by the speaker and her adoption of a different judge or her real disagreement on the same proposition with the intended judge correctly resolved.

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# Two puzzles about requirements 

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#### Abstract

Modal expressions like have to, require, need, must etc. are standardly considered to be universal quantifiers over possible worlds. In this extended abstract, I point out that this is problematic for cases in which these expressions interact with scalar operators. In particular, I argue that such modals appear to be able to express existential modal force.


## 1 First puzzle: Minimum requirements

My friend and me are having a bet in which I claim to be able to score at least 300 points in the game of scrabble we are about to start. The following would be an accurate paraphrase for the bet in question.
(1) The minimum number of points I need to score to win the bet is 300 .

That is, the bet involves a minimum requirement: If I score 300, I win. If I score more, I also win. But if I score less, then I lose. To be sure, at first sight it seems obvious why (1) is interpreted as such, for I do need to score 300, and 300 is the minimum score that makes me win the bet. Yet, when we make things precise, and given common assumptions on the semantics of modal auxiliaries, it turns out that it is rather mysterious why (1) means what it means.

The common assumptions I am alluding to are, first of all, that need is a universal quantifier over possible worlds and, second, that the to-phrase in (1) restricts quantification over possible worlds (von Fintel and Iatridou 2005). In other words, "to $p$, need to $q$ " is true if and only if all the $p$-worlds are $q$-worlds; i.e. if $p$ entails $q$. At first sight, this view appears to make good predictions. For example, a case like (2) is now interpreted as saying that you went to the Twijnstraat in all the worlds where you got good cheese.
(2) To get good cheese, you need to go to the Twijnstraat.

However, when we apply the above assumptions to (1), the outcome is very puzzling. Note first the following: in the scenario I sketched about the scrabble bet, there are no worlds in which I win the bet while scoring fewer than 300 points. Furthermore, the worlds where I do win come in many variations: in some (but not all) of them I score 300 points, in some (but not all) my score is 301 , in some (but not all) it is 302,310 , or even 550 . The problem is that

```
    \Downarrow
I scored 303 points
    \Downarrow
I scored 302 points
    \Downarrow
I scored 301 points
    \Downarrow
I scored 300 points
    \Downarrow
```

Fig. 1. The at least interpretation for numerals
the most obvious referent for the minimum number of points I need to score is the smallest number $x$ such that $I$ scored $x$ points is true in all relevant worlds. However, for no value for $x$ is this open sentence true in all bet-winning worlds. It would seem then that the definite description the minimum number of points I need to score fails to refer in the described situation.

It might appear that there is an obvious solution. If we assume that numerals are interpreted as lower-bounded only (usually, this is dubbed the at least interpretation for numerals), then we get an entailment scale as in figure 1.

Given this scale, it is now true that in all bet-winning worlds I scored 300 points, for the worlds where my exact score was higher will be worlds in which I scored at least 300 points. Unfortunately, if we assume that such an entailment scale is appropriate then, by entailment, it is also true that in all bet-winning worlds I scored 200 points. In fact, it is entailed that I score a single point in every bet-winning world. Consequently, the minimum number of points I need to score to win the bet is now predicted to be 1 , not 300 . Yet, (3), obviously, seems an unacceptable way of paraphrasing the bet between my friend and me.
(3) The minimum number of points I need to score to win the bet is 1 .

In sum, independent of how we interpret numerals, it appears far from straightforward how to come to a compositional interpretation of (1).

## 2 Second puzzle: Maximum requirements

If we assume the entailment scale in figure 1, then there is a further puzzle. The proposition I scored 1 point is true in all bet-winning worlds, and so is the proposition I scored 300 points. The proposition I scored 301 points, however, is the first proposition in the scale that is not true in all bet-winning worlds. (It's only true in some.) This makes 300 the highest value for $x$ such that $I$ scored $x$ points is true in all victorious worlds and so we predict that instead of
(1), the correct way of paraphrasing the bet is, in fact, (4). Clearly, this is an unwelcome prediction, for the scenario I sketched was a prime example of what we call minimum requirements, not of maximum ones.
(4) The maximum number of points I need to score to win the bet is 300 .

In the given scenario there was no upper limit on my score. That is, the bet is only about me scoring 300 or more. No matter how much higher than 300 I score, I will keep on winning. In certain other scenarios maximal requirements do make sense, however. Take the following example.
(5) The maximum number of sets needed to decide a men's tennis match is 5.

In men's tennis, the first player to win three sets wins, hence (5). At the same time, this means that there can be no men's tennis match which lasts for fewer than 3 sets. In other words:
(6) The minimum number of sets needed to decide a men's tennis match is 3.

Once again, we derive the wrong interpretation for such examples under the standard assumptions discussed above. Let us first assume that numerals create entailment scales, as in figure 1. That is, if 4 sets were played in a match, then this entails that 3 sets were played, as well as that 2 sets were played, etc. The minimum number $n$ of sets such that $n$ sets are played in every world in which the match is decided is now 1 . The maximum number $n$ of sets such that $n$ sets are played in every match-deciding world is 3 , since all such worlds contain (at least) 3 sets, while only some contain a 4 th or a 5 th one.

Things are no better if we interpret numerals as doubly-bound. In that case the definite descriptions in (5) and (6) will fail to refer, for there exists no $n$ such that in all possible ways in which a tennis match could be decided the match counted exactly $n$ sets.

## 3 Modal Force

The two puzzles above point out a problem with the interaction between universal modals and scalar operations. Abstracting away from the scenarios above, the puzzles can be generalised as follows. Let $\mathcal{P}$ be a scale of propositions, as in (7).

$$
\begin{equation*}
p_{1}<p_{2}<p_{3}<\ldots<p_{i}<p_{i+1}<\ldots \tag{7}
\end{equation*}
$$

Following standard assumptions, a proposition $p_{k}$ is a minimum requirement for $q$ if it is the case that $p_{k}$ is entailed by $q$, while for no $l<k, p_{k}$ is entailed by $q$. If (7) is an entailment scale, however, then for any $p_{k}$ it holds that $p_{k} \models p_{k-1}$ and, in fact, $p_{k}=p_{1}$. So, if $q$ entails $p_{k}$, then it also entails $p_{1}$. In other words, the minimum requirement for $q$ could only ever be $p_{1}$, which renders the notion
of minimum requirement quite useless. If, however, $\mathcal{P}$ is not an entailment scale, then it is easy to imagine that $p_{k}$ is entailed by $q$ while this is not the case for any proposition that is lower on the scale. Unfortunately, this is not how we normally understand the notion of minimum requirement. In fact, part of the problem with our assumed definition of minimum requirement is that if $p_{k}$ is a minimum requirement for $q$, then $q$ need not entail $p_{k}$. For instance, if my bet is that I will score 300 or more in the game of scrabble, then me winning the bet does not entail me scoring exactly 300 points.

There is a surprising way out: minimal and maximal requirements are not about necessity, but rather about possibility. Assume $\mathcal{P}$ to be a non-entailment scale: $p_{k}$ is a minimal (maximal) requirement for $q$ iff $p_{k}$ is compatible with $q$ and there is no $l<k(l>k)$ such that $p_{l}$ is compatible with $q$. In the scrabble bet scenario, the proposition that I scored exactly 300 points is the lowest ranked proposition such that there exists a bet-winning world in which that proposition is true. Furthermore, 3 is the smallest number $n$ such that there is a world in which the tennis match is decided in such a way that the number of played sets is exactly $n$. Also, 5 is the highest number $n$ such that there is a world in which the match is decided such that the number of played sets is exactly $n$. Thus, under the assumption that the modal force of need is existential, the analysis of examples like (1), (5) and (6) appears straightforward.

There is however clear evidence that the modal force of need and it's kin is not existential. For instance, if it were, we would predict (8) to be true. The intuition, however, is that it is false.
(8) To decide a men's tennis match, you have to play exactly 3 sets.

Furthermore, with an existential semantics one would expect (9-a) to entail (9-b), a rather unwelcome prediction.
(9) a. In order to win the bet, I need to score more than 300 points.
b. In order to win the bet, I need to score more than 400 points.

In fact, the intuition is that (9-b) entails (9-a). This intuition is captured under the assumptions I have considered to be standard. ${ }^{1}$

[^102](i) a. To get good cheese, you have to go to the Twijnstraat.
b. $\Rightarrow$ To get good cheese, you have to breathe.

If you go to the Twijnstraat in all worlds in which you get good cheese, then since you breathe in all the worlds in which you go to the Twijnstraat, it follows that you breathe in all worlds in which you get good cheese. Von Fintel and Iatridou judge (i-b) true, yet unhelpful in the context of (i-a), an intuition I agree with. However, the truth of the following example, suggested to me by David Beaver, is a further prediction of the theory, but it is not clear that it is a welcome one.

## 4 Interlude: data

Central to the puzzles that I presented above is a rather specific family of noun phrases, namely definite descriptions that contain some sort of minimality or maximality operator (minimum, smallest, maximum, highest etc.) and a necessity modal like need, or require, or have to, etc. Since these noun phrases play a crucial role in my arguments, I would like to take away any skeptical reader's impression that such constructions are somewhat artificial. To this end, I will give some (natural) examples. (Below, I moreover argue that the puzzle is part of a larger set of phenomena that includes, for instance, certain modified numerals.)

Examples like (10) are typical and common cases where operators expressing minimality (smallest in this case) interact with modality.

## Question:

One-half of a road construction project was completed by 6 workers in 12 days. Working at the same rate, what is the smallest number of workers needed to finish the rest of the project in exactly 4 days?

## Answer:

The smallest number of workers needed to finish the project in 4 days is 18 .

The answer A in (10) spells out a minimal requirement: 18 workers allow you to finish the project in 4 days, fewer than 18 workers won't allow you to do so.

Explicit minimal requirement formulations are quite common even outside the realm of maths problems, as is illustrated by (11). (Here, (11-b) and (11-c) are naturally occurring examples.)
(11) a. The smallest amount of butter you need for a nice and tasty cake is 250 grams.
b. The minimum number of partitions you need to install linux is 3 .
c. The minimum number of credits you need to graduate is 85 .

It should be pointed out that minimal requirement statements are not limited to the modal to need. In fact, must, require, should and have to allow for similar constructions, witness the following naturally occurring examples.
(12) a. Determine the smallest number of digits that must be removed from x so that the remaining digits can be rearranged to form a palindrome. ${ }^{2}$
b. REM level is the minimum number of BYTES you require to continue. ${ }^{3}$
(ii) To climb Everest you need 3 to equal $2+1$.
${ }^{2}$ http://cemc.uwaterloo.ca/Contests/past_contests/2008/2008FryerContest.pdf
${ }^{3} \mathrm{http}: / /$ www.cramsession.com/articles/files/checking-free-space-9262003-1044.asp
c. What is the minimum number of karanga I should know before I can say that I can karanga? ${ }^{4}$
d. We are usually interested in knowing the smallest number of colors that have to be used to color a graph. ${ }^{5}$

## 5 Modified Numerals

So far, I have been assuming that, in statements of minimum or maximum requirement, the scope of minimum and maximum is wider than that of the modal. So, I have been analysing (1) as (13-a), rather than (13-b). ${ }^{6}$
a. $\quad \min _{n}(\square[$ I score $n$ points $])=300$
b. $\quad \square\left[\min _{n}(\right.$ I score $n$ points $\left.)=300\right]$

Note that an analysis along the lines of (13-b), however, does not solve our puzzles. On an 'exactly' reading for $n$ points, there is just the single value for $n$ which makes I score n points true. The use of minimally would then be vacuous. Worse, we would expect that there is no difference between (14) and (15).
(14) The minimum number of points I need to score to win the bet is 300 .
(15) The maximum number of points I need to score to win the bet is 300 .

On an at least perspective for $n$ points, (13-b) will be a contradiction. Since for any $n$, I score $n$ points entails that I scored a single point, (13-b) ends up stating that $\square[1=300]$.

Interestingly, there is a variation on (13-b) that yields the correct truthconditions without the need for a change in modal force for need.

$$
\begin{equation*}
\square\left[\iota_{n}(\text { I score } n \text { points }) \geq 300\right] \tag{16}
\end{equation*}
$$

[^103](i) \#The minimum number of marbles that must be in the box is 10 .

This analysis is not as far fetched as it might seem at first sight. As a numeral modifier, minimally shares its semantics with at least. In other words, the proper treatment of (14) could be thought to be whatever works for (17) or (18).
(17) To win the bet, I need to score minimally 300 points.
(18) To win the bet, I need to score at least 300 points.

Unfortunately, there are reasons to believe that (16) is too simplistic as an analysis for (17) or (18). As Geurts and Nouwen (2007) argue in detail, at least does not correspond to the $\geq$-relation. Moreover, Nouwen (2010) shows that both minimally and at least are part of a class of numeral modifiers that is incompatible with specific amounts. That is, whereas (19) is felicitous and true, (20) is unacceptable.
(19) A hectagon has more than 2 sides.
(20) A hectagon has \{ at least / minimally \} 2 sides.

A further property of numeral modifiers like minimally is that they trigger readings of speaker uncertainty (Geurts and Nouwen 2007; Krifka 2007; Nouwen 2010). For instance, (21) is interpreted as being about the minimum number of people John might have invited (according to the speaker).
(21) John invited \{ minimally / at least \} 30 people to his party.
(\#To be precise, he invited 43.)
Such speaker uncertainty readings carry over to adjectives like minimum. ${ }^{7}$
(22) The $\{$ minimum / smallest $\}$ number of people John invited to the party is 30 .
(\#To be precise, it's 43.)
Apart from understanding (22) as a case of speaker uncertainty, one might also understand it as saying that 30 is the smallest number of people that John at some time in the past invited to the party. Crucially, all available readings somehow involve existential quantification.

The point I want to make is that it seems to me that there is a general puzzle underlying the interaction of universal modals and scalar operators, be they adjectives like minimum, smallest, highest etc. or numeral modifiers like minimally and at least. ${ }^{8}$ What such expressions appear to have in common is that they operate on existential structures.

[^104](i) I need a minimum of 300 points to win the bet.

## 6 Conclusion: towards an account of existential needs

I will conclude by suggesting a way forward. In her 2005 AC paper, Schwager argues that imperatives and modals verbs like need cannot always be interpreted as universal operators. For instance, (23) has a paraphrase: having a lot of money is an example of something you could do to get into a good university.
(23) To get into a good university, you must for example have a lot of money.

Schwager proposes that necessity modals are essentially exhaustified possibility modals, where $\operatorname{exh}(\diamond)=\square$. (See Schwager's paper for details.) Expressions like for example are de-exhaustifiers, which can reveal the existential nature of the modal.

Schwager's proposal helps to solve the two puzzles of minimal and maximal requirement. The above suggests that scalar operators like minimum/maximum can intervene with exhaustification. If this idea is on the right track, then we might expect to find that the interaction between necessity modals and scalar operators is generally mystifying.

## Acknowledgments

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# Two Sources of again-ambiguities: Evidence from Degree-Achievement Predicates* 

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#### Abstract

This paper provides evidence that again-ambiguities derive from two distinct sources, with the precise nature of a particular ambiguity being dependent on the particular type of predicate (Result-State or DegreeAchievement) present in the sentence. Previous research has focused primarily on sentences containing Result-State predicates (e.g. to open) rather than Degree Achievements (e.g. to widen), and has located the source of the ambiguity in the scope that again takes with respect to BECOME in a syntactically decomposed predicate. I argue that entailment facts preclude such an analysis from applying to sentences containing Degree Achievements and again. Instead, I propose that Degree Achievement predicates should be decomposed into comparative structures, and that the ambiguity in such sentences arises from the scope again takes with respect to a comparative Degree Phrase, rather than a BECOME operator.


## 1 Introduction

The proposal that certain morphologically simple words should be realized as multiple syntactic objects in order to explain paraphrasabilty and to capture certain entailment patterns originated in the late 1960s and early 1970s with the Generative Semantics (GS) movement; since Dowty [3], an analysis of this type has often been referred to as a 'lexical decomposition' account. Evidence brought forth for a decompositional analysis came in part from purported ambiguities found in sentences containing (i) an adverbial such as again, and (ii) an achievement-type verb. That is, it was claimed that there are two readings available for a sentence such as (1).
(1) The door opened again.

In one reading of this sentence, termed the repetitive reading, the door is understood to have opened previously; in the other reading, termed the non-repetitive or

[^105]restitutive reading, the door is understood to have merely been in an open state before (though it need not ever have been opened before).

According to a GS-style analysis, the ambiguity found in (1) is said to result from the scope of again with respect to elements in a decomposed predicate (see [1], [3], [8], [9]). A sentence like The door opened is said to be decomposable into two propositional levels: the level of the small clause, and the level of BECOME plus the small clause. This leaves two possible attachment sites for again, shown below, which correspond to the two readings for (1).

$$
\begin{array}{ll}
\text { a. [again [BECOME [the door open]] } & \text { repetitive }  \tag{2}\\
\text { b. [BECOME [again [the door open]] } & \text { non-repetitive }
\end{array}
$$

Intuitively, a repetitive reading includes a non-repetitive one; if the door was previously opened, it follows that the door was previously open. Evidence that there are two distinct readings comes from the fact that when again is preposed, as in (3), only a repetitive reading is available.

Again, the door opened.
This entailment between readings will turn out to be crucial in the discussion that follows. As it turns out, a BECOME-again analysis of an again-ambiguity always predicts such an entailment to hold between readings. Thus, such an analysis is problematic when we consider sentences containing Degree Achievement (DA) predicates and again; such sentences do demonstrate an ambiguity, but it is one in which neither reading entails the other. Examples of DA predicates include many deadjectival verbs, such as widen, narrow, lengthen, shorten, as well as predicates such as grow and shrink.

Consider the sentence below, which contains the DA predicate widen.
(4) The river widened again.

Like (1), the sentence in (4) has both a repetitive and a non-repetitive reading. The repetitive reading is true only if the river widened previously. The non-repetitive reading of (4) (called the counter-directional reading by von Stechow [9]) is true only if the river narrowed previously. Crucially, neither reading entails the other. The sentences in (5) highlight both of these readings.
(5) a. The river widened two months ago, and this month it widened again. (rep.)
b. The river narrowed last month, but this month it widened again. (non-rep.)

To demonstrate more precisely the nature of the two readings, consider the following set of situations.

Table 1.

|  | Sit. 1 | Sit. 2 | Sit. 3 |
| :--- | :--- | :--- | :--- |
| April 1 $^{\text {st }}$ | 12 m | 10 m | 10 m |
| May 1 $^{\text {st }}$ | 12 m | 11 m | 12 m |
| June 1 1 $^{\text {st }}$ | 10 m | 11 m | 10 m |
| July 1 $^{\text {st }}$ | 12 m | 12 m | 12 m |

In situation 1, the river narrows between May $1^{\text {st }}$ and June $1^{\text {st }}$, and widens between June $1^{\text {st }}$ and July $1^{\text {st }}$; in such a situation the non-repetitive, but not the repetitive, reading is true. In situation 2 , the river widens between May $1^{\text {st }}$ and June $1^{\text {st }}$, keeps a constant width for the month of June, and then widens between June $1^{\text {st }}$ and July $1^{\text {st }}$; in such a situation, only the repetitive reading is true. We thus see that the two readings have distinct truth-conditions. Note that we can, however, have a situation in which both readings are true; situation 3 is such a case.

In general, we find a similar pattern of non-entailing readings for all sentences containing an atelic DA predicate and again; for more discussion on telicity and DA predicates, see [6], [7]. As §2 will demonstrate, the lack of entailment between readings in sentences like (4) shows clearly that the source of the ambiguity for such sentences cannot be explained in terms of the relative scope of again and a BECOME operator. In §3 it will be argued that the correct decomposition of DA predicates does not contain a BECOME operator, but instead contains a comparative structure. The ambiguity found in (4) will then be accounted for in terms of the scope again takes with respect to the comparative Degree Phrase in the decomposed predicate.

## 2 BECOME and again

In what follows, a semantics relativized to time intervals is assumed [2], [3].
(6) A time interval is a subset $i$ of a dense linear order $T$ of moments $t_{n}$ such that $\forall \mathrm{t}_{1}, \mathrm{t}_{3} \in i$ where $\mathrm{t}_{1}<\mathrm{t}_{3}$, if $\mathrm{t}_{1}<\mathrm{t}_{2}<\mathrm{t}_{3}$, then $\mathrm{t}_{2} \in i \quad$ (from Bennett \& Partee [2])

Only closed time intervals are assumed below; note that it is possible for an interval to contain only one moment. Intervals are ordered as follows:

$$
\begin{equation*}
i[<] i^{\prime} \text { iff for all } t \text { in } i \text { and all } t^{\prime} \text { in } i^{\prime}, t<t^{\prime} \tag{7}
\end{equation*}
$$

(from Bennett \& Partee [2])
The BECOME-again analysis of again-ambiguities requires that predicates like the verb open be decomposed into BECOME and a small-clause containing a stative predicate, which denotes a stative property of intervals. Stative properties are defined as follows.
$P$ is a stative property of intervals only if
i. $\quad P(i)$ can be true of a single-moment interval
ii. $\quad P(i)$ is true of an interval $i$ containing $n>1$ moments only if $\forall i^{\prime} \subseteq i, \phi\left(i^{\prime}\right)$ is true
(from Dowty [3])

An example of a stative property is the property denoted by the adjective open.

$$
\begin{equation*}
\| \text { open }_{\text {ADJ }} \|=[\lambda x . \lambda i: \forall t \in i, x \text { is open at } t] \tag{9}
\end{equation*}
$$

Also assumed here is the standard meaning for BECOME from Dowty [3].

$$
\begin{align*}
& \|\mathrm{BECOME}\|^{g, \mathrm{i},}(\mathrm{P}) \text { is defined only if } \exists i^{\prime} \mid P\left(i^{\prime}\right)=1 \quad \text { where defined, }  \tag{10}\\
& \|\mathrm{BECOME}\|^{g, \mathrm{i}}(\mathrm{P})=1 \text { iff } P(\operatorname{beg}(i))=0 \& P(\text { end }(i))=1 \quad
\end{align*}
$$

Finally, the denotation assumed for again is based on von Stechow [9]. Again introduces presuppositional content in the form of a definedness condition.
$\|$ again $\|^{g, \mathrm{i}}(\mathrm{P})$ is defined only if
(i) $\quad \mathrm{P}(i)$ is defined
(ii) $\quad \exists g, h|g<h \& \operatorname{end}(h) \leq \operatorname{beg}(i)| \mathrm{P}(g)=1 \& \mathrm{P}(h)=0$
where defined:
$\|$ again $\|^{\mathrm{g}, \mathrm{i}}(\mathrm{P})=1$ iff $\mathrm{P}(i)=1$
The definition given above for again differs from the standard one in that it allows end $(h) \leq b e g(i)$, rather than requiring $h<i$. More will be said on this below.

A simple example demonstrates how again introduces presuppositional content into the truth-conditions of a sentence.
(12) $\|[$ again [the door is open $]] \|^{g, i}$ is defined only if
$\exists g, h \mid g<h \& e n d(h) \leq b e g(i) \&$
$\forall t \in g$, the door is open at $t$
$\exists t \in h$, the door is not open at $t$
where defined, is true iff
$\forall t \in i$, the door is open at $t$
Under these assumptions, the sentence The door is open again asserts that the door is open, and presupposes both that it was open then closed prior to its current state of being open.

It can be demonstrated that the BECOME-again analysis predicts an entailment between readings, no matter what stative property is in the scope of BECOME. The following proof shows that this is the case. The claim that we prove is the following.
$\forall S$, if $\|S\|=$ a stative property, then
[again [BECOME [S]]] entails [BECOME [again [S]]]
Proof:
We assume that the repetitive reading assertion and presupposition are met. Let $a, b, c$ be arb. chosen intervals, and $P$ an arb. chosen stative property such that
(i) $c<b \& \operatorname{end}(b) \leq \operatorname{beg}(a)$
(ii) $\quad \neg P(\operatorname{beg}(c)) \& P(\operatorname{end}(c)) \quad$ (i.e. $\operatorname{BEC}(P)(c))$
(iii) $\quad P(\operatorname{beg}(b)) \vee \neg P($ end $(b))] \quad$ (i.e. $\neg \operatorname{BEC}(P)(b))$
(iv) $\quad \neg P(\operatorname{beg}(a)) \& P(\operatorname{end}(a)) \quad$ (i.e. $\operatorname{BEC}(P)(a))$

Given these assumptions, we can automatically find intervals that satisfy the presupposition of the non-repetitive reading. Note that it is important for P to be a stative predicate, since we rely on the fact that it can be true of single moment intervals when defining the intervals $d$ and $e$ below.

Let $d=\operatorname{end}(c)$. Let $e=\operatorname{beg}(a)$. Then,
(i) $d<e \& \operatorname{end}(e) \leq \operatorname{beg}(a)$
(ii) $\quad \mathrm{P}(d) \& \quad \neg \mathrm{P}(e)$
(iii) $\quad \neg P(b e g(a)) \& P(e n d(a))$

The above proof shows that whenever we have intervals that satisfy the repetitive reading of an again-sentence, we automatically have intervals that satisfy the nonrepetitive reading. This is the case regardless of what stative predicate is in the scope of BECOME; hence, we can say that the fact that a repetitive reading entails a nonrepetitive one is a direct consequence of the BECOME-again analysis.

The revision to again mentioned above is what allows for the proof to go through. However, it is important to stress that the main argument does not crucially depend on this revision. First of all, the revision does not change the truth-conditions of againsentences in any noticeable way. Second, if we adopt the standard definition of again rather than the revised one, the repetitive reading of (1) will not logically entail the non-repetitive reading, but it will still practically entail it. The repetitive reading of (1) asserts that the door became open; thus, for the reading to be true the door must thus be closed at the beginning of the topic interval. The repetitive reading presupposes (i) that the door became open before the topic interval, and also (ii) that between these two openings it did not become open. However, the negation of $\operatorname{BEC}(P)(i)$ is $P(\operatorname{beg}(i)) \vee \neg P(e n d(i))$; it thus does not follow from the fact that something did not become open that thing became not open. With both versions of again, the repetitive reading is predicted to be true in a situation where the door did not actually close until the very beginning of the topic interval, i.e. for a situation in which the door was only fully closed for a single moment. Thus, taking the standard definition of again rather than the revised one, the entailment will fail only in a situation in which the door is closed for precisely one moment; in such a case the repetitive reading, but not the non-repetitive one, will hold. Since such situations do not play any role in what follows, the revised version of again will be adopted for the remainder of the discussion.

## 3 Degree Achievements and again

As we saw above, there is no entailment between the two readings of The river widened again; the BECOME-again analysis thus cannot apply to this sentence. Von Stechow [9] assumes that the decomposition of a sentence like (4) does contain a BECOME operator, along with a comparative structure. While he derives the correct presupposition for the non-repetitive reading (i.e. a reading which only presupposes a previous narrowing), he derives the incorrect presupposition for the repetitive reading; his analysis predicts that the repetitive reading of a sentence like (4) can only be uttered truthfully in a situation that includes both a previous widening and a narrowing. His account thus predicts that (4) cannot be uttered truthfully in a situation like situation 2 in table 1 ; it also predicts that a sentence like (4) demonstrates the same kind of entailment as (1). Both of these results are intuitively incorrect.

The account argued for here follows von Stechow [9] in assuming that DA predicates are decomposed into comparative structures, but holds that this decomposition does not contain BECOME at all. The proposed structure is shown in (14).
(14) The river widened.
at END [the river is [more than [at BEG it is wh wide]] wide]
The assumptions regarding comparatives adopted here are based on Heim [5], with a maximality semantics for morel-er and an 'at least' semantics for gradable adjectives.
$\|$ more $\|^{\mathrm{g}, \mathrm{i}}=\left[\lambda \mathrm{f}_{\text {<d<el>> }} \cdot \lambda \mathrm{g}_{<\mathrm{d}<\mathrm{et}\rangle>}: \max \{\mathrm{d} \mid \mathrm{g}(\mathrm{d})=1\}>\max \{\mathrm{d} \mid \mathrm{f}(\mathrm{d})=1\}\right]$
(to be slightly amended below)
$\|$ wide $\|^{g, i}=[\lambda \mathrm{d} . \lambda \mathrm{x}: \forall t \in i, x$ is at least $d$ wide at $t]$
The structure in (14) also contains two sentential operators BEG and END, which shift the interval of evaluation to, respectively, the initial and final moment of the index interval.
a. $\|$ at $\operatorname{BEG} \|^{g, \mathrm{i}}(\mathrm{P})=1$ iff $\mathrm{P}(\operatorname{beg}(i))=1$
b. $\|$ at $\operatorname{END} \|^{s, i}(\mathrm{P})=1$ iff $\mathrm{P}($ end $(i))=1$

The structure in (14) is uninterpretable as is, since llmorell requires two predicates of degrees as input. However, following Heim [5], if we assume that a comparative DegP - like an object quantifier - raises for interpretation, the structure becomes interpretable (also assuming null-operator movement in the than-clause). The interpretable structure is shown in (18), along with the derived truth-conditions.
more than [wh 2 at BEG it is $d_{2}$ wide] [ 1 at END the river is $d_{1}$ wide]
$\|(18)\| \|^{\mathrm{g}, \mathrm{i}}=1 \mathrm{iff}$
$\max \{\mathrm{d} \mid$ river is d-wide at $\operatorname{end}(i)\}>\max \{\mathrm{d} \mid$ river is d -wide at $\operatorname{beg}(i)\}$

Given this analysis, the sentence The river widened can be paraphrased as 'the river is wider at the end of the interval than at the beginning of the interval'.

Heim [5] proposes that certain ambiguities can be explained by allowing a comparative DegP to scope above or below certain elements; the elements she considers are the intensional verbs require and allow. The ambiguity displayed in a sentence like (4) can be explained in a similar fashion, with again being the relevant element which DegP can scope over. The pre-LF structure for (4) is shown below.

```
The river widened again
before LF movement:
again [at END the river is [more than at BEG it is wh wide] wide]
```

The DegP in (19), like that in (14), must move for interpretation. However, there are now two possible movement sites for DegP to move to: above again, or below. If DegP moves below again, the repetitive reading of (4) is derived; if it moves above again, the non-repetitive reading is derived. The repetitive reading is shown below.

```
repetitive reading
again [more than [wh 2 at BEG it is }\mp@subsup{d}{2}{}\mathrm{ wide] [1 at END the river is }\mp@subsup{d}{l}{}\mathrm{ wide]]
```

$\|(20)\|^{g, i}$ is defined only if:
$\exists g, h \mid g<h \& e n d(h) \leq b e g(i) \&$
$\max \{\mathrm{d} \mid$ river is d -wide at $\operatorname{end}(g)\}>\max \{\mathrm{d} \mid$ river is d -wide at $\operatorname{beg}(g)\}$
$\max \{\mathrm{d} \mid$ river is d -wide at $\operatorname{end}(h)\} \leq \max \{\mathrm{d} \mid$ river is d -wide at $\operatorname{beg}(h)\}$
Where defined, is true iff
$\max \{\mathrm{d} \mid$ river is d -wide at $\operatorname{end}(i)\}>\max \{\mathrm{d} \mid$ river is d -wide at $\operatorname{beg}(i)\}$
The truth-conditions derived for (20) assert that the river widened over the topic interval $i$, and presuppose only that the river also widened at some time $g$ prior to $i$. The presupposition is silent as to whether the river narrowed or stayed at the same width during the interval $h$ between $g$ and $i$. This is the desired result for the repetitive reading, as it allows the sentence to be true in both situation 2 and situation 3 in table 1.

We turn now to the non-repetitive reading of (4), where the DegP moves above again.
non-repetitive reading
more than [wh 2 at BEG it is $d_{2}$ wide] [ 1 again at END the river is $d_{l}$ wide]]
Roughly, this reading can be paraphrased 'at the end of $i$ the river is again wider than its width at the beginning of $i \prime$. Notice that, in the non-repetitive LF, again scopes over a clause containing an unbound variable of degrees, i.e. over the trace left by DegP movement; again thus introduces its definedness condition over the clause in the DegP only. Assuming predicate abstraction limits input degrees to ones that
satisfy the presupposition (see Heim \& Kratzer [4] p.125), the denotation for the lamda-abstracted function is as follows.
(22) \|l 1 again [at END [river is $d_{1}$ wide]] $\|^{g, i}$ is defined only for degrees $d$ such that $\exists g, h \mid g<h \& e n d(h) \leq b e g(i) \&$
(i) the river is $d$-wide at $\operatorname{end}(g)$
(ii) the river is not $d$-wide at end $(h)$.
where defined, is true of a degree $d$ only if the river is $d$-wide at $\operatorname{end}(i)$

This function will only have a non-empty domain if the river narrowed sometime prior to the beginning of the topic interval $i$, as can be deduced from conditions (i) and (ii) in (22). To see examples how this follows, consider again the following situations.

Table 1.

|  | Sit. 1 | Sit. 2 | Sit. 3 | Sit. 4 |
| :--- | :--- | :--- | :--- | :--- |
| April 1 1 $^{\text {st }}$ | 12 m | 10 m | 10 m | 12 m |
| May 1 $^{\text {st }}$ | 12 m | 11 m | 12 m | 12 m |
| June 1 1 $^{\text {st }}$ | 10 m | 11 m | 10 m | 10 m |
| July 1 $^{\text {st }}$ | 12 m | 12 m | 12 m | 10 m |

Let $g$ be the interval between April $1^{\text {st }}$ and May $1^{\text {st }}, h$ be the interval between May $1^{\text {st }}$ and June $1^{\text {st }}$, and $i$ be the interval between June $1^{\text {st }}$ and July $1^{\text {st }}$. In situations 1, 3 and 4, the function in (22) will be defined for all degrees in the half-open interval ( 10 m $12 \mathrm{~m}]$; in situation 2 it will not be defined for any degrees. In situations 1 and 3, the function will be true of all degrees for which it is defined. In situation 4, it will be not be true of any degrees for which it is defined.

The situations in which the domain of the function in (22) is non-empty (situations 1,3 and 4) thus match those situations in which the presupposition of the nonrepetitive reading is intuitively satisfied. In order to derive the correct presupposition for the entire sentence (i.e. in order to have the presupposition in the DegP project), we need to assume that the comparative morpheme has a definedness condition which requires that its two input <dt> functions are also defined. This condition is shown below.
(23) $\quad \|$ more $\|(\mathrm{f})(\mathrm{g})$ is defined iff $\exists \mathrm{d} \mid \mathrm{f}(\mathrm{d})$ is defined $\& \exists \mathrm{~d} \mid \mathrm{g}(\mathrm{d})$ is defined

Note that this condition seems seems to be independently needed, as comparative sentences appear in general to allow for presupposition projection in both the matrix and the DegP clause. For example,

My boat is longer than your boat.
presupposes
I have a boat \& you have a boat
Assuming the above definedness condition for more, the truth-conditions for the nonrepetitive reading come out as follows:
$\|(21)\|^{g, i}$
is defined only if:
$\exists \mathrm{d}, \exists g, h \mid g<h \& \operatorname{end}(h) \leq \operatorname{beg}(i) \&$
the river is d-wide at $\operatorname{end}(g) \&$
the river is not d-wide at $\operatorname{end}(h)$
Where defined, is true iff $\max \{\mathrm{d} \mid$ river is d -wide at $\operatorname{end}(i)\}>\max \{\mathrm{d} \mid$ river is d -wide at $\operatorname{beg}(i)\}$

These truth-conditions contain the presupposition only that the river narrowed sometime before the beginning of $i$. As such, the sentence is predicted to be true in situations 1 and 3, which correctly matches speaker intuitions. The DegP scope account thus correctly derives a repetitive and a non-repetitive reading for (4), neither of which entails the other.

## 4 Conclusion

The DegP scope account presented above derives the correct truth-conditions for both readings of the sentence in (4), which can be seen as a general case of a sentence containing a Degree Achievement predicate and again. A number of conclusions follow from the above discussion. First of all, it is clear that not all again-ambiguities can be explained by the BECOME-again scope analysis, since not all ambiguities demonstrate the entailment between readings that such an analysis predicts.

Second, the again-ambiguity found in sentences with DA predicates like widen can be explained in terms of the position a comparative DegP takes with respect to again, if we assume that DA predicates are decomposed into the comparative structures proposed in §3. This account follows Heim [5], where it is proposed that DegP can scope above certain elements. If the current proposal is on the right track, again should be added to this list of elements.

Finally, the fact that DA predicates give rise to a different type of again-ambiguity than result-state predicates provides strong evidence that the two types of predicates have different internal structure. In particular, the specific ambiguity found in sentences with DA predicates demonstrates that such predicates cannot contain a BECOME operator.

While the above discussion has shown it to be quite plausible that againambiguities have different sources in different sentences, it is left to future work to determine whether a more general account of again-ambiguities can be provided which can apply to all of the various cases.

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# Equatives, measure phrases and NPIs ${ }^{\star}$ 

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#### Abstract

Standard semantic accounts of the equative ascribe it an 'at least' meaning, deriving an 'exactly' reading when necessary via scalar implicature. I argue for a particular formulation of this scalar implicature account which considers that (i) equatives license NPIs in their internal arguments, and (ii) equatives whose internal arguments are measure phrases (MPs) are, in contrast to clausal equatives, ambiguous between 'at most' and 'exactly' interpretations. The analysis employs particular assumptions about MPs, scalar implicature and the notion of set complementation to enable 'at least' readings to be sensitive to the direction of a scale, thereby becoming 'at most' readings in certain constructions.


## 1 Introduction

### 1.1 Equatives and MPs

It's been observed that equatives are ambiguous. These two possible meanings are reflected in the two felicitous responses to (A) in (1). In (B), John's being taller than Sue is incompatible with (A) (on the 'exactly' reading); in (B'), John's being taller than Sue is compatible with (A) (on the 'at least' reading).
(1) (A) John is as tall as Sue is.
(B) No, he's taller than Sue is. ( $\mathrm{B}^{\prime}$ ) Yes, in fact he's taller than Sue is.

To be exactly as tall as Sue is to be at least as tall as Sue, which means that the 'exactly' interpretation of an equative entails its 'at least' interpretation (but not vice-versa). Drawing a parallel with other scalar implicature phenomena, we can identify the 'exactly' reading as the strong one and the 'at least' reading as the weak one, and derive the former from the latter via scalar implicature where context allows (Horn, 1972; Klein, 1980; Chierchia, 2004). This suggests an analysis in which the equative looks something like (2).

$$
\begin{equation*}
\llbracket \mathrm{as} \rrbracket=\lambda D^{\prime} \lambda D \cdot \operatorname{Max}(D) \geq \operatorname{Max}\left(D^{\prime}\right) \tag{2}
\end{equation*}
$$

Equatives with measure phrases or numerals in their internal argument ('MP equatives') present a challenge to this account. Whereas an equative like John is as tall as Sue is is ambiguous between an 'at least' and 'exactly' reading, an equative like (3) is ambiguous between an 'at most' and 'exactly' reading.

[^106](3) John biked as far as 500 miles yesterday.
(3) is consistent with John having biked 500 miles yesterday (the 'exactly' reading); it's also consistent with John having biked 450 miles yesterday (the 'at most' reading). It is not however consistent with John having biked 550 miles yesterday (the 'at least' reading). Although MP equatives are slightly more marked than other equatives (and than their MP construction counterparts), this important distinction between possible readings of MP equatives and other equatives poses a challenge to a comprehensive account of the meaning of the equative.

My proposal for a semantics of equatives accounts for this variation. I argue that: (1) while the internal argument of (positive antonym) clausal equatives denotes a downward-monotonic scale, the internal argument of MP equatives denotes an upward-monotonic scale; and (2) equatives invoke a mechanism of comparison that is sensitive to the directions of the scales being compared.

### 1.2 Background assumptions

I'll start by outlining some basic assumptions about the semantics of degrees and comparative constructions. First, I follow many others in assuming that gradable adjectives denote relations between individuals and degrees.

$$
\begin{equation*}
\llbracket \operatorname{tall} \rrbracket=\lambda x \lambda d \cdot \operatorname{tall}(x, d) \tag{4}
\end{equation*}
$$

The order of arguments in (4) is consistent with Schwarzschild's observation that MPs like 5ft in e.g. John is 5ft tall function as predicates of scales (ordered, dense sets of degrees), rather than arguments of the adjective. I assume that numerals denote degrees (type $\langle d\rangle$ ) and combine with measure expressions (like inch) to form these predicates via a null measure function $\mu$, which also enables numerals to combine with other common nouns like cats (Cartwright, 1975; Nerbonne, 1995; Schwarzschild, 2002, 2006).

I also assume that positive and negative antonyms (like tall and short) differ in their ordering, which is observable in their behavior in comparatives (Seuren, 1984; von Stechow, 1984, a.o.). Positive antonym scales are downward-montonic, with open lower bounds of zero and closed upper bounds (5a). Negative antonym scales like short are upward-monotonic, with closed lower bounds and closed upper bounds of infinity (5b).
(5) Context: John is 5 ft tall.

$$
\text { a. } \quad \lambda d . \text { tall }(\text { john }, d)=(0,5] \quad \text { b. } \lambda d . \text { short }(\text { john }, d)=[5, \infty]
$$

## 2 Comparatives

Following Hankamer (1973), I will use the terms target and correlate to refer to the subordinate and matrix material in comparatives, respectively (6a).

$$
\begin{equation*}
\text { a. } \frac{\text { John is taller than } \frac{\text { Sue is. }}{\text { correlate }}}{\text { target }} \tag{6}
\end{equation*}
$$

## b. John is taller than [ ${ }_{\mathrm{CP}} \mathrm{OP}_{d}$ Sue is $d$-tall ]

Following Bresnan (1973), I assume that comparatives and equatives with overt tense morphology are clauses that have undergone elision along the lines of (6b). I follow Pancheva (2006) in using the term 'phrasal' to refer to comparatives and equatives whose target cannot have overt clausal material (7), and 'clausal' to refer to those whose target is either clausal or has a plausible clausal source.
a. John is taller than $6 \mathrm{ft}\left({ }^{*} \mathrm{is}\right)$.
b. No man is stronger than himself ( ${ }_{\mathrm{i} i s}$ ). (Hoeksema, 1983, 405)

Based in part on arguments in Schwarzschild (2008), I adopt the 'A-not-A' account of the comparative in (8) (McConnell-Ginet, 1973; Kamp, 1975; Hoeksema, 1983; Seuren, 1984, a.o.). An important consideration of this theory is the fact that NPIs are licensed in the targets of (clausal) comparatives (9).

$$
\begin{equation*}
\lambda D^{\prime} \lambda D \exists d\left[D(d) \wedge \neg D^{\prime}(d)\right] \tag{8}
\end{equation*}
$$

a. He would rather lose his honor than so much as a dime.
b. She is happier now than ever before.

This generalization comes with two caveats, one significant and the other less so. Less significant is that the any licensed in comparative targets (e.g. John is taller than anyone in his class) is modifiable by almost and thus appears to instead be a free-choice any (Hoeksema, 1983). More significantly is the issue of how NPIs could possibly be licensed in comparatives given the apparent lack of superset-to-subset entailment in the target ((10); Seuren, 1984; von Stechow, 1984; Hoeksema, 1983, 1984; Heim, 2003).
(10) Cheetahs are faster than lions. $\nrightarrow$ Cheetahs are faster than speedy lions.

What these sorts of tests - common in discussions of NPIs in comparatives overlook is that the comparative is a degree quantifier, not an individual one. Testing for subset-to-superset entailment of degree sets (instead of individual sets) shows that the targets of comparatives are in fact downward-entailing. ${ }^{1}$
(11) Context: Mary is 6 ft tall, John is 5 ft tall, Sue is 4 ft tall.
a. Mary is taller than John. $\rightarrow$ Mary is taller than Sue.
b. Mary is taller than Sue. $\rightarrow$ Mary is taller than John.
(A side note: The problem with using individual sets to test for monotonicity in degree quantifiers isn't just that tests like (10) predict the targets of comparatives aren't DE. It's that they predict that all arguments of all degree quantifiers are non-monotonic. Degree quantifiers differ from individual quantifiers in containing an individual predicate - the one that adjoins to the quantifier, fast in

[^107](10) - in addition to the set-denoting predicates that can occur in their arguments. As a result, there is always at least one subset/superset pair with which the additional predicate can interfere, thus making it impossible to reliably infer from all subsets to supersets (and vice-versa). In other words, testing the monotonicity of the arguments of degree quantifiers using sets of individuals predicts that all arguments of degree quantifiers are non-monotonic, because interference with the comparative predicate will always prevent entailment in every case.)

To sum up: NPIs appear to be licensed in the targets of comparatives, and entailment patterns between supersets and subsets of degrees (11) confirm that the targets of comparatives are downward-entailing (DE). These facts are appropriately captured by the 'A-not-A' analysis in (8) because it properly characterizes the target of comparatives as DE. Before ending this discussion, I would like to point out Hoeksema's (1983) observation that the definition in (8b) is equivalent to the one in (12) that invokes set complements (written as $\bar{D}$ ).

$$
\begin{equation*}
\llbracket-\mathrm{er} \rrbracket=\lambda D^{\prime} \lambda D \lambda d \cdot d \in D \wedge d \in \overline{D^{\prime}} \tag{12}
\end{equation*}
$$

(12) additionally differs from (8b) in not existentially binding the differential degree $d$. This allows for further modification by e.g. much and 3 inches in John is much/3 inches taller than Sue. I assume that, in the absence of a differential modifier, the differential argument $d$ is bound via existential closure.

## 3 Equatives

I'll begin this section by discussing the MP equative data more indepthly. My claim is that all of the equatives in (13) are ambiguous between an 'exactly' and 'at most' reading, and can never have an 'at least' reading.
(13) a. (I think) John biked as far as 500 miles yesterday.
b. (I heard that) the DOW dropped as much as 150 points yesterday.
c. The moon is as far as 240,000 miles away.
d. The waves reached as high as 6 ft .
e. GM plans on laying off as many as 5,000 employees.

For instance, (13e) is true if GM is planning on laying off 4,500 employees, but not if they're planning on laying off 5,500 . This is in distinct contrast with the truth conditions of the clausal equative GM plans on laying off as many employees as Chrysler (did) in a context in which Chrysler laid off 5,000 employees.

Importantly, the distribution of MP equatives is restricted relative to clausal ones. They are licensed when: (a) their value is significantly high given the context (is 'evaluative'; Rett, 2008); and (b) the value of the correlate is indeterminate. This second restriction is manifested in a variety of ways: the speaker can be unsure of the amount at issue (13b), the measure need not be precise in the context (13c), or the correlate can denote a range, either via a plurality (13d), or a modal (13e). These restrictions on the distribution of MP equatives seem directly related to their being more marked than their (intuitively synonymous) MP construction counterparts (e.g. John biked 500 miles yesterday).

Nouwen (2008, to appear) makes a similar point about the distribution of what he calls 'Class B' comparative quantifiers (e.g. at most 6ft, up to 6ft). He argues that they can only quantify over ranges, and that they equate the maximum of that range to, say, 6 ft . It's not clear to me whether MP equatives fall under this description. On the one hand, the correlates in (13a) and (13b) don't appear to be ranges, and (13c) seems to be acceptable in a context in which the moon is 200,000 miles away. The fact that e.g. (13b) is unacceptable in a situation in which the DOW dropped a mere 5 points can be attributed to the evaluativity of MP equatives, which we already know provides a lower bound (a contextually valued standard $s$ ), and which is perhaps a result of their competition with less marked MP constructions.

On the other hand, the MP equatives which do involve clear ranges, like (13d), seem to pattern like Nouwen's Class B quantifiers. (13d) seems false if the highest wave only reached $5 \frac{1}{2}$ feet. It's possible, then, that the MP equatives in (13a) and (13b) involve ranges, too (manifested as a range of epistemic possibilities). If this is the case (if all MP equatives associate the maximum value of the correlate range with the measure denoted by the MP), then it's more appropriate to characterize MP equatives as having only an 'exactly' interpretation.

Still, there is a stark contrast between clausal and MP equatives: in GM plans on laying off as many employees as Chrysler, the minimum value in the range of employees laid off by GM is that of Chrysler's. In (13e) it's the maximum value that measures 5,000. Regardless of the precise nature of the semantics of MP equatives, we need an account that explains this contrast.

### 3.1 MPs and scalar implicatures

The equatives in (13), of course, all have in common that their targets are MPs. They have other things in common: they're all evaluative, for instance. But some clausal equatives (John is as short as Sue) are evaluative without having an 'at most' reading. I argue that the equatives that are 'at most'/'exactly' ambiguous are those and only those whose targets are MPs because MPs (and numerals) are themselves scalar. The traditional SI account of sentences like John has 3 children assigns the numeral an 'at least' semantics $(\geq 3)$, deriving the 'exactly' interpretation via scalar implicature, where appropriate (contra Geurts, 2006).

This means that the denotation of an MP target (in a positive-antonym equative, like those in (13)) is an upward-monotonic set of degrees, with a lower bound of $d$ (for a $d$-denoting numeral) and an upper bound of $\infty$. In a context in which Sue is 5 ft tall, the target of the equative John is as tall as Sue (is) denotes the degrees to which Sue is tall (14a), which is downward-monotonic. The target of the equative John could be as tall as 5ft, on the other hand, denotes the degrees greater than or equal to $5 \mathrm{ft}(14 \mathrm{~b})$, which is upward-monotonic.
a. $\quad \llbracket \mathrm{Op}_{d}$ Sue is $d$-tall $\rrbracket=\lambda d$.tall $($ sue,$d)=(0,5]$
b. $\quad \llbracket 5 \mathrm{ft} \rrbracket=\lambda d . d \geq 5 \mathrm{ft}=[5, \infty]$

This particular characterization of MPs wouldn't be an issue if it wasn't for the independent observations tying it to SIs in DE contexts. Chierchia (2004)
claims that SIs (a) can be calculated sub-sententially, and (b) are calculated differently in DE contexts.

I'll illustrate this point as Chierchia does, independently of equatives and MPs. Or is typically characterized as scalar (on a Horn scale with and), ambiguous between a weak reading ( $A$ or $B$ or both) and a strong reading ( $A$ or $B$ but not both). The strong reading is then characterized as coming about, where pragmatically possible, as a result of scalar implicature (15a). In DE environments, though, this SI is affectively cancelled; (15b) cannot be used to negate the claim that Sue didn't meet both Hugo and Theo (and is therefore incompatible with Sue having met both). Chierchia's explanation is that SIs are calculated in terms of informativity, and what counts as the most informative in upward-entailing contexts is actually the least informative in DE contexts (and vice-versa).

## a. Sue met Hugo or Theo. b. Sue didn't meet Hugo or Theo.

Extending this generalization to equatives, whose targets are DE, means that the targets of MP equatives always (across all contexts) have their weak meaning.

### 3.2 A more sensitive semantics

The crux of the analysis that follows is a reformulation of the equative morpheme, motivated by the fact that NPIs are licensed in the targets of equatives, too:
a. He would just as much lose his honor as he would a dime.
b. She is as happy now as ever before.

We thus need a semantics of the equative in which its target, too, is DE. Drawing on the set-complement definition of the comparative (12), I propose (17). ${ }^{2}$

$$
\begin{align*}
& \llbracket \operatorname{as} \rrbracket=\lambda D^{\prime} \lambda D\left[\operatorname{Max}(D) \in \widehat{D^{\prime}}\right] \text {, where }  \tag{17}\\
& \widehat{D}=\text { def } \text { the smallest } D^{\prime} \text { such that } \bar{D} \subseteq D^{\prime} \text { and } D^{\prime} \text { is a closed set. }
\end{align*}
$$

This definition invokes the notion of a 'closure of the complement', the smallest superset of the complement with closed bounds. ${ }^{3}$ It is downward-entailing in its target $\left(D^{\prime}\right)$, correctly predicting the licensing of NPIs.
(18) Context: Mary is 6 ft tall, John is 5 ft tall, Sue is 4 ft tall.

$$
\begin{aligned}
& \text { Mary is as tall as John. } \rightarrow \text { Mary is as tall as Sue. } \quad \text { is true iff } \\
& \operatorname{Max}((0,6]) \in \widetilde{(0,5]} \rightarrow \operatorname{Max}((0,6]) \in \widetilde{(0,4]} \quad \text { is true iff } \\
& 6 \in[5, \infty] \rightarrow 6 \in[4, \infty] \checkmark
\end{aligned}
$$

${ }^{2}$ The definition in (17) is a simplified version of $=\lambda D^{\prime} \lambda D \lambda d\left[d=\operatorname{Max}(D) \wedge d \in \widehat{D^{\prime}}\right]$, which is required for an account of modified equatives (see $\S 4$ ).
${ }^{3}$ Direct application of (17) will result in some scales having a closed lower bound of zero. This is formally unattractive but actually harmless, assuming that it is infelicitous to predicate a gradable property of an individual if that individual doesn't exhibit that property at all (cf. \#That couch is intelligent). We could alternatively reformulate the definition of a closure of a complement to omit this possibility.

Positive-antonym MP equatives differ from positive-antonym clausal equatives in that their target is upward-monotonic. The definition in (17) allows the 'greater than' relation we implicitly associate with the 'at least' reading of the equative to be sensitive to the ordering on the target scale; it affectively employs a different relation ('at least', 'at most') based on the direction of the target scale.
(19) John is as tall as Sue. (John's height $=5 \mathrm{ft}$; Sue's height $=5 \mathrm{ft}$; true)

$$
\operatorname{MAX}((0,5]) \in \widehat{(0,5]} \rightsquigarrow 5 \in[5, \infty] \checkmark
$$

(20) John is as tall as Sue. (John's height $=6 \mathrm{ft}$; Sue's height $=5 \mathrm{ft}$; true)

$$
\operatorname{Max}((0,6]) \in \widehat{(0,5]} \rightsquigarrow 6 \in[5, \infty] \checkmark
$$

(21) John is as tall as Sue. (John's height $=5 \mathrm{ft}$; Sue's height $=6 \mathrm{ft}$; false)

$$
\operatorname{Max}((0,5]) \in \widehat{(0,6]} \rightsquigarrow 5 \in[6, \infty] \boldsymbol{x}
$$

(22) The waves reached as high as 6 ft . (waves' height $=6 \mathrm{ft}$; true)

$$
\operatorname{Max}((0,6]) \in \widehat{[6, \infty}] \rightsquigarrow 6 \in[0,6] \checkmark
$$

(23) The waves reached as high as 6 ft . (waves' height $=5 \mathrm{ft}$; true)

$$
\operatorname{Max}((0,5]) \in \widehat{[6, \infty}] \rightsquigarrow 5 \in[0,6] \checkmark
$$

(24) The waves reached as high as 6 ft . (waves' height $=7 \mathrm{ft}$; false)

$$
\operatorname{Max}((0,6]) \in \widehat{[6, \infty]} \quad \rightsquigarrow 7 \in[0,6] \boldsymbol{x}
$$

(17) works just as well for negative-antonym equatives, whose clausal arguments are upward-monotonic (see (5b)). I assume a definition of the maximality operator in which it is sensitive to the direction of the scale (Rett, 2008).
(25) John is as short as Sue. (John's height $=5 \mathrm{ft}$, Sue's height $=5 \mathrm{ft}$; true) $\operatorname{Max}([5, \infty]) \in \widehat{[5, \infty}] \rightsquigarrow 5 \in[0,5] \checkmark$
(26) John is as short as Sue. (John's height $=4 \mathrm{ft}$, Sue's height $=5 \mathrm{ft}$; true) $\operatorname{MAX}([4, \infty]) \in \widehat{[5, \infty}] \quad \rightsquigarrow 4 \in[0,5] \checkmark$
(27) John is as short as Sue. (John's height $=5 \mathrm{ft}$, Sue's height $=4 \mathrm{ft}$; false) $\operatorname{Max}([5, \infty]) \in \widehat{[4, \infty]} \rightsquigarrow 5 \in[0,4] \boldsymbol{x}$

To extend the analysis to negative-antonym MP equatives (like The temperature dropped as low as $2^{\circ}$ Kelvin), we must recall that the target also involves a negative antonym (e.g. $2^{\circ}$ low, rather than $2^{\circ}$ high). This is consistent with Bresnan's (and Kennedy's (1999)) assumptions about the syntax of comparatives and equatives $((28)$, cf. ( 6 b$)$ ).

John has fewer children than Sue.
-er ( $\left[\mathrm{Op}_{d}^{\prime}\right.$ Sue has $d^{\prime}$-few children $]$ ) ([ $\mathrm{Op}_{d}$ John has $d$-few children $\left.]\right)$
MP targets of negative-antonym equatives are thus in fact downward-monotonic, which results in the correct truth conditions.
(29) The temperature dropped as low as $2^{\circ}$ Kelvin. (highest temp $=2^{\circ}$; true) $\operatorname{MAx}([2, \infty]) \in \widehat{(0,2}] \quad \rightsquigarrow 2 \in[2, \infty] \checkmark$
(30) The temperature dropped as low as $2^{\circ}$ Kelvin. (highest temp $=3^{\circ}$; true) $\operatorname{Max}([3, \infty]) \in \widehat{(0,2}] \quad \rightsquigarrow 3 \in[2, \infty] \checkmark$
(31) The temperature dropped as low as $2^{\circ}$ Kelvin. (highest temp $=1^{\circ}$; false) $\operatorname{MAX}([1, \infty]) \in \widehat{(0,2}] \rightsquigarrow 1 \in[2, \infty] \boldsymbol{x}$

## 4 Extensions and conclusions

Equative modifiers. Importantly, this analysis calls for a semantics of superlative modifiers like at least and at most that are not sensitive to the direction of the scale. This is because at least can modify MP equatives, forcing them to have an 'at least' interpretation (32a), and at most can modify clausal equatives, forcing them to have an 'at most' interpretation (32b).
a. John biked at least as far as 500 miles yesterday.
b. John is at most as tall as Sue (is).

I argue that such an analysis requires the assumption that pragmatic strengthening is applied to equatives before the equatives are modified. The modifiers therefore take strengthened, 'exactly' equative meanings as their arguments, and add a restricting clause based on an objective scale direction ( $\leq$ or $\geq$ ).

MP comparatives. The assumptions made above about the denotation of MPs in DE contexts doesn't extend straightforwardly to comparatives given the definition in (12). In particular, feeding an upward-monotonic denotation of MPs into (12) erroneously predicts that all MP comparatives are true.

$$
\begin{align*}
& \text { John is taller than 5ft. (John's height }=4 \mathrm{ft} \text {; false) }  \tag{33}\\
& \exists d[d \in(0,4] \wedge d \in \overline{[5, \infty]]} \rightsquigarrow \exists d[d \in(0,4] \wedge d \in(0,5)
\end{align*}
$$

Instead, it seems that the incorrect truth conditions in (33) underscore the argument in Pancheva (2006) that comparative subordinators are meaningful and differ in their meanings. In fact, some languages employ different comparative subordinators for MP targets than they do for clausal targets (cf. Spanish de lo que DP versus de MP). One possible way of adopting Pancheva's analysis while holding fixed this particular characterization MPs as denoting their weak meaning in DE contexts is to argue that the comparative morpheme -er is a simple quantifier over degrees, while clausal than is a function from a set to its complement (thus resulting in the NPI data above), and MP than is an identity function over degree sets.
a. $\quad \llbracket-\mathrm{er} \rrbracket=\lambda D^{\prime} \lambda D \lambda d . d \in D \wedge d \in D^{\prime}$
b. $\llbracket t \operatorname{than}_{\text {clausal }} \rrbracket=\lambda D \lambda d . d \notin D \quad$ b. $\llbracket \operatorname{than}_{M P} \rrbracket=\lambda D \lambda d . D(d)$

Slavic languages provide independent evidence that MP targets of comparatives are treated differently from clausal targets of comparatives. ((35) is Pancheva's example from Russian, in which clausal comparatives are formed with the whphrase čem, and phrasal comparatives are formed with a covert subordinator.)
a. ??Ivan rostom bol'še čem dva metra.

Ivan in-height more what two meters
b. Ivan rostom bol'še dvux metrov.

Ivan in-height more [two meters] $]_{\text {GEN }}$
'Ivan measures in height more than two meters.'
In effect, this discussion of MPs in comparative and equative targets helps provide an explanation for why languages would employ two different subordinators for clausal comparatives and MP comparatives: the two types of targets denote two different types of scales, and as a result need to be dealt with differently. It is also compatible with the observation that some languages disallow MP equatives entirely (e.g. German, Daniel Büring, p.c.). These languages, at first glance, appear to be those that employ $w h$-phrases as equative subordinators.

DP equatives. Some phrasal equatives have DP rather than MP targets.
a. John can reach as high as the ceiling $\left({ }^{*}\right.$ is $)$.
b. This rubber band can stretch as wide as a house $\left({ }^{*}\right.$ is).

It appears as though these equatives, too, must be indeterminate, or a range of some sort (37a), but this requirement comes in the absence of any obvious unmarked counterparts ((37b), cf. MP contructions).
a. ??John reached as high as the ceiling.
b. ??John can reach the ceiling's height.

It's not clear to me which of the three readings ('at least', 'at most', 'exactly') DP equatives have. (36a), for instance, seems both compatible with John being capable of reaching lower than the ceiling's height and with John being capable of reaching higher than the ceiling. I suspect that the meaning of these DPs rely heavily on the contextual salience of the DP, not just the measure denoted by the DP. This point is made especially clear by DP equatives like This train will take you as far as Berkeley, which is intuitively false if the train will take you somewhere equidistant to Berkeley (but not to Berkeley itself).

Conclusion. Clausal equatives are ambiguous between 'at least' and 'exactly' interpretations, while MP equatives are ambiguous between 'at most' and 'exactly' interpretations. I argue that these phenomena can be assimilated in a neo-Gricean SI framework if we characterize the weak meaning of the equative in a way that is sensitive to the scalar ordering of its internal argument. The account relies on independent observations that numerals (and therefore MPs) are themselves scalar, and that scalar implicature is calculated sub-sententially and differently in downward-entailing contexts (Chierchia, 2004).

## General Program

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# Squiggly Issues: Alternative Sets, Complex DPs, and Intensionality 

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#### Abstract

In this paper, we investigate a number of long-standing issues in connection with (i) focus interpretation and its interrelation with complex definite descriptions, and (ii) the intensional properties of sentences with focus constituents. We revitalize the use of Rooth's (1992) ~ operator, clarify its definition as an anaphoric operator, discuss the principles that govern its placement in logical forms and show how it can be succesfully employed to replace the notion of Krifka's (2006) focus phrases. Finally, we argue that a proper view of the intensional dimension of retrieving the antecedent sets required by the operator can account for problems relating to the intensionality of sentences with focus sensitive operators that are discussed by Beaver \& Clark (2008).


## 1 Introduction: Focus Semantic Values and Context Sets

According to Rooth $(1985,1992,1996)$ focusing - the semantic reflex of an F feature assigned to some constituent X in logical form - leads to the creation of a focus semantic value $\llbracket X \rrbracket^{f}$ (FSV). The FSV is simply the domain of objects having the same semantic type as the ordinary semantic value $\llbracket X \rrbracket^{o}$ relative to some model. For instance, the FSV of the phrase [THEodore] $F_{F}$ is simply the domain of individuals $\mathrm{D}_{e}$.

Note that, other than in the case of mathematical models, natural discourse does not enable us to exhaustively list all entities that belong to $\mathrm{D}_{e}$ since we are not omniscient. All we know is that if $d$ is an individual then it is a member of $\mathrm{D}_{e}$. We shall therefore consider focus semantic values to be (anonymous) characterizations rather than extensionally determined sets.

It is well-known since Rooth (1992) that FSVs are not as such suited to function with conventionally focus-sensitive particles ${ }^{3}$; they need to undergo contextual restriction. Consider the sequence in (1).
(1) a. We have invited all siblings of your mom but, I noticed, we have really neglected your father's relatives.
b. So far, we have only invited [uncle THEodore] ${ }_{F}$.
(2) $\quad \forall x[x \in C \wedge$ invite $(\mathbf{w e}, x) \rightarrow x=\mathbf{t}]$

[^108]Using a standard semantics for only yields (2) as the reading for (1b). We get the wrong result if the quantificational domain $C$ for only is set to $D_{e}$ since this set also comprises Mom's invited siblings and (2) would falsely rule them out. Therefore, in order to get the proper meaning for (1b), $C$ must be restricted to a contextually available set, in this case "your father's relatives".

For this and a number of other focus-related purposes, Rooth (1992, 1996) defines, in addition to the focus feature F, a focus interpretation operator $\sim$, which can in principle attach to arbitrary constituents. If X is some constituent, $\llbracket X \rrbracket^{o}$ is the ordinary meaning of X and $\llbracket X \rrbracket^{f}$ is the FSV, then $\sim \mathrm{X}$ triggers a presupposition such that a context set $C$ containing a contrastive item $y$ must be identified, with the properties given in (3). ${ }^{4}$
(3)
(i) $C \subseteq \llbracket X \rrbracket^{f}$
(ii) $y \in C$
(iii) $y \neq \llbracket X \rrbracket^{o}$

In the following we would like to scrutinize the anaphoric nature of $\sim$. For that purpose we provide a translation of the constraints in (3) into DRT, which is geared to the treatment of presuppositions and anaphora in the framework of van der Sandt (1992), Geurts (1999) and Kamp (2001). Definite descriptions like in the second sentence of (4) are represented as in Fig. 1a, where the anaphoric variable $\underline{z}$ is waiting to get bound to the previously mentioned customer $x .{ }^{5}$
(4) A customer entered. Mary greeted the man.


Fig. 1a.
Preliminary DRS for (4)


Fig. 1b.
Presupposition triggered by $\sim X$

In this vein, we formulate the $\sim$ conditions from (3) as in Fig. 1b.

[^109]
## 2 Squiggle Placement

A representation like the one in Fig. 1b - in particular the treatment of $C$ as an anaphoric variable - clearly shows that the semantic type which these variables adopt is dependent on the attachment site of $\sim$. If $\sim$ attaches to a DP then $C$ must be a set of individuals. If it attaches to a VP then $C$ is a set of properties or, preferably, a set of events or states. Seen in this light, it is surprising that Rooth (1992: 89) chooses to attach the $\sim$ in (5) at VP level.
(5) Mary only $\sim\left[V P\right.$ introduced BILL $_{F}$ to Sue $]$.

Rooth assumes that only is syntactically adjoined to VP and that it quantifies over the set provided by a variable $C$ which gets instantiated by means of $\sim$. The squiggle operator, in its designated location, triggers the presupposition in Fig. 2a,b.


Fig. 2a
Presupposition triggered by $\sim\left[{ }_{V P} \ldots\right]$


Fig. 2b
Same issue, using event semantics

We provide two variants of this presupposition. Figure 2a is immediately derived from Rooth's original account, Fig. 2b is a reformulation in Neo-Davidsonian semantics, which uses discourse referents for events rather than properties (as it is common practice in DRT). ${ }^{6}$ The meaning of (5) is correctly represented as $(6 a)^{7}$ or (6b).
a. $\forall P[P \in C \wedge P(\mathbf{m}) \rightarrow P=\lambda x \cdot \operatorname{introd}(x, \mathbf{b}, \mathbf{s})]$
b. $\forall e[e \in C \wedge \mathrm{AG}(e, \mathbf{m}) \rightarrow \mathrm{TH}(e, \mathbf{b})]$

The question is whether it is plausible to assume that the instantiation of $C$ is due to anaphoric retrieval as suggested by the definitions in Fig. 2a,b. Consider the discourse in (7).
a. At the party, there were Alex, Bill, and Carl, none of whom Sue had met before.
b. Mary only introduced BILL $_{F}$ to Sue.

There are no introduction events in the discourse context given by (7a). It seems therefore wrong to assume that (7b) involves anaphoric retrieval of a set of VP-

[^110]meanings of the form［introduced z to Sue］．On the other hand，it is highly likely that retrieval is of a set of alternatives to Bill．But in that case it is more intuitive for $\sim$ to attach to $\left[\mathrm{BILL}_{F}\right]$ as shown in（8）．
（8）Mary only introduced $\sim\left[_{D P}\right.$ BILL $\left._{F}\right]$ to Sue．
The problem is how to bring this insight in line with the semantics in（6a）， which was found to be essentially correct．First of all，since $C$ is now the set of individuals $\{\mathbf{a}, \mathbf{b}, \mathbf{c}\}$ rather than a set of predicates，it can no longer be used in formula（6a）as before．What we want instead is（9）．
\[

$$
\begin{align*}
& \forall P\left[P \in \llbracket \text { introd. } \sim\left[B I L L_{F}\right] \text { to } S u e \rrbracket^{A} \wedge P(\mathbf{m}) \rightarrow P=\lambda x \operatorname{introd}(x, \mathbf{b}, \mathbf{s})\right] ;  \tag{9}\\
& \text { where } \llbracket \text { introd. } \sim\left[B I L L_{F}\right] \text { to Sue } \rrbracket^{A}=\{\lambda x . \operatorname{introd}(x, z, \mathbf{s}) \mid z \in C\}
\end{align*}
$$
\]

We call $\llbracket \cdot \rrbracket^{A}$ simply an alternative set in order to distinguish it from the previ－ ously defined FSV $\llbracket \cdot \rrbracket^{f}$ ，the difference being that，on our treatment，alternative sets contain elements that can be extensionally listed because they are ultimately grounded via a process of anaphoric identification．Of course，the anaphorically retrieved context set $C$ is itself a basic alternative set，but alternative sets can also derive from semantic composition based on $C$ ．In switching from Rooth＇s （6a）to（9），we are reversing the order of compositional focus semantics and anaphoric retrieval as shown in Table 1．In doing so，we maintain the desired reading but avoid implausible anaphoric processes and，furthermore，establish a clear criterion for $\sim$ placement．

| Rooth（1992） | Our Account |
| :---: | :---: |
|  | $\llbracket B I L L_{F} \rrbracket^{f}=D_{e}$ |
| Foc．int．$\rightarrow \llbracket \sim\left[B I L L_{F}\right] \rrbracket^{A}=\{\mathbf{a}, \mathbf{b}, \mathbf{c}\}$ |  |
| 【introd．$B I L L_{F} \rrbracket^{f}$ | 【introd．$\sim\left[B I L L_{F}\right] \rrbracket^{A}$ |
| $=\left\{\lambda y \lambda x \cdot \operatorname{introd}(x, z, y) \mid z \in D_{e}\right\}$ | $=\{\lambda y \lambda x \cdot \operatorname{introd}(x, z, y) \mid z \in\{\mathbf{a}, \mathbf{b}, \mathbf{c}\}\}$ |
| 【introd．BILL ${ }_{\text {F }}$ to Sue】 ${ }^{f}$ | 【introd．$\sim\left[B I L L_{F}\right]$ to Sue】 ${ }^{\text {A }}$ |
| $=\left\{\lambda x \operatorname{introd}(x, z, \mathbf{s}) \mid z \in D_{e}\right\}$ | $=\{\lambda x \operatorname{cintrod}(x, z, \mathbf{s}) \mid z \in\{\mathbf{a}, \mathbf{b}, \mathbf{c}\}\}$ |
| $\begin{aligned} & \mathbb{\llbracket \sim [ \text { introd. BILL } L _ { F } \text { to } S u e ~} \rrbracket^{A} \\ & =\{\lambda x \operatorname{introd}(x, z, \mathbf{s}) \mid z \in\{\mathbf{a}, \mathbf{b}, \mathbf{c}\}\} \end{aligned}$ |  |

Table 1．Alternative Semantics reversed

## 3 Benefits of our Account

In $(8) \sim$ is adjoined to the focus constituent itself．But we do not propose that this is always so．Our interpretation of the $\sim$ operator allows us，for instance， to handle the issue of focus phrases（Drubig，1994，Krifka，2006）．Sentence（10） demonstrates what Krifka calls＂the problem of the only child＂．
(10) Sam only talked to $\left[\text { BILL's }_{F} \text { mother }\right]_{F P}$.

Drubig and Krifka noticed the problem that (10) presents for a Structured Meanings account which would analyse the sentence as involving only-quantification over Bill and the other members of his alternative set. If the set contains a sibling of Bill then Sam must both have talked to their mother and, at the same time, not have talked to her, and the sentence would come out as a contradiction, although intuitively it isn't. Krifka (2006) solved the problem by postulating that only instead associates with focus phrases (FP), cf. (10), which means that quantification is about referentially distinct alternatives to Bill's mother rather than alternatives to Bill.

By applying our strictly anaphoric definition of the squiggle we automatically get the correct semantics for (10). $\sim$ is attached to ${ }_{[D P}$ BILL's $_{F}$ mother], giving rise to the presupposition in Fig. 3.


Fig. 3. $\sim\left[\right.$ BILL's ${ }_{F}$ mother $]$
a. $\quad \llbracket B I L L^{\prime} s_{F}$ mother $\rrbracket^{o}=\iota x$.mother_of $(x, \mathbf{b})$
b. $\llbracket B I L L^{\prime} s_{F}$ mother $\rrbracket^{f}=\{d \mid \exists x$.mother_of $(d, x)\}$

The ordinary value occuring in Fig. 3 is simply Bill's mother - representable as yet another embedded presupposition or the $\iota$-expression in (11a). The focus semantic value is the anonymous set given in (11b), the set of all mothers of individuals in $D_{e}$. During the process of anaphoric retrieval this set undergoes restriction, and $C$ is resolved to whatever mothers play a role in a certain context. Compare, for instance, sentence (12).

At the party there were Alex, Bill, Carl and Daniel, and also Bill's mother and Carl's mother. I only knew $\sim\left[\right.$ BILL's ${ }_{F}$ mother].

The second sentence of (12) is naturally interpreted as saying that the speaker knew Bill's mother but not Carl's mother, leaving it open whether he also knew the unmentioned mothers of Alex and Daniel. This interpretation can be obtained when $\sim$ is attached to [BILL's ${ }_{F}$ mother], but not when it is attached to [ BILL's $\left._{F}\right]$. Note also that the semantics correctly predicts that the other mentioned persons, who are not mothers, do not become elements of $C$.

As a side remark, Krifka (2006) argues in his article for the use of a "hybrid" system combining insights from Structured Meanings Theory and Alternative Semantics. Our suggestions concerning the use of $\sim$ are very much in the spirit of this proposal. In fact, we might have replaced all bits dealing with focus
semantic values by background expressions．Instead of（11b）we could have used （13），which is simply the characteristic function of（11b）．

$$
\begin{equation*}
\lambda x\left[\exists y . m o t h e r_{-} o f(x, y)\right] \tag{13}
\end{equation*}
$$

Backgrounds and FSVs are interchangeable．However，interchangeability ends as soon as the $\sim$ has anaphorically turned the FSV into a true alternative set $\llbracket B I L L^{\prime} s_{F}$ mother $\rrbracket^{A}$ ，for instance $\{e, f\}$ consisting of Bill＇s mother（Eva）and Carl＇s mother（Florence）．This is where Alternative Semantics takes over from Structured Meanings．

A further benefit of the way we propose to use $\sim$ arises in connection with an example discussed in von Heusinger（2007）．He notices a problem with complex definite descriptions like the one occurring in（14a），which involves adjectival modification．${ }^{8}$
a．John only talked to［the GERman ${ }_{F}$ professor］．
b．\｛【the German professor】，«the French professor】，
【the English professor】，．．．\}
Something is wrong if（14a）is analyzed under the assumption that determin－ ing the truth conditions of the sentence involves computing denotations of ex－ pressions of the form［the A professor］${ }^{9}$ ，in other words a set like（14b）．For it might well be that on the occasion that（14a）speaks of there were besides the one German professor several French professors and therefore the expression【the French professor】 would fail to properly refer．Still，if the only professor that John talked to was the only German professor there，then（14a）is a per－ fectly good way of saying that John only talked with this one professor．

The solution we offer for this case is as follows．The FSV of the phrase［the GERman $_{F}$ professor］is determined by a purely mechanical process as the set characterized by（15a），which does not run into the problems that（14b）caused． The set can even be further simplified to（15b）．

$$
\begin{equation*}
\text { a. } \quad\{d \mid \exists P[P(d) \wedge \operatorname{professor}(d)]\} \quad \text { b. } \quad\{d \mid \operatorname{professor}(d)\} \tag{15}
\end{equation*}
$$

The $\sim$ is then adjoined to［ $D P$ the GERman ${ }_{F}$ professor］，which simply defines the task of retrieving from the context a set of professors $\mathbf{a}, \mathbf{b}, \mathbf{c}, \mathbf{d}, \ldots$ who are naturally distinct from each other and whose nationality doesn＇t play any role．

## 4 Intensionality

Discussions of the intensional aspects of information structure are not very com－ mon，but an exception is Beaver and Clark（2008）（in the following：B \＆C）， which contains a detailed discussion of the sentence in（16a）（the F－marking is theirs，a translation to our account is（16b））．

[^111]a. Sandy only met $[\text { the PREsident }]_{F}$.
b. Sandy only met $\sim[$ the PREsident $F]$.

B \& C argue roughly as follows. An extensional evaluation of (16) involves a set $A$ of alternatives for the denotation (= the extensional value) of the president. $A$ is a set of ordinary individuals (of which the actual president is one) that enters into the determination of the extensional value of the sentence (its actual truth value), like the actual president himself does. If instead we want to obtain the intensional value of the sentence (i.e. the proposition it expresses), then we must start with the intensions of its smallest constituents and compute the intensions of the complex constituents from the intensions of their components, in the manner familiar from Montague Grammar, arriving eventually at the intension of the sentence as a whole. In this way we obtain as intension for the president an individual concept $p r$ (a function from possible worlds to individuals; for each possible world $w, \operatorname{pr}(w)$ is the president in $w)$. $\mathrm{B} \& \mathrm{C}$ 's next assumption is that if the semantic value of the president is an individual concept, then the members of the alternative set invoked by the F-marking of this phrase must consist of individual concepts as well. But if that is what we want to assume about the alternative set $A$, we have to be a very careful. For one thing we cannot assume $A$ to be the set of all individual concepts. For if there is at least one world $w$ other than the actual world, and there are at least two individuals in $w$, then there will be different individual concepts that both assign the actual president to the actual world (but differ in what they assign to $w$ ). And then the usual semantics for only will yield a contradiction for a sentence like $(16)^{10}$. Furthermore, even when we accept that in general the alternative set is contextually restricted, it isn't immediately clear how this kind of conflict can be avoided. B \& C discuss a number of options. But as we see it, the problem that these options are trying to deal with need not arise in the first place.

The solution we suggest starts from the observation that all compositional steps in the computation of the truth value of sentences like (17) (in any possible world $w$ ) are extensional. In this regard (16) is no different than e.g. (17).
(17) Sandy met the president.

The intension of such a "purely extensional" sentence s can be obtained by simple "abstraction with respect to possible worlds". (In an intensional model $M=\langle\mathrm{W}, \mathrm{M}\rangle$, where W is a set of possible worlds and M a function which assigns each $w \in \mathrm{~W}$ an extensional model $\mathrm{M}(w)$, the intension $\llbracket s \rrbracket_{M}$ of s in $M$ can be obtained as $\lambda w . \llbracket s \rrbracket_{M, w}$, where $\llbracket s \rrbracket_{M, w}$ is the truth value of s in $\mathrm{M}(w)$.)

Our second assumption is that retrieval of alternative sets is in actual fact always retrieval of a set - description - or, if you prefers, of a predicate. Intuitively, interpreting the focus of (18b) triggers retrieval of the predicate (member of) the president's family.

[^112](18) a. Sandy wanted to meet the members of he presdent's family.
b. But she only met $\sim\left[\right.$ the PREsident $\left._{F}\right]$.

In the preceding sections, in which we were only concerned with the extensional semantics of information structure, only the actual extension of the retrieved predicate would have been relevant and we could have represented the alternative set presupposition triggered by $\sim\left[\right.$ the PREsident $\left._{F}\right]$ in (16) as in Fig. 4.


Fig. 4. $\sim\left[\right.$ the PREsident $\left._{F}\right]$

Here $\llbracket t h e ~ p r e s i d e n t \rrbracket$ stands for the actual president (that is, somewhat simplified, the unique $x$ such that $x$ is president) and $\llbracket$ the president $\rrbracket^{f}$ is the set of all individuals $D_{e}$ ).

This is all that the presupposition needs to say when we are interested just in the actual alternative set. Since resolution of the anaphoric (higher order) discourse referent $\underline{C}$ is to a predicate $C^{0}$, this predicate will determine extensions not just for the actual world, but for other possible worlds as well. In order to make sure that these extensions $C_{w}^{0}$ can serve properly as alternative sets in the evaluations of (16) the constraints on the resolution of $C^{0}$ that are given in Fig. 4 need to be generalised. That is, what we need instead of Fig. 4 is a presupposition of the form given in Fig. 5. In order to avoid all possible sources of ambiguity we now treat $C$ as a discourse referent for a predicate. $\square$, as usual, stands for 'necessity' i.e. for implicit universal quantification over worlds.


Fig. 5. Intensional treatment of $\sim\left[\right.$ the PREsident $\left._{F}\right]$

If $\underline{C}$ is resolved by a predicate $C^{0}$ that satisfies the constraints in Fig. 5, then in every $w$ the president will be a member of the extension of $C^{0}$ in $w$ and (18b) will evaluate to the proposition that is true in a world $w$ iff the president is the only individual in the extension of $C^{0}$ in $w$ that Sandy met in $w$. Intuitively, this seems pretty much what is wanted.

But pretty much is not quite all. Our presentation of Fig. 5 has been deliberately cagey on one point. From Fig. 4 we took over the abbreviatory notation

【the president】for the denotation of the president. But now that this term is embedded under the necessity operator $\square$ it is no longer clear which denotation is intended: that in the actual world (i.e. the actual president) or the "local" president (i.e. the president in the world $w$ that is quantified over by $\square$ ). This second option, which may be termed the de dicto interpretation of the president in Fig. 5, resembles de dicto interpretations in the familiar sense of the term, of noun phrases occurring in opaque contexts like the president in (19).
(19) Mary believes that Sandy only met the president.

Let us call the de dicto interpretation of (19) that according to which the sentence claims that a world $w$ belongs to the set of Mary's belief worlds iff the president in $w$ is the only member of the relevant alternative set in $w$ that Sandy met in $w$, Here the alternative set is determined in $w$ via the president in $w$. In other words, the de dicto interpretation of (19) involves a "local" interpretation of the president, both in the role it plays in determining the different alternative sets and in its contributions to the proposition that is expressed given these alternative sets. Its contribution to the proposition which (19) identifies as one of Mary's beliefs and as part of the presupposition for the alternative set predicate. If as we assumed for (18b), this predicate is resolved to member of the president's family (with the president interpreted de dicto), then the belief ascribed to Mary is the proposition that is true in $w$ iff the president in $w$ is the only member of his family in $w$ that Sandy met in $w$.

But this is not the only way $\llbracket t h e ~ p r e s i d e n t \rrbracket$ can be taken in Fig. 5. The interpretation of the president in (18b) goes hand in hand with a de re interpretation of the president in (19) in the familiar sense; that of attributing to Mary, with regard to the actual president, the belief that he is the only member of his family that Sandy met. On this interpretation the belief attributed to Mary is the proposition that is true in $w$ iff the actual president is the only member of the actual president's family in $w$.

This is surely a different proposition from the one we get on the de dicto interpretation. But our description doesn't make fully clear which proposition it is. There are still two ways of understanding which set is meant by "member of the president's family in $w^{\prime \prime}$. This could either be the set of actual members of the (actual) president or the set of those that are family members of the actual president in $w$. As far as we can tell, both these interpretations are in principle available once $C$ has been resolved to "member of the president's family".

We believe the three interpretations we have described are the only ones, but we are not sure and leave this as an open question.

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Disjunctive questions, intonation, and highlighting Floris Roelofsen E3 Sam van Gool

# Disjunctive questions, intonation, and highlighting ${ }^{\star}$ 

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This paper examines how intonation affects the interpretation of disjunctive questions. The semantic effect of a question is taken to be three-fold. First, it raises an issue. In the tradition of inquisitive semantics, we model this by assuming that a question proposes several possible updates of the common ground (several possibilities for short) and invites other participants to help establish at least one of these updates. But apart from raising an issue, a question may also highlight and/or suggest certain possibilities, and intonation determines to a large extent which possibilities are highlighted/suggested. We will introduce a compositional version of inquisitive semantics, and extend this framework in order to capture the highlighting- and suggestion potential of sentences. This will lead to a systematic account of the answerhood conditions and implications of disjunctive questions with different intonation patterns.

## 1 Preliminaries: basic assumptions and data

Syntactic structure. Syntactically, we distinguish between two kinds of disjunctive interrogatives. On the one hand there are those that consist of a single interrogative clause containing a disjunction. On the other hand there are those that consist of two interrogative clauses, conjoined by disjunction. We will refer to the former as narrow-scope disjunctive interrogatives, and to the latter as wide-scope disjunctive interrogatives. Some examples are given in (1) and (2) below.
(1) Narrow-scope disjunctive interrogatives:
a. Does Ann or Bill play the piano?
b. Does Ann love Bill or Chris?
(2) Wide-scope disjunctive interrogatives:
a. Does Ann play the piano, or does Bill play the piano?
b. Does Ann play the piano, or Bill?

We will assume that (2b) has exactly the same underlying syntactic structure as (2a); only some material is left unpronounced.

Intonation patterns. Disjunctive questions can be pronounced in different ways, and their interpretation is partly determined by the choice of intonation pattern. We concentrate on two prosodic features that seem to have significant semantic impact. ${ }^{1}$ First, in the case of a narrow-scope disjunctive interrogative it is important whether the disjunction is pronounced 'as a block' or whether each of the disjuncts is given separate emphasis. Second, in case the disjuncts are given separate emphasis, it is important whether there is a rising or a falling pitch contour on the second disjunct. The different intonation patterns are given in (3) and (4), where underlining is used to represent emphasis, and $\uparrow$ and $\downarrow$ indicate rising and falling pitch. ${ }^{2}$
(3) Intonation patterns for narrow-scope disjunctive interrogatives:
a. Block intonation: Does Ann-or-Bill $\uparrow$ play the piano?
b. Open intonation: Does Ann $\uparrow$ or Bill $\uparrow$ play the piano?
c. Closed intonation: Does $\underline{A n n} \uparrow$ or Bill $\downarrow$ play the piano?

[^113]
## General Program

(4) Intonation patterns for wide-scope disjunctive interrogatives:
a. Open intonation: Does Ann $\uparrow$ play the piano, or Bill $\uparrow$ ?
b. Closed intonation: Does $\underline{\text { Ann }} \uparrow$ play the piano, or Bill $\downarrow$ ?

Focus and closure. We take it that emphasis in the acoustic signal is a reflex of a focus feature in the logical form, and that the rising-and-falling pitch contour in (3c) and (4b) correlates with a closure feature in the logical form. It seems that this closure feature affects the pronunciation of the entire sentence (not just of, say, the contrastive elements in both disjuncts). Therefore, we assume that it is adjoined to the sentence as a whole. The ensuing logical forms are listed in the table below. Focus features, closure features, and interrogative complementizers are denoted by F, C, and Q , respectively.

| Pattern | Acoustic signal | Logical form |
| :---: | :---: | :---: |
| Narrow |  |  |
| - block | Does Ann-or-Bill $\uparrow$ play? | [Q-does [Ann or Bill] ${ }_{\text {F }}$ play] |
| - open | Does Ann $\uparrow$ or Bill $\uparrow$ play? | $\left[\mathrm{Q}\right.$-does [Ann] ${ }_{\mathrm{F}}$ or $[\mathrm{Bill}]_{\mathrm{F}}$ play] |
| - closed | Does Ann $\uparrow$ or Bill $\downarrow$ play? | $\left[\mathrm{Q} \text {-does }[\mathrm{Ann}]_{\mathrm{F}} \text { or }[\text { Bill }]_{\mathrm{F}} \text { play }\right]_{\mathrm{C}}$ |
| Wide |  |  |
| - open | Does Ann $\uparrow$ play, or Bill $\uparrow$ ? | [[Q-does [Ann $]_{\mathrm{F}}$ play] or [Q-does [Bill ${ }_{\text {F }}$ play $\left.]\right]$ |
| - closed | Does Ann $\uparrow$ play, or Bill $\downarrow$ ? | $\left[\left[Q-d o e s ~[A n n]_{F} \text { play] or [Q-does [Bill] }{ }_{\text {F }} \text { play }\right]\right]_{C}$ |

Basic data. Our theory should capture, at the very least, the effects of intonation on answerhood conditions. The basic empirical observations are summed up in (5), (6), and (7) below (wide-scope disjunctive interrogatives are not explicitly listed here; they behave exactly like their narrow-scope counterparts in the relevant respects). Notice that open intonation behaves in some ways like block intonation, but in others more like closed intonation: it licenses a no answer, but it does not license a yes answer. To the best of our knowledge, this observation has not been taken into account before.

Does Ann-or-Bill $\uparrow$ play?
a. No. $\Rightarrow$ neither
b. Yes. $\Rightarrow$ at least one
c. (Yes,) Ann does.
d. (Yes,) Bill does.
(6) Does Ann $\uparrow$ or Bill $\uparrow$ play?
a. No. $\Rightarrow$ neither
b. \#Yes. $\Rightarrow$ yes what?!
c. Ann does.
d. Bill does.

Does Ann $\uparrow$ or Bill $\downarrow$ play?
a. \#No.
b. \#Yes.
c. Ann does.
d. Bill does.

A further observation that should be accounted for is that disjunctive interrogatives with closure intonation convey that the speaker expects that exactly one of the disjuncts is true. In this respect, disjunctive interrogatives with closure intonation are similar to the corresponding disjunctive declaratives. However, there is also an important difference, as illustrated in (8) and (9):
(8) $\underline{\text { Ann }} \uparrow$ or $\underline{\text { Bill }} \downarrow$ plays the piano.
a. No, neither of them does.
(9) Does $\underline{A n n} \uparrow$ or $\underline{B i l l} \downarrow$ play the piano?
a. \#No, neither of them does.
b. Actually, neither of them does.

The difference is subtle but clear: (8) really excludes the possibility that neither Ann nor Bill plays, while (9) merely conveys an expectation on the speaker's part that at least one of them does. In the first case, disagreement can be expressed with no; in the second case, actually must be used instead.

The next section presents an analysis of disjunctive interrogatives in inquisitive semantics. This will not directly account for the above observations, but it will serve as a useful basis.

Disjunctive questions, intonation, and highlighting

## 2 Inquisitive Semantics

In inquisitive semantics, a sentence is taken to propose one or possibly several ways to update the common ground of a conversation. Formally, the proposition expressed by a sentence is a set of possibilities, each of which is in turn a set of indices, and represents a possible update of the common ground.

In previous work (Groenendijk, 2009; Mascarenhas, 2009; Groenendijk and Roelofsen, 2009; Ciardelli and Roelofsen, 2009; Ciardelli, 2009; Balogh, 2009, among others), inquisitive semantics has been defined for the language of propositional logic and the language of first-order predicate logic, largely abstracting away from issues of sub-sentential syntactic and semantic composition. In the present paper, we are specifically interested in this process of semantic composition at the sub-sentential level, and especially in the role that certain prosodic features play in that process. So, to start with, we need to define a compositional inquisitive semantics for a suitable fragment of English. Fortunately, much of the technical machinery that we need is familiar from alternative semantics (Hamblin, 1973; Kratzer and Shimoyama, 2002; AlonsoOvalle, 2006, among others).

Basic ingredients. As usual, we will say of each expression in our language that it is of a certain type. The basic types are $e, s$, and $t$, and whenever $\sigma$ and $\tau$ are types, $(\sigma \tau)$ is also a type. Our semantics will map each expression to a certain model-theoretic object. The type of an expression determines the kind of object that it is mapped to. Each model-theoretic object belongs to a certain domain. There is a domain $D_{e}$ of individuals, a domain $D_{s}$ of indices, and a domain $D_{t}$ consisting of the truth values 0 and 1. Furthermore, for every complex type $(\sigma \tau)$ there is a domain $D_{(\sigma \tau)}$ consisting of all functions from $D_{\sigma}$ to $D_{\tau}$. As in alternative semantics, each expression of type $\tau$ is mapped to $a$ set of objects in $D_{\tau}$. The semantic value of an expression $\alpha$ will be denoted by $\llbracket \alpha \rrbracket$. Notice that $\llbracket \alpha \rrbracket$ is always a set. Therefore, we will refer to it as the denotation set of $\alpha$.

Semantic values are composed by means of pointwise function application:
Pointwise Function Application
If $\llbracket \alpha \rrbracket \subseteq D_{(\sigma \tau)}$ and $\llbracket \beta \rrbracket \subseteq D_{\sigma}$, then
$\llbracket \alpha \beta \rrbracket:=\llbracket \beta \alpha \rrbracket:=\left\{d \in D_{\tau} \mid \exists a \in \llbracket \alpha \rrbracket . \exists b \in \llbracket \beta \rrbracket, d=a(b)\right\}$
Basic lexicon. Most lexical items are mapped to singleton sets, consisting of their standard denotations.
a. $\llbracket \mathrm{Ann} \rrbracket:=\{\mathrm{Ann}\}$
b. $\quad$ Billl $:=\{$ Bill $\}$
c. $\quad$ play』 $:=\left\{\lambda x . \lambda w . \operatorname{play}_{w}(x)\right\}$
d. $\llbracket$ love】 $\rrbracket:=\left\{\lambda y \cdot \lambda x \cdot \lambda w \cdot\right.$ love $\left._{w}(x, y)\right\}$

Disjunction. Disjunction introduces alternatives. The denotation set of a phrase ' $\alpha$ or $\beta$ ', where $\alpha$ and $\beta$ are two expressions of some type $\tau$, is the union of the denotation set of $\alpha$ and the denotation set of $\beta$ :
(12) $\quad$ For any type $\tau$, if $\llbracket \alpha \rrbracket, \llbracket \beta \rrbracket \subseteq D_{\tau}$, then $\llbracket \alpha$ or $\beta \rrbracket:=\llbracket \alpha \rrbracket \cup \llbracket \beta \rrbracket$

For example:

$$
\text { a. } \llbracket \text { Ann or Bill } \rrbracket=\left\{\begin{array}{c}
\text { Ann, }  \tag{13}\\
\text { Bill }
\end{array}\right\} \quad \text { b. } \quad \llbracket \text { Ann or Bill plays } \rrbracket=\left\{\begin{array}{c}
\lambda w . \text { play }_{w}(\text { Ann }), \\
\lambda w \cdot \text { play }_{w}(\text { Bill })
\end{array}\right\}
$$

Notice that the denotation set of a complete sentence, such as 'Ann or Bill plays' is a set of objects in $D_{(s t)}$. Such objects are functions from indices to truth values, or equivalently, sets of indices. In inquisitive semantics, sets of indices are referred to as possibilities, and a set of possibilities is called a proposition. So complete sentences express propositions.

Visualization. As long as we limit our attention to a language that contains, besides disjunction, just two names, 'Ann' and 'Bill', and a single intransitive verb 'play', the propositions expressed by the sentences in our language can be visualized in a helpful way. For instance, the sentence 'Ann plays' expresses the proposition $\left\{\lambda w\right.$. play $\left._{w}(\mathrm{Ann})\right\}$, which contains a single possibility consisting of all indices in which Ann plays. This proposition is depicted in figure 1(a), where 11 is the index in which both Ann and Bill play, 10

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Fig. 1. Some propositions visualized.
the index in which only Ann plays, etcetera. Figure 1(b) depicts the proposition expressed by 'Ann or Bill plays'. As we saw in (13b), this proposition consists of two possibilities: the possibility that Ann plays, and the possibility that Bill plays.

Excluded possibilities. Recall that the possibilities for a sentence $\alpha$ embody the ways in which $\alpha$ proposes to update the common ground. If some index $i$ is not included in any possibility for $\alpha$, then we say that $i$ is excluded by $\alpha$. For in this case, $i$ will be eliminated from the common ground by any of the updates proposed by $\alpha$. If $\alpha$ excludes any indices, then we refer to the set of all such indices as the possibility excluded by $\alpha$. If $\alpha$ does not exclude any indices, then we say that it does not exclude any possibility. We use $[J \alpha \|]$ to denote the set of possibilities excluded by $\alpha$ (which is always either a singleton set, or empty).

Interrogative clauses. The interrogative complementizer, $\mathbf{Q}$, always operates on an expression $\alpha$ of type ( $s t$ ), and the resulting clause $[\mathrm{Q} \alpha]$ is always again of type $(s t)$. So even though there is a shift in syntactic category, there is no shift in semantic type. The proposition expressed by $[\mathrm{Q} \alpha]$ consists of the possibilities for $\alpha$ itself, plus the possibility that $\alpha$ excludes.

$$
\begin{equation*}
\llbracket \mathrm{Q} \alpha \rrbracket:=\llbracket \alpha \rrbracket \cup[ \rfloor \alpha \rrbracket] \tag{14}
\end{equation*}
$$

For example, the proposition expressed by the simple polar interrogative 'Does Ann play?' consists of two possibilities: the possibility that Ann plays, and the possibility that she does not play. These possibilities embody two possible updates of the common ground, and the responder is invited to provide information such that either one of these updates can be established.

$$
\begin{align*}
& \llbracket \mathrm{Q} \text {-does Ann play } \rrbracket  \tag{15}\\
= & \llbracket \text { Ann plays } \rrbracket \cup[ \rfloor \text { Ann plays } \rrbracket]=\left\{\begin{array}{c}
\lambda w \cdot \text { play }_{w}(\mathrm{Ann}), \\
\lambda w \cdot \neg \operatorname{play}_{w}(\mathrm{Ann})
\end{array}\right\} \quad \Rightarrow \text { see figure } 1(\mathrm{c})
\end{align*}
$$

Disjunctive interrogatives. Given these assumptions, the propositions expressed by wide- and narrowscope disjunctive interrogatives are the following:

> Wide-scope disjunctive interrogative: Does Ann play or does Bill play? $\llbracket \mathrm{Q}$-does Ann play or Q-does Bill play $\rrbracket$ $=\llbracket \mathrm{Q}$-does Ann play $\rrbracket \cup \llbracket \mathrm{Q}$-does Bill play $\rrbracket$ $=\left\{\begin{array}{c}\lambda w . \text { play }_{w}(\text { Ann }), \\ \lambda w . \neg \text { play }_{w}(\text { Ann })\end{array}\right\} \cup\left\{\begin{array}{c}\lambda w . \text { play }_{w}(\text { Bill }), \\ \lambda w . \neg \text { play }_{w}(\text { Bill })\end{array}\right\}$

Narrow-scope disjunctive interrogative: Does Ann or Bill play?

$$
\begin{align*}
& {[\text { Q-does Ann or Bill play } \rrbracket}  \tag{17}\\
= & \llbracket \text { Ann or Bill plays } \rrbracket \cup[\ \text { Ann or Bill plays } \downarrow] \\
= & \left\{\begin{array}{c}
\lambda w \cdot \text { play }_{w}(\text { Ann }), \\
\lambda w \cdot \text { play }_{w}(\text { Bill })
\end{array}\right\} \cup\left\{\lambda w . \neg \text { play }_{w}(\text { Ann }) \wedge \neg \text { play }_{w}(\text { Bill })\right\} \quad \Rightarrow \text { see figure } 1(\mathrm{e})
\end{align*}
$$

So much for the compositional treatment of our basic fragment in inquisitive semantics. Notice that this treatment does not yet say anything about the licensing and interpretation of yes/no answers, or about 368
the 'exactly one implication' of disjunctive interrogatives with closure intonation. The following sections propose an extension of the system that will allow us to capture these phenomena.

## 3 Focus and highlighting

The general idea that we would like to pursue in this section is that a sentence, besides proposing one or more possible updates, may also highlight certain possibilities, and that focus plays an important role in determining the possibilities that a sentence highlights.

We think that highlighting is of particular relevance for the licensing and interpretation of yes/no answers. More specifically, we hypothesize that a yes answer to a question $\alpha$ presupposes that $\alpha$ highlighted exactly one possibility, and if this presupposition is met, yes confirms that highlighted possibility. A no answer on the other hand, if felicitous, simply rejects all the possibilities highlighted by $\alpha$ (for now we will assume that a no answer is always felicitous; a felicity condition will be specified in section 4).

Initial motivation: opposing polar questions. Initial motivation for this idea comes from an old puzzle concerning polar questions, exemplified by the contrast between (18a) and (18b):

## a. Is the door open?

b. Is the door closed?

According to inquisitive semantics, as it has been developed so far, (18a) and (18b) are equivalent: they both express a proposition consisting of two possibilities, the possibility that the door is open, and the possibility that the door is closed. However, there is a clear empirical difference between the two: in reply to (18a), yes means that the door is open, while in reply to (18b), it means that the door is closed. ${ }^{3}$

This difference is captured straightforwardly if we assume that (18a) highlights the possibility that the door is open, that (18b) highlights the possibility that the door is closed, and that the interpretation of yes and $n o$ is as hypothesized above. Our aim is to give a similar explanation of the licensing and interpretation of yes/no answers in response to disjunctive questions. In order to do so, we must first specify how the possibilities highlighted by a given sentence are compositionally determined, and in particular how focus affects this process.

Proposing and highlighting. We will henceforth assume that the semantic value of a sentence $\alpha$ consists of two components, $\llbracket \alpha \rrbracket_{\mathrm{P}}$ and $\llbracket \alpha \rrbracket_{\mathrm{H}}$. Both $\llbracket \alpha \rrbracket_{\mathrm{P}}$ and $\llbracket \alpha \rrbracket_{\mathrm{H}}$ are sets of possibilities; $\llbracket \alpha \rrbracket_{\mathrm{P}}$ embodies the proposal that $\alpha$ expresses, and $\llbracket \alpha \rrbracket_{\mathrm{H}}$ consists of the possibilities that $\alpha$ highlights.

The semantic value of subsentential expressions will also consist of these two components. For any expression $\alpha$, sentential or subsentential, we will refer to $\llbracket \alpha \rrbracket_{\mathrm{P}}$ as its P-set, and to $\llbracket \alpha \rrbracket_{\mathrm{H}}$ as its H-set. Both P -sets and H -sets are composed by means of pointwise function application.

What we used to call the denotation set of an expression, then, is now called its P-set. As far as names, verbs, and disjunction are concerned, H -sets are defined just as P -sets. However, as soon as interrogative complementizers enter the derivation, P -sets and H -sets start to diverge. Recall that the proposal expressed by $[\mathrm{Q} \alpha]$ consists of the possibilities for $\alpha$ itself, plus the possibility that $\alpha$ excludes:

$$
\begin{equation*}
\llbracket \mathrm{Q} \alpha \rrbracket_{\mathrm{P}}:=\llbracket \alpha \rrbracket_{\mathrm{P}} \cup[\downarrow \alpha \|] \tag{19}
\end{equation*}
$$

We will assume that $[\mathrm{Q} \alpha]$ simply highlights the possibilities that $\alpha$ itself highlights, not the possibility that $\alpha$ excludes:

$$
\begin{equation*}
\llbracket \mathrm{Q} \alpha \rrbracket_{\mathrm{H}}:=\llbracket \alpha \rrbracket_{\mathrm{H}} \tag{20}
\end{equation*}
$$

These assumptions are sufficient to capture the contrast between opposing polar questions:

[^114]
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(21) [Q-is the door open]

Proposes: open/closed
Highlights: open
yes $\Rightarrow$ the door is open
$n o \Rightarrow$ the door is closed
[Q-is the door closed]
Proposes: open/closed
Highlights: closed
yes $\Rightarrow$ the door is closed
$n o \Rightarrow$ the door is open

Highlighting and focus. We will assume that focus affects the computation of H -sets. To see why, consider the two focus structures that give rise to block intonation and open intonation, respectively:
a. Does [Ann or Bill] $]_{\mathrm{F}}$ play the piano? $\quad \Rightarrow$ block intonation
b. Does $[\mathrm{Ann}]_{\mathrm{F}}$ or $[\text { Bill }]_{\mathrm{F}}$ play the piano? $\quad \Rightarrow$ open intonation

Recall that (23a) licenses both yes and no as an answer, while (23b) only licenses no. Our hypothesis about the interpretation of yes and no captures this contrast if we assume that (23a) highlights a single possibility (the possibility that Ann or Bill plays), while (23b) highlights two possibilities (the possibility that Ann plays, and the possibility that Bill plays). But this can only be if focus affects the computation of H -sets. For, apart from their focus structures, (23a) and (23b) are perfectly identical.

The intuitive idea that we will pursue is that 'focus makes H-sets collapse'. Let us first make this more precise for the case where $\alpha$ is a complete sentence, of type ( $s t$ ):

## If $\alpha$ is of type ( $s t$ ), then:

$$
\begin{equation*}
\llbracket \alpha_{\mathrm{F}} \rrbracket_{\mathrm{H}}:=\left\{\bigcup_{\pi \in \llbracket \alpha \rrbracket_{\mathrm{H}}} \pi\right\} \tag{24}
\end{equation*}
$$

If $\alpha$ is of type (st), then every element of $\llbracket \alpha \rrbracket_{\mathrm{H}}$ is a possibility $\pi$, a set of indices. The focus feature collapses all these possibilities into one big possibility, $\bigcup_{\pi \in \llbracket \alpha \rrbracket_{H}} \pi$. This, then, is the unique possibility in $\llbracket \alpha_{\mathrm{F}} \rrbracket_{\mathrm{H}} .{ }^{4}$

If $\alpha$ is a sub-sentential expression, of some type $\sigma$ different from (st), then the elements of $\llbracket \alpha \rrbracket_{\mathrm{H}}$ are not full-fledged possibilities, so we cannot simply take their union. However, following Partee and Rooth (1982), we can take their 'generalized union':

If $\alpha$ is of some type $\sigma$, different from (st), then:

$$
\begin{equation*}
\llbracket \alpha_{\mathrm{F}} \rrbracket_{\mathrm{H}}:=\left\{\lambda z . \bigcup_{y \in \llbracket \alpha \rrbracket_{\mathrm{H}}} z(y)\right\} \quad \text { where } z \text { is a variable of type }(\sigma(s t)) \tag{25}
\end{equation*}
$$

For our examples, the relevant case is the one where $\alpha$ is of type $e$. In this particular case, we have: ${ }^{5}$

$$
\begin{equation*}
\llbracket \alpha_{\mathrm{F}} \rrbracket_{\mathrm{H}}:=\left\{\lambda P . \bigcup_{y \in \llbracket \alpha \rrbracket_{\mathrm{H}}} P(y)\right\} \quad \text { where } P \text { is a variable of type }(e(s t)) \tag{26}
\end{equation*}
$$

Let us first consider what this means for some disjunctive declaratives with different focus structures:

$$
\begin{align*}
& \mathbb{U}[\mathrm{Ann}]_{\mathrm{F}} \text { or }[\text { Bill }]_{\mathrm{F}} \text { plays } \mathbb{\rrbracket}_{\mathrm{H}}=\left\{\begin{array}{c}
\lambda w \cdot \text {.play }_{w}(\mathrm{Ann}), \\
\lambda w . \text { play }_{w}(\mathrm{Bill})
\end{array}\right\}  \tag{27}\\
& \mathbb{U}[\text { Ann or Bill }]_{\mathrm{F}} \text { plays } \mathbb{1}_{\mathrm{H}}=\left\{\lambda w \cdot \text { play }_{w}(\mathrm{Ann}) \cup \lambda w . \text { play }_{w}(\text { Bill })\right\} \tag{28}
\end{align*}
$$

With narrow focus on each individual disjunct, 'Ann or Bill plays' highlights two possibilities. But, as desired, focus on the whole disjunctive subject NP collapses these two possibilities into one. Now let us turn to disjunctive interrogatives. First consider the narrow-scope variant. Recall that, by definition, an interrogative clause $[\mathrm{Q} \alpha]$ highlights the same possibilities as $\alpha$ itself. So we have:

[^115]Disjunctive questions, intonation, and highlighting Floris Roelofsen E3 Sam van Gool
$\llbracket$ Q-does $[\mathrm{Ann}]_{\mathrm{F}}$ or $[\text { Bill }]_{\mathrm{F}}$ play $\rrbracket_{\mathrm{H}}=\left\{\begin{array}{c}\lambda w . \text { play }_{w}(\mathrm{Ann}), \\ \lambda w \cdot \text { play }_{w}(\mathrm{Bill})\end{array}\right\}$
$\llbracket$ Q-does $[\text { Ann or Bill] }]_{\mathrm{F}}$ play $\rrbracket_{\mathrm{H}}=\left\{\lambda w\right.$. play $_{w}(\mathrm{Ann}) \cup \lambda w$. play $_{w}($ Bill $\left.)\right\}$
Thus, it is predicted that the question 'Does Ann or Bill play?' only highlights two distinct possibilities if it has narrow focus on 'Ann' and on 'Bill'. Finally, it is predicted that wide-scope disjunctive interrogatives always highlight two distinct possibilities:

$$
\llbracket \text { Q-does }[\mathrm{Ann}]_{\mathrm{F}} \text { play or Q-does }[\text { Bill }]_{\mathrm{F}} \text { play } \rrbracket_{\mathrm{H}}=\left\{\begin{array}{c}
\lambda w \cdot \text {.play }_{w}(\mathrm{Ann}),  \tag{31}\\
\lambda w \cdot \text { play }_{w}(\mathrm{Bill})
\end{array}\right\}
$$

The analysis so far yields a number of satisfactory predictions:
(32) Does [Ann or Bill $]_{\text {F }}$ play?
a. Highlights the possibility that Ann or Bill plays.
b. $\quad y e s \Rightarrow$ at least one of them plays
c. $n o \Rightarrow$ neither Ann nor Bill plays

Does $[\mathrm{Ann}]_{\mathrm{F}}$ or $[\mathrm{Bill}]_{\mathrm{F}}$ play?
a. Highlights the possibility that Ann plays and the possibility that Bill plays.
b. $\quad y e s \Rightarrow$ presupposition failure (the question highlights more than one possibility)
c. $n o \Rightarrow$ neither Ann nor Bill plays
(34) $\quad$ Does $[\mathrm{Ann}]_{\mathrm{F}}$ play or does [Bill1 $]_{\mathrm{F}}$ play?
a. Highlights the possibility that Ann plays and the possibility that Bill plays.
b. $\quad y e s \Rightarrow$ presupposition failure (the question highlights more than one possibility)
c. $n o \Rightarrow$ neither Ann nor Bill plays

We seem to have obtained a better understanding of the basic difference between block intonation and open intonation. Now let us consider the effect of closure.

## 4 Closure and suggestions

Our basic intuition is that closure suggests that exactly one of the highlighted possibilities can be realized. (Recall that possibilities embody possible updates of the common ground; as such it makes sense to speak of them as 'being realized'.) To see what this amounts to, consider our running examples (35a) and (35b):
a. Does $\underline{A n n} \uparrow$ or Bill $\downarrow$ play the piano?
b. Does $\underline{\text { Ann } \uparrow}$ play the piano, or Bill $\downarrow$ ?

These questions both highlight two possibilities: the possibility that Ann plays, and the possibility that Bill plays. To suggest that exactly one of these possibilities can be realized is to suggest that exactly one of Ann and Bill plays the piano. In particular, it is to suggest that at least one of them plays, and that they do not both play. Such a suggestion does indeed seem to be part of what (35a) and (35b) communicate.

There are several ways to formalize this intuition. We will assume here that the meaning of a sentence $\alpha$ does not just consist of $\llbracket \alpha \rrbracket_{\mathrm{P}}$ and $\llbracket \alpha \rrbracket_{\mathrm{H}}$, but has a third component, $\llbracket \alpha \rrbracket_{\mathrm{S}}$, which is the set of possibilities/updates that $\alpha$ suggests. We will refer to $\llbracket \alpha \rrbracket_{\mathrm{S}}$ as the S-set of $\alpha$.

We will assume that the $S$-set of expressions that do not bear a closure-feature is always empty. The S-set of expressions that do bear a closure-feature is defined as follows:
(36) The effect of closure: $\quad \llbracket \alpha_{\mathrm{C}} \rrbracket_{\mathrm{P}}:=\llbracket \alpha \rrbracket_{\mathrm{P}} \quad \llbracket \alpha_{\mathrm{C}} \rrbracket_{\mathrm{H}}:=\llbracket \alpha \rrbracket_{\mathrm{H}} \quad \llbracket \alpha_{\mathrm{C}} \rrbracket_{\mathrm{S}}:=\mathcal{E} \mathcal{X}\left(\llbracket \alpha \rrbracket_{\mathrm{H}}\right)$

The definition of $\llbracket \alpha_{\mathrm{C}} \rrbracket_{\mathrm{S}}$ makes use of the exclusive strengthening operator $\mathcal{E X}$. For any set of possibilities $\Pi$, and for any possibility $\pi \in \Pi$, the exclusive strengthening of $\pi$ relative to $\Pi$ is defined as:

$$
\begin{equation*}
\mathcal{E X}(\pi, \Pi):=\pi-\bigcup\{\rho \mid \rho \in \Pi \text { and } \pi \nsubseteq \rho\} \tag{37}
\end{equation*}
$$

and the exclusive strengthening of $\Pi$ itself is defined as:

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Fig. 2. Exclusive strengthening illustrated.

$$
\begin{equation*}
\mathcal{E X}(\Pi):=\{\mathcal{E} X(\pi, \Pi) \mid \pi \in \Pi\} \tag{38}
\end{equation*}
$$

The effect of exclusive strengthening is illustrated for example (35a) in figure 2. Recall that (35a) proposes three possibilities, as depicted in figure 2(a), and highlights two possibilities, as depicted in figure 2(b). Applying $\mathcal{E X}$ to these two highlighted possibilities removes the overlap between them, resulting in the two possibilities in figure 2(c). This reflects the fact that (35a) suggests that exactly one of Ann and Bill plays the piano. The same result is obtained for (35b), since (35a) and (35b) highlight exactly the same possibilities. ${ }^{6}$

Accepting and canceling suggestions. Suggestions can either be accepted or canceled by a responder. We will assume that acceptance is the default. That is, if a suggestion is not explicitly contradicted, then all conversational participants assume that it is commonly accepted, and the suggested information is added to the common ground. Thus, if you ask (35a) or (35b), and I reply: 'Ann does', then I tacitly accept your suggestion. As a result, the common ground will not only be updated with the information that Ann plays, but also with the information that Bill does not play. ${ }^{7}$

Licensing no. At the beginning of section 3 we hypothesized that no, in response to a question $\alpha$, simply denies all the possibilities that $\alpha$ highlights. We left the felicity condition on the use of no unspecified at that point. Now that suggestions have entered the picture, we are ready to make this felicity condition explicit.

Recall the contrast between disjunctive declaratives and interrogatives mentioned at the outset:
$\underline{\text { Ann } \uparrow}$ or Bill $\downarrow$ plays the piano.
a. No, neither of them does.
(40) Does Ann $\uparrow$ or Bill $\downarrow$ play the piano?
a. \#No, neither of them does.
b. Actually, neither of them does.

The declarative licenses a no response; the interrogative does not. What is the relevant difference between the two? -The answer is that the declarative really asserts that at least one of Ann and Bill plays the piano (in the sense that it excludes-technically speaking-the possibility that neither Ann nor Bill plays), whereas the interrogative merely suggests that at least one of Ann and Bill plays. Thus, this example illustrates that no can be used to deny an assertion, but not to cancel a suggestion. Rather, as illustrated in (40b), cancellation of a suggestion requires a 'weaker' disagreement particle such as actually or in fact (if a disagreement marker is used at all). ${ }^{8}$

Thus, $n o$, in response to a question $\alpha$, denies the possibilities that $\alpha$ highlights, but is felicitous only if denying these possibilities does not cancel the suggestion that $\alpha$ expresses. This accounts for the contrast between (39) and (40), and also for the licensing and interpretation of no in response to disjunctive interrogatives with block intonation or open intonation.

[^116]Sincerity requirements. Grice's (1975) quality maxim, formulated in our present terms, says that if a cooperative speaker $s$ utters a sentence $\alpha$, then $s$ must take himself to know that at least one of the updates proposed by $\alpha$ can indeed be established (informative sincerity). In inquisitive pragmatics (Groenendijk and Roelofsen, 2009), it is further assumed that if $\alpha$ is inquisitive, then for each update that $\alpha$ proposes, $s$ must be genuinely uncertain as to whether that update can indeed be established or not (inquisitive sincerity). In the present setting there is a third requirement, namely that if $\alpha$ suggests certain updates, then $s$ must genuinely expect that exactly one of these updates can indeed be established (expectative sincerity).

One consequence of this is that denying an assertion is much more likely to give rise to conflicts than canceling a suggestion. For, in the first case, the speaker's supposed knowledge is contradicted, while the second case may require merely a revision of expectations. This is illustrated by the following contrast:

A: $\underline{\text { Ann } \uparrow}$ or Bill $\downarrow$ is coming tonight.
$B$ : No, neither of them is.
A: What?! (\# Oh, thanks)
(42) A: Is Ann $\uparrow$ or Bill $\downarrow$ coming tonight?

B: Actually, neither of them is.
A: Oh, thanks.

## 5 Repercussions

The proposed analysis may shed light on a much wider range of phenomena than the ones explicitly discussed here. Let us end by briefly mentioning some such phenomena:

Disjunctive declaratives. The analysis directly accounts for the 'exclusive component' of declarative disjunctions. In particular, it makes the right predictions for sentences like (43), which have received much attention in the recent literature (see Alonso-Ovalle, 2006, chapter 3, and references given there).

$$
\begin{equation*}
\text { Ann } \uparrow \text { is coming, or Bill } \uparrow \text {, or both } \downarrow \text {. } \tag{43}
\end{equation*}
$$

Might. Ciardelli, Groenendijk, and Roelofsen (2009) provide an analysis of might in inquisitive semantics. Adopting this analysis, and assuming that a sentence might $\alpha$ highlights exactly the same possibilities as $\alpha$ itself, seems to give a satisfactory account of sentences like:
a. Jim might talk to Ann-or-Bill.
b. Jim might talk to Ann $\uparrow$ or to Bill $\uparrow$.
c. Jim might talk to Ann $\uparrow$ or to Bill $\downarrow$.
d. Jim might talk to Ann $\uparrow$, or he might talk to Bill $\uparrow$.
e. Jim might talk to $\underline{A n n} \uparrow$, or he might talk to $\underline{\text { Bill }} \downarrow$.
f. Jim might talk to $\underline{A n n} \uparrow$, or to Bill $\uparrow$, or to both $\downarrow$.

Ignorance implicatures. Inquisitive pragmatics (in particular the inquisitive sincerity requirement mentioned above) accounts for ignorance implicatures triggered by disjunction, questions, and might in a uniform way. This account carries over straightforwardly to the extended semantic framework presented here.

Closure variability. One aspect of the data that we abstracted away from entirely is that the rising-andfalling pitch contour that was taken to signal closure may be pronounced more or less dramatically, and this seems to correlate with the strength of the corresponding 'exactly one' suggestion. This could be captured by construing the closure feature not as a binary-valued feature-that is either 'on' or 'off'-but rather as a continuous-valued feature-with values, say, between 0 and 1 . Phonologically, this value would then determine the sharpness of the rising-and-falling pitch contour, and semantically it would determine the strength of the corresponding 'exactly one' suggestion.

Cross-linguistic application. Of course, the syntactic structure and phonological characteristics of disjunctive questions differ widely across languages. However, the interpretation of disjunctive questions in different languages is usually reported to be similar or identical to the interpretation of their English counterparts. Therefore, we suspect that the general semantic mechanisms of proposing, highlighting, and suggesting possibilities may play a role cross-linguistically, even though the way in which these mechanisms are 'implemented' will differ from language to language. To give one example, it seems quite reasonable to hypothesize that while closure is signaled in English by intonation, it is expressed in other languages by designated lexical items. Haspelmath (2007) and Alonso-Ovalle (2006, chapter 5) provide data from Basque, Mandarin Chinese, Finnish, and several other languages that seems to support such a hypothesis.

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# The Semantics of Count Nouns 

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#### Abstract

We offer an account of the semantics of count nouns based on the observation that for some count nouns, the set of atoms in the denotation of the singular predicate is contextually determined. We derive the denotation of singular count nouns relative to a context k , where k is a set of entities which count as atoms in a particular context. An operation $\mathrm{COUNT}_{\mathrm{k}}$ applies to the mass noun denotation $\mathrm{N}_{\text {mass }}$ and derives the count meaning: a set of ordered pairs $<\mathrm{d}, \mathrm{k}>$ where d is a member of $\mathrm{N} \cap \mathrm{k}$ and k is the context k relative to which d counts as one. Count nouns and mass nouns are thus typally distinct and the grammatical differences between them follow from this. We distinguish between naturally atomic predicates, which denote sets of inherently individuable entities or boolean algebras generated from such sets, and semantically aomic predicates, which denote sets which are atomic relative to a particular context k . This distinction is shown to be orthogonal to the mass count distinction.


Keywords: mass/count distinction, atomicity, counting, measuring, homogeneity, nominal interpretations, $\wedge$ semantics of number.

## 1 Introduction

This paper proposes a semantics for count nouns which makes explicit the grammatical basis of counting. We assume the semantics for mass nouns proposed in Chierchia,[1], according to which mass nouns denote atomic Boolean algebras generated under the complete join operation from a possibly vague set of atoms. However, we differ from Chierchia in our analysis of count nouns. Chierchia argues that the atomic elements in mass denotations cannot be grammatically accessed because a mass noun is lexically plural, i.e. the root lexical item denotes a boolean algebra. Singular count nouns denote a unique set of salient atoms, which as a consequence are grammatically accessible. Plural count nouns denote the closure of the singular denotation under the complete join operation, thus plural count nouns and mass nouns denote the same kinds of entities. The grammatical difference is only whether the set of atoms from which the boolean algebra is generated is or is not lexically accessible, where lexical accessiblity is to determined by the pragmatic accessibility of a salient, stable set of atoms (Chierchia, [2]). We argue in this paper that Chierchia's account is inadequate and that the salience or non-vagueness of a presupposed atomic set cannot be at the basis of count noun semantics. There are two reasons for this: (i) the existence of mass predicates such as furniture which denote
sets generated from a set of non-vague, salient atoms and (ii) the existence of context dependent count nouns such as wall and hedge.

### 1.1 Mass nouns may denote sets of salient atoms

As Chierchia[1],[2] and Gillon [3] have pointed out, mass nouns may, like furniture, denote boolean algebras generated from sets of inherently individuable atoms. Barner and Snedeker [4] show that these mass nouns, in contrast to mass nouns like mud but like count nouns, allow quantity judgements in terms of number rather than overall volume. Thus who has more furniture? will be answered by comparing numbers of pieces of furniture, while who has more sand/mud? will be answered by comparing overall quantities of mud or sand no matter how many individual piles or heaps or units the stuff is arranged in. Rothstein[5] and Schwarzschild[6] independently show that these predicates (which Rothstein calls 'naturally atomic' and Schwarzschild calls 'stubbornly distributive) make the atomic entities salient for distributive adejctives such as big. Pires d'Oliviera and Rothstein [7] show that naturally atomic predicates may be antecedents for reciprocals in Brazilian Portguese, although this is impossible in English.

### 1.2 Singular Count Noun Denotations may be Contextually Determined

There are a significant number of count nouns which are not associated with a unique set of salient atoms: instead the set of atoms in the denotation of these count nouns may be variable and highly context dependent. Krifka [8] shows that nouns such as sequence and twig are non-quantized, and Mittwoch [9] shows that this is true also of mathmatical terms such as plane and line. Rothstein [10] shows that this generalises to clases of singular count nouns denoting sets of entities with context-dependent physical dimensions. These include nouns such as fence, wall, hedge and lawn, where the boundaries of the atomic entities are defined by cartesian coordinates, and classificatory nominals such as bouquet/bunch. For example, if a square of land is fenced or walled in on four sides, with the fence or wall on each side built by a different person, we can talk of one (atomic) fence/wall enclosing the field, or we can talk of the field being enclosed by four fences or wall, each one built by a different person, with the atomic units depending on the contextually relevant choice of what counts as one wall. Similarly, flowers are often sold in bunches, but I may decide that a 'predesignated' bunch of flowers is not big enough for my purposes and buy two bunches which I then put together and deliver as a single bunch. Many other such examples can be constructed. Thus, count nouns meanings must involve sets of context dependent atoms. Crucially, fences, walls and bunches in these contexts can be counted, as in four fences/two walls/two bunches of flowers, whereas furniture cannot be counted (*three furnitures), even though furniture may be naturally associated with a uniquely determined set of salient atomic entities. This indicates that the counting operation can be applied to count nouns because the association with the set of contextually relevant atoms is grammatically encoded.

## 2 Count Noun Denotations

We encode contextual dependence of count nouns in the following way.
We assume that nominals are interpreted with respect to a complete atomic Boolan algebra $\mathrm{M} . \sqcup_{\mathrm{M}}$, the sum operation on M is the complete Boolean join operation (i.e. for every $X \subseteq M: \sqcup_{M} X \in M$ ). With Chierchia, we assume that the set of atoms A of $M$ is not fully specified, vague. The denotation of a root noun $N_{\text {root }}$ is the Boolean algebra generated under $\sqcup_{M}$ from a set of atoms $\mathrm{A}_{\mathrm{N}} \subseteq \mathrm{A}$ (so root noun denotation $\mathrm{N}_{\text {root }}$ has the same 0 as $M$, its atoms are $A_{N}$, and its 1 is $\sqcup_{M}\left(A_{N}\right)$ ). Mass nouns have the denotations of root nouns, so $\operatorname{NOUN}_{\text {mass }}=$ NOUN $_{\text {root }}$. (Note that the choice of this particular theory of mass nouns is not essential to what follows. We assume it for simplicity.) For mass nouns like furniture, the atoms in the denotation of the nominal will be be the salient individuable entities, while for mass nouns like mud the atoms will be an underdetermined vague set of minimal mud parts.
Singular count nouns denote sets of countable atoms. Counting is the operation of putting entities which are predesignated as atoms, i.e. entities that count as 1 , in one-to-one correspondence with the natural numbers. We have seen that what counts as one entity is contextually determined, and hypothesise that this decision is grammatically encoded. This grammatical encoding is what makes a noun count.
We propose that singular count nouns are interpreted relative to a context k . A context k is a set of objects from $\mathrm{M}, \mathrm{k} \subseteq \mathrm{M}, \mathrm{K}$ is the set of all contexts. The set of count atoms determined by context $k$ is the set $A_{k}=\{\langle\mathrm{d}, \mathrm{k}\rangle: \mathrm{d} \in \mathrm{k}\}$. $\mathrm{A}_{\mathrm{k}}$ is going to be the set of atoms of the count structure $B_{k}$ to be determined below. The objects in $k$ are not mutually disjoint with respect to the order in $M$, since we may want, in a single context my hands and each of my fingers to count as atoms, i.e. to be members of the same contextual set of atoms. Thus it may be the case that for two entities lt and lh (my left thumb and my left hand), $\mathrm{lt} \sqsubseteq_{\mathrm{M}} \mathrm{lh}$, but nevertheless $\mathrm{lt}, \mathrm{lh} \in \mathrm{k}$. In that case $\langle\mathrm{lt}, \mathrm{k}\rangle,\langle\mathrm{lh}, \mathrm{k}\rangle \in \mathrm{A}_{\mathrm{k}}$. So both my left thumb and my left hand are atoms to be counted in context k . Given this we cannot lift the order on the count Boolean domain from the mass domain.
We want the count domain $B_{k}$ to be a complete atomic Boolean algebra generated by the set of atoms $A_{k}$. Up to isomorphism, there is only one such such structure, $B_{k}$.

Definition of $\mathbf{B}_{\mathrm{k}}: \mathrm{B}_{\mathrm{k}}$ is the unique complete atomic Boolean algebra (up to idomorphism) with set of atoms $\mathrm{A}_{\mathrm{k}}$. We let $\mathrm{\bigsqcup}_{\mathrm{k}}$ stand for the corresponding complete join operation on $B_{k}$.

However, we would like to lift this order from the mass domain as much as we can. If $\mathrm{k}^{\prime} \subseteq \mathrm{k}$ and $\mathrm{k}^{\prime}$ is a set of mutually non-overlapping objects in M , there is no problem in lifting part-of relations of the sums of $\mathrm{k}^{\prime}$-objects from the mass domain. ( $\mathrm{k}^{\prime}$ is a set of mutually non-overlapping objects in $M$ iff for all $d, d^{\prime} \in \mathrm{k}^{\prime}: \mathrm{d} \Pi_{\mathrm{M}} \mathrm{d}^{\prime}=0$ ). Thus we impose the following constraint on $\mathrm{B}_{\mathrm{k}}$ :

Constraint on $\mathbf{B}_{\mathrm{k} \text { : }}$ For any set $\mathrm{k}^{\prime} \subseteq \mathrm{k}$ such that the elements of $\mathrm{k}^{\prime}$ are mutually M disjoint, the Boolean substructure $\mathrm{B}_{\mathrm{k}^{\prime}}$ of $\mathrm{B}_{\mathrm{k}}$ is given by: $\mathrm{B}_{\mathrm{k}^{\prime}}=\left\{<\sqcup_{M} \mathrm{X}, \mathrm{k}>: \mathrm{X} \subseteq \mathrm{k}^{\prime}\right\}$ with the order lifted from $\sqcup_{M}$.

The plurality order is not lifted from the mass domain for objects that overlap. i.e. the sum of my hands and my fingers is a sum of twelve atoms, hence not lifted from the mass domain (atom, here is a metalanguage predicate).
(Singular) count predicates, in particular count nouns, denote subsets of $\mathrm{A}_{\mathrm{k}}$, and are derived as follows. All lexical nouns N are associated with a root noun meaning $\mathrm{N}_{\text {root }}$. (see above). This root noun meaning is a Boolean algebra generated under $\sqcup_{M}$ from a set of M-atoms. As noted above, $\mathrm{N}_{\text {mass }}=\mathrm{N}_{\text {root }} \subseteq \mathrm{M}$.

Count nouns are derived from root noun meaning by an operation $\operatorname{COUNT}_{\mathrm{k}}$ which applies to the root noun $\mathrm{N}_{\text {root }}$ and picks out the set of ordered pairs $\{<\mathrm{d}, \mathrm{k}>\mathrm{d} \varepsilon \mathrm{N} \cap$ $\mathrm{k}\}$. These are the entities which in the given context k count as atoms, and thus can be counted. The parameter k is a parameter manipulated in context. Thus, in the course of discourse we have as many relevant ks around as is contextually plausible. We can think of these contexts as contextually defined perspectives on a situation or model, and the set of contextually relevant contexts is rich enough so that there may be different numbers of N entities in a situation depending on the choice of k , i.e the choice of counting perspective that is chosen. In sum:

$$
\begin{equation*}
\text { For any } \mathrm{X} \subseteq \mathrm{M}: \operatorname{COUNT}_{\mathrm{k}}(\mathrm{X})=\{\langle\mathrm{d}, \mathrm{k}>: \mathrm{d} \varepsilon \mathrm{X} \cap \mathrm{k}\} \tag{1}
\end{equation*}
$$

The interpretation of a count noun $\mathrm{N}_{\text {count }}$ in context k is: $\mathrm{N}_{\text {count }}=\operatorname{COUNT}_{\mathrm{k}}\left(\mathrm{N}_{\text {root }}\right)$.
We will use $\mathrm{N}_{\mathrm{k}}$ for this interpretation of $\mathrm{N}_{\text {count }}$ in k .
The denotation of a singular count noun is thus an ordered pair whose first projection is a set of entities $\mathrm{N}_{\text {root }} \cap \mathrm{k}$, and whose second projection is context k .
We call such sets semantically atomic sets, since the criterion for what counts as an atom is semantically encoded by the specification of the context. The set $\mathrm{N}_{\text {root }} \cap \mathrm{k}$ is the set of semantic atoms in $\mathrm{N}_{\text {root }}$ relative to k . This is the set of atomic N -entities used to evaluate the truth of an assertion involving $\mathrm{N}_{\text {count }}$ in a particular context k , i.e. $\mathrm{N}_{\mathrm{k}}$.

The atoms in k are not constrained by a non-overlap condition, since we want to allow examples such as those I can move my hand and my five fingers and It took 2500 bricks to build this wall which make reference to atomic elements and their atomic parts. Non-overlap is not irrelevant though, I assume it comes in as a constraint on default contextual interpretations:

Constraint on count predicates: In a default context $k$, the interpretation of singular count predicate P is a set of mutually non-overlapping atoms in k (where $<\mathrm{a}, \mathrm{k}>$ and $<\mathrm{a}^{\prime}, \mathrm{k}>$ don't overlap iff a $\Pi_{\mathrm{M}} \mathrm{a}^{\prime}=0$ )

This guarantees that when we count entities in the denotation of $\mathrm{N}_{\mathrm{k}}$ we will be counting contextually discrete, non-overlapping entities.

Plural count nouns are are derived from singular count noun meanings, using the standard plural operation, defined in the current count structures, and thus adapted to thefor the meaning of the count noun. The plural operation gives the closure of $\mathrm{N}_{\text {root,k }}$
under the sum operation, while keeping track of the context. Link's plural operation (Link 1983) is as follows:

$$
\begin{equation*}
\text { *A }=\left\{\mathrm{d}: \exists \mathrm{Y} \subseteq \mathrm{~A}_{\mathrm{k}}: \mathrm{d}=\mathrm{L} \mathrm{Y}\right\} \tag{2}
\end{equation*}
$$

For a relation $N_{k}$ we define the $n$-th projection of $N_{k}$ as follows:

$$
\begin{align*}
& \pi_{1}\left(\mathrm{~N}_{\mathrm{k}}\right)=\left\{\mathrm{d}:<\mathrm{d}, \mathrm{k}>\in \mathrm{N}_{\mathrm{k}}\right\}  \tag{3}\\
& \pi_{2}\left(\mathrm{~N}_{\mathrm{k}}\right)=\mathrm{k} \tag{4}
\end{align*}
$$

For convenience we also define $\pi_{\mathrm{n}}$ directly for pairs:

$$
\begin{align*}
& \pi_{1}(<\mathrm{d}, \mathrm{k}>)=\mathrm{d}  \tag{5}\\
& \pi_{2}(<\mathrm{d}, \mathrm{k}>)=\mathrm{k}
\end{align*}
$$

Note that for any $<\mathrm{d}, \mathrm{k}>\in \mathrm{N}_{\mathrm{k}}, \pi_{2}(<\mathrm{d}, \mathrm{k}>)=\pi_{2}\left(\mathrm{~N}_{\mathrm{k}}\right)=\mathrm{k}$.
With this we lift the ${ }^{*}$-operation to the present count structures:

$$
\begin{equation*}
\text { In default context } \mathrm{k}: \operatorname{PL}\left(\mathrm{N}_{\mathrm{count}}\right)={ }^{*} \mathrm{~N}_{\mathrm{k}}=\left\{<\mathrm{d}, \mathrm{k}>: \mathrm{d} \in{ }^{*} \pi_{1}\left(\mathrm{~N}_{\mathrm{k}}\right)\right\} \tag{6}
\end{equation*}
$$

(In non-default contexts, we don't lift plurality from the mass domain. Thus in nondefault context k: * $\pi_{1}\left(\mathrm{~N}_{\mathrm{k}}\right)=\left\{\mathrm{d}: \exists \mathrm{Y} \subseteq \mathrm{A}_{\mathrm{k}}: \mathrm{d}=\mathrm{L}_{\mathrm{k}} \mathrm{Y}\right\}$ )

We stress several important points: first, the non-overlap condition in the constraint on count predicates guarantees that in default contexts, the order of the plural count noun denotation is lifted directly from M. So the denotation of the plural count noun depends on the contextually determined denotation of the singular $\mathrm{N}_{\mathrm{k}}$. The plural noun denotes a set of ordered pairs where the first element is in the closure of $\mathrm{N}_{\text {root, } \mathrm{k}}$ under sum and the second element is the context k.. $\mathrm{N}_{\text {root, } \mathrm{k}}$ may vary depending on choice of k , and the denotation of the plural set will similarly vary, depending on $\mathrm{N}_{\text {root, } k}$. Crucially, the information about the context determining the set of atoms is preserved in the plural denotation. There is no guarantee that, even with a predicate like hair, $\operatorname{HAIR}_{\text {root,k }}$ and the set of atoms in the $\operatorname{HAIR}_{\text {root }}$ is the same set. So though the hair and the hairs may well refer to the same real-world entity, there is no guarantee that they do so. Second, since k itself is not constrained by a non-overlap condition, the plural domain may contain elements not lifted from M. These will not be in the denotations of lexical predicates, but they will be in the denototations of other expressions built up in the grammar like the conjunctive definite my hand and its five fingers. The grammatical operation of counting will consist of the modification of N expressions by numerical modifiers and it will apply at the N level. In a normal context, my hand counts as an atom, and its five fingers counts as a sum of five finger, consequently in k my hand and its five fingers will denote a sum of 6 atoms. However, we will not normally count across conjunctions, thus, I moved my hand and its five fingers, does not imply a felicitous use of Hence I moved six body parts, since the predicate body part in a default context will be interpreted as denoting a set of non-overlapping objects. For a discussion of non-default contexts, and situations where overlapping entities are felicitously counted, see Rothstein 2009.

To conclude this section, we survey the range of possible nominal denotations:
Root nouns: $\mathrm{N}_{\text {root }} \subseteq \mathrm{M}$ : Root nouns denote a Boolean algebra of mass entities, the closure of a set of atoms in M under the sum operation $\sqcup_{\mathrm{M}}$.
Mass nouns: $\mathrm{N}_{\text {mass }}=\mathrm{N}_{\text {root }}$ : Mass nouns just are root nouns.
Singular count nouns: $N_{k} \subseteq M \times\{k\}$ : A singular count noun denotes a set of ordered pairs of which the first projection is $\mathrm{N}_{\text {root, }} \cap \mathrm{k}$, a subset of $\mathrm{N}_{\text {root }}$ whose members do not (generally) overlap, and the second projection is the context $k$. The denotation of a count noun such as fence is context dependent, since the choice of atoms depends on the $\mathrm{COUNT}_{\mathrm{k}}$ operation, which itself is dependenton the choice of context k.
Plural nount nouns: In a default context $\mathrm{k}, \mathrm{PL}\left(\mathrm{N}_{\mathrm{k}}\right) \subseteq \mathrm{M} \times\{\mathrm{k}\}$, where the first projection is the closure of $\mathrm{N}_{\text {root }} \cap \mathrm{k}$ under sum, and the second projection is k .

## 3 Implementing the Analysis

Mass nouns and count nouns are of different types: mass nouns denote subsets of D , and thus of type <d,t>; count nouns denote subsets of $\mathrm{D} \times \mathrm{K}$ and are of type $\ll \mathrm{d} \times \mathrm{k}>, \mathrm{t}>$. In this section we explore how this works compositionally:

### 3.1 Operations which are not Sensitive to the Count/Mass distinction

Adjectival modification: Some grammatical operations apply equally well to both types, for example adjectival modification as in an expensive chair, expensive furniture. We treat expensive as denoting a property of individuals, which in its attributive reading shifts to the predicate modifier type $\langle<\mathrm{d}, \mathrm{t}\rangle,<\mathrm{d}, \mathrm{t}\rangle>$. As a predicate modofier, expensive applies to mass nominal expressions of type $<\mathrm{d}, \mathrm{t}>$, denoting the function $\lambda \mathrm{P} \lambda \mathrm{x} . \mathrm{P}(\mathrm{x}) \wedge \operatorname{EXPENSIVE}(\mathrm{x})$. ( P is a variable over expressions of type $<\mathrm{d}, \mathrm{t}$.) We assume a count modifier EXPENSIVE Count modifying expresions of type $<\mathrm{d} \times \mathrm{k}, \mathrm{t}>$, and which is defined in terms of EXPENSIVE, using the $\pi_{\mathrm{n}}$ function defined in (5). ( $\mathcal{P}$ is a predicate variable type $<\mathrm{d} \times \mathrm{k}, \mathrm{t}>$, and $x$ is a variable of type $\mathrm{d} \times$ k). EXPENSIVE Count denotes the function $\lambda \mathcal{P} \lambda \mathrm{x} . \mathcal{P}(\mathrm{x}) \wedge \operatorname{EXPENSIVE}\left(\pi_{1}(\mathrm{x})\right)$.

Conjunction: Conjunction of count and mass nouns such as tables and other furniture must be at the type of mass noun. This is shown in the partitive constructions in (6), where a conjunction of mass and count noun can occur in the partitive only with mass determiners:

> *Three/Many of [the tables and the furniture] arrived damaged. Some/Much of the tables and the furniture arrived damaged.

We assume that and conjoins arguments at the same type. In cases of type mismatch, the count nouns lowers to a mass reading via the $\pi_{\mathrm{n}}$ function.

$$
\begin{equation*}
\text { ||tables and (other) furniture } \|=\operatorname{AND}\left(\pi_{1}(\| \text { tables } \|), \| \text { furniture } \|\right) \tag{9}
\end{equation*}
$$

$$
\left.=\text { AND }^{*} * \text { TABLES }_{\text {rootk }}, \text {, FURNITURE }\right)
$$

### 3.2 Operations Which Distinguish Between Mass and Count Nouns

Grammatical counting: Grammatical counting, i.e. modification by numerical expressions is sensitive to the count/mass distinction. We propose that number expressions are sensitive to the typal difference between mass and count nouns. Numerical expressions such as three denote functions from $<\mathrm{d} \times \mathrm{k}, \mathrm{t}\rangle$ into $<\mathrm{d} \times \mathrm{k}, \mathrm{t}>$, and thus cannot apply to mass nouns. Three applies to a set of ordered pairs $\mathrm{N}_{\mathrm{k}}$ and gives the subset of $N_{k}$, such that all members of $\pi_{1}\left(N_{k}\right)$ are plural entities with three parts each of which is an entity in k .

$$
\begin{equation*}
\| \text { Three } \|\left(\mathrm{N}_{\text {count }}\right)=\lambda \mathcal{P} \lambda x . \mathcal{P}(x) \wedge\left|\pi_{1}(x)\right|_{\pi 2(\mathcal{P})}=3 \tag{10}
\end{equation*}
$$

Three denotes a function which applies to a count predicate $\mathrm{N}_{\mathrm{k}}$ and gives the subset of ordered pairs in $\mathrm{N}_{\mathrm{k}}$, where the first projection of each ordered pair has three parts which count as atoms in k .

Determiner selection: Determiners are sensitive to the typal difference between $<\mathrm{d}, \mathrm{t}>$ and $<\mathrm{d} \times \mathrm{k}, \mathrm{t}>$, as in every chair vs *every furniture.

Partitive constructions: Partitive constructions such as three of the chairs of the furniture are sensitive to the properties of the nominal head of their complement, The determiner heading a partitive shows the same selectional restrictions with respect to the nominal head of its complement as determiners usually show within a bare DP: three of the chairs/three chairs; *three of the furniture/*three furniture(s);*much of the chairs/*much chairs; much of the furniture/much furnitures; We thus need to recover the predicate expression from the DP. This is possible because operations involved in the construction of the DP keep track of the original context k at all stages. The partitive operates on a definite complement, which is defined using Link's [11] operation:

For mass nouns: the $\mathrm{N}=\sqcup \mathrm{N}$, the (unique) maximal entity in N
For count nouns: the $\mathrm{N}_{\mathrm{k}}=\left\langle\sqcup \pi_{1}\left(\mathrm{~N}_{\mathrm{k}}\right), \mathrm{k}>\right.$

We lift the part-of relation on ordered pairs in $\mathrm{M} \times\{\mathrm{k}\}$ from M : $\left.<\mathrm{x}_{1}, \mathrm{k}\right\rangle \sqsubseteq_{\mathrm{k}}<\mathrm{x}_{2}, \mathrm{k}>$ iff $\mathrm{x}_{1} \sqsubseteq_{\mathrm{M}} \mathrm{x}_{2}$.

The partitive operation follows the following definition schema: it operates on a definite complement and gives the set of parts: PARTITIVE $(\sqcup N)=\{\mathrm{X}: \mathrm{X} \sqsubseteq(\sqcup \mathrm{N})\}$

For a mass predicate, PARTITIVE $\left(\sqcup_{M}\left(\mathrm{~N}_{\text {mass }}\right)\right)=\left\{\mathrm{x}: \mathrm{x} \sqsubseteq_{\mathrm{M}} \sqcup_{\mathrm{M}}\left(\mathrm{N}_{\text {mass }}\right)\right\}$, i.e. $\mathrm{N}_{\text {mass }}$.

For a count predicatein context $k$, PARTITIVE $\left(\sqcup_{k}\left(\mathrm{~N}_{\mathrm{k}}\right)\right)$ is again lifted from M:
PARTITIVE $\left.\left.\left(\sqcup_{\mathrm{k}} \mathrm{N}_{\mathrm{k}}\right)=\{\langle\mathrm{x}, \mathrm{k}\rangle:<\mathrm{x}, \mathrm{k}\rangle \sqsubseteq_{\mathrm{k}}<\mathrm{\bigsqcup}_{\mathrm{M}}\left(\pi_{\mathrm{l}}\left(\mathrm{N}_{\mathrm{k}}\right)\right), \mathrm{k}\right\rangle\right\}$
Crucially, since we kept track of the context k during all the operations involving the composition of the embedded DP, the operation giving the set of parts of $\sqcup N_{k}$ will still have access to the original context k . Partitive determiners apply to the result of applying PARTITIVE to the DP meaning, exactly as they would apply to NP within the DP. Since three makes use of the parameterized cardinality function which makes reference to k ., it can apply to PARTITIVE(the chairs) or PARTITIVE(the pieces of furniture) which denote sets of type $<\mathrm{d} \times \mathrm{k}, \mathrm{t}>, \quad$ but not to PARTITIVE(the furniture), which denotes a set of type $<\mathrm{d}, \mathrm{t}>$. Some applies equally well to both types.

Reciprocal resolution: Reciprocal resolution is sensitive to the mass/count distinction. A reciprocal must have cannot take a mass noun as antecedent although it is 'lexically plural'. We assume that reciprocals (in English) are constrained to take as antecedents plural entities in $\mathrm{D} \times\{\mathrm{k}\}$. We assume that the antecedent for a reciprocal must be a plural entity in We use this constraint to explain Gillon's observation in [3] that The curtains and the carpets resemble each other (the 'count' reciprocal) is ambiguous between the collective reading in which the sum of curtains resembles the sum of carpets and vice versa and the distributive reading in which each member of the set CURTAINS $\cup$ CARPETS resembles all the other members of the set. The mass counterpart, the curtaining and the carpeting resemble each other, has only the first collective reading. Space constraints prevent giving a full analysis here, but the outline of the explanation is as follows.
On the distributive reading of the count reciprocal, the conjoined DP the curtains and the carpets denotes the sum of the maximal plurality of curtains and the maximal plurality of carpets. and the interpretation of the reciprocal requires every two atomic entities (i.e. atomic individuals in the denotation of CURTAINS ${ }_{k} \cup$ CARPETS $_{k}$ ) to resemble each other. On the second reading of this sentence, the curtains as a group, or singular collectivity, resemble the curtains as a group, or singular collectivity, and vice versa. On this reading LCURTAINS and the sum of carpets, LCARPETS are treated as collections (see [12]) and are raised to the group-atoms GR(UCURTAINS ${ }_{k}$ ) and GR( $\sqcup$ CARPETS ${ }_{k}$ ). We assume that raising to group atoms is relative to a context k , and that the group atoms are indexed for the context in which they are atomic. Group atoms thus have their denotations in $\mathrm{D} \times\{\mathrm{k}\}$, and pluralities of group atoms such as the curtains and the carpets can be antecedents for reciprocals.
When the antecedent of the reciprocal is the curtaining and the carpeting, the distributive reading is not available. This is because curtaining and carpeting are nominals of type $<\mathrm{d}, \mathrm{t}>$ and the definites denote maximal sums of entities in the mass domain M. However, the group reading is available since UCURTAINING and பCARPETING can be raised to atomic collectivities GR(UCURTAINING) and GR(பCARPETING) respectively, and the conjunction denotes a plurality of atoms in the count domain.

## 4 Formal Atomicity, Natural Atomicity and Semantic Atomicity

This account we have assumes a single domain M , and analyses the count/mass distinction as a typal distinction between mass predicates which are simple predicates denoting subsets of the domain M and (singular) count predicates denoting denoting sets of indexed entities, where the index indicates the context in which they count as one. Count nouns are derived from mass nouns (or root nouns) by a lexical operation COUNT ${ }_{k}$, picking out those entities in $\mathrm{N}_{\text {root }}$ which count as atoms in the context k and indexing them as such. While similar to Krifka [13,14], insofar as both this and Krifka's account derives count nouns from mass nouns by a lexical operation, the theories are very different conceptually and formally. Krifka proposes analysing count nouns as extensive measure functions of type $<\mathrm{n},<\mathrm{d}, \mathrm{t} \gg$ which apply to a number to give a measure predicate. Cattle is a mass predicate of type $<\mathrm{d}, \mathrm{t}>$, denoting $\lambda \mathrm{x}$. CATTLE( x ). It is similiar in meaning to the root noun COW, in fact we can assume for our purposes that they are synonymous. The count nouns COW' is derived from COW (or CATTLE) and denotes $\lambda n \lambda x . C O W(x) \wedge$ NATURAL $\operatorname{UNIT}(x)=n$. This applies to a number and yields a count predicate, indistinguishable in type from the mass noun, but with a different meaning. In the absence of an explicit number word, the predicate is reduced from $<\mathrm{n},<\mathrm{d}, \mathrm{t} \gg$ to $<\mathrm{d}, \mathrm{t}>$ via existential quantification over the n argument. Crucially, for Krifka, the typal difference between mass and count terms is neutralised before the higher nodes of the N tree are constructed. In the theory presented here, the typal difference persists up to the DP level and allows grammatical operations such as partitive construction and reciprocal resolution to exploit the typal constrast. This technical difference reflects a deeper conceptual difference. Krifka analyses count nouns as extensive measure functions directly analogous to expressions such as kilo and litre. We start here from the premise that measuring and counting are very different operations: measuring assigns a quantity a value on a dimensional scale, while counting puts entities in one-to-one correspondence with the natural numbers. I pursue this contrast between measuring and counting in ongoing research. [15].
The theory developed here allows allows us to distinguish three kinds of atomicity. (i) Formally atomic sets are sets of atoms which generate atomic Boolean algebras under the complete join operation. These sets may be vague and/or underspecified; (ii) Semantically atomic sets which are derived via the $\mathrm{COUNT}_{\mathrm{k}}$ operation and denote sets of entities which are atomicin a specified context k.; These sets are grammatically countable. (iii) Naturally atomic sets, which are sets of inherently individuable entities, and which may generate denotations for mass nouns as well as for plural count nouns e.g. child and furniture are naturally atomic count and mass predicates respectively, while fence and mud are examples of count and mass predicates which are not naturally atomic. Naturally atomic mass predicates make possible quantity judgements based on number rather than volume as in "who has more furniture" [4](Barner and Snedeker 2005). They are semantically relevant since they may host districutive predicates such as big [which distribute over natural atoms (see 3). Pires d'Oliveira and Rothstein [ ] show that in Brazilian Portuguese they may be antecedents for reciprocals. However, natural atomicity is neither a necessary nor sufficient condition for count semantics.

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# Donkey Anaphora in Sign Language: Evidence from LSF and ASL 

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#### Abstract

There are two main approaches to the problem of donkey anaphora (e.g. If John owns a donkey, he beats it). Proponents of dynamic approaches take the pronoun to be a logical variable, but they revise the semantics of quantification so as to allow an indefinite to bind a variable that is not within its syntactic scope. Older dynamic approaches (e.g. Kamp \& Reyle 1993) took this measure to apply solely to indefinites; recent dynamic approaches extended it to all quantifiers (e.g. van den Berg 1996, Nouwen 2006, Brasoveanu 2007). By contrast, proponents of E-type analyses take the pronoun to go proxy for a definite description (e.g. the donkey, or the donkey that John owns); in order to satisfy its uniqueness presupposition, they combine this approach with an analysis of $i$-clauses (as well as other operators) as quantifiers over finegrained situations. Thus competing accounts of donkey anaphora make rather different claims about the coindexing relations that should be found. While these are not morphologically visible in spoken languages, they arguable are in sign languages (Sandler and Lillo-Martin 2004); these are thus an interesting testing ground for the debate. We argue that data from French and American Sign Language favor recent dynamic approaches: in those cases in which Etype analyses and dynamic analyses make different predictions about the formal connection between a pronoun and its antecedent, dynamic analyses are at an advantage; and it appears that the same formal mechanism is used irrespective of the indefinite or non-indefinite nature of the antecedent, which argues in favor of recent dynamic approaches over older ones.


Keywords: anaphora, E-type anaphora, donkey anaphora, dynamic semantics, sign language, LSF, ASL

## 1 The Debate

### 1.1 The Problem

We attempt to bring new light to the debate on donkey anaphora by investigating data from two sign languages, French Sign Language (LSF) and American Sign Language (ASL). Our enterprise is motivated by the following considerations:
(i) Competing approaches to donkey anaphora make different predictions about the patterns of coindexing that are found in different examples.
(ii) In sign languages, coindexing is arguably realized overtly, by way of pointing (Sander and Lillo-Martin 2004).
(iii) Therefore sign language could bring new data to bear on this debate, which has remained open despite quite a bit of work in formal semantics.

The problem is illustrated by the examples in (1) and (2).

## (1) Indefinites

a. John owns a donkey. He beats it.
b. If John owns a donkey, he beats it.
(2) Non-Indefinites
a. John owns fewer than 5 donkeys. He beats them
b. If John owns fewer than 5 donkeys, he beats them.

In each case, the pronoun is semantically dependent on the quantifier; but it is not c-commanded by it. This poses a problem if the following two standard assumptions are adopted:
(i) Pronouns are logical variables.
(ii) The semantics of quantifiers gives rise to a standard notion of scope, namely ccommand.
Dynamic approaches preserve (i) but revise (ii). E-type approaches preserve a version of (ii) but revise (i), taking pronouns to go proxy for definite descriptions (e.g. the donkey, or the donkey that John owns). As we will see below, however, when all the necessary refinements of the E-type approach are taken into account, the two theories diverge considerably less than this cursory characterization suggests (Dekker 2004).

### 1.2 E-type Approaches

E-type approaches have the following ingredients (which depend on the approach under consideration):
(3) Pronouns as descriptions

Pronouns are treated as being (syntactically and/or semantically) descriptions in disguise. Depending on the approach, (1)a gets analyzed as in a. or b. below, where $i t$ has the semantics of the definite description operator.
a. If John owns a donkey, he beats it-donkey he has
b. If John owns a donkey, he beats it-donkey (Elbourne)
(4) Quantification over situations / events

In order for the uniqueness presupposition of the definite description to be satisfied, proponents of E-type approaches take if-clauses (and more generally all operators) to quantify over very fine-grained situations or events.

## (5) Formal Link

In order to account for the classical contrast between a. and b. below, E-type theories must establish a 'formal link' between the pronoun and its antecedent.
a. Every man who has a wife is sitting next to her.
b. ?* Every married man is sitting next to her (Heim 1982)

Elbourne 2005 takes the formal link to result, quite simply, from a syntactic ellipsis of the NP (e.g. her = the wife)

Importantly, this account treats the case of indefinite and non-indefinite antecedents on a par, as is illustrated in (6).
(6) a. If John owns a donkey, he beats it donkey.
b. If John owns fewer than 5 donkeys, he beats them donkeys.

### 1.3 Dynamic Approaches

Dynamic approaches share the following properties.
(7) Pronouns as variables

Pronouns are treated as logical variables, and can be coindexed with non-ccommanding indefinites, as illustrated in a . and b .
a. John owns [a donkey $]_{\mathrm{i}}$. He beats $\mathrm{it}_{\mathrm{i}}$
b. If John owns [a donkey $]_{i}$, he beats $\mathrm{it}_{\mathrm{i}}$
(8) Revision of quantification

Quantification is revised so as to make it possible for a variable to depend on a non-commanding quantifier. This can be done in purely semantic terms, by way of quantification over assignment function; or through syntactic stipulations such as those illustrated in a. and b., where $\exists$ and $\forall$ are unselective quantifiers (in such an implementation, indefinites are taken to introduce variables).
a. $\exists$ [John owns [a donkey] $]_{i}$. He beats $i_{i}$ ]
b. $\forall[\text { John owns [a donkey }]_{\mathrm{i}}\left[\right.$ he beats $\left.\mathrm{it}_{\mathrm{i}}\right]$
(9) Formal Link: coindexing

Coindexing provides a formal link between a pronoun and its antecedent, and it has a direct semantic reflex.

Dynamic approaches differ in their treatment of donkey pronouns that depend on quantifiers that are not indefinites. To see why there is an issue in the first place, consider a the kind of truth conditions that a simple-minded extension of (8)a would predict for (10):

## (10) Problem

a. John owns [at least 2 donkeys]. He beats them.

Bad: ヨX [John owns X \& $\geq 2$ donkeys(X) \& John beats X]
b. John owns [fewer than 5 donkeys]. He beats them.

Bad: $\exists \mathrm{X}$ [John owns X \& $<5$ donkeys(X) \& John beats X]
It is immediate that the truth conditions captured by (10) are inadequate.
-Intuitively, (10)a entails that John beats all the donkeys that he has. But this
entailment is not captured in the proposed truth conditions: the fact that the pronoun refers to the maximal group of donkeys that John is left unaccounted for.
-The same problem arises in (10)b: the inference that John beats all the donkeys that he has is not captured. But in addition, the proposed truth conditions do not even entail that John owns fewer than five donkeys (all they entail is that it is possible to find a group of fewer than five donkeys that John owns - which is far too weak).

There are two broad solutions to the problem. One is a mixed approach (Kamp and van Eijck 1993): for indefinite antecedents, the standard dynamic line is adopted; for other antecedents, a version of the E-type approach is posited, one in which the quantifier has its 'usual' meaning and where the pronoun goes proxy for a definite description - which directly accounts for the maximality condition observed in (10)a.
(11) Mixed Solution (Kamp \& van Eijck 1993)
a. Indefinites are treated in the dynamic way.
b. Other quantifiers are treated with some version of the E-type account.

The alternative is a pure dynamic approach, one in which all quantifiers (not just indefinites) introduce discourse referents and can bind variables that they do not c-command. In order to address the problems seen in (10), quantifiers such as at least two and fewer than five are taken to introduce discourse referents together with explicit maximality conditions. As is illustrated in (10), this measure makes it possible to derive the correct truth conditions within a pure dynamic system.
(12) Pure Solution (e.g. van den Berg 1996, Nouwen 2003, Brasoveanu 2007)
a. John owns [at least 2 donkeys]. He beats them.
$\exists \mathrm{X}$ [John owns X \& X = Max Y: donkey(Y) \& John owns Y \& $\geq 2$
donkeys(X) \& John beats X]
b. John owns [fewer than 5 donkeys]. He beats them.

ヨX [John owns X \& X = Max Y: donkey(Y) \& John owns Y \& <5 donkeys(X) \& John beats X]

### 1.4. The Complexity of the Debate

The debate between dynamic and E-type approaches is more subtle than it looks at first sight. In a nutshell, some recalcitrant examples have forced the E-type approach to adopt a mechanism of quantification over extremely fine-grained situations, which looks quite a bit like quantification over assignment functions (Dekker 2004). Consider the sentences in (13):
(13) a. A bishop met a bishop. He blessed him.
b. If a bishop meets a bishop, he blesses him.

The potential difficulty is immediate for Elbourne's (2005) theory: if he and him are both construed as the bishop, it is not clear how their uniqueness presuppositions will be satisfied. But versions of the E-type analysis that resort to a longer descriptive content are no better off: resolving he as the bishop that met a bishop and him as the
bishop that a bishop met won't help a bit. The difficulty is that, to put it roughly, the two bishops of the antecedent clause play entirely symmetric roles.

How can the symmetry be broken? There are in fact two difficulties, which we illustrate on the example of (13)b (which is discussed in detail in Elbourne 2005).
(i) First, situations must be made sufficiently fine grained so the 'symmetry' between the bishops mentioned in the antecedent can in principle be broken. An old insight, called 'Chierchia's Conjecture' in Dekker 2004, is that in the end situation-theoretic analyses might have to make situations as fine-grained as assignment functions. Dekker 2004 shows that with quite a few assumptions - which he takes to go against the spirit of situation theory - situations are indeed isomorphic to assignment functions. One of these assumptions is that a situation in which bishop B meets bishop $B^{\prime}$ is different from a situation in which situation $B^{\prime}$ meets bishop $B$. Such an assumption is accepted by Elbourne 2005, and it is an important ingredient of his solution.
(ii) Second, even if situations are made extremely fine-grained, the situation-theoretic analysis must endow the pronouns in the consequent clause with enough descriptive content to pick out different individuals. Suppose for instance that we took if-clauses to quantify over situations that are just equated with tuples of individuals - thus accepting Dekker's isomorphism between situations and tuples of individuals. We would still have to explain how the pronouns he and him manage to pick out different individuals in the same situation (i.e. in the same tuple). One way to do so would be to stipulate that they come with some equivalent of indices, so that for instance $h e_{l}$ evaluated with respect to a situation $s$ with $s=\left\langle B, B^{\prime}>\right.$ denotes $B$, while in the same situation $h e_{2}$ denotes $\mathrm{B}^{\prime}$. But it is immediate that such a radical step would make the situation-theoretic analysis even closer to the dynamic analysis.

These formal points are worth keeping in mind when one seeks to assess the donkey anaphora debate on empirical grounds. If indeed the two approaches can in principle converge, it might be hard to decide the debate in favor of one analysis and against any version of the other. Rather, we can only hope to show something weaker, namely that either one theory is incorrect, or it will have to borrow essential formal tools from the second. This is what we will now set out to do by considering data from sign language.

## 2 Predictions for Sign Language

### 2.1 Pronouns in Sign Language

In the sign languages that have been described, the relation between a pronoun and its antecedent is usually realized through the intermediary of loci, which are positions in signing space which are associated to nominal elements. A pronoun that depends on a proper name will thus point towards ('index') the locus in which the proper name was signed. Since there appears to be an arbitrary number of possible loci, it was suggested that the latter are the morphological realization of indices (Sandler and Lillo-Martin 2004). This makes it particularly interesting to use sign language to
investigate a theoretical debate that revolves around the nature of coindexing relations.

Of course, it could be that the anaphoric system found in sign language is entirely different from that found in spoken languages. If so, we would be getting from sign language morphological evidence on a different system from the one that prompted the debate about donkey anaphora in the first place. But despite the difference in modality, there are some striking similarities between sign language pronouns and their spoken language counterparts:
(i) In simple cases, the same ambiguity between strict and bound variable readings is found in both modalities, as is illustrated in (14) and (15).
(14) LSF
a. FANTASTIC. PIERRE LIKE WIFE aPOSS. bIX JEAN TOO.
(Informant A 369; cf. Informant C, 193)
'It's fantastic. Pierre loves his wife, and Jean does too.'
b. COMPLICATED. PIERRE LIKE WIFE aPOSS. bIX JEAN bIX TOO.
(Informant A, 374; cf. Informant C, 201)
'Things are complicated. Pierre loves his wife, and Jean does too.'
(15) ASL

IX-1 POSS-1 MOTHER LIKE. IX-a TOO. (Inf 1 108)
Ok I like my mother. He too <likes my mother>
Ok I like my mother. He too <likes his mother>
(ii) Sign language pronouns appear to be constrained by at least some of the syntactic constraints on binding studied in syntax. For instance, versions of the following constraints have been described for ASL:
-Condition A
-Condition B
-Strong Crossover (recently extended to Weak Crossover)

### 2.2 The Importance of Bishop Sentences

The simplest donkey sentences appear to provide initial evidence in favor of dynamic accounts because pronouns appear to index antecedents that do not c-command them. In the following, sign language sentences are glossed in capital letters; subscripts correspond to the establishment of locations ('loci') in signing space; pronouns, glossed as IX (for 'index') as well as other expressions can then point back towards these locations; in such cases, the location is suffixed to the pronoun (e.g. IX-a is a pronoun that points words location a, while IX-b is a pronoun that points towards location b ; the number 1 corresponds to the position of the signer - hence $1^{\text {st }}$ person).
(16) LSF
a. ${ }_{a}$ STUDENT ${ }_{\mathrm{b}}$ PRIEST BOTH-a,b DISCUSSED. IX-b KNOW BIBLE IX-a NOT-KNOW
'I talked to a student and a priest. The priest knew the Bible but the student didn't know it'. (Informant E; 2, 62)
b. EACH-TIME ${ }_{a}$ LINGUIST ${ }_{b}$ PSYCHOLOGISTALL-THREE- b,a, 1

TOGETHER WORK, IX-a HAPPY BUT IX-b HAPPY NOT.
'Whenever I work with a linguist and a psychologist, the linguist is happy but the psychologist is not happy.'( $\mathbf{E} ; 2,63$ )

These examples appear to provide initial support for dynamic analyses because they display patterns of coindexing without c-command. But they are by no means decisive. For the E-type approach could account these examples along the following lines:
(i) In sign language, a pronouns indexes the Noun Phrase that provides its descriptive content. In the implementation of Elbourne 2005, we may simply posit that a pronoun points towards the Noun Phrase which provides its antecedent under NP ellipsis. Since we already know from spoken languages that some formal link must be provided between the pronoun and its antecedent, it comes as no particular surprise that the same phenomenon can be observed in sign language.
(ii) In all cases such as (16), pronouns index exactly the syntactic element that they should - in particular under Elbourne's approach. Therefore (some) E-type approaches make exactly the same predictions as standard dynamic approaches.

When it comes to bishop sentences such as (13), however, things are different; some E-type accounts make different predictions from dynamic accounts (recall that by 'Chierchia's conjecture' and Dekker's results, there generally to develop E-type accounts that makes them converge with dynamic accounts; so we can't expect that all conceivable E-type accounts will be distinguished from dynamic accounts). One conceivable E-type account (which corresponds to my understanding of Elbourne 2005) posits that extra-linguistic material is used to enrich the descriptive content of the pronouns to allow them to pick out different bishops. Following Elbourne 2005, we can introduce some additional material $\boldsymbol{D}$ and $\boldsymbol{N}$ to refer to the 'distinguished' and 'non-distiguished' bishop in a situation (note that situations are sufficiently finegrained that the two bishops can indeed play asymmetric role).

## (17) If a bishop meets a bishop, he $\mathbf{D}$ bishop blesses him $\mathbf{N}$ bishop.

Crucially, the formal link between a pronoun and its antecedent is provided in this analysis by syntactic ellipsis. But in this case the very same results are obtained no matter which antecedent is used, since all that is elided is the noun bishop. For this reason, each pronoun could in principle take the same NP as its antecedent under ellipsis. And there certainly are other cases in which two elided NPs can the same antecedent, as shown in (18); so this possibility should be open here too.
(18) If two bishops meet, one bishop blesses the other bishop.

So we end up with the following prediction:
a. An E-type theory in which the denotations of the pronouns in bishop sentences are distinguished by extra-linguistic material allows both pronouns to have the same antecedent. Thus if pointing in sign language realizes the antecedence relation (= formal link) found in bishop sentences, both pronouns
could index the same antecedent while denoting different individuals.
b. For dynamic analyses, by contrast, coindexing is semantically interpreted, and thus both pronouns of a bishop sentence could not index the same antecedent.

## 3 Bishop Sentences in ASL and LSF

### 3.1 Standard Cases

The patterns of indexing found with bishop sentences in ASL are in agreement with the predictions of dynamic analyses, and contradict the version of the E-type analysis discussed above:
(20) ASL

WHEN ${ }_{\mathrm{a}}$ ONE a-MEET-b ${ }_{\mathrm{b}}$ ONE...
a. IX-a TELL IX-b HAPPY a-MEET-b (Inf $1,2,285 ; 111)$
b. IX-b TELL IX-a HAPPY a-MEET-b (Inf 1, 2, 285; 111)
c. \# Any patterns in which both pronominals index the same position.
'When someone meets someone, he tells him that he is happy to meet him'
(21) LSF
a. PRIEST ${ }_{\mathrm{a}}$ IX ${ }_{\mathrm{b}}$ IX ONE PRIEST a-MEET-b. ${ }_{\mathrm{b}}$ IX BLESS-a.
'A priest met a priest. He blessed him.' (Informant B; 323)
b. WHEN ONE PRIEST ${ }_{a}$ CL MEETS OTHER PRIEST ${ }_{b}$ CL, a-GIVE-b book
'When a priest meets another priest, he gives him a book.' (Informant A; 28)
These patterns extend to cases in which several semantically parallel propositions are conjoined in the antecedent of the conditional:
(22) ASL
a. IF ${ }_{\mathrm{a}}$ FRENCH MAN HERE OTHER ${ }_{\mathrm{b}}$ FRENCH MAN HERE IX-a GREET

IX-b (Informant 1, 2, 114)
'If a Frenchman were here and another Frenchman were here, he would greet him'
b. IF ${ }_{a}$ FRENCH MAN HERE OTHER ${ }_{b}$ FRENCH MAN HERE OTHER
${ }_{c}$ FRENCH MAN HERE IX-a GREET THE-TWO-b, c (Informant 1, 2, 115)
'If a Frenchman were here and another Frenchman were here and yet another Frenchman were here, the first would greet the second and the third'.
(23) LSF
${ }_{\mathrm{a}}$ PRIEST DISCUSS. ALSO OTHER ${ }_{\mathrm{b}}$ PRIEST DISCUSS. BOOK BIBLE IX-a a-GIVE-b
'I talked to a priest. I also talked to another priest. The former gave a Bible to the latter.' (Informant E; 2, 69)

The latter observation matters because it has sometimes been suggested within event semantics that the thematic roles corresponding to subject vs. object of meet are crucial to break the symmetry between the indefinite antecedents in examples such as (20). It does not seem that this strategy can extend to cases of propositional conjunction in (22)-(23), where the antecedents bear exactly the same thematic role.

### 3.2 Intransitive Cases

Elbourne 2005 argues that in some cases a 'symmetry problem' does in fact arise in bishop sentences:
(24) a. If a bishop meets a bishop, he greets him.
b. \#If a bishop and a bishop meet, he greets him.

Elbourne suggests that the contrast in (24) is predicted by his E-type analysis, but not by its dynamic competitors. Without taking a stand on the analysis of the English data, we note that such examples appear to be unproblematic in ASL - as is predicted by dynamic analyses if pointing is the morphological realization of coindexing. Furthermore, all indexing patters predicted by dynamic analyses are in fact realized:
(25) ASL

WHEN ${ }_{\mathrm{a}}$ ONE AND ${ }_{\mathrm{b}}$ ONE $\mathrm{a}-\mathrm{MEET}-\mathrm{b}$
a. IX-a TELL IX-b HAPPY a-MEET-b (Inf 1, 2, 306)
b. IX-b TELL IX-a HAPPY a-MEET-b (Inf 1, 2, 306)
'When someone meet someone, he tells him that he is happy to meet him'
(26) ASL

WHEN $_{\mathrm{a}}$ ONE AND ${ }_{b}$ ONE AND ${ }_{\mathrm{c}}$ ONE MEET
a. IX-a TELL THE-TWO-b, c HAPPY MEET
b. IX-b TELL THE-TWO-a, c HAPPY MEET
c. IX-c TELL THE-TWO-a, b HAPPY MEET (Inf 1, 2, 307)
'When someone meets someone, he tells him that he is happy to meet him' 4.1 Arguments for a Pure Dynamic Account

## 4. Anaphora to Negative Quantifiers

Having determined that the sign language data initially favor dynamic over E-type accounts, it remains to see which version of the dynamic account best fits the sign language data. Let us remind ourselves of their main properties:
(27) a. Mixed Dynamic Accounts
-Donkey pronouns with indefinite antecedents are treated as variables which are dynamically bound.
-Donkey pronouns with non-indefinite antecedents are treated as E-type pronouns.
b. Pure Dynamic Accounts
-All donkey pronouns are treated as variables which are dynamically bound.
-Non-indefinite quantifiers introduce not just discourse referents, but also maximality conditions.
Thus the prediction of pure dynamic accounts is that the formal link between a donkey and its antecedent should be the same when the latter is indefinite as when it is non-indefinite. Mixed dynamic accounts make no such prediction. We will now show that the same formal link is used whether the antecedent is an indefinite or not. This does not strictly refute the mixed account - it could be that both types of anaphoric link are realized in the same way; but it makes this account less plausible.

The striking fact, then, is that in all the following examples the very same mechanism (establishment of a locus for the antecedent, pointing towards that locus for the pronoun) is used for non-indefinite antecedents as for indefinite antecedents.
(28) LSF
a. LESS FIVE ${ }_{a}$ STUDENT COME PARTY. IX-a-plural STAY.
'Less than five students came to the party. They stayed.' (Informant A; 37)
b. PIERRE FOUR LESS ${ }_{b}$ STUDENTS. IX-b HATE IX-a.
'Pierre has less than 4 students. They hate him.' (Informant B; 328)
(29) LSF
a. IF LESS FIVE ${ }_{2}$ STUDENT COME PARTY, IX-a-plural BE-BORED
'If less than five students come to the party, they will be bored.' (Informant
C; 210)
b. IF FOUR ${ }_{a}$ CL-plural LESS COME CLASS DANCE, IX-a-plural HAPPY NOT
'If less than four people come to the dance lesson, they won't be happy.' (Informant A; 233)
c. LESSON DANCE IF ${ }_{a}$ PEOPLE FEW IX-a HAPPY NOT
'If few people show up at the dance lesson, they won't be happy' (Informant E; 2, 73c)

### 4.2 The Presupposition of Pronouns

There are well-known cases in spoken language in which a donkey pronoun appears to have a negative quantifier $N o N P$ as its antecedent. However this is only possible when an existence presupposition associated with the pronoun is satisfied:
(30) a. *?There is no bathroom. It is (not) large.
a'. ??There is no bathroom. The bathroom is (not) large.
b. Either there is no bathroom in this house, or it is in a funny place. (Partee)
b'. Either there is no bathroom in this house, or the bathroom is in a funny place.

This paradigm is unsurprising for an E-type account; for instance, on Elbourne's analysis (2005), it goes proxy for the bathroom, and thus (30)a-b are predicted to
pattern like (30)a'-b', which seems right. Furthermore, these contrasts can easily be explained given standard theories of presupposition projection: the definite description has an existence presupposition which is not satisfied in (30)a-a'; whereas it is satisfied in (30)b-b' because, quite generally, the presupposition of the second disjunct can be satisfied by the negation of the first one (e.g. Beaver 2001).

Dynamic theories could account for these data in at least two ways. In the spirit of the pure account, one could posit that variables introduced by pronouns come with an existence presupposition. Alternatively, one could posit with the mixed account that examples such as (30)b are handled by a variant of the E-type account. Once again, the sign language data argue in favor of a pure dynamic account, in the sense that the same formal link established in the sign language counterparts of (30) is exactly the same as in sentences involving indefinite antecedents.

## (31) ASL

RECENTLY LOTTERY (FINISH).
There recently was a lottery.
a. (a) ONE WIN. IX-a / Ø WANT NAME ANONYMOUS.
'Someone won. He wanted his name to remain anonymous'
b. * ${ }_{(\text {a }}$ NOBODY WIN. IX-a WANT NAME ANONYMOUS. (Inf 1, 2, 217)
(32) ASL

RECENTLY LOTTERY (FINISH).
There recently was a lottery.
a. I NOT-THINK NOBODY WIN. I THINK IX-a / ??Ø WANT NAME ANONYMOUS.
'I don't think nobody won. I think he wanted his name to remain anonymous' (Inf 1, 2, 221; cf. 220).
b. EITHER NOBODY WIN OR IX-a WANT NAME ANONYMOUS.
'Either nobody won, or he wanted his name to remain anonymous' (Inf 1, 2, 218)
c. EITHER NO ${ }_{\text {a }}$ DEMOCRAT CL WILL CO SUPPORT HEALTH BILL WITH ${ }_{b}$ REPUBLICAN CL OR IX-a WILL a-GIVE-b A-LOT MONEY.
'Either no Democrat will cosponsor the healthcare bill with a Republican, or he [=the Democrat] will give him [=the Republican] a lot of money. (Inf 1, 2, 230)
(32)c is particularly striking: different loci are introduced for Democrat and Republican in the first disjunct; these loci are then indexed in the second disjunct, despite the fact that in the first disjunct the corresponding quantifiers do not have existential force. This argues for a version of pure dynamic accounts (e.g. Brasoveanu 2007) in which all non-indefinite quantifiers introduce discourse referents with maximality conditions, while the interpretation of pronouns is constrained by an existence presupposition.

# Modality and speech acts: troubled by German ruhig 

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#### Abstract

The paper aims to explain the distribution and effect of the German modal particle ruhig. It is argued to be licensed only in utterances that induce a particular change in the contextual settings with respect to the status of a particular possible future course of events.


## 1 Introduction

### 1.1 Modal particles in German

German makes abundant use of modal particles, especially in spoken discourse. While rarely obligatory, they often render utterances more natural. Most modal particles are tied to particular clause or speech act types. Therefore, it is often argued that they modify or specify the speech act (to be) executed (e.g. Zeevat 2003, Karagjosova 2004). Characteristically, their particular semantic or pragmatic contribution is very hard to pin down. In this paper I focus on the German modal particle ruhig, which has gained less attention than e.g. ja, doch or wohl (cf. Zimmermann t.a.). I consider ruhig particularly interesting in that its distributional restrictions raise far reaching questions about the relation between modality and speech acts, as well as some core-distinctions in the realm of modal verbs (i.e., universal vs. existential modal force; performative vs.descriptive; strong vs. weak necessity).

### 1.2 The friendly particle

When ruhig is added to a sentence, we mostly obtain a flavor of reassurance, roughly 'no worries'. Typically, the resulting sentences are used as permissions or recommendations. Examples are given in (1) and (2):
(1) Du kannst/solltest ruhig weiterschlafen.
you can/should RUHIG sleep.on
'You can/should just go back to sleep, no worries.' [declarative]

* I would like to thank the audiences of a particle workshop (Budapest, August 2009) as well as LENLS VI (Tokyo).
(2) Schlaf ruhig weiter.
sleep.Imp RUHig on
'Just go back to sleep, no worries.' [imperative]
In their written form, these sentences are ambiguous in that they could also contain the homophonous adverb ruhig 'calm, quiet, composed,... 'from which the particle is derived. The two items are distinguished prosodically, as the particle is always unstressed. Moreover, many examples are unambiguous thanks to word order. In the following, I'm concerned exclusively with the particle. If there is ambiguity in the written form, grammaticality judgements pertain to the realization of ruhig as a particle. As the contribution of the particle ('no worries') seems closely related to the adjective/adverb one might wonder if the particle could semantically be equated to the adverb, contributing 'in a quiet way'/'without worrying'. But such an interpretation fails to account for the intricate pattern of distributional restrictions (discussed in 1.3). In many cases, such a contribution is also inadequate in either scopal relation with a co-occurring modal operator.


## 1.3 ruhig is picky after all

ruhig imposes two sorts of restrictions on the contexts of its occurrence. On the one hand, a formal restriction: the particle seems to occur exclusively in sentences that contain possibility modals or in imperatives. ${ }^{1}$ On the other hand, a functional restriction: sentences containing the particle ruhig are used mostly for permissions or recommendations, but e.g. not for commands, assertions, or questions. The only formal analysis of ruhig proposed so far, Grosz (2009a, 2009b), starts out from the form side. In the following, I discuss his approach and argue that the formal restrictions are more intricate than what he assumes. I sketch an alternative account that starts out from the functional restriction. More work needs to be done to understand all details of the contribution of ruhig, but I hope to show that this strategy is more promising.

## 2 ruhig lizenced by a possibility operator

## 2.1 ruhig and modal concord (Grosz 2009a, 2009b)

In declaratives, ruhig seems to require the presence of a possibility modal. (3) contains kann 'can' and is acceptable; both (4) containing the necessity modal muss (roughly, 'must') and the unmodalized declarative (5) are unacceptable. ${ }^{2}$
(3) Du kannst ruhig weiterschlafen.
you can RuHIG sleep.on
'You can just go back to sleep, don't worry.'
${ }^{1}$ declarative, interrogative and imperative are understood as clause types, i.e. sentential form types with prototypical functions, Sadock and Zwicky (1985).
${ }^{2}$ For the moment, I do not want to make a case as to which grammatical level causes the violation. Crucially, it is not possible to come up with context of use in which the sentence would be acceptable.
(4) \#Du musst ruhig weiterschlafen. you must RUHIG sleep.on $\square$-modal
(5) $\# D u$ schläfst ruhig weiter. you sleep Ruhig on unmodalized declarative

Grosz concludes that this is an instance of modal concord. Two elements that match in modal force can sometimes give rise to a reading on which apparently only one of them is interpreted. The sentence in (6) contains a modal verb and a modal adverb that both express possibility. It can be interpreted either surface-compositionally with one modal operator in the scope of another (doubly modal reading in (6-a)), or as if there was just one modal element present (modal concord reading in (6-b)).
(6) You may possibly be familiar with my story.
a. 'It is possible that you are allowed to be familiar with my story.'
doubly modal reading
b. 'It is possible that you are familiar with my story.'
modal concord reading, standard view
No matter if the cancellation happens in syntax or in semantics, ruhig is interpreted as a test on whether it co-occurs (locally) with a modal verb of possibility. More recently, Grosz (2009b) argues that modal concord does not amount to a simple cancellation of one of the modal elements, but that they jointly express a high degree of possibility (or necessity). On this view, the modal concord reading has to be paraphrased as in (7).
(7) 'It is very possible that you are familiar with my story.'
modal concord reading, gradable modality view
ruhig is thus claimed to - roughly - turn 'possible' into 'very possible'. It is not entirely clear to me if this captures the intuitive 'no worries'-meaning of the particle. Yet, my main objection against a treatment in terms of modal concord is that the restriction of co-occurrence with a possibility modal is too strong. Before going into that, I would like to point out two issues that have to be added independently to the modal concord approach.

### 2.2 Addenda for modal concord

First, ruhig can never co-occur with epistemic possibility modals.
(8) \#Dieser Student könnte ruhig Peter sein.
this student could Ruhig Peter be
intended: 'This student could be Peter, no worries.'
It seems that ruhig can only occur with modals that express possibility with respect to preferences or goals (deontic or teleological modality, cf. Kratzer 1981).

Second, ruhig does not occur in interrogatives, even if they contain a possibility modal of the right flavor:

4 Particle ruhig
(9) \#Kannst du ruhig weiterschlafen?
can.2SGInd you Ruhig sleep.on
Principles that take care of these two observations can easily be added to the modal concord analysis. Yet, we will see that the analysis faces independent problems. The alternative analysis in section 3 offers a straightforward account of the incompatibility of ruhig with epistemic modality, as well as its absence from interrogatives.

### 2.3 Problems with modal concord

A question of modal force Grosz (2009a,2009b) claims that ruhig can never appear with necessity modals. Yet, ruhig often occurs with the modal verb soll (roughly 'shall'/'should') as well as in imperatives. Both are not standardly assumed to constitute or contain possibility modals. soll is usually considered a necessity modal (Kratzer 1981), but this is not undisputed: Ehrich (2001) argues that soll is truly ambiguous and is, on its weak reading, interpreted as a possibility modal. ${ }^{3}$ For the presence of a modal operator in imperatives, Grosz draws on Schwager (2006), who argues that imperatives contain an operator that is interpreted like a necessity modal, so:

Go home! $\approx$ You should go home!
This forces her to give a pragmatic account of permission-imperatives, i.e. imperatives that seem to constitute less an effort to get the addressee to do something, but rather open up the possibility for him to do so.

Take a cookie (if you like).
a. $\quad$ 'You can take a cookie (if you like).'
b. $\not \approx$ 'You should take a cookie (if you like).'

Schwager (2006) argues that this effect can and should be dealt with in pragmatics (cf. also Portner 2007). ${ }^{4}$ In contrast, Grosz argues that the modal operator in imperatives is semantically ambiguous between possibility and necessity. Moreover, for sollen, he argues that it passes Horn's (1972) tolerance test. Conjunctions of possibility modals with contradictory prejacents (cf. (12-a)) give rise to consistent modal states of affairs, while conjunctions of necessity modals with contradictory prejacents (cf. (12-b)) give rise to contradictory states of affairs.
(12) a. You may A and you may $\neg \mathrm{A}$.

[^117]b. \#You have to A and you have to $\neg \mathrm{A}$.

According to Grosz (2009a), soll can behave like a possibility modal. This is contradicted by the data in Ehrich (2001) as well as the judgments of all ten native speakers I consulted. ${ }^{5}$ Grosz does not test imperatives, but they fail likewise, cf. (13-a). This cannot be blamed on the performativity of the imperative: explicit performatives that constitute permissions pass the test as expressions of possibility, cf. (13-b). (For more natural utterances, with $B \subseteq \neg A$.)
a. \#Come in by the front door and come in by the back door (it's up to you, really).
b. I hereby allow you to come in by the front door, and I hereby allow you to come in by the back door.

The German equivalents of (13-a) and (13-b) behave analagously.

Absence of modal operator On closer examination, ruhig can even occur in sentences that do not seem to contain any modal operator at all. First, consider the free relative in (14): there is no modal verb and both finite verbs are marked present indicative.
(14) Wer also eines der Hefte haben will, who therefore one of.the booklets wants.Presind, writes.Presind schreibt ruhig schon mal eine Email.
Ruhig already Prt an email
'Who wants to have one of the booklets should simply write an email.'
Second, ruhig often occurs in subsentential constituents that are inserted in parenthesis and spell out how the details of a particular plan (presented in present indicative) could be filled out.

> Du gehst einfach zu O2 (ruhig schon 2 Wochen bevor you go.PresInd simply to O2 (RUHIG already 2 weeks before dein Vertrag abläuft), schilderst denen das, dann your contract expires), explain.PRESInd to.them that, then geht das mit der Rufnummernmitnahme. works.PRESIND that with the take-number-with-you
'You simply go to [the mobile phone company] O2 (Ruhig already 2 weeks before your contract expires), you explain it to them, and they'll let you keep your number.' [google]

[^118]Third, ruhig occurs in unmodalized declaratives that set up a plan for joint action:
Weißt du was? Du gehst jetzt ruhig schon mal in
know you what? you go.PRESIND now RUHIG already Q-PART in
den Speisewagen, und ich komm nach, sobald der
the dining-car and I come.PRESIND VPART as-soon-as the
Schaffner die Tickets kontrolliert hat.
conductor the tickets controlled has
'You know what? (We do the following:) you go to the dining car and I
follow you as soon as the conductor has controlled the tickets.'

Intermediate conclusions The distributional restrictions of ruhig cannot be explained in terms of modal concord with a possibility modal. ruhig occurs both with necessity modals and in the absence of modal operators as long as the sentences in question are used to guide future action. ${ }^{6}$ This suggests that we should draw on the speech act theoretic side of the restriction. The idea is to endow ruhig with suitable restrictions on the speech act types/updates that can be performed with an utterance that contains the particle. The form restriction is then derived indirectly: sentences that cannot contain ruhig (e.g. muss-modalized ones) are sentences that cannot perform an update of the required type. To provide a formal account along these lines we have to bring together the semantics assigned to modalized declaratives with global notions relevant for speech acts (action alternatives, criteria for decision, ...). This is not without challenge as in particular: non-epistemic - modal verbs are standardly interpreted pointwise.

## 3 Modeling utterance contexts for ruhig

### 3.1 Conditions on ruhig

I introduce a simplified notion of an utterance context with a decision problem as a quadruple $C=\left\langle s_{c}, a_{c}, C S_{c}, A^{x}{ }_{c}\right\rangle$ where $s_{c}$ is the speaker, $a_{c}$ is the addressee, $C S_{c}$ Stalnaker's $(1978,2002)$ context set, i.e. the set of worlds compatible with mutual joint belief of $s_{c}$ and $a_{c} . A_{c}^{x}$ is a set of possible future courses of events (here, a set of propositions) that constitute a salient decision problem for some agent(s) $x$. Moreover, $C S_{c}$ determines a set of criteria $K_{c}$ that are known to constitute $x$ 's criteria for deciding among $A_{c}^{x}$. Given a precontext $C$, update with an utterance $\phi$ (written $C+\phi$ ) results in a postcontext $C^{\prime}=\left\langle s_{c^{\prime}}, a_{c^{\prime}}, C S_{c^{\prime}}, A_{c^{\prime}}^{x}\right\rangle$, where $s_{c^{\prime}}=s_{c}, a_{c^{\prime}}=a_{c}, A_{c^{\prime}}^{x}=A_{c}^{x}$, and $C S_{c^{\prime}}=C S_{c} \cap \llbracket \phi \rrbracket^{c}$ iff $\llbracket \phi \rrbracket^{c}$ is defined. ${ }^{7}$

[^119]Solving the decision problem means to establish a single $\alpha \in A_{c}^{x}$ as optimal. An action $\alpha$ is optimal in $C$ iff it is optimal at all worlds in $C S_{c}$. Optimality at a given world is spelt out in terms of Kratzer's (1981) framework of graded modality that relies on two parameters,

- a modal base, e.g. $f: W \rightarrow(W \rightarrow T)$ that assigns to $w$ the set of propositions describing the relevant circumstances, and
- an ordering source, e.g. $g: W \rightarrow(W \rightarrow T)$ that assigns to $w$ the set of propositions consituting the relevant preferences.
$g$ induces the partial-order $<_{g(w)} \subseteq W \times W$ ('strictly better') in (17-a). Under the assumption that $g$ is always finite, this allows us to define the set of optimal worlds w.r.t. $w, f$, and $g$ as in (17-b):
a. For all worlds $w_{i}, w_{j}: w_{i}<_{g(w)} w_{j}$ iff $\left\{p \in g(w) \mid p\left(w_{j}\right)\right\} \subset\left\{p \in g(w) \mid p\left(w_{i}\right)\right\}$
b. The optimal worlds in $w$ w.r.t. circumstances $f$ and wishes $g$ : $O(f, g, w):=\left\{w_{1} \in \bigcap f(w) \mid \neg \exists w_{2} \in \bigcap f(w): w_{2}<_{g(w)} w_{1}\right\}$
As usual, can and must express compatibility and entailment w.r.t. $O(f, g, w)$. The pointwise notion of optimality can also be used to define optimality in a context $C$. For this, the relevant ordering source is fixed as $g_{c}=\lambda w \cdot \lambda p \cdot p \in K_{c}$. Moreover, in deciding one has to take into account all possibilities the world could be like, therefore, as a modal base, we use $f_{c}=$ ' $\lambda w$.the relevant circumstances in $w^{\prime}$, where $\bigcup_{w \in C S_{c}} \cap f_{c}(w)=C S_{c}$.
a. An action $\alpha \in A_{c}^{x}$ is optimal in context $C$ iff $\left(\forall w \in C S_{c}\right)\left[O\left(f_{c}, g_{c}, w\right) \subseteq \alpha\right]$.
b. An action $\alpha \in A_{c}^{x}$ is locally optimal in context $C$ iff $\left(\forall w \in C S_{c}\right)$

$$
\left[\left(\exists w_{i} \in \bigcap f_{c}(w) \cup \alpha\right)\left[\left(\forall w_{j} \in \bigcap f_{c}(w)\right)\left[w_{j}<_{g_{c}(w)} w_{i} \rightarrow \alpha\left(w_{j}\right)\right]\right]\right.
$$

ruhig occurs in contexts $C$ where $K_{c}$ does not suffice for $x$ to resolve the issue of what course of events to chose from $A_{c}^{x}$. This lack of an optimal candiate can be due to a lack of knowledge about the facts or to conflicting preferences in $K_{c}$. The requirements of ruhig are spelt out by making it a partial identity function on the set of proposition that returns its complement $\alpha_{s t}$ iff it occurs in a sentence $\phi$ whose LF is a sequence $\left[\psi_{1}[\operatorname{ruhig}[\alpha]] \psi_{2}\right]$ (with $\psi_{1}$ and $\psi_{2}$ possibly empty) and $C+{ }^{'} \psi_{1} \alpha \psi_{2}{ }^{\prime}=C^{\prime}$ s.t.: ${ }^{8}$

[^120]a. $\quad \alpha \in A_{C}^{x}$ and $\alpha \in A_{c^{\prime}}^{x}$
b. $\quad \alpha$ is locally optimal in $C$
c. $\quad \alpha$ is optimal in $C^{\prime}$

We can now see why ruhig occurs in permissions: permitting $\alpha$ requires that the addressee is (taken to be) interested in realising $\alpha$, but also in not violating the rules (Searle 1969). Therefore, as long as either, $\alpha$ is prohibited, or it is unkonwn if $\alpha$ is prohibited, $\alpha$ cannot be optimal. An utterance like (20) (without ruhig) rules out worlds at which following the rules and having a cookie are incompatible. This is why ruhig is acceptable.

Du kannst dir von mir aus ruhig ein Keks nehmen. you can yourself by me of Ruhig a cookie take
'You can take a cookie, no worries.'

In the absence of ruhig, the possibility modal could also be understood teleologically, and would then express a trivial truth: if we evaluate it at $w^{\prime}$ s.t. having a cookie is permitted, the best worlds are worlds where the addressee has a cookie and follows the rules. If we evaluate it at $w^{\prime \prime}$ s.t. having a cookie is prohibited, the best worlds are partioned into ones where she has a cookie (but violates the rules) and ones where she follows the rules (but doesn't have a cookie). Therefore, at both $w^{\prime}$ and $w^{\prime \prime}$, the optimal worlds have a non-empty intersection with having a cookie. The update does not eliminate any worlds, therefore $C S_{c}=$ $C S_{c^{\prime}}$, taking a cookie is not globally optimal in $C^{\prime}$ and ruhig is not licensed. Although it is not absolutely clear what governs the interpretation of contextual parameters of modal verbs (we can think of them as of covert pronouns), the pressure for a consistent interpretation is clearly a deciding factor. From this it follows immediately that, while ruhig does not tinker with the truth-conditions themselves, it can in many contexts help to trigger a particular ordering source (here, speaker deontic rather than hearer teleological). ${ }^{9}$ Updates that constitute recommendations, plans and suggestions work slightly differently. For reasons of space I cannot discuss further examples. ${ }^{10}$

[^121]
### 3.2 The must-problem

Besides sentences containing kann 'can', also those containing soll 'shall' or imperatives can give rise to the required update effect, in particular when occurring in recommendations. Consider a scenario described by Grosz: a cable car is about to depart. A passenger wants to use the restroom, but is insecure if he can make it back in time. The conductor issues (21):

$$
\begin{align*}
& \text { Gehen Sie ruhig noch auf die Toilette! }  \tag{21}\\
& \text { go.Imp you.Polite Ruhig still to the toilet } \\
& \text { 'Just go to the restroom (if you like).' }
\end{align*}
$$

Apparently, $C S_{c}$ contains worlds $w$ ' where the preference 'go to the toilet' is compatible with the goal 'reach the cable car', and worlds $w^{\prime \prime}$ where this is not so. By saying that all the optimal worlds according to the circumstances and preferences verify that the addressee goes to the toilet, the speaker rules out worlds at which the two events are incompatible. Clearly, in the post-, but not in the precontext going to the toilet has the status of a globally optimal action. Given that this ruhig-permissible update was achieved by a necessity modal, why is it that it could not be achieved by a sentence containing must? In principle, two lines of reasoning suggest themselves, both of which have to do with the question what (kind of) ordering sources are involved. First, von Fintel \& Iatridou (2008) point out that weak necessity modals like ought and should (historical subjunctives) differ from strong necessity modals like must in that they involve two ordering sources of different status. Loosely speaking, one of them is not actually binding, but only counterfactually. This idea merits closer investigation. Second, Ninan (2005) considers must inherently performative ${ }^{11}$ because it is infelicitous with follow-ups that indicate that the particular necessity will not be respected:

$$
\text { (22) } S a m\{\# m u s t, \text { has to }\} \text { go to confession; but he won't go. }
$$

This contrast could also be accounted for if we require that must comes with an ordering source $g$ that is considered 'binding' ( $C S_{c}$ entails that all $g$-optimal events will be realised). In contrast, ruhig seems to require an ordering source for which it is not granted that it is being followed (e.g. the speaker's rules in the cookie case, the hearer's preferences in the cable car case). A satisfactory implementation of this, as well as an answer to why imperatives and sollen 'should' are nearly but not fully interchangable, have to await further insight into the nature of modal bases, and, in particular, ordering sources.

## 4 Conclusions

I have argued that the German modal particle ruhig imposes both formal and functional restriction on its contexts of occurrence. On the one hand, it has to

[^122]combine with the description of a possible future course of events $\alpha$ s.t. $\alpha$ belongs to a set of contextuall given alternatives. On the other hand, ruhig has to occur in a sentence that gives rise to an update that renders $\alpha$ a globally optimal choice. Some of the problems discussed show that we need a better understanding of the parameters involved in the standard Kratzer semantics for modality.

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# German noch so: Scalar Degree Operator and Negative Polarity Item* 

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## 1 Introduction

An approach pioneered by [1] relates polarity sensitivity to semantic triviality. [2], [3], and [4] let unlicensed negative polarity items (NPIs) yield contradictory presuppositions or implicatures. In these proposals, an NPI requires the asserted proposition to be stronger, or less likely, than certain alternative propositions. This requirement is designed to be satisfiable in licensing contexts only.

The present paper describes a problem for applying such a contradiction based anlaysis to the German expression noch so, a polarity sensitive degree operator. It is first shown that under standard assumptions about gradable predicates and degree operators, a contradiction based account is straighforward to state. It merely requires a minor innovation concerning the nature of alternative propositions: where in previous work propositions are generated by alternative predicates or domains restrictions, noch so invokes propositions generated by alternative degrees.

However, while such a contradiction based account helps derive polarity sensitivity of noch so, it is shown not to capture the contribution to meaning it makes in cases where it is licensed. An alternative analysis is presented, designed to capture this contribution. This analysis, however, does not without further assumptions derive polarity sensitivity. Ways of reconciling the requirements imposed by the distribution of noch so and its perceived contribution to meaning are discussed, although with no conclusive outcome.

## 2 Some properties of noch so

Noch so is a degree operator. It shares a signature distributional restriction with familiar comparative, equative or superlative morphemes: as (1) and (2) illustrate, noch so can combine with a gradable predicate such as lang 'long', but not with nongradable predicates such as zweiköpfig 'two-headed'.

[^123](1) Peter hatte vor keiner [noch so lang.en] Schlange Angst. Peter had of no NOCHSO long.infl snake fear 'Peter wasn't even afraid of any LONG snake.'
(2) \#Peter hatte vor keiner [noch so zweiköpfig.en] Schlange Angst. Peter had of no NOCH SO two-headed.infl snake fear

Noch so is also "scalar". As the translation in (1) indicates, noch so sentences allow for paraphrases containing the scalar particle even. ${ }^{2}$ Finally, noch so is a NPI. In (1), noch so appears in the restrictor of the downward entailing determiner kein 'no'. Example (3), where upward entailing einige 'some' replaces kein, is unacceptable.
(3) *Peter hatte vor einigen [noch so lang.en] Schlangen Angst.

Peter had of some NOCH SO long.infl snakes fear
Also, (4) and (5) show that noch so can appear in the scope of downward entailing keiner 'no one', but not in the scope of upward entailing jeder 'everyone'.
(4) Keiner hat ein [noch so lukrativ.es] Angebot angenommen. no one has a NOCH SO lucrative offer accepted
'No one even accepted a LUCRATIVE offer.'
(5) *Jeder hat ein [noch so lukrativ.es] Angebot angenommen. everyone has a nOCH SO lucrative offer accepted

Building most directly on [4], the following explores how, under standard assumptions about gradable predicates and degree phrases, the polarity sensitivity of noch so can be derived from its scalarity.

## 2 A Contradiction Based Account

The scalarity of certain polarity items is exploited in several existing accounts of polarity sensitivity (e.g. [4], [5], [6], [7]). Most relevant here is Lahiri's work [4], where the scalarity of certain NPIs in Hindi is argued to yield contradictions in upward entailing contexts. This section formulates a Lahirian analysis of noch so.

### 2.1 Gradable predicates, degree phrases, and monotonicity

In a standard view (e.g. [8], [9]), gradable adjectives relate individuals to degrees under an at least semantics. According to (6), for example, the denotation of lang maps a degree d and individual x to the proposition that x 's length is at least d .

[^124][^125]Given such lexical meanings, degree phrases, including noch so, can be considered generalized quantifiers over degrees, which for interpretabilty move covertly from the adjective's degree argument position to combine with a derived degree property (cf. [9]). In this approach, (7) and (8) are conceivable logical forms for (3) and (1).
(7) noch-so $\lambda \mathrm{d}[$ Peter hatte vor einigen [d langen] Schlangen Angst ]
(8) noch-so $\lambda \mathrm{d}[$ Peter hatte vor keiner [d langen] Schlange Angst ]

The at least semantics in (6) ensures that the degree property denoted by the lambda abstract in (7) is downward monotone in the sense of (9) below (cf. [8]). That is, propositions to which it maps higher degrees entail propositions to which it maps lower degrees. If Peter is afraid of some snakes whose length is 60 cm or more, then he is also afraid of some snakes whose length is 50 cm or more.
(9) P is downward monotone $: \Leftrightarrow \forall \mathrm{d}_{1}, \mathrm{~d}_{2}\left[\mathrm{~d}_{1} \leq \mathrm{d}_{2} \rightarrow\left[\mathrm{P}\left(\mathrm{d}_{2}\right) \subseteq \mathrm{P}\left(\mathrm{d}_{1}\right)\right]\right]$
(10) P is upward monotone $: \Leftrightarrow \forall \mathrm{d}_{1}, \mathrm{~d}_{2}\left[\mathrm{~d}_{1} \leq \mathrm{d}_{2} \rightarrow\left[\mathrm{P}\left(\mathrm{d}_{1}\right) \subseteq \mathrm{P}\left(\mathrm{d}_{2}\right)\right]\right]$

In contrast, the degree property denoted by the lambda abstract in (8) is upward montone in the sense of (10). It maps lower degrees to propositions that entail propositions to which it maps higher degrees. If Peter is not afraid of any snake that is 50 cm long or more, then he is also not afraid of any snake that is 60 cm long or more.

### 2.2 Even ONE

Entries like (6) invite an analysis of the polarity sensitivity of noch so in the spirit of [4]. [4] deals with Hindi, but English even ONE makes much the same point, participating in contrasts like the one between (11) and (12).
(11) *Even ONE student called.
(12) Not even ONE student called.

Following [10], [4] assumes that a scalar particle triggers the presupposition that the sentence minus the scalar particle expresses a proposition which is less likely than all relevent alternative propositions. In the case at hand, alternatives are obtained by replacing the focused numeral one with alternative numerals two, three, etc. Under an at least semantics for numerals, (11) is then predicted to presuppose that the proposition that one ore more students called is less likely than the proposition that two or more students called, etc. But this presupposition is contradictory. The asserted proposition is entailed by each of its alternatives, and so it has to be at least as likely as any of them. So the unacceptability of (11) can be credited to a necessarily false presupposition.

The contradiction is correctly predicted to dissipate in (12), where negation reverses the direction of entailment. The prejacent proposition now entails each of its alternatives, making it possible for it to be less likley than each of them, hence rendering the scalar presupposition satisfiable.

### 2.3 Noch so and contradictory scalar presuppositions

Assuming an at least semantics for gradable adjectives, the scalarity of noch so invites a straighforward Lahirian analysis of its polarity sensitivity. The entry in (13) lets noch so impose a condition on the common ground comparing propositions obtained by applying its degree property argument to different degrees.
(13) noch-so $\phi$ presupposition: $\forall \mathrm{d}_{1}, \mathrm{~d}_{2}\left[\mathrm{~d}_{1}<\mathrm{d}_{2} \rightarrow|\phi|\left(\mathrm{d}_{1}\right) \ll_{c}|\phi|\left(\mathrm{d}_{2}\right)\right]$
$\mathrm{p} \ll_{c} \mathrm{q}$ conveys that p is less likley than q relative to the common ground c . So (13) requires that the degree property argument of noch so maps higher degrees to contextually likelier propositions than lower ones.

This condition has the intended effect for (3). Recall that the degree property expressed by the lambda abstract in (7), is downward montone: propositions for higher degrees entail propositions for lower degrees. Given this, the presupposition that (13) assigns to (7) is necessarily false, again because a proposition is bound to be at least as likely, in any context, as any proposition entailing it. The unacceptability of (3) can be credited to this contradiction.

In contrast, no offending presupposition is predicted for (1). Recall that in the logical form (8), the lambda abstract denotes an upward monotone degree property, with propositions for lower degrees entailing propositions for higher degrees. As a consequence, the presupposition triggered according to (13) is consistent and (1) is correctly expected to be acceptable. The Lahirian analysis, then, offers a straightforward account of the polarity sensitivity of noch so.

It will be useful to also consider a minor variant of this account. The entry in (13) follows [4] in the assumption that scalar implications compare the (contextual) likelihood of propositions. This view goes back to the analysis of even in [10]. In an alternative approach, taken in [11], even compares propositions in terms of (contextual) semantic strength or informativity. In fact, [2] presents a general perspective on NPI licensing that is based on [4] but substitutes informativity for likelihood as the semantic relation operative in scalar implications. With that substitution, (13) becomes (14), where $\mathrm{p} \subset_{\mathrm{c}} \mathrm{q}$ conveys that p asymmetrically entails q relative to the common ground c , that is, $\mathrm{p} \cap \mathrm{c} \subset \mathrm{q} \cap \mathrm{c}$.
(14) noch-so $\phi$ presupposition: $\forall \mathrm{d}_{1}, \mathrm{~d}_{2}\left[\mathrm{~d}_{1}<\mathrm{d}_{2} \rightarrow|\phi|\left(\mathrm{d}_{1}\right) \subset_{c}|\phi|\left(\mathrm{d}_{2}\right)\right]$

Entry (14) also supports a contradiction based account of the polarity sensitivity of noch so, and even more straightforwardly so than (13). The condition is obviously contradictory in (7), where the degree property is downward monotone. Evidently, no proposition can be asymmetrically entailed, in any context, by a semantically weaker proposition. Again, the contradiction is avoided in (8), where the degree property is upward monotone. ${ }^{3}$

[^126]
## 3. When scalar presuppositions are too weak

While the conditions in (13) and (14) derive the polarity sensitivity of noch so, the question is whether they correctly characterize the meaning of acceptable noch so examples such as (1).

Note that the degree property in (8) is not merely upward monotone but moreover strictly upward monotone in the sense of (15). That is, it maps lower degrees to (strictly) stronger propositions than higher degrees. ${ }^{4}$
(15) P is strictly upward monotone $: \Leftrightarrow \forall \mathrm{d}_{1}, \mathrm{~d}_{2}\left[\mathrm{~d}_{1}<\mathrm{d}_{2} \rightarrow\left[\mathrm{P}\left(\mathrm{d}_{1}\right) \subset \mathrm{P}\left(\mathrm{d}_{2}\right)\right]\right]$

As a consequence, it does not take much for (8) to satisfy the condition in (14), which requires strict upward montonicity under common ground assumtions. For the condition not to be met, the context would have to obliterate the asymmetric entailment between some or all relevant propositions, rendering them contextually equivalent. This would be the case, for example, if the common ground entailed that Peter either was afraid of all snakes (of all lengths) or was not afraid of any snakes (of any lengths). A felicitous use of (1) should merely require that no such assumption is established.

More formally, asymmetric entailment between propositions p and q is obliterated in common ground c if $\mathrm{p} \cap \mathrm{c}=\mathrm{q} \cap \mathrm{c}$ despite $\mathrm{p} \subset \mathrm{q}$. The condition that no such obliteration obtains is the requirement that c contain a possible world where q is true while p is false, for all propositions p and q of the relevant form. It is worth noting that this condition is not a presupposition in the usual sense. Ordinarily, if a sentence is said to presuppose a proposition p , this is understood as the requirement that the common ground entail p (e.g. [13]). In the case at hand, in contrast, the common ground is required not to have certain entailments.

The situation is much the same if the condition in (13) is assumed instead of (14). If, as seems plausible, greater (contextual) semantic strength is a sufficient condition for lesser (contextual) likelihood, then (13) too is guaranteed to be satisfied in (8) unless the common ground contains assumptions rendering some or all of the relevant propositions contextually equivalent. ${ }^{5}$

To be sure, these predictions do not square well with the actual interpretation of (1). A felicitous utterance of the sentence does certainly not require that assumptions of any kind not be established in the conversation. Nor is it consistent with intuitions that the absence of established assumptions of any sort could be a sufficient condition for a felicitous use of the sentence.

[^127]Instead, an utterance of (1) is judged to introduce a scalar implication similar to the one associated with the (merely approximate) English translation given: it suggests that fear of shorter snakes is less likely, or perhaps entails, fear of longer snakes.

This type of scalar implication is even more salient in (16), where kein 'no' is replaced by (equally downward entailing) jeder 'every'. In this case, a scalar implication is perceived that is diametrically opposed to default assumptions on how fear of snakes might relate to their length. Implausibly, (16) suggests that fear of longer snakes is less likely, or entails, fear of shorter snakes.
(16) \#Peter hatte vor jeder [noch so lang.en] Schlange Angst. Peter had of every NOCH SO long.infl snake fear 'Peter was even afraid of every LONG snake.'

Replacing lang 'long' in (10) with (equally gradable) teuer 'expensive' has a similar effect. (17) implies that fear of snakes that cost less is less likely, or entails, fear of snakes that cost more. Since it is hard to see how a snake's price could have any bearing on its potential to induce fear, the implication is again implausible.
(17) \#Peter hatte vor keiner [noch so teuer.en] Schlange Angst.

Peter had of no NOCH SO expensive.infl snake fear
'Peter was even afraid of every EXPENSIVE snake.'
It is worth noting that the contradiction based accounts given above are correct in one respect: scalar implications are indeeed presuppositions. This, at least, is what their projection behavior suggests. For example, scalar implications are judged to survive embedding under the modal adjective möglich 'possible', and the plausibility contrasts described above persist under such embedding.

Having confirmed that noch so triggers a presupposition, it remains to determine its content, generalizing from the examples presented in this section.

## 4 Presupposing downward montonicity

The observations reported in the last section suggest that the correlation between the ordering of degrees and likelihood or informativity of propositions is roughly the reverse of what contradiction based accounts would posit. Settling on informativity as the relevant semantic notion, an entry like (18) suggests itself.
(18) noch-so $\phi$ presupposition: $\forall d_{1}, \mathrm{~d}_{2}\left[\mathrm{~d}_{1}<\mathrm{d}_{2} \rightarrow|\phi|\left(\mathrm{d}_{2}\right) \subseteq \subseteq_{\mathrm{c}}|\phi|\left(\mathrm{d}_{1}\right)\right]$

Here $\mathrm{p} \subseteq_{\mathrm{c}} \mathrm{q}$ conveys that p entails q relative to the common ground c , that is, $\mathrm{p} \cap \mathrm{c} \subseteq$ $\mathrm{q} \cap \mathrm{c}$. Using established terminology, (18) requires that the degree property in question is downward monotone under common ground assumptions.

Assuming as before that noch so must outscope its licenser, the entry in (18) makes sense of the observations reported in the last section. According to (18), the logical form of (1) in (8) presupposes that Peter's not being afraid of any longer snakes
entails his not being afraid of any shorter snakes, which is plausible enough. The corresponding logical forms for (16) and (17), shown in (19) and (20), are assigned less plausible presupposition, viz. that Peter's being afraid of all longer snakes entails his being afraid of all shorter snakes, and that Peter's not being afraid of more expensive snakes entails his not being afraid of less expensive ones.
(19) noch-so $\lambda \mathrm{d}[$ Peter hatte vor jeder [d lang.en] Schlange Angst ]
(20) noch-so $\lambda \mathrm{d}[$ Peter hatte vor keiner [d teuer.en] Schlange Angst ]

Similarly, (18) seems to apply correctly to example (4) above. The presupposition assigned to the logical form in (21) is that no one accepting a more lucrative offer entails no one accepting a less lucrative offer. Again, this presupposition is rather plausible and fits with intuitions on what the sentence conveys.

## (21) noch-so $\lambda \mathrm{d}$ [ keiner hat ein [d lukrativ.es] Angebot angenommen]

Intuitions on meaning, then, suggest that the condition in (18) is on the right track. Moreover, this condition turns out to derive a distributional constraint on noch so not mentioned so far. While noch so is correctly characterized as a NPI in so far as it must occur in a downward entailing context, noch so is subject to an additional distributional restriction that it does not share with more familiar NPIs. Consider (22).
(22) *Kein Gedicht ist noch so lang. no poem is NOCH SO long

This case is structurally similar to the acceptable sentence in (4), the only relevant difference being that the adjective phrase hosting noch so is a modifier in (4) but the main predicate in (22). Why would this difference matter?

Under (18), a semantic explanation of the contrast becomes available. According to (18), the logical form of (22) in (23) presupposes that, if there is a given length that no poem reaches, then no poem reaches a lesser length either.
(23) noch-so $\lambda \mathrm{d}[$ [kein Gedicht] ist d lang]

This scalar presupposition is in obvious conflict with the assumptions that every poem has some length or other and that there are lengths that no poem reaches. ${ }^{6}$ The former assumption can in fact be considered another presupposition of the sentence: degree predicates can be assumed to only be defined for individual arguments in the domain of the underlying measure function (e.g. [14]); hence the denotation of lang will only be defined for individuals who have a length, and this presupposition is expected to project universally in (23). So the unacceptability of (22) can be blamed on inconsistent presuppositions.

This type of inconsistency is expected to be avoided in the otherwise similar case in (4). After all, while every poem necessarily has some or other length, it is not necessary for every, or any, person to have accepted a more or less lucrative offer.

[^128]Likewise, no inconsistency is expected to arise in (1), as it is not necessary for Peter to have fear of any snakes. Examples (24) and (25) further illustrate the point.
(24) *Kein Student war [noch so vorsichtig]. no student was NOCH SO tentative
(25) Kein Student hat sich [noch so vorsichtig] beschwert. no student has self NOCH SO tentatively complained 'No student complained even TENTATIVELY.'

This contrast is again expected. While (24) is expected to presuppose that every student was tentative (to some degree), (25) clearly does not presuppose that every student complained (with any degree of tentativeness).

## 5 Back to polarity sensitivity

The discussion in the last section continued to assume, without much comment, that noch so is a NPI that must outscope its downward entailing licenser. The question is whether the current analysis provides a rationale for this requirement. Another open question concerns the truth conditional content of noch so. These two related issues are addressed below, although with no conclusive outcome.

In the account explored here, a noch so sentence presupposes that the degree property combining with noch so is downward monotone under common ground assumptions. But, unless noch so scopes over a non-upward entailing operator, the relevant degree property is guaranteed to be downward monotone, irrespectively of assumptions established in the common ground. So, unless noch so scopes over a nonupward entailing operator, the presupposition derived is tautologous.

It is tempting to relate this observation to the polarity sensitivity of noch so. However, it is not clear that a necessarily true presuppositions alone can be the source of unacceptability. After all, a sentence that carries no (non-tautologous) presupposition might still be informative by virtue of its asserted content. This the raises to salience a question skirted so far: what is the asserted content of a noch so sentence? The following briefly explores two options, concluding that neither is able to derive the polarity sensitivity of noch so.

Sentence (1) is judged to convey that Peter was not afraid of snakes of any lengths. Similarly, (4) conveys that none of them accepted any offer of any degree of lucrativity. This implication could be captured straightforwardly by making noch so a universal quantifier, as in (26).
(26) noch-so $\phi$ assertion: $\lambda \mathrm{w} . \forall \mathrm{d}[|\phi|(\mathrm{d})(\mathrm{w})=\mathrm{T}]$

One might hope that letting noch so quantifiy universally sheds light on its polarity sensitivity. In fact, (26) would render a sentence like (27) below contradictory, given that a poem's length is necessarily finite. Since the scale of length has no upper bound, the segment of the scale charcaterized by the relevant degree property in (23)
is guaranteed to be a proper subset of the scale of length, which contradicts the condition in (26).
(27) *Das Gedicht ist noch so lang. the poem is nOCH SO long

Much the same applies to the unacceptable case in (3). One might hope, then, that all cases of unlicensed noch so can be excluded on the grounds of being contradictory. Note that, in contrast to the contradiction based accounts discussed above, here the contradiction would be in the asserted, not the presupposed, content.

Unfortunately, such an explanation falls short of excluding all cases of unlicensed noch so. One case that (26) would not render contradictory is (28). Assuming that the scale of fullness contains a maximal degree (see e.g. [15]), (26) predicts (28) to merely convey that the glass was full. Similarly, the truth conditions that (26) assigns to (29) could be met if the relevant modal base fails to set an upper bound for the permitted length of the poem.
(28) *Das Glas war [noch so voll]. the glass was NOCH SO full
(29) *Das Gedicht darf [noch so lang] sein. the poem may noch so long be

The fact that (28) and (29) are neverthless no more acceptable than (27) suggests that the universal analysis is insufficient to derive the polarity sensitivity of noch so.

An alternative analysis makes noch so quantify over degree existentially as in (30), rather than universally.

## (30) noch-so $\phi$ assertion: $\lambda \mathrm{w} . \exists \mathrm{d}[|\phi|(\mathrm{d})(\mathrm{w})=\mathrm{T}]$

Note that (30) is still consistent with the intuition that acceptable noch so sentences quantify over degrees universally. Consider again (1) and the logical form in (8). There the degree property combining with noch so is necessarily upward monotone. Moreover, in order to satisfy the presupposition in (18), the degree property in (8) must also be downward monotone under common ground assumptions. According to (18), then, the degree property in (8) is presupposed to be either true of all degrees of length or false of all such degrees. So in conjunction with the scalar presupposition, the existential quantification in (30) acquires universal force.

Under the semantics in (30), a possible reason for the unacceptability of (27) is that it is tautologous at the level of both presupposition and assertion. As said, downward monotonicity of the relevant degree predicates guarantees satisfaction of the condition in (18). Under the assumption that every poem as some length, the existential condition is necessarily satisfied as well. Under (30), the examples in (28) and (29) arguably come out trivial as well. Perhaps, then, noch so must scope over a downward entailing licenser in order to avoid a trivially true interpretation.

Unfortunately, however, this rationale again does not extend to all examples of unlicensed noch so. Example (3) is a case in point. According to (30), the logical form in (7) has the contingent entailment that there are some snakes (of some length) that

Peter was afraid of. Similarly, (30) does not derive the contrast between (25) above and (31). Under (30), (31) should have the non-trivial entailment that some student complained.
(31) *Ein Student hat sich [noch so vorsichtig] beschwert. some student has self NOCH SO tentatively complained

As present, then, it is unclear whether the meaning contribution by noch so detectable in acceptable examples can help one derives the distribution of noch so.

## 6 Conclusion

This paper has identified a dilemma for the analysis of noch so. A contradiction based account of its distribution along the lines of [4] fails to account for its meaning in good cases. Conversely, an account that derives the perceived meaning of noch so does not seem to derive its polarity sensitivity. Hopefully future work will resolve the dilemma.

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# Some New Observations on 'because (of) ^^ 

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#### Abstract

Because (of) is ambiguous between a reason and a plain cause interpretation. Presenting a semantic analysis framed in Discourse Representation Theory, I argue that the two variants can be represented by an underspecified semantic representation involving a causal relation. After showing how the two interpretations are dependent on the ontological nature of the arguments of this causal relation, I point to a difference between sentential-complement because and nominal-complement because of with regard to their interaction with modals. Whereas both because and because of may outscope e.g. deontic necessity modals, only because may outscope epistemic modal operators.


## 1 Introduction: plain causes and reasons

Causal because (of) adjuncts are ambiguous between a reason and a plain cause interpretation as exemplified by the sentences in (1)-(2): ${ }^{1}$
(1) Reason:
a. The dog was put down because of its aggressiveness.
b. I picked out the painting because it matches my wall.

Plain cause:
a. Last winter, a homeless person died because of low temperatures.
b. The stunt plane crashed because it ran out of petrol.

In (1a), the complement of because of, its aggressiveness, is interpreted as (part of) the reason or motive of some agent for putting down the dog. Similarly in (1b), the picking out a specific painting is motivated by the fact that it matches the wall of the speaker. Assuming that because (of) introduces a causal relation, I will assume that what is caused in the case of the reason interpretation is an attitudinal state.

With regard to the plain cause interpretation in (2a), on the other hand, the complement of because of, low temperatures, is interpreted as the direct or

[^129]indirect cause of the death of the homeless person. ${ }^{2}$ Similar remarks apply for (2b). The plain cause interpretation emerges when the caused events is not under the control of an agent.

Despite its frequent occurence in the literature on causation in general, there exist surprisingly few formal analyses of sentential-complement because (Hara 2008, Johnston 1994, Kratzer 1998), and - to my knowledge - no such analyses of nominal-complement because of. Thus, one of the primary goals of this paper is to contribute towards a better understanding of the semantics of because (of) and a precisification of some of the factors which determine its interpretation. Accordingly, the paper consists of two main parts: I first provide a discourse representation theoretic analysis of because (of) which is more eleborate than previous ones, showing what a (uniform) account of the interpretational variation of because (of) must encompass. I then discuss some subtle differences between because and because of having to do with their interaction with deontic and epistemic modal operators.

The remainder of this paper is organized as follows: In Section 2, I present the semantics for because (of) including some thoughts on the lexical organization for the interpretational variants. In Section 3, I discuss some differences between the sentential and the nominal complement variants with regard to scopal interaction with modals. Section 4 concludes the paper and offers a brief outlook.

## 2 A DRT Semantics for 'because of'

The semantic analysis of because (of) is framed within the framework of Discourse Representation Theory (DRT, cf. Kamp \& Reyle 1993, van Genabith et al. to appear for an overview; cf. Kamp \& Roßdeutscher 1994, Solstad 2007 for a treatment of some aspects of event-based causality within DRT). Before turning to the semantic analysis, I would like to make some brief remarks on the relation between because and because of. Basically, I regard the two to make a very similar semantic contribution, representing them both by means of the same, underspecified semantics. The variation which may be observed (cf. Section 3) is due to the fact that because takes sentential, whereas because of takes nominal complements. I will however remain neutral with regard to the issue whether the preposition because of and the conjunction because may also be regarded to be one lexeme, only subject to morphosyntactic variation with respect to the realisation of their complement. When discussing the distributional differences with regard to modal operators mentioned above (cf. Section 3), this issue will be of some importance. ${ }^{3}$

[^130]

Fig. 1. DRS showing plain cause interpretation of because (of)

The main idea of my analysis of because (of) is that it introduces a causal relation and that the interpretational variance which can be observed with regard to plain cause or reason interpretations is determined by the ontological nature of the arguments which enter into this causal relation. As we will see below, a reason interpretation can - not very surprisingly - only occur if intentionality is present. However, we will also see that this feature alone is not sufficient to predict the interpretation of because (of).

Although approaching the semantics of because (of) from a different perspective than Kratzer (1998), who focuses on the interaction of (sententialcomplement) because with indefinites, I share with Kratzer the idea that the ambiguity of because (of) can be dealt with by means of a common underspecified semantic representation. However, it is an important objective of this paper to enrich the insights offered by Kratzer (1998) and e.g. Johnston (1994), showing more explicitly how the different interpretations of because (of) emerge.

I assume that because (of) always involves a causal relation between a causing fact (as introduced by its syntactic complement) and some caused entity, which may be a state, an event, an attitudinal or a modal state (corresponding to the syntactic phrase to which the PP is adjoined). I will first turn to the plain cause reading in (2a), repeated below for convenience:
(2a) Last winter, a homeless person died because of low temperatures.
As modifiers of predicates which designate states or unintentionally performed events, such as the anti-causative die, because (of) phrases can trivially only be interpreted as plain causes. In the case of (2a), a (simple) event (not involving intentionality) enters the causal relation as the caused entity. The semantics of (2a) is provided in the Discourse Representation Structure (DRS) in Figure 1 (ignoring tense and other issues not relevant to my present purpose). The causal relation introduced by because is printed in boldface as the topmost condition of the DRS. The causing fact of this relation occurs below this con-

[^131]dition. In the case of $(2 a)$, the fact $\mathbf{f}$ of the temperatures being low causes the event of dying, which is the only eventuality that can be modified by the because of phrase.

Before discussing the reason interpretation, let me make some brief remarks on the nature of the causing entity in the causal relation introduced by because (of). As stated above, this causing entity always needs to be of fact type. Informally, facts are taken to be true propositional entities involving existential quantification. Although this is certainly not wholly uncontroversial (Fine 1982, Kratzer 2002), it is a useful approximation that helps explain a number of distributional facts with respect to the possible arguments of nominal-complement because of. Since only very few nouns can be claimed to have referential arguments of fact type (possible exceptions include fact, circumstance among others, cf. Asher 1993), we expect the occurence of most nouns as complements of because of to be accompanied by a process of reinterpreting (Egg 2005) the referential arguments as a fact. Thus, the complement of because of will be subject to reinterpretation if the complement involves no predication of an appropriate type, cf. e.g. (3):
(3) People are telling us they are using the bus because of the gas prices.

In (3), the because of phrase cannot be adequately intepreted as simply saying that the fact that gas is priced causes people to take the bus. Rather, it is a particular quality of that price, very likely that it is high (or far above its normal level), which is the cause of people taking the bus. Comparing (3) with (4), it could be argued that event nouns do not necessarily call for any reinterpretation, intuitively. Still, I contend that also in this case, the eventive referential argument which is contributed by the noun, needs to be reinterpreted as a fact (involving existential quantification) when accident occurs as an argument of because of:
(4) The road is closed because of the accident.

Turning now to the reason interpretation of because (of), consider again the example in (1a), repeated below for convenience:
(1a) The dog was put down because of its aggressiveness.
In general, because (of) phrases are interpreted as reasons or motives in combination with intentional predicates such as put down. In this case, as can be seen from the DRS for (1a) in Figure 2, the discourse referent which enters the causal relation as the caused entity, is an attitudinal state $s_{\text {att }}$ of some agent $x$ (the argument of DO), which consists of an intention INT to put down the dog (van Genabith et al. to appear). ${ }^{4}$ Importantly, this analysis amounts to viewing reasons as caused attitudinal states. What is more, assuming the causative relation to be transitive, the fact f may also indirectly be seen as a cause of death.

[^132]

Fig. 2. DRS for reason intepretation of because (of)

The ambiguity of because (of) between the plain cause and reason interpretations is not directly derivable from the representations in Figures 1 and 2. In both figures, the (underspecified) relation CAUSE occurs. Ultimately, the above analysis needs to be complemented by an appropriate theory of causality which makes clear how a causal relation may be subject to interpretational variation depending on the ontological nature of its argument. Short of being able to present such a theory, I will, for the sake of simplicity, assume that this theory allows us to state meaning postulates specifying how the occurence of certain arguments in the causal relation leads to a difference in realisation of the causal relation. Thus, (5) should be taken to state that whenever an attitudinal stated is caused by a fact - the latter not being subject to any variation in the case of because (of) - the fact is a reason of the holder of the attitudinal state for being in whatever state this is:
(5) f CAUSE $s_{\text {att }} \Longrightarrow f$ REASON $s_{a t t}$

Having presented the basic characteristics of the plain cause and reason interpretations of because (of), I want to point at some data which show that the interpretational variation is not only dependent on the presence or absence of an agent capable of intentional action. Interestingly, the presence of intentionality is not enough to predict a reason interpretation of the because (of) phrase. Thus, in contexts involving modals expressing deontic necessity (6a), possibility (6b) or ability (not exemplified here), no reason interpretations are available. The because of phrases in (6) can only be interpreted as plain causes:
(6) a. The dog had to be put down because of its aggressiveness.
b. Because of the high crystallisation energies it is possible to measure the crystal growth in transdermal patches even at $25^{\circ} \mathrm{C}$.

Sentence (6a) can only be interpreted as saying that the aggressiveness of the dog caused the necessity to put it down. The because of phrase cannot target the attitudinal state associated with put down. There is no reading available for (6a) according to which it is necessary for the agent to put the dog down for the reason of the dog being aggressive (as opposed to it being three-legged, for instance). Since (6a) is identical to (1a) apart from the presence of the deontic necessity modal had to, it seems reasonable to make the modal responsible for the unavailability of the reason interpretation. As indicated by the DRS for (6a) in Figure 3, this is accounted for by assuming that in this case, the causal relation persists between the fact f and the modal state $\mathrm{s}_{[\mathrm{D}]}$ consisting of a deontic modal operator $[\mathrm{D}]_{\mathrm{MB}}$ (MB is short for modal base) which takes scope over the DRS for (1a) in Figure 2. The modal blocks access to the attitudinal state in its scope. Consequently, the map in (5) is not applicable in the case of Figure 3. The absence of a reason interpretation is seen to have its rationale in the observation that if something is necessarily the case, reasoning or motives are of no importance. Put differently, if an obligation pertains, it does so regardless of someone's attitudinal state.


Fig. 3. DRS representation of 'because of' outscoping a deontic necessity modal

So far, I have said next to nothing about the syntax of because (of). Unfortunately, I cannot go into details here, but it may be noted that the behaviour of because (of) in combination with deontic modals, not allowing a reason interpretation, seems to indicate that the assumptions in Johnston (1994) are not adequate for my purposes. Johnston assumes that because adjuncts (he does not discuss because of) have two possible adjunction sites, one at IP level and one at VP level. If this were the case, one should expect the excluded reason interpretation to be available e.g. in the case of (6a) after all, assuming that the VP level constitutes a position below any modal operators. Unless one wants to make use of any semantic filtering mechanism, I think it is fair to conclude that the semantic observations above suggest that it is more plausible that because (of) has a fixed adjunct position which is above not only VP, but also above any projections where (deontic) modals are introduced. The data which Johnston seeks to explain (having to do with the interaction between negation and because adjuncts) must thus be explained differently. In the next section, I will make some remarks on possible syntactic adjunction sites for because and because of adjuncts.

## 3 'Because of' vs. 'because' in Epistemic Modal Contexts

I claimed that the above observations are valid for both sentential-complement because and nominal-complement because of. However, there is one interesting aspect for which the two variants differ with respect to their possible interpretations. Consider the examples in (7), in which must should be interpreted epistemically:
(7) a. Bill must have gone back home because the jacket is missing.
b. Bill must have gone back home because of the missing jacket.

Whereas (7a) is ambiguous, (7b) is not. In (7a), the because phrase specifies either (i) Bill's reason or motive for going back home, parallel to (1a) as analysed in the DRS in Figure 2, or (ii) the speaker's reason (evidence) for inferring that Bill must have gone back home, i.e. the speaker sees that the jacket is missing and concludes from this that Bill must have gone back home. In (7b), however, only the former interpretation (i) is available for the because of phrase. Thus, although one might expect that if the complement of because (of) is a proposition-like fact, its semantics should principally be identical to that of because, the examples in (7) show that this cannot be the whole story.

Although the ambiguity of because in (7a) is well-known (cf. e.g. Sweetser 1990), the difference in interpretational possibilities displayed between (7a) and (7b) is not very well understood, which is partly due to the fact that nominalcomplement because of has not been the object of attention of any formal analyses. In fact, the only discussion of the contrast in (7) that I am aware of, is found in Degand (2000), which I will return to below. Admittedly, I do not have a final answer to why this difference shows up, either, but in what follows, I want to
point out how my analysis could be extended towards explaining the difference displayed in (7).

One possibility towards dealing with the data in (7) would be to assume that scopal differences with regard to different modal operators are involved in the varying behaviour in (7). Thus, one could assume that because and because of do display a difference in syntactic behaviour, despite their semantic parallels, where only because adjuncts may outscope epistemic modals. Thus, Degand (2000: p. 692) assumes that because of adjuncts appear at an "intra-clausal" level where no epistemic modal operators are available. On the other hand, because clauses are adjoined at an "inter-clausal" level, where epistemic operators may be embedded under the causal relation introduced by because. Related to this take on the problem, it is also imaginable to say that what matters for the difference is the possibility of modifying speech act operators, as discussed by Scheffler (2005), thus making a parallel to Austin's (1961) famous biscuit conditionals (cf. e.g. Siegel 2006 and Predelli 2009 for discussion). In this case, because would unite the split behaviour of German denn and weil, the latter of which does not allow an the evidential reading in (7a). The matter is not quite clear to me though, since the evidential interpretation in (7a) seems intuitively different from the "biscuit causal" in (8):
(8) What are you doing tonight, because there's a good movie on. (Sweetser 1990: p. 77)

A last possibility towards explaining the difference in (7) that I would like to mention is exploiting the categorical difference between the complements of because and because of: On this view, only the (syntactically) clausal complements of because and no DPs such as the complements of because of may be interpreted evidentially as it would be needed for the reading which (7b) lacks. This could be connected to the process of reinterpretation which is involved in the case of nominal-complement because of. According to this view, the proposition-like reinterpretation of the complement of because of would only seemingly be parallel to the propositional status of the sentential complements of because. However, this solution cannot be any less murky than the assumptions concerning the nature of facts are. Thus, the difference in adjunction sites seems to be the most plausible and promising option for solving the problems posed by the data in (7).

## 4 Conclusion and outlook

Summarizing, I argued that the factive causal relation introduced by because (of) phrases, $\mathbf{f}$ cause er or cause $\mathbf{s}$ in the DRSs in Figures 1, 2 and 3, is assumed to be neutral with regard to its interpretation as a plain cause or reason. If what is caused is a non-intentional state or event, a plain cause interpretation results, whereas whenever an attitudinal state is caused, the because (of) complement is interpreted as a reason. In case what is caused is a deontic modal state, only plain cause interpretations are possible, regardless whether the modal embeds an
attitudinal state or not. I also discussed some data involving epistemic modals for which because and because of differed: only because adjuncts seem able to outscope epistemic modal operators.

Future work needs to involve an attempt at clarifying the notion of facts and an explication of the theory of causation, at least to the extent that it is needed for the purpose of the present analysis. In addition, because should be compared with other causal expressions in English such as since, which only seems to have the reason interpretation. Finally, comparing because (of) to similar expressions in other languages would be helpful. Whereas the German preposition wegen 'because of' seems to behave completely parallel to nominal-complement because of, sentential-complement because unites the function of denn and weil in German.

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# Much support and more 

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#### Abstract

This paper examines the semantics of much when it occurs as a dummy element, in so-called much support (Fred is diligent; in fact he is too much so) and more comparatives (more intelligent, where more $=$ much $+-e r$ ). It is shown that far from being anomalies, much support and more comparatives provide a clue to the correct analysis of much more generally: much is essentially contentless, serving only as a carrier of degree morphology. In short, much always acts as much support. These findings provide evidence towards a theory of quantity adjectives (many, few, much and little) as predicates of scalar intervals, with the remainder of the content traditionally ascribed to them contributed instead by null syntactic elements and operations. The vacuous nature of much itself is also argued to account for its infelicity in unmodified form in many contexts (e.g. ?? We bought much rice.).


## 1 Introduction

### 1.1 The Problem

A curiosity about much is its ability to act as a dummy element. Much otherwise has uses as a quantifier meaning 'a large quantity of' (1), and as an adverbial element meaning 'to a high degree' (2):
(1) a. Much alcohol was consumed last night
b. Much office work is tedious
c. We don't have much rice
(2) a. I much prefer wine to beer
b. Isabelle works too much

But consider cases such as (3), an example of what Corver (1997) refers to as much support. If so is a pronominal copy of the adjective diligent (or of some projection of the adjective), which is modified by the degree modifier too, much does not appear to make any semantic contribution at all.
(3) John is diligent; in fact, he is too much so

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A similar issue is posed by comparatives formed with more. In (4), more intelligent and smarter seem parallel in interpretation, involving the comparative forms of intelligent and smart, respectively. This would suggest that the comparative morpheme -er and more are semantically equivalent. But more in its quantificational uses has beeen analyzed as the comparative of much (and many) (5) (cf. Bresnan 1973). If this approach is extended to cases such as (4a) (i.e. more intelligent $=$ much $+-e r+$ intelligent), we again have an extra much without apparent semantic content.
(4) a. Sue is more intelligent than Fred
b. Sue is smarter than Fred
(5) I have more [much + -er] rice than I need

### 1.2 Previous Treatments

Within the literature, there have been two main approaches to the facts outlined above. On the one hand, Bresnan (1973) posits an underlying much in adjectival projections generally, such that the adjective phrase in (6a) is underlyingly (6b). In pre-adjectival contexts, much is then deleted via a rule of much-deletion (7):
(6) a. Mary is too intelligent
b. [ AP [QP too much] intelligent]

$$
\begin{equation*}
\text { much } \rightarrow \emptyset[\text { AP } \ldots---\mathrm{A}] \tag{7}
\end{equation*}
$$

In this way, a parallel can be reestablished between cases such as (4a), where much is present (in its comparative form much + -er $=$ more ), and (4b), where much has been deleted via (7).

Corver (1997), on the other hand, distinguishes two much's: the lexical contentful much of examples such as (2) and the 'dummy' much of much support (3). The former is an adjectival element that introduces its own degree argument; the latter is a dummy element that is inserted as a last resort to establish a local relationship between a degree operator (e.g. too in (3)) and the degree argument of the pro-form so. See also Kennedy and McNally (2005) and Rett (2006) for analyses of some instances of much as a dummy element.

Questions can be raised about both of these alternatives. As noted by Corver, Bresnan's rule of much-deletion gets the facts right, but otherwise does not have much explanatory force. Conversely, as will be discussed further below, there is also little independent support for a dichotomy between two versions of much. In fact, I argue that neither of these approaches is necessary.

### 1.3 Main Claim

The central claim of this paper is that there is nothing anomalous about the much of much support and more comparatives. Much in these contexts has precisely the same semantics as it does in the apparently contentful cases (1) and
(2). Specifically, much in its lexical semantics is essentially contentless, serving only as a carrier of degree morphology, which can be inserted as needed for morphological or syntactic reasons, without affecting the compositional semantics. To put it differently, much in essence is always much support.

## 2 Proposal

### 2.1 The Decomposition of much

The broader context for the present analysis is a theory according to which the adjectives of quantity (Q-adjectives) many, few, much and little are taken to denote predicates of scalar intervals, an approach that builds on Schwarzschild (2006) and Heim $(2000,2006)$. This is independently motivated by the need to account for their differential uses, as in (8) and (9).
(8) a. We have much more than 10 kg of rice
b. We have little more than 10 kg of rice
c. We have much less than 10 kg of rice
(9) a. John is much shorter than Fred
b. John is much younger than Fred

Q-adjectives are most commonly analyzed as quantifying determiners (e.g. Barwise and Cooper 1981, Higginbotham 1995), as in (10a). Alternately, building on analyses of cardinal numbers as cardinality predicates (e.g. Landman 2004), one might treat Q-adjectives as predicates over groups or portions of matter (10b) (along these lines, see Partee 1989 for a predicative treatment of many and few).
a. $\llbracket \operatorname{much}_{\text {quant }} \rrbracket=\lambda P \lambda Q . \exists x\left[P(x) \wedge Q(x) \wedge \mu_{D I M}(x)>d_{S t d}\right]$
b. $\llbracket$ much $_{\text {pred }} \rrbracket=\lambda x \cdot \mu_{D I M}(x)>d_{S t d}$
where $\mu_{D I M}(x)$ is a measure function that associates a portion of matter with a degree on some dimension DIM (e.g. weight, volume, etc.) and $d_{S t d}$ is a context-dependent standard of comparison

However, neither of the entries in (10) can be applied to the differential examples in (8) and (9). Here much and little first of all cannot be analyzed as quantifying determiners (per (10a)), in that there are not two predicates that could serve as arguments. But they also cannot be analyzed as predicates of portions of matter (per 10b)). In (8a), we might be tempted to say that much is predicated of that portion of the rice we have in excess of the first 10 kg ; but in (8c), there is no equivalent portion of rice of which much could be predicated. This same issue applies even more clearly in the case of (9), where there is no stuff of any sort that could serve as an argument for the Q-adjective.

Instead, from an intuitive perspective, much and little in these cases describe the gap between two values or degrees on a scale (cf. Klein 1982). That is, (8c) specifies that the gap between the amount of rice we have and 10 kg is large;
(9b) specifies that the gap between John's height and Fred's is large. This can be formalized as follows: First, the gap between two scalar values is represented as a scalar interval, that is, a convex set of degrees (11). Much and little are then taken to denote predicates of scalar intervals (12) (cf. Heim 2006); much is true of an interval if its length exceeds some context-dependent standard, while little is true of an interval if its length falls short of some (possibly different) standard.
(11) A set of degrees $I_{\langle d t\rangle}$ is an interval iff
$\forall d, d^{\prime}, d^{\prime \prime}$ such that $d>d^{\prime}>d^{\prime \prime},\left(d \in I \wedge d^{\prime \prime} \in I\right) \rightarrow d^{\prime} \in I$
a. $\llbracket \operatorname{much} \rrbracket=\lambda I_{\langle d t\rangle} \cdot \operatorname{length}(I)>d_{S t d}$
b. $\llbracket l i t t l e \rrbracket=\lambda I_{\langle d t\rangle}$. length $(I)<d_{\text {Std }}$
where $\operatorname{length}(I)=\max (I)-\min (I)$
The entries in (12) provide what is needed to analyze the differential examples in (8) and (9). For example:
(13) $\llbracket(8 \mathrm{c}) \rrbracket=1$ iff $\llbracket \operatorname{much} \rrbracket(\lambda$ d.amount of rice we have $\leq d \leq 10 \mathrm{~kg})$
iff length $(\{d$ : amount of rice we have $\leq d \leq 10 \mathrm{~kg}\})>d_{S t d}$
Thus to accommodate the differential uses of much and other Q-adjectives, some of the semantic content typically ascribed to these terms (as in (10)) must be stripped away. Specifically, much and little as defined in (12) are not inherently quantificational; and second, much and little also do not in their lexical semantics include a measure function, that is, a function that associates portions of matter with degrees (cf. (10)). This would seemingly leave the entries in (12) unable to handle quantificational examples such as (1). But these too can be accomodated with the interval-based semantics given above, by attributing the missing semantic content to other elements. To this end, I first propose that quantificational force arises via existential closure. Second, I follow Schwarzschild (2006) (and less directly, Kayne 2005) in proposing that the measure-function role is played by a functional head Meas in whose specifier position the quantifier phrase headed by quantificational much or little occurs. Meas has the semantics in (14):
(14) $\llbracket$ Meas $\rrbracket=\lambda x \lambda d \cdot \mu_{D I M}(x)=d$

To work out a relevant example, (1a) has the surface structure in (15a). But much cannot be interpreted in situ due to a type mismatch, so raises at LF (15b), leaving a trace of type $d$ in its base position. The semantic derivation proceeds as in (16).
a. SS: [[DP [MeasP[QP much] Meas [NP alcohol]]] was consumed]
b. LF: $\left[[\text { QP much }]_{1}\left[\left[D P\left[\right.\right.\right.\right.$ MeasP $\mathrm{t}_{1}$ Meas [NP alcohol $\left.\left.]\right]\right]$ was consumed $\left.]\right]$

【 much $_{1} \rrbracket\left(\llbracket \mathrm{t}_{1}\right.$ Meas alcohol was consumed $\left.\rrbracket\right)$
$=\llbracket \operatorname{much}_{1} \rrbracket\left(\lambda d_{1} \cdot \exists x\left[\operatorname{alcohol}(x) \wedge \operatorname{consumed}(x) \wedge \mu_{D I M}(x)=d_{1}\right]\right)$
$=\operatorname{length}\left(\left\{d: \exists x\left[\operatorname{alcohol}(x) \wedge \operatorname{consumed}(x) \wedge \mu_{D I M}(x)=d\right]\right\}\right)>d_{S t d}$

The end result in (16) specifies that length of the interval from 0 to the degree corresponding to amount of alcohol consumed exceeds $d_{S t d}$ (or in simpler terms, that the amount of alcohol consumed exceeds $d_{S t d}$ ).

Note also that while the examples discussed here pertain to much and little, the same approach can be extended to their count counterparts many and few, by taking the degrees in question to be degrees of cardinality.

However, the analysis outlined here is not, in the present form, quite adequate. Much and little are gradable expressions, able to combine with degree modifiers (too much, so much, as much as, etc.). In their modified forms, they do not have the 'greater than standard' interpretation that characterizes the positive (i.e. unmodified) form (for example, 'I have as much rice as Fred' does not entail 'I have much rice'). This is not captured by the entries in (12), in which the standard of comparison $d_{S t d}$ is part of the lexical semantics of much and little.

Within the literature on gradable adjectives (e.g. Cresswell 1977, Heim 2000, Kennedy 2007), which is extended to Q-adjectives in particular by Hackl (2000), the usual approach to this issue is to remove the standard of comparison from the semantics of the positive form itself. Instead, the gradable expression is given a degree argument as its first argument, which may be be saturated or bound by a degree modifier (e.g. by too or $a s$ ). In the case of the bare positive form, where there is no overt degree morphology, a phonologically null degree operator POS (for 'positive') plays this role.

Applied to much and little, we obtain the following revised forms:
a. $\llbracket \mathrm{much} \rrbracket=\lambda d \lambda I_{\langle d t\rangle} \cdot d \in I$
b. $\llbracket$ little $\rrbracket=\lambda d \lambda I_{\langle d t\rangle} . \neg d \in I$

A possible definition for the null positive morpheme is the following, taken from von Stechow (2006) and Heim (2006):

$$
\begin{equation*}
\llbracket \mathrm{POS} \rrbracket=\lambda I_{\langle d t\rangle} \cdot N_{S} \subseteq I \tag{18}
\end{equation*}
$$

Here POS introduces as a standard of comparison the range $N_{S}$ consisting of values that would be considered neither large nor small with respect to the context. ${ }^{1}$

According to the revised semantics in (17), little has the semantics of degree negation (a conclusion argued for on independent grounds by Heim 2006), associating an interval with the degrees not contained within it. But much simply associates an interval with the degrees within it. The result is that it functions essentially as an identity function on intervals. This becomes evident through an example. With the semantics for much and POS introduced above, (1a) has the revised LF in (19), where both much and POS have raised from their DP-internal

[^133]surface positions for type-driven reasons. The semantic derivation proceeds as in (20):
(19) LF: [DegP POS $]_{2}\left[\left[Q_{Q P} \mathrm{t}_{2} \text { much }\right]_{1}\left[\left[\left[D_{D P}\left[\right.\right.\right.\right.\right.$ Meas $P \mathrm{t}_{1}$ Meas [ $N P$ alcohol $\left.\left.]\right]\right]$ was consumed]]]
$\llbracket \mathrm{POS}_{2} \rrbracket\left(\llbracket \mathrm{t}_{2} \mathrm{much}_{1} \rrbracket\left(\llbracket \mathrm{t}_{1}\right.\right.$ Meas alcohol was consumed $\left.\left.\rrbracket\right)\right)$
$=\llbracket \mathrm{POS}_{2} \rrbracket\left(\llbracket \mathrm{t}_{2} \operatorname{much}_{1} \rrbracket\left(\lambda d_{1} \cdot \exists x\left[\operatorname{alc}(x) \wedge \operatorname{consumed}(x) \wedge \mu_{D I M}(x)=d_{1}\right]\right)\right)$
$=\llbracket \mathrm{POS}_{2} \rrbracket\left(\lambda d_{\mathcal{2}} \cdot \exists x\left[\operatorname{alcohol}(x) \wedge \operatorname{consumed}(x) \wedge \mu_{D I M}(x)=d_{2}\right]\right)$
$=N_{S} \subseteq\left\{d: \exists x\left[\operatorname{alcohol}(x) \wedge \operatorname{consumed}(x) \wedge \mu_{D I M}(x)=d\right]\right\}$
'The amount of alcohol consumed exceeds $N_{S}$ '
Here, much takes as argument the set of degrees (interval) formed by lambda abstraction over the trace of type $d$ in its base position. Subsequently, lambda abstraction over the trace of POS again produces a set of degrees. But as can be verified above, the second set of degrees is identical to the first. Thus much is essentially semantically inert, simply mapping a set of degrees (interval) to itself. It makes no other contribution to the semantics of the sentence.

To summarize, in analyzing much as a gradable expression, yet more of its content must be stripped away, and transfered instead to POS, leaving much itself as a pure identity element. Put differently, much essentially has no content of its own, but serves only as a carrier of degree morphology (in the case above, of POS). It is therefore not surprising that it is able to function as a dummy element.

### 2.2 Applied to much Support and more Comparatives

With this framework in place, an analysis of much support and more comparatives is now straightforward.

I begin with much support. With regards to the syntactic structure, I assume that in the case of a degree modifier plus gradable adjective (e.g. too diligent), the degree modifier constitutes a Degree Phrase ( DegP ) located in the specifier position of the adjective phrase AP (Heim 2006). ${ }^{2}$ I take so to be a pro-form for the adjective, which differs in that it cannot combine directly with a degree modifier (I do not address here why this is the case; presumably the reason is morphosyntactic in nature). To remedy this, much is inserted, in the form of a QP headed by much in SpecAP. That is:
(21) a. He is [ $\mathrm{AP}[\mathrm{DegP}$ too] diligent]
b. He is [ $\mathrm{AP}[\mathrm{QP}[\mathrm{DegP}$ too] much] so diligent $]$

However, due to the vacuous nature of much, the resulting interpretation is semantically equivalent to what would obtain if much were not present:

$$
\begin{align*}
& \llbracket \mathrm{too}_{2} \rrbracket\left(\llbracket \mathrm{t}_{2} \operatorname{much}_{1} \rrbracket\left(\lambda d_{1} \cdot h e \text { is } d_{1} \text { diligent }\right)\right)  \tag{22}\\
& =\llbracket \mathrm{too}_{2} \rrbracket\left(\lambda d_{2} \cdot h e \text { is } d_{2} \text { diligent }\right)
\end{align*}
$$

[^134]More comparatives can be treated similarly. Adjectives that form more comparatives (e.g. intelligent) cannot compose directly with the comparative morpheme -er. I propose that while -er comparatives feature a DegP -er in SpecAP, more comparatives have a QP more (i.e., [QP [DegP -er] much]) in this position.

> a. Sue is $[\mathrm{AP}[\mathrm{DegP}-\mathrm{er}]$ smart $]$
> b. Sue is $[\mathrm{AP}[\mathrm{QP}[\mathrm{DegP}-\mathrm{er}]$ much $]$ intelligent $]$

But again, the interpretation is parallel to that which would obtain without much:
(24) $\llbracket-\mathrm{er}_{2} \rrbracket\left(\llbracket \mathrm{t}_{2}\right.$ much $_{1} \rrbracket\left(\lambda d_{1}\right.$. Sue is $d_{1}$ intelligent $\left.)\right)$
$=\llbracket-\mathrm{er}_{2} \rrbracket\left(\lambda d_{2}\right.$. Sue is $d_{2}$ intelligent $)$
Thus in both cases, much can be inserted to host degree morphology (e.g. too or -er), without affecting the compositional semantics.

### 2.3 Summary

In summary, much support and more comparatives are not anomalies at all, but rather are indicative of the true semantic nature of much in general: as a basically content-less dummy element. These data thus provide further evidence for a decompositional analysis of quantity adjectives, according to which these words themselves denote predicates of scalar intervals, with other components of their apparent content instead attributed to null syntactic elements (Meas, POS) and semantic operations (existential closure).

## 3 The Infelicity of Bare much

It has often been noted that bare much is only marginally acceptable in many contexts. The (carefully chosen) original example (1a) is itself somewhat awkward; and other examples of unmodified quantificational much are typically quite bad (25a). By contrast, in the very same positions, much in combination with an overt degree morpheme (-er, too, that, etc.) is perfectly felicitous ( $25 \mathrm{~b}-\mathrm{g}$ ).
(25) a. ??I bought much rice
b. I bought more rice than I needed
c. I bought too much rice
d. I bought as much rice as I could
e. I bought so much rice that it doesn't fit in the jar
f. I didn't realize that I bought that much rice
g. How much rice did you buy?

The present analysis suggests an account for this. Much is essentially semantically vacuous: Its primary role is as a carrier of degree morphology. As such, it is infelicitous in the absence of an overt degree morpheme. In combination with the
null morpheme POS, whose interpretation is entirely context dependent, much does not have enough content to stand on its own. This is particularly the case because much does not even specify a dimension of measurement (e.g. too much rice could be an excessive amount in terms of weight, volume, etc.).

While I believe this to be fundamentally correct, what is somewhat problematic for this story is that bare much is not always infelicitous, a case in point being differential examples such as (8) and (9). In fact, Corver (1997) uses this distinction as support for the existence of two much's, the lexical contentful much (acceptable bare) and the dummy much (which must occur with degree morphology). But a closer look at the facts suggests that the pattern of felicitous vs. infelicitous bare much does not line up in any obvious way with a contentful vs. dummy division.

Specifically, unmodified much is typically awkward (if not outright ungrammatical) in quantificational use (26a-c), as a post-verbal modifier (26d) and in much support (26e).
(26) a. ??Much wine is left
b. ??I bought much rice
c. ??Sue lost much money in the stock market crash
d. ??John slept much (cf. John slept too much; John slept as much as he wanted)
e. ??I'm tired; in fact, much so (cf. ...in fact, too much so to go to the party)

But it does not seem plausible to group the quantificational and adverbial uses in (26) with much support as examples of dummy much.

In all of the above contexts, much in its modified forms is entirely acceptable. And interestingly, unmodified much is acceptable in the equivalent negative contexts:
(27) a. Not much wine is left
b. I didn't buy much rice
c. John didn't sleep much
d. Sue didn't lose much money in the stock market crash
e. I'm not tired; at least, not much so

Yet lest we conclude that bare much is a negative polarity item, there are also non-negative contexts where it is in fact felicitous: the differential use (28a,b), in partitives (28c), as a pre-verbal adverb with a small group of verbs (28d,e), and as a modifier of deverbal adjectives (28f) and two ordinary adjectives, alike and different $(28 \mathrm{~g})$.
a. We have much more/much less than 10 kg of rice
b. John is much taller/much shorter than Fred
c. Sue lost much of her money in the stock market crash
d. I much prefer wine to beer
e. I (very) much appreciate your assistance
f. a much improved effort; a much loved teacher
g. Mice and moles are much alike/much different

While I do not have a conclusive explanation for these facts, a look at the examples in (26)-(28) suggests that interpretive factors play a role. Here, a comparison of the quantificational (26c) to the partitive (28c) is particularly illuminating. What counts as much money is entirely context dependent. But partitives necessarily receive a proportional interpretation; much of her money means a large proportion of her money, an interpretation which is much more constrained than that available in the quantificational case. Differential uses of much are also constrained in interpretation. While only the context determines what qualifies as much rice (26b), in the case of much more than 10 kg of rice (28a), the difference must be significant in comparison to 10 kg (i.e. the extra amount required to count as much more than 10 kg is different than that needed to count as much more than a ton). Other of the examples in (28) can perhaps be assimilated to this: alike and different $(28 \mathrm{~g})$ have been analyzed as inherent comparatives (Alrenga 2007), and prefer (28d) likewise has a comparative feel. Even the contrast between positive and negative contexts could perhaps be explained in these terms: How much rice is needed to qualify as much rice depends on the context (in the formalism developed above, it depends on the scalar location of the standard of comparison $N_{S}$ ); but some amounts will always fall below the standard and count as not much rice.

On this view, then, the infelicity of unmodified much in some (but not all) contexts could be attributed to semantic underspecification. This seems a promising direction, and one that would benefit from further investigation.

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# Quantifiers and Working Memory 

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#### Abstract

The paper presents a study examining the role of working memory in quantifier verification. We created situations similar to the span task to compare numerical quantifiers of low and high rank, parity quantifiers and proportional quantifiers. The results enrich and support the data obtained previously in $[1-3]$ and predictions drawn from a computational model [4, 5]. Keywords: working memory; generalized quantifiers; computational semantics; span test


## 1 Introduction

The role of working memory in language comprehension has been extensively studied (see e.g. [6]). The theory of the specific aspects of memory has been developed by Baddeley and colleagues [7, 8]. They proposed to extend the concept of a short-term memory, suggesting that it could be divided into three separable components. It has been assumed that working memory consists not only from temporary storage units (phonological or visual) but also from a controlling system (central executive). Working together, these components form a unified memory system that is responsible for the performance in complex tasks.

Danemamn and Carpenter (1980) developed span test to asses the working memory construct proposed in [7]. In the task subjects read series of sentences and are asked to remember the final word of each sentence. Data suggest that the result of the span test (the number of correctly memorized words) is a good predictor of language comprehension and other language-processing tasks [912]. The main idea of the span test is that solving it requires engagement of both processing and storage functions. In an experimental study a trade-off between them is usually observed. There are two possible explanations of this phenomenon. One is a computational theory according to which storage and processing use the same cognitive resource and compete for a limited capacity $[13,11]$. The second is 'multiple resource' theory, where the working memory is viewed as a group of cognitive subsystems each having a specialized function [8, 14]. According to that account performance in a particular task relies on one or more subsystems acting together.

The paper presents a study examining the role of working memory in quantifier verification. We created situations similar to the span task [15]. The aim
of our research is to verify the contribution of working memory for a few specific natural language quantifiers.

### 1.1 Quantifier Verification Model

In [1] the pattern of neuroanatomical recruitment while subjects were judging the truth-value of statements containing natural language quantifiers have been examined using neuroimaging methods. The authors were considering two standard types of quantifiers: first-order (e.g., 'all', 'some', 'at least 3'), and higherorder quantifiers (e.g., 'more than half', 'an even number of'). They presented the data showing that all quantifiers recruit the right inferior parietal cortex, which is associated with numerosity, but only higher-order quantifiers recruit the prefrontal cortex, which is associated with executive resources, like working memory.

The distinction between first-order and higher-order quantifiers does not coincide with the computational resources, like working memory, required to compute the meaning of quantifiers. Cognitive difficulty of quantifier processing might be better assessed on the basis of complexity of the minimal corresponding automata $[4,5]$. Taking this perspective, in [3] an analogical reaction time experiment carefully differentiating between the following classes of quantifiers has been conducted (see Table 1). The study has shown that the increase in reaction

| Quantifiers | Examples | Minimal automata |
| :--- | :--- | :--- |
| logical <br> numerical | 'all cars', | at least $k$ ' |$\quad$| acyclic 2-state FA |
| :--- |
| acyclic FA with number |
| of states depending on $k$ |

time is determined by the minimal automata corresponding to the quantifier. Among others, the results indicate that the numerical and parity quantifiers are processed faster than the proportional quantifiers. This is consistent with computational analysis as only proportional quantifiers demand a recognition mechanism with unbounded internal memory, like a stack in push-down automata (see [3]). Therefore, there is not only a quantitative but also qualitative difference between memory resources which are necessary to compute these two types of quantifiers. This conclusion also follows from the differences in the brain recruitments observed in [1].

### 1.2 The Present Study

The data obtained so far support the assumption that the difficulty of mental processing of quantifiers depends on the complexity of the corresponding minimal
automata. This complexity can be explained by a difference in needed memory resources, e.g., different number of states in the case of various numerical quantifiers. The present paper extends previous results by studying the engagement of working memory during quantifier verification tasks.

We examined three groups of quantifiers: proportional, parity and numerical (high and low rank). We predicted that when subjects are asked to maintain arbitrary information in short-term memory then similar differences between quantifiers should be revealed as those described in [3] as well as in [16]. In particular, the difficulty (indicated by reaction time and accuracy) should decrease as follows: proportional quantifiers, numerical quantifiers of high rank, parity quantifiers, numerical quantifiers of low rank. Additionally, processing of the proportional quantifiers should influence the storage functions. The effect should be stronger in more demanding situation, for instance when the number of elements to be stored in the memory is increasing.

## 2 Method

### 2.1 Participants

Sixty native Polish-speaking adults took part in the study. They were volunteers from Warsaw University of Finance and Management undergraduate population. Of these, 18 were male and 42 were female. The mean age was 24 years (SD $=4.75)$ with a range of $21-40$ years. Each subject was tested individually in exchange for partial fulfillment of course credits.

### 2.2 Materials and Procedure

The general aim of this study was to assess how subjects are judging the truthvalue of statements containing natural language quantifiers with an additional memory load. The experiment was a combined task and consisted of two elements. It required participants to verify sentences and to memorize a sequence of single digits for the later recall.

Sentence Verification Task The task consisted of sixty-four grammatically simple propositions in Polish containing a quantifier that probed a color feature of a car on a display, e.g., 'Więcej niż połowa samochodów jest czerwona' (More than half of the cars are red) or 'Parzysta liczba samochodów jest niebieska' (An even number of cars are blue). The same number of color pictures presenting a car park with 15 cars were constructed to accompany the propositions. The colors used for the cars were red, blue, green, yellow, purple and black. Each picture contained objects in two colors (see Figure 1).


Fig. 1. An example of stimulus used in the first study.

Eight different quantifiers were used in the study. They were divided into four groups:
(1) parity (divisibility) quantifiers (odd, even), DQ;
(2) proportional quantifiers (less than half, more than half), PQ;
(3) numerical quantifiers of relatively low rank (less than 5 , more than 4 ), NQ4/5;
(4) numerical quantifiers of relatively high rank (less than 8 , more than 7 ), NQ7/8.

Each quantifier was presented in 8 trials. Hence, there were in total 64 tasks in the study.

Half of each type of items was true and half false. Propositions were accompanied with a quantity of target items near the criterion for validating or falsifying the proposition. Therefore, these tasks required a precise judgment (e.g. seven targets in 'less than half'). Debriefing following the experiment revealed that none of the participants had been aware that each picture consisted of exactly fifteen objects.

Each quantifier problem involved one 15.5 s event. In the event the proposition and a stimulus array containing 15 randomly distributed cars were presented for 15000 ms followed by a blank screen for 500 ms . Subjects were asked to decide if the proposition accurately described the presented picture. They responded by pressing the button with letter ' p ' if true; the button with letter ' f ' was pressed if false. The letters refer to first letters of Polish words for 'true' and 'false'.

Memory Task At the beginning of each trial the subjects were presented a sequence of digits consisting of four or six elements from the range between 0 and 9 . After completing the sentence verification task they were asked to recall the string. Each quantifier type was accompanied by the same number of four and six digits.

## 3 Results

### 3.1 Sentence Verification Task

ANOVA with type of quantifier (4 levels) and number of digits to memorize (2 levels) as two within-subject factors was used to examine differences in means in reaction time and accuracy of sentence verification task. Greenhouse-Geiser adjustment was applied where needed.

The analysis of reaction time indicated that two main effects - of quantifier type $\left(F(2.282,134.62)=41.405 ; p<0.001 ; \eta^{2}=0.412\right)$ and of number of digits $\left(F(1,59)=4.714 ; p<0.05 ; \eta^{2}=0.075\right)$ as well as quantifier $\times$ digits interaction $\left(F(2.544,150.096)=2.931 ; p<0.05 ; \eta^{2}=0.05\right)$ - were significant (see Figure 2).


Fig. 2. Mean RT in 4- and 6-digit memory load conditions.

For simple effects we analyzed differences between quantifiers separately for two memory conditions. We found that mean reaction time was determined by quantifier type while subjects were maintaining 4 digits in memory. Pairwise comparisons among means revealed that PQ were solved longer than other types of quantifiers while NQ $4 / 5$ were processed shorter than the rest of quantifiers; finally, there was no difference between DQ and $\mathrm{NQ} 7 / 8$. In 6 -digit condition we also found a significant effect - NQ $4 / 5$ had shorter average RT than other quantifiers. One-way ANOVA revealed that only PQ differed between memory load conditions (see Table 2).

## General Program

| Quantifier M (4-digit) | M (6-digit) |  |
| :--- | :--- | :--- |
| PQ | 7582 | 6976 |
| DQ | 6644 | 6595 |
| NQ $7 / 8$ | 6784 | 6598 |
| NQ $4 / 5$ | 5144 | 5179 |

Table 2. Mean RT in milliseconds for each quantifier type.

The main effects of quantifier type $(F(2.574,151.867)=22.238 ; p<0.001$; $\left.\eta^{2}=0.275\right)$ and of digits $\left(F(1,59)=4.953 ; p<0.05 ; \eta^{2}=0.078\right)$ were found in accuracy. All four types of quantifiers differed significantly from one another besides DQ and NQ 7/8 (see Table 3 for mean score). In 4-digit condition all quantifiers were performed worse $(\mathrm{M}=6.22)$ than in 6 -digit condition ( $\mathrm{M}=$ 6.43).

| Quantifier M |  |
| :--- | :--- |
| PQ | 5.57 |
| DQ | 6.36 |
| NQ 7/8 | 6.45 |
| NQ 4/5 | 6.93 |

Table 3. Mean (M) of the accuracy for each type of quantifier.

Summing up, we observed that in 4-digit memory load condition proportional quantifiers were solved longer and poorer than other types of quantifiers. On the other hand, numerical quantifiers with low rank were performed shorter and better than others. There was no difference between parity quantifiers and numerical quantifiers of high rank.

In 6 -digit condition we observed lower average reaction time of numerical quantifiers of low rank in comparison with proportional, parity and numerical quantifiers of high rank, which had equal means. Analysis of accuracy showed the following increase of difficulty: numerical quantifiers of low rank, then parity quantifiers and numerical quantifiers of high rank (the same level), and finally proportional quantifiers.

Finally, the accuracy on all types of quantifiers was better in 6-digit condition. However, as we will see in the next section there was a significant drop in recalling task.

### 3.2 Memory Task

ANOVA with two within-subject factors was used to examine how strings of digits (2 levels: four and six elements) were recalled with respect to quantifier
type (4 levels) they were accompanied by. Greenhouse-Geiser adjustment was applied where needed.

The analysis indicated main effect of digits $(F(1,59)=90.646 ; p<0.001$; $\left.\eta^{2}=0.606\right)$ and digits $\times$ quantifier interaction $(F(3,177)=4.015 ; p<0.05$; $\eta^{2}=0.065$ ) (see Figure 3).


Fig. 3. Accuracy of 4- and 6-digit recall with respect to quantifier type.

To examine the interaction effect we compared recall accuracy for 4 and 6 digits. Significant differences between two situations for each level of second variable were obtained. Performance on digit recall with respect to quantifier type was also analyzed separately for 4 - and 6 -digit strings. In the former condition digits accompanying PQ were memorized worse in comparison with other determiners, while in the latter condition we did not observe any differences (see Table 4).

| Number of digits M (PQ) M (DQ) M (NQ 7/8) M (NQ 4/5) |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| 4 | 5.33 | 6.20 | 5.90 | 5.90 |
| 6 | 3.90 | 3.73 | 4.01 | 4.20 |

Table 4. Means of recalling accuracy with respect to quantifier type.

## 4 Discussion

Our study assessed quantifier verification task with additional memory load conditions. Obtained data revealed that in the 4-digit load condition the most difficult were proportional quantifiers (the longest RT and the poorest accuracy). Subjects performed better on numerical quantifiers with low ranks than on the other determiners, and finally there were no differences between parity quantifiers and numerical quantifiers of high rank. The results support our predictions and are consistent with the previous findings in [3] and [17].

We expected similar effects in 6 -digit memory load condition. This hypothesis was only confirmed with respect to sentence verification accuracy. The score increased in all types of quantifiers but differences between them remained at the same level as in 4-digit condition. Moreover, we observed that numerical quantifiers of low rank had the lowest average reaction time. Proportional, parity and numerical quantifiers of high rank had equal means.

The discrepancy between performances under two memory load conditions needs explanation. We believe that the analysis of digits retrieval sheds some light on the obtained data. The real differences between quantifiers occurred only in 4 -digit condition. Holding six elements in memory was probably too difficult in face of processing secondary task. The decrease of accuracy in digits recall with simultaneous increase in performance on quantifier verification task could be described as a trade-off between processing and storage (see [15, 14]).

Another interesting observation concerns proportional quantifiers. In 4-digit condition the strings of numbers accompanying this class of quantifiers were recalled worst. However, in the case of 6 -digit memory load there were no differences among quantifier types. It is worth to put those results together with the data on the reaction time for proportional quantifier verification. The mean RT decreased because subjects focused only on the sentence verification task ignoring the recalling task. This may be interpreted as supporting the hypothesis, following from the computational model, that working memory engagement in the case of proportional quantifier processing is qualitatively different than in the processing of quantifiers corresponding to finite-automata.

An interesting result is tied up with numerical quantifiers and the number of states in the corresponding minimal automata. In [5] it has been hypothesized that the number of states is a good predictor of cognitive load. Indeed, our current results show the difference between numerical quantifiers of low and high ranks. This fact strongly supports that claim.

Finally, let us briefly discuss a problematic case. The relation between parity and numerical quantifiers of high rank is somewhat unclear. In our previous study [3] we observed a significant difference in reaction time between those two types of quantifiers. However, the size effect of the difference was smaller than in other pairwise comparisons among quantifiers. Can the computational model account for the discrepancy? It draws an analogy between states and stack, on the one hand, and working memory resources, on the other hand. The difference between parity and numerical quantifiers can not be explained in that way. Minimal automata corresponding to parity quantifiers have two states while in the
case of numerical quantifiers one needs in principle more. However, the critical factor might be that numerical quantifiers unlike parity quantifiers correspond to automata without loops (see Table 1). Clearly, 2-state automata with loops are more complex than 2 -state acyclic machines (corresponding to Aristotelian quantifiers) and indeed our previous research has shown a difference between the two quantifier groups [3]. However, drawing only from the computational model it is by no means obvious which factor adds more to cognitive difficulty: additional states or loops ${ }^{3}$. This constitutes one of the most interesting problems for our approach (see [2] for a more detailed discussion). A future research focusing on neurocognitive modeling of quantifier comprehension could help in clarifying the interrelations among computational aspects and their cognitive correlates. The aim would be to pin down the specific cognitive mechanisms responsible for quantifier comprehension, taking into account factors like the role of central executive, attentional costs, storage functions as well as aspects of representing and approximating quantities, like distant effect (see e.g. [18]). After all, quantifiers might be viewed as a way of embedding number system [19] in natural language. The perspective needs to be carefully investigated in the future.

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# Pluractionality and the unity of the event 

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#### Abstract

This paper exposes shortcomings of an analysis to single event plural verbs (Cusic's event-internal plural verbs) based on temporal discontinuity. It proposes an approach based on the violation of Krifka's property of Mapping-to-SubObject on a theta role. The proposal extends to other cases when we assume that the semantic contribution of pluractional morphology in these verbs is more generally to break correspondences between mereological relations between participants in predications.


## 1 Introduction

Verbal plurality is often understood as plurality of events that may arise from various sources, e.g. subsequent times, distinct places or participants (Dressler, 1968; Newman, 1980; Cusic, 1981). These sources could be seen as the key in a form of distribution where the event predicate would be the share. The classic formal definition of pluractional verbs (Lasersohn, 1995) is recalled in (1). Whatever key is selected in the sentence, i.e. independently of the $f$ considered, the formula enforces plurality of events and X is a variable that denotes sets of events. The non-overlap condition specifies the distributive key. Lasersohn also adds that $\mathrm{P}=\mathrm{V}$ unless X is a plurality of phases - i.e. the elements that constitute the plurality within a single event according to Cusic's (1981) hierarchy, and an additional constraint on minimal cardinality, i.e. $n$ must be $\geq 2$, that relies on pragmatic contextual information for fixing the value of $n$.
(1) $\operatorname{V-PA}(X) \Leftrightarrow \forall e^{\prime} \in X\left[P(e) \& \neg f(e) \circ f\left(e^{\prime}\right)\right] \& \operatorname{card}(X) \geq n$
$\mathrm{PA}=$ pluractional affix, $f$ is a temporal/spatio-temporal trace function or a thematic role assigned by V
Recently, attention has been paid to cases where there are forms of multiplicity that have a source that does not impact on the singularity of the event, and the events involve single participants. In this paper, I pursue an analysis where distribution takes place over the cells of a cover applied to a participant/value relevant for measuring a dimension of the event correlated with its unfolding. I will discuss shortcomings in grounding phases of a discontinuous event on time, and then make a more general point on differentiating between phases and minimal units of an event.

## 2 Event-internal plurality

Two proposals have been recently put forth to deal with possible forms of event-internal plurality, one seeks to identify phases via their temporal trace (Tatevosov, 2007), the other via their local participants (Tovena, 2007, to app.; Tovena and Kihm, 2008).
Tatevosov has argued that the morpheme -kala- in Chuvash (Altaic, Turkic) introduces a form of verb plurality arising from discontinuity of subevents in a single event. ${ }^{1}$ This morpheme is analysed as a degree modifier that lowers below standard a contextually determined gradable property of an event predicate.
$\|-$ kala- $\|=\lambda \mathrm{P} \lambda \mathrm{e} \exists \mathrm{d}\left[\mathrm{F}_{c}(\mathrm{P})(\mathrm{e})=\mathrm{d} \wedge \mathrm{d}<\operatorname{Standard}\left(\mathrm{F}_{c}\right)(C)\right]$
$\mathrm{F}_{c}=$ variable over degree functions specifying the degree of a gradable property of an event, $\mathrm{P}=$ type of event, $C=$ comparison class

Continuity is the property discussed, and $\mathrm{F}_{c}$ in (2) is assigned the function $\mathrm{F}_{\text {continuity }}$ as a value. The standard of comparison for the scale of continuity is the maximal degree, because this is an upper closed scale. In order to define continuity of an event (and lack of), Tatevosov defines the function $\tau^{C}(e)$, called the COVERING Time for $e$, as a temporal trace function that returns the total minimal interval of duration of an event by identifying its initial and final moments. An event $e$ is continuous if all intervals in its covering time are the temporal trace of some subevent of $e$. It has a degree of continuity which is less than maximal whenever its covering time has at least a gap in it, i.e. a subinterval which is the temporal trace of no subevent of $e$, cf. (3).
(3) $\mathrm{F}_{\text {Continuity }}(\mathrm{P})(\mathrm{e})<1 \rightarrow \forall \mathrm{e}\left[\mathrm{P}(\mathrm{e}) \rightarrow \exists \mathrm{t}\left[\mathrm{t}<\tau^{C}(\mathrm{e}) \wedge \neg \exists \mathrm{e}^{\mathrm{e}}\left[\mathrm{e}^{\mathrm{e}}<\mathrm{e} \wedge \mathrm{t}=\tau\left(\mathrm{e}^{\mathrm{e}}\right)\right]\right]\right]$

Crucially, the definition of continuity relies on the possibility for $\tau^{C}(e)$ of identifying the initial and final moments of $e$. This is quite a standard assumption if one has a continuous event to start with, cf. (Krifka, 1998), and gaps are subsequently added in its trace. The reverse order of action

[^136]is problematic, i.e. identifying the event by taking away gaps in an interval, as discussed below. Assuming a VP modifier status - rather than V modifier-defuses the potential problem of talking of a subevent $e^{\prime}<e$ in (3) when $e$ is an event with gaps. This is presumably why Tatevosov treats -kala- as a VP modifier but he does not provide evidence or explicit motivation for this characterisation. The data show that -kala- is an affix that combines with the verb base before perfective affixes and verb inflection are added.
Another way of characterising single events with an internal form of multiplicity has been explored by Tovena in single and joint work, who consider a class of (semi)derived verbs in Italian and French, e.g. It. tagliuzzare (cut into many small pieces) Fr. mordiller (nibble). The plurality is claimed to arise from distributing over the cells of a cover applied to the object. Two devices are exploited to bring about plurality: i) at least one participant is fragmented via the mass role ${ }^{M} \mathrm{R}$ (Landman, 2000), and ii) this role is assigned by an event predicate that denotes in a plural domain.
(4) $\|$ tagliuzzare $\|=\lambda x \lambda y \lambda e[(\operatorname{TAGLIUZZARE}(e) \& \operatorname{Ag}(e, y) \& \operatorname{Pat}(e, x)) \Leftrightarrow$ $\exists e^{\prime}\left({ }^{*}\right.$ TAGLIUZZAREPart $\left.\left.\left(e^{\prime}\right) \& e=\uparrow e^{\prime} \&{ }^{*} \operatorname{Ag}\left(e^{\prime}, y\right) \&{ }^{M} \operatorname{Pat}\left(e^{\prime}, x\right)\right)\right]$

Phases are viewed as the reflect of the application of the predicate to the parts of the participant demoted to a sum of parts. These parts work as the distributive key and the predicate is the distributive share. Proper plurality of phases is ensured by the use of a cover necessarily weaker than the cover that has the atom as its unique cell, and the equation $e=\uparrow e^{\prime}$ links event level and phase level in the representation. The plurality of phases is given an explicit status at event level through groupification.
The verb does not make phases accessible at discourse referent level. Tovena shows that phases cannot be counted, the cardinality of the plurality cannot be compared even when left unspecified, and there are thematic restrictions that do not apply to pluralities of other levels. The unity of the event is not affected, because the plurality of the distributive-key becomes visible only within the event, via the action of the mass role ${ }^{M}$ R. This accounts for the connectedness of event-internal plurals noted by Cusic. The proposal in (4) generalizes by considering property scales measuring an abstract dimension instead of the patient/theme, e.g. the volume of a physical entity, and also scales associated to the event because of implicit arguments. The unfolding of an event is measured by adjacent isomorphic transitions of (an extended version of) the theme along a scale. The scale is related to the event by Krifka's (1998) Movement Relation. The semantic contribution of event-internal pluractional morphology is to disrupt the
correlation between a dynamic predicate and a form of gradability. Fragmenting means to cancel the homomorphism between the mereological structures of scales and events.
Both proposals are about single events that exhibit a form of plurality and describe a situation as non canonical. They share the view that the source of multiplicity is to be sought somewhere in the unfolding of the event, and differ in the conception of plurality invoked.

## 3 Problems for grounding discontinuity on time

Tatevosov's notion of continuity is problematic. In general terms, total absence of discontinuity-i.e. strict continuity - is not enforced in canonical events described by unmodified predicates. Therefore, in principle, it cannot be taken as a discriminating criterion. Let's call disc-V this class of verbs describing discontinuous events. The type of subevents that characterise these verbs are not what gaps are usually thought to be, since they are not accidental breaches in the applicability of the predicate to the interval. They are part of the definition of the event type, and 'lulls' may be a better term for them. Since they are a required component, the trace function applied to the event must return a time interval that contains them too, otherwise the event is not of the disc-V type by definition. This trace is the total minimal interval called the covering time by Tatevosov and corresponds to the minimal convex interval which has the whole temporal trace of the V type event as a subinterval. Note that lulls are visible when the event is considered at the standard level of granularity, and are not an effect of zooming in too much.
Once we acknowledge that lulls are definitional for disc-V type of events, strictly speaking, there is no temporal discontinuity anymore, hence no source of multiplicity. In this respect, the characterisation of -kala- in Chuvas as VP modifier is instrumental, because it allows one to have what looks like a single discontinuous event, but which is not directly defined as one event. The indirect definition as modified event offers an easy way out, in the sense that the original property of event is used to vouch for the composition of all the relevant discontinuous subevents into one event and prevent their being taken as independent. But it also raises the question of why invoking a property that needed to be modified precisely because it was not able to adequately characterise the event under examination. A discontinuous event shows the limits of the entreprise of properly defining/identifying phases by using temporal intervals, which by themselves do not provide event properties.

Furthermore, what said for the event applies to subevents. Either, subevents are of the disc-V type and thus contain lulls, which means that disc-V events cannot be made of just two disc-V subevents, because these subevents themselves must contain lulls. We have a sorites paradox of the heap type here. Or, being continuous subevents, as Tatevosov assumes, they cannot be of disc-V type. They actually are of the V type. But this is a way to stipulate that all V-type subevents cannot cluster at one end of the temporal trace of a disc-V event. Moreover, lulls cannot last too long lest the connectedness of the event is jeopardised. Something should be said about what prevents discontinuity from disrupting the single event into a collection of (partially realised) events of ploughing (parts of) the same field, in the example discussed by Tatevosov.

## 4 Grounding discontinuity on a measure of increment

Taking out lulls from the temporal trace of a kala-V event gives us the trace of a canonical event of the V type. Lulls should not be defined in direct temporal terms as gaps in the trace of an event. Consider again ploughing the field. If events of the disc-V type must have discontinuous subevents, i.e. phases, this means that there must be some subevent(s) in which no part of the field is in a $\theta$ relation with the event and the event's temporal progression is not suspended. Lulls are the subintervals whereby the $\theta$ role assigned by the disc- V to the object is proven not to have the property MSO (mapping-to-subobjects (Krifka, 1998)) exhibited by the corresponding $\theta^{\prime}$ that would be assigned by V to the same entity if the event where realised (or described as realised) in its canonical form.
As said above, events described by event-internal pluractional verbs are perceived as non-canonical instantiations of an event type. The notion of non-canonical/substandard event can be redefined as the case of an event exhibiting localised losses of MSO for a $\theta$ role that should have this property, instead of using the problematic notion of continuity. This localised effect is characterised by saying that a disc-V event must contain subevents that are V events - in all of which $\theta$ satisfies MSO - and subevents that are not, and therefore are lulls. Generalising, i) the $\theta$ assigned by the pluractional- V verb to the object is the closure of $\theta^{\prime}$ under sum formation of the object, where $\theta^{\prime}$ is the role assigned by simplex V to the object, and ii) $\theta^{\prime}$ has MSO and MO (mapping-to-object), while $\theta$ has not. The mapping must be extended to include measures used in the definition of event incrementality.

Discontinuity comes out from a modification of a property of a $\theta$ role instead of using a temporal definition. The multiplicity of phases perceived in the event is anchored in the parts of an entity/value relevant to the conceptualisation of the event and not in its temporal interval, and this is akin to what Tovena and Kihm have proposed. The non-canonical event is characterised indirectly as a modification of the semantic characterisation of the canonical form. This derived semantic characterisation matches the understanding that we are dealing with a class of verbs that consist of morphologically derived forms. The approach defended in this paper provides explicit motivation for the disequation $\mathrm{P} \neq \mathrm{V}$ that Lasersohn (1995) had to stipulate in his treatment of event-internal pluralities. As we have seen, the nature of the event, i.e. its being non-canonical in a way that allows the expression of a local form of plurality, does not lend itself to a recursive definition, and phases cannot be described by the predicate that describes the event. Implicitly, this can also be seen behind Tatevosov's constraint on continuous subevents. Furthermore, note that the issue of the duration of lulls, but not of their presence, boils down to the general, albeit non-trivial, issue of defining continuity for an event.
The complexity of the issue of the locus of modification highlights the fact that, as we just said, the event property utilised for describing the pluractional event cannot be the same as that used to describe phases, but also that the modification has consequences at various levels. On the one hand, properties of the theta roles assigned by the verb naturally belong to the content of the verb, and altering them is tantamount to modifying the ingredients of the aspectual characterisation of the verb, the so-called lexical or inner aspect. On the other hand, the aspectual properties of the whole VP are affected in turn, and a change in the nature of the event description is the most salient output of the use of a pluractional form. We can add to this discussion two language specific pieces of data from Italian and French, languages that use evaluative affixes to form pluractional verbs of the event-internal type. ${ }^{2}$ First, an analysis as VP modifier is not suitable for Italian and French because affixes can form denominal pluractional verbs, beside deverbal ones, see (5). Hence the impact of the affix must be assessed below VP level.
(5) a. Italian: sorseggiare (sip) $\leftarrow$ sorso $_{N}$ (sip)
b. French: pointiller $(\operatorname{dot}) \leftarrow$ point $_{N}$ (dot)

[^137]Second, the affix can affect the conjugation of the verb in deverbal cases, as shown in (Tovena, 2009). Simplex verb forms may belong to any class of conjugation, whereas the derived pluractional forms all belong to the first class. Evaluative affixes bring about the same effect of normalisation in the nominal domain, where all modified nouns belong to the broadest inflection class, independently of the class of the base.

## 5 On phases and minimal units

According to Cusic, event-internal pluractionals denote pluralities of phases. Phases are subevents endowed with some form of atomicity that makes it possible to appreciate their multiplicity, but does not warrant their identification. These single events are durative, and Tatevosov and Lasersohn have claimed that they are minimally composed of sets of $n \geq 2$ subevents. But phases cannot be counted, e.g. a claim of victory like Marie a mordillé plus de Marc (Mary nibbled more than Marc) cannot be foiled by replying Non, parce que lui il est plus rapide (no, because he is faster) with the intention of saying that he gave more little bites in the same time span. It is far from clear that the minimal cardinality of the set of phases can be defined unambiguously for these verbs. Again, the situation hints at a sorites paradox, where the beginning of a sorites series does not coincide with the beginning of a series. There may be a cut-off separating nibbling from biting when going in this direction-as one may concede that an event of two little bites is still a nibbling, yet an event with one is certainly not. There isn't necessarily one when going the other way. A plurality of phases is homogeneous in cumulative terms once we have a point from which to start.
However, the issue is more complex than just having two series with non coinciding beginnings. Questions concerning the beginning of the event surface again when we qualify the units we add. Given what we said on subevents in section 4 , only subevents understood as bigger than single phases can be added as units of a series and be properly called subevents of the same type of event. In this respect, event-internal pluractionals are reminiscent of semelfactives, but also are a different case. Let's first recall some claims about semelfactives.
According to Smith (1991), semelfactives, e.g. jump, cough, are dynamicas they can occur in the imperative form - and atelic instantaneous - as they combine with punctual adverbs. Their peculiarity is the absence of change. In my opinion, this means that the realisation of the event does not modify the preconditions, and, as a consequence, iteration is possi-
ble without gaps. Rothstein (2004) assumes that semelfactives are event predicates that 'denote single instances of events usually considered to be activities'. They denote extended events, cf. they combine with duration adverbs, take progressive form and are said to induce the imperfective paradox, as well as 'single events', cf. they combine with at $x$ time expressions and in x time. Next, Rothstein recalls that Smith acknowledges that semelfactive are events conceptualised as instantaneous though they take time to reach a completion in reality. But Rothstein argues that semelfactives denote events that have internal structure - as opposed to achievements, analysed as near-instantaneous changes from $\neg \phi$ to $\phi$, and uses the occurrence in the progressive and the imperfective paradox as linguistic evidence for such a structure. She concludes that semelfactives must be telic, interval predicates related to homonymous activity predicates.
The series of movements that must occur as part of an event denoted by a semelfactive, in Rothstein terms, are constitutive of its internal structure. It is a single instantiation of this structure that Rothstein takes as paralleling the minimal parts of an activity in Dowty's (1979) terms, i.e. the smallest events in P that count as events of P . The difference with ordinary activities, I suggest, is in the non-arbitrary way of dividing minimal events that is peculiar to semelfactives. We can see activities as characterised by cycles of parts, but in general their cycle does not have a specific first/prominent element, whereas in semelfactives it does.
Rothstein assumes that activities denote in a domain where minimal events are not in an atomic set but in a singular set. On the contrary, in the semelfactive use of a predicate, a natural atomic function pick out the atomic set. The difference is that a singular set contains minimal singular but overlapping entities. Rothstein claims that this means that two minimal events of walking may overlaps but two minimal events of jumping will not. The point about overlapping may mean that the minimal event of a singular set may have structure inside, but that no part in it qualifies as the beginning or the apex of the cycle, contrary to the minimal event in an atomic set. This special role of prominent part in the cycle may be relevant to count units that are viewed as events. The recursion of the distinguished part signals the completion of a cycle, but what precede or follow it qualify as part of the cycle too. The prominent part may act as the identifier for the whole event, as usual with achievements. Since the whole cycle is short, the event may be conceptualised as instantaneous. As an aside, it is an open question whether Rothstein's analysis can predict that the combination of a semelfactive with an for $x$
time expression results in a 'reaction time' reading and not in a loss of telicity, as in painted the wall for two hours, and that the combination with an in x time expression does not result in a telic planned activity, as swam in two hours (her usual distance) according to Dowty (1979). ${ }^{3}$
The identifying capacity of a minimal unit in an activity is an artefact and cannot be used to count events. The uninterrupted cycle is what we count, leaving aside the important but independent issue of continuity. The combination of having well defined minimal units, which are perceived and characterised as such by a language, and having output conditions that meet input conditions, which amounts to what has been dubbed as absence of change in the literature, are the ingredients for semelfactives. These minimal units are single phases mapped onto events in Cusic's hierarchy. The activity reading of a semelfactive predicate corresponds to its denoting sums of events, and minimal events can be added one at the time and yield an incremental process. The semel use corresponds to denoting single minimal events. By contrast, event-internal pluractionals share the second ingredient, but crucially differ with respect to the first. Phases may still be viewed as cycles containing a prominent part that makes it possible to see a multitude, but are not mapped onto events, hence cannot be counted. They may be added, and be the witness when moving up a chain structure, but this does not make them minimal units of the plural event, because they do not partake in the same event type.

## 6 Conclusion

Phases of an event-internal plurality appear as a result of altering a $\theta$ relation of an event description in a way that reduces cohesion. More specifically, at least one theta role lacks a property that is found in the description taken as canonical. The loss of MSO has to do with multiplication, hence it is coupled by a loss of MO. The same pattern of modification can be used to create new verbs from nominal bases.
Phases are viewed as the reflect of the application of the predicate to the parts of the participant demoted to a sum that works as the distributive key. This gives them a form of atomicity sufficient for event-internal plurality. But the modification makes the recursive application of the event property impossible, and phases do not qualify as minimal units of the event they are part of.

[^138]
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[^0]:    ${ }^{1}$ The idea that the extensions of color categories are best modeled as fuzzy sets has been argued for on the basis of theoretical considerations by Kay and MacDaniel (1978).

[^1]:    ${ }^{2}$ The main reasons for the popularity of SVMs in statistical learning are that they are easily adaptable to non-linear classification tasks and that they find separators that generalize well to unseen data. These features are of lesser importance here. See (Schölkopf and Smola, 2002) for a comprehensive account.

[^2]:    ${ }^{1}$ The presence of the non-specific transparent readings is attested by other examples as well; cf. Bäuerle [2], Abusch [1], Percus [9].

[^3]:    ${ }^{2}$ This argument goes back to Ioup [6]. My presentation follows Keshet [7].
    ${ }^{3}$ Compare this suggestion with what we would say in the case of Partee's marble example. The reason (i) I lost ten marbles and found all but one can but (ii) I lost ten marbles and found nine cannot be felicitously continued with (iii) It must be under the sofa has to do with the fact that (i) does and (ii) does not contain the word one. One might conclude from this example (as proponents of dynamic approaches have) that (i) and (ii) are not synonyms. But one would certainly not want to say that (i) and (ii) differ in their truth-conditions. Similarly, I am inclined to accept that (4) and (5) cannot mean the same while I reject the suggestion that they cannot have the same truth-conditions.

[^4]:    ${ }^{4}$ See Percus [9], von Fintel and Heim [3], and Keshet [7].

[^5]:    ${ }^{5}$ The puzzle of summative readings for tense was discovered a long time ago. Sextus Empiricus in Against the Physicists 2.98. attributes a puzzle to Diodoros Chronos. The puzzle concerns Helen of Troy was consecutively married to three different men - Menelaus, Paris, and Deïphobus. Thus, it seems like we can use Helen had three

[^6]:    husbands to say something true. Since the husbands are no more, it is false that three husbands are such that each was at some time in the past Helen's. Since Helen is not guilty of trigamy it is false that at some time in the past Helen had three husbands.
    ${ }^{6}$ I argue for the existence of such readings in Szabó [10].
    ${ }^{7}$ The most prominent defense of the anti-establishment view is Parsons [8]. Zucchi [12] is the standard critique of this aspect of Parsons's work. In Szabó [11] I argue for an account of the progressive that takes a middle course - it takes the sentence Jack is building a house to entail the existence of an actual object Jack is building without characterizing this object as a house.

[^7]:    ${ }^{8}$ Thanks to Itamar Francez, Tamar Szabó Gendler, Justin Khoo, and Anna Szabolcsi for comments.

[^8]:    * Our thanks to David Clausen, Noah Constant, Marie-Catherine de Marneffe, Sven Lauer, Florian Schwarz, and Jess Spencer for discussion.

[^9]:    ${ }^{3}$ In fact, the is about 4.5 more frequent than all of the demonstratives combined (216, 407 tokens).

[^10]:    * Many thanks to Philippe Schlenker, Danny Fox and Bart Geurts as well as to Thomas Andrillon, Vincent Berthet, Isabelle Brunet, Paul Égré, Anne-Caroline Fievet, Greg Kobele and Inga Vendelin.
    ** Chemla and Spector (2009) is an extended presentation of this work, with many more results and discussions.

[^11]:    ${ }^{3}$ These theories do not derive this reading by localist means, of course. They argue instead that the proposition: 'Some students solved all the problems' should be added to the list of negated scalar alternatives of (1).

[^12]:    ${ }^{4}$ See Chemla (2009a,c) for the use of a similar methodology to collect judgments in pragmatics, and the references cited therein.
    ${ }^{5}$ Note that French certains, unlike its singular counterpart un certain or English certain, does not force a specific reading.

[^13]:    ${ }^{6}$ The experiment involved 16 native speakers of French, with no knowledge of linguistics, ranging in age from 19 to 29 years ( 10 women)

[^14]:    ${ }^{7}$ SOME: false vs. literal: $F(1,15)=14, p<.01$; literal vs. weak: $F(1,15)=27$, $p<.001$; weak vs. strong: $F(1,15)=25, p<.001$. OR: false vs. literal: $F(1,15)=$ $6.2, p<.05$; literal vs. weak: $F(1,15)=22, p<.001$; weak vs. strong: $F(1,15)=$ $17, p<.001$. Note that $4.6 \%$ of the responses were excluded as outliers or for technical reasons. Statistical analyses presented here are computed per subject, per item analyses yield similar resuts.

[^15]:    ${ }^{8}$ SOME: false vs. ?local: $F(1,15)=6.5, p<.05$; ?local vs. both: $F(1,15)=43$, $p<.001$. OR: $F(1,15)=.45, p=.51$ and $F(1,15)=60, p<.001$, respectively.

[^16]:    ${ }^{9}$ The global reading (11b) is obtained by adding to the literal reading the negation of the alternative sentence "Exactly one letter is connected to all its circles".

[^17]:    ${ }^{10}$ This experiment involved 16 native speakers of French, with no prior exposure to linguistics, ranging in age from 18 to 35 years ( 9 women). $14 \%$ of the responses had to be excluded for various technical reasons. All statistical analyses presented below are computed per subject; per item analyses yielded similar results.
    ${ }^{11}$ SOME: false vs. literal: $F(1,15)=12, p<.01$, literal vs. local: $F(1,15)=6.7$, $p<.05$, local vs. all: $F(1,15)=10, p<.01$. OR: false vs. literal: $F(1,15)=11$, $p<.01$, literal vs. local: $F(1,15)=2.3, p=.15$, local vs. all: $F(1,15)=18, p<.001$.

[^18]:    ${ }^{12}$ SOME: false vs. ?local: $F(1,14)=20, p<.001$; ?local vs. literal: $F(1,14)=28$, $p<.001$. OR: $F(1,15)=6.1, p<.05$ and $F(1,15)=190, p<.001$, respectively.

[^19]:    ${ }^{1}$ For some speakers, the disjunction in (2) seems to be felicitous under a reading where it is understood as a directive to choose one of the questions and answer it (thanks to Stefan Kaufmann for pointing this out to us). [9] discuss question disjunctions in the context of questions that have a choice-reading, e.g. What did someone read? This question can be understood as a directive to the answerer to choose a person and say for that person what s/he read, e.g. John read 'War and Peace'. In this sense, such a question can be understood as a disjunction of wh-questions, e.g. What did John read or what did Mary read or what did Paul read...? The answerer is to choose one of these questions and answer it. We assume here that a question with a choice reading is a special semantic object - a set of questions which is quite different from the question denotations in all semantic question theories that have been proposed.

[^20]:    ${ }^{1}$ Many thanks to Emmanuel Chemla, Vincent Homer and Benjamin Spector for suggestions and criticisms. This work is still quite preliminary.

[^21]:    ${ }^{2}$ Thanks to B. Spector for discussion of this and related examples.

[^22]:    lawyer.
    $\neq>$ If Jean had called his mother, she would have called her lawyer.
    b. *Il est concevable que Jean ait appelé sa mère. Elle ait appelé son avocat. It's conceivable that Jean has-sub called his mother. She had-subj called her lawyer.
    a'. Il est concevable que Jean ait appelé sa mère, qui aurait/aura appelé son avocat.
    It's conceivable that Jean has-subj called his mother, who would/will have called her lawyer.
    => If Jean had called his mother, she would have called her lawyer.
    b'. Il est concevable que Jean ait appelé sa mère. Elle aurait/aura appelé son avocat.
    It's conceivable that Jean has-subj called his mother. She would/will have called her lawyer.
    => If Jean had called his mother, she would have called her lawyer.

[^23]:    ${ }^{1}$ By the way, one can also change the semantics to require that $\llbracket X \rrbracket \neq \emptyset$ in order that All $X$ are $Y$ be true. One can make similar modifications to other semantics in the area. The point is that one can work with data provided by real people ignorant of logic and mathematics and then try to find logical systems for such data.

[^24]:    ${ }^{2}$ These objections are my formulations. I would not want to give the impression that Quine or anyone else agreed with them. In another direction, I do have to wonder how anyone could see what logic for sentences as they come would look like without actually doing it.

[^25]:    ${ }^{1}$ Early contributions to natural logic are [14] and [20]. The research line we base ourselves upon is exemplified in $[9,10,2,3,19,8,4,11,22,15,16]$.

[^26]:    ${ }^{2}$ Types will be relational, as in [18].

[^27]:    ${ }^{3}$ In natural language there are entailment relations within many categories [12]. If $A \subset B$ is true in all models under consideration, we say that $A$ entails $B$. For example, sparrow entails bird and each entails most.

[^28]:    ${ }^{4}$ We follow the convention, usual in type-logical work, that association in terms is to the left, i.e. $A B C$ is short for $(A B) C$ (which in its turn is short for $((A B) C))$.

[^29]:    ${ }^{1}$ By this I really mean $\vdash T a \overline{\bar{T}}$ and $\vdash \overline{\bar{T}} a T$.
    ${ }^{2}$ I will always assume that $\phi_{1}, \phi_{2} \vdash \psi$ iff $\phi_{2}, \phi_{1} \vdash \psi$.

[^30]:    ${ }^{3}$ This by itself is not general enough. To express the mathematical property of density, for instance, we need to be able to combine a binary relation with a ternary relation.
    ${ }^{4}$ Of course, the active-passive transformation only works for binary relations. For more-ary relations it fails. Fortunately, we can do something similar here, making use of some functions introduced by Quine in his proof that variables are not essential for first-order predicate logic. We won't go into this here.

[^31]:    ${ }^{5}$ Cf. Sommers (1982) and van Benthem (1983)

[^32]:    ${ }^{6}$ In terms of our framework, Leibniz assumed that all terms being part of the predicate within sentences of the form $S a P$ and $S i P$ occur positively. But this is not necessarily the case once we allow for all types of complex terms: $P$ doesn't occur positively in $S a(P a R)$, for instance. On Leibniz's assumption, some invalid inferences can be derived (cf. Sanches, 1991). These invalid inferences are blocked by our more fine-grained calculation of monotonicity marking.
    ${ }^{7}$ From this rule we can derive that $S i(O i R) \equiv O i\left(S i R^{\cup}\right)$ is also valid. And that is correct: the sentence 'A man loves a woman' is truth-conditionally equivalent to 'A woman is loved by a man'.

[^33]:    ${ }^{8}$ With $\Gamma=M a, \Theta=W i, R=L$, and $M=M a L^{U}$.

[^34]:    * Preliminary Draft: substantial revisions anticipated/hoped for final version.

[^35]:    ${ }^{1}$ But we are claiming that vagueness is not a result of degrees of truth or likelihood. Vagueness rides atop distributions of certain facts. I.e. contra fuzzy logic, an individual is either tall or not tall, rather than tall to a degree $x$ and not tall to a degree $1-x$.

[^36]:    ${ }^{2}$ Accounts of the semantics of scalar predicates fall into two broad categories: those in which the semantics refers directly to a standard of comparison or threshold degree ( $d$, above), which may be derived normatively, and those in which the semantics refers to a comparison class. Our main claims could be stated either way, but for simplicity and concreteness we stick to an account based on explicit mention of a degree. In terms of the statistical model we advance, we take it that the comparison class would act as a prior in determining the distribution over values for the threshold, though we leave the details as an open issue. Likewise, we do not explicitly consider here how normative factors affect the threshold: it suffices for our main claims that while normative factors may constrain the threshold, they will typically not constrain the threshold to be a single, perfectly precise value.
    ${ }^{3}$ Actually, the arguments of $[4,5,6,7]$ fall short in a second way: these authors do not distinguish fuzzy truth-valued from probabilistic accounts of the truth of vague sentences. But in fact many criticisms of fuzzy accounts do not extend to statistical approaches. For example, fuzzy accounts fail to explain the contradictoriness of

[^37]:    ${ }^{4}$ Thanks to Nicholas Asher for pointing out the parallel.

[^38]:    ${ }^{5}$ This is not a measure or quantity of information or information content such as entropy, self information, or mutual information. It is more akin to the notions of semantic information or meaningful data [see 16]. It is a way of drawing inferences or mapping from observations to unobserved but possible observations; not the facts but a tool that could be used to narrow in on them.

[^39]:    ${ }^{6}$ Pragmatic accounts have also contributed to our understanding of vagueness: we are friends of the idea that vagueness is tied to the purposes and practices of communication and that the uncertainties present in the communicative situation impact what speakers and hearers are willing to accept or find useful [21, 22]. There have also been other models of vagueness as language games. As we do, these [6, 23] derive vagueness from assumptions about communication, but our model is unique in being an information channel game and in providing a criterion for vagueness along with a notion of the information conveyed by vague expressions.
    ${ }^{7}$ De Jaeger [23] also notes a deep connection between vague communication and epistemic uncertainty as suggested by a signaling game with correlated equilibria.

[^40]:    ${ }^{1}$ Nothing hinges on this type of an analysis of gradability. If an analysis without degrees can be made to work out, then probably it can also be made compatible with the present proposal.

[^41]:    ${ }^{2}$ Notice that in this formulation $X_{t}$ is given in each word/ completion separately, which allows us to represent vagueness with regard to the set of 'relevant' individuals (cf., Sassoon, 2009).

[^42]:    ${ }^{3}$ For other examples and implications, see Sassoon (2009) and references therein.
    ${ }^{4}$ von Fintel and Gilles (2008) develop also a pragmatic theory of usage of epistemic modals. The present paper provides a theoretical setup, based on which this theory can be tested against data about taste statements. The discussion in the next section is preliminary, but nonetheless suggests that doing so can indeed be fruitful.

[^43]:    ${ }^{5}$ In fact von Fintel and Gilles (2008) illustrate this with epistemic modals, e.g., following a blood test that may rule out the possibility that John has cancer, an utterance of I don't know whether john might have cancer; I will ask the doctors cannot mean "I don't know whether, in view of what I know, John might have cancer". The doctors' knowledge is at stake.

[^44]:    ${ }^{6}$ In Hebrew we find: Bill gavoha le-gilo ('Bill is tall for his age'); Ha-uga teima le-Bill/ lexatulim ('The cake is tasty for Bill/ for cats') and Le-or ha-yeda shely, ... ('For all that I know,...'). In Italian we find: È grande per la sua età ('( $\mathrm{s} / \mathrm{he}$ ) is big for his age'); La torta e' gustosa per me / per (i) gatti ('The cake is tasty for me /for (the) cats'); and Per tutto ciò che so, ... ('For all that I know,...')

[^45]:    ${ }^{1}$ Differences between speakers are particularly difficult to accommodate in epistemicist (i.e., "vagueness as ignorance" approaches to vagueness, which often assume that there is always only one true answer to the question "Is this person tall". See Van Deemter (to appear, Chapter 7) for discussion.

[^46]:    ${ }^{2}$ Parikh does not discuss this possibility, but he does hint briefly at a closely related one, without analysing it further or discussing its implications: "It may be worth pointing out that probably Bob does have another larger set of Bluish(Bob) books which includes both Blue(Ann) and Blue(Bob). After looking through Blue(Bob), he will most likely look only through the remaining Bluish(Bob) books. (Parikh (1994), p. 533)." See also our section 4, where expressions like "somewhat tall" are discussed.

[^47]:    ${ }^{3}$ Other assumptions can have similar consequences. See e.g. section 2, where we assumed that $\|\overline{\operatorname{tall}}\|_{\mathcal{A}}=\|\overline{\operatorname{tall}}\|_{\mathcal{B}}$.

[^48]:    ${ }^{1}$ Note that there is a reading of (4) and (5) in which the eventive predicates are acceptable. Such a reading, however, exemplifies a distinct now, which is not discussed in this paper; it is morphologically distinguished from the now considered here in languages like Russian (cf. sejcas vs. teper discussed in [6]) and Korean (cf. cikum and icey discussed in [7]).
    ${ }^{2}$ A potential problem is that it violates Kaplan's prohibition: natural language operators do not shift indexical expressions ([13]). This prohibition explains why, e.g. we cannot say Spinoza thought that I am God to mean "Spinoza thought that he is God." According to another

[^49]:    analysis, advanced in [14], FID is a special case of direct speech or quotation. However, to the best of knowledge, this view does not shed any new light on (2)-(6).

[^50]:    ${ }^{3}$ On this analysis, the contribution of tense is superfluous in the presence of certain adverbs. Following [24], I take this to reflect a remarkable property of natural language that in the presence of an adverbial like $a$ week ago, the past tense must still be expressed.

[^51]:    4 (15) is infelicitous out-of-the-blue whether then occurs sentence-initially or sentence-final. See [28] and references therein for more discussion about the different uses of then.

[^52]:    5 This assumption is independently needed to explain why past perfect clauses often form a narrative progression in flashback discourses (cf. [5], pp. 593-611).

[^53]:    ${ }^{3}$ This "ternary" view of logical consequence is advocated in particular by van Benthem [2], who traces it back to Bolzano.

[^54]:    ${ }^{4}$ Essentially the conditions in Peter Aczel's notion of a replacement system from [1].
    ${ }^{5}$ Writing $\psi R \varphi$ instead of $\{\psi\} R \varphi$.
    ${ }^{6}$ The notion of a consequence relation could be varied in various ways, but in this paper we stick to Definition 2.

[^55]:    ${ }^{7}$ For readability, we use ${ }^{\text {' }} \Rightarrow_{X}$ in two ways: as a relation symbol, which enables us to write things like $\Gamma \Rightarrow_{X} \varphi$, and as the value of the function $\Rightarrow_{\_}: S y m b_{L} \longrightarrow B C O N S_{L}$ for the argument $X$.

[^56]:    ${ }^{8} u / u^{\prime}$ is the replacement which maps $u$ to $u^{\prime}$ but is the identity on all other symbols.
    ${ }^{9}$ This is a variation on a similar idea first introduced in [4], Ch. 9.

[^57]:    ${ }^{10}$ Writing $\Rightarrow_{X} \varphi$ for $\emptyset \Rightarrow_{X} \varphi$, i.e. $\varphi$ is valid relative to the constants in $X$.

[^58]:    * I want to thank Lucas Champollion for mentioning this problem in the context of plural logic and for subsequent discussion and comments, Pranav Anand, Rick Nouwen, Livio Robaldo, the UCSC S-Circle audience (11/23/2009) and two anonymous Amsterdam Colloquium 2009 reviewers for comments on earlier versions of this paper and Melissa Frazier, Grant McGuire and Jessica Rett for data discussion.
    ${ }^{1}$ As Krifka (1999), Landman (2000) and Ferreira (2007) observe. See Robaldo (2009) for a different take on the data.

[^59]:    ${ }^{2}$ I am indebted to Lucas Champollion for many helpful comments on this subsection.
    ${ }^{3}$ From the Corpus of Contemporary American English, www.americancorpus.org.

[^60]:    * I thank Adrian Brasoveanu for sharing his insights and for the stimulating discussion, which has led to many connections between our two papers in this volume. My thanks also go to my advisor, Cleo Condoravdi, and to the friendly environment at PARC, particularly Danny Bobrow, Lauri Karttunen, and Annie Zaenen. I am grateful to Johan van Benthem and Eric Pacuit for providing a forum for presentation of an early version of this work. Eytan Zweig gave helpful feedback on an earlier version.

[^61]:    ${ }^{1}$ In this paper, I talk of models and logical representation languages only for convenience. I don't make any ontological claims about their existence. Readers who doubt that we should ascribe existence to models or logical representation languages in the first place should interpret the claims about whether events and thematic roles "exist" as claims about whether natural language is rich enough to express meanings which, if we choose to represent them formally, go beyond what can be expressed without using notational devices such as event variables and thematic relations.
    ${ }^{2}$ In algebraic frameworks, the domains of individuals and, if present, of events are each partially ordered by a mereological part-of relation $\sqsubseteq$. On the basis of $\sqsubseteq$, an operation $\oplus$ is defined that maps entities onto their sum, or least upper bound. $\sqsubseteq$ orders the domains of individuals and events each into a complete join semilattice; in other words, the sum operation is defined for arbitrary nonempty subsets of these domains. Singular common nouns denote predicates over atomic individuals (individuals that have no parts); plural common nouns hold of sums. The pluralization operator, written ${ }^{*}$, closes predicates $P$ under sum, i.e. ${ }^{*} P$ is the smallest set such that (i) if

[^62]:    $P(X)$ then ${ }^{*} P(X)$; (ii) if ${ }^{*} P\left(X_{1}\right)$ and ${ }^{*} P\left(X_{2}\right)$ then ${ }^{*} P\left(X_{1} \oplus X_{2}\right)$. For more details, see e.g. Link (1998).
    ${ }^{3}$ Schein's argument against sums is based on Russell's paradox. For a rebuttal of this argument, see (Link, 1998, ch. 13).
    ${ }^{4}$ Not all native speakers I consulted report that Kratzer's reading is in fact available from (1), though it seems present for everybody in the paraphrase that adds between them). In the following, I will grant that Kratzer's factual claim about (1) is correct. In any case, it is possible that her argument could also be based on the paraphrase, once the semantics of between them has been worked out.

[^63]:    ${ }^{5}$ The ${ }^{* *}$ operator makes sure that the cumulated relation applies to every member of the two sums. Here, it enforces that each of the three editors was involved in catching mistakes. This avoids the "leakage" problem of the account in Bayer (1997).

[^64]:    ${ }^{6}$ Alternatively, the shift could be to a predicative interpretation, one that holds precisely of the sum of all mistakes. This solution is independently needed for variants every other and almost every which do not have a unique minimal witness. It could be exploited for explaining in terms of type mismatch why every is never interpreted in situ. For clarity of exposition, I stick to the referential interpretation of every.
    ${ }^{7}$ The granularity of every is determined by its complement and not by atomicity, as pointed out by Schwarzschild (1996), using examples like Every three houses formed a block. Here, quantification is over sums of three entities, not over atomic entities. So the level of granularity is sensitive to the restrictor of every.
    ${ }^{8}$ To name just a few: Ruys (1992), the papers in Szabolcsi (1997), Matthewson (2001); Sauerland (2003, 2004); Kratzer (2005); Johnson (2007); Abels and Marti (2009).

[^65]:    ${ }^{9}$ Alternatively, one can assume in the style of Matthewson (2001) that every $N$ is interpreted as a covert variant of the partitive construction each of the $N s$, and furthermore that the $N s$ can raise out of that construction to take part in a cumulative relation. This way, subject quantifiers can be interpreted in situ.
    10 This assumption is independently necessary to model the fact that if two mistakes A and B get caught, this always implies that A gets caught and B gets caught. It is necessary for the proof because Kratzer's representation in (4) does not actually exclude the technical possibility that the sum event E contains some catching events in which a sum of mistakes gets caught whose parts do not get caught individually.

[^66]:    ${ }^{1}$ Some (e.g., Portner [2008]: 366) have taken the stronger position that the unavailability of non-performative interpretations of imperatives means that the force dimension exhausts the dimensions of imperative meaning. This latter position is too strong. As I argue in Charlow [2009a], there are dimensions of imperative meaning (e.g., facts about their inferential and logical properties) that are paradigmatically static and do not emerge straightforwardly from an account of the force dimension.

[^67]:    ${ }^{2}$ See Krifka [2004]. The traditional idea might be motivated by the idea that there is some sort of map from speech-acts onto propositional attitudes: every speech-act expresses some propositional attitude, and speech-act types are individuated by the sort of attitude they generally function to express-asserting that $\phi$ expresses belief that $\phi$, questioning whether $\phi$ expresses wondering whether $\phi$, etc.

[^68]:    ${ }^{3}$ UIS are trivially restricted: $!\phi:=O(\phi / T)$.
    ${ }^{4}$ The Limit Assumption simplifies our discussion (with no worrying commitments).

[^69]:    ${ }^{5}$ Note: allowing ! to take widest scope in CIs lets us handle cis with quantificational adverbials in consequent position. Consider the CI if your boss comes in, never stare at him. Schwager [2006] assigns this sentence a wide-scope LF: the antecedent restricts the domain of the quantificational adverbial, and the necessity modal takes scope over the adverbial. Schwager takes this to be evidence for the modal analysis, but simply allowing! to take widest scope (thus allowing the conditional antecedent to subsequently restrict the adverbial) lets us mimic her analysis.

[^70]:    ${ }^{6}$ People do quibble with this judgment. Kolodny \& MacFarlane [2009] argue that they are mistaken. Space prevents me from rehearsing the arguments here.

[^71]:    ${ }^{7}$ We could predict the right relationship between CIs and cos by rewriting the Kratzer semantics as a strict conditional semantics, so that $\llbracket O(\phi / \psi) \rrbracket^{c, w}=1$ iff $\forall v \in \llbracket \phi \rrbracket^{c}$ : $\llbracket O(\psi / T) \rrbracket^{c, v}=1$. But this seems like an ad hoc revision of the semantics.

[^72]:    ${ }^{8}$ The issues here are discussed in more detail in my [2009b].
    ${ }^{9}$ This step relies on a kind of montonicity property of the Kratzer semantics: if $u \in$ $\min (\Phi, \preceq)$, then for any $\Psi$ such that $\bigcap \Psi \subseteq \bigcap \Phi$ and $u \in \bigcap \Psi, u \in \min (\Psi, \preceq)$.

[^73]:    ${ }^{10}$ Cf. the dynamic treatment of conjunction as function-composition: $\sigma[\phi \wedge \psi]=\sigma[\phi][\psi]$. On this treatment, the assertion of a conjunction $\phi \wedge \psi$ is a composite speech-act: an assertion of $\phi$ sequenced with an assertion of $\psi$.

[^74]:    ${ }^{11}$ Cf. Krifka [2001, 2004], who argues for representing pair-list readings of questions with universal quantification into questions.

[^75]:    ${ }^{12}$ There are possible interpretations for $\vee$ that preserve determinism. For instance, 'disjoined' speech-acts might map a context into a set of alternative contexts (cf. Mastop 2005). But this gets formally unwieldy very quickly (see esp. Krifka [2004]).

[^76]:    * I would like to thank Jeroen Groenendijk and Floris Roelofsen for their comments and suggestions, which triggered important improvements of the paper. Part of the research reported here was financially supported by the Dutch Organization for Scientific Research (NWO).

[^77]:    ${ }^{1}$ For the precise definition of resolutions of a formula, the reader is referred to Ciardelli (2009)

[^78]:    ${ }^{1}$ We denote this as $Q(\sigma)$, defined by $p \in Q(\sigma)$ iff $\exists i \in p: \forall j(j \in p \leftrightarrow\langle i, j\rangle \in \sigma)$. Notice that, if we would drop transitivity, in order to cope with conditional questions, we would need to use a pseudopartition on the dataset of $\sigma$, defined by $p \in Q(\sigma)$ iff $\forall j(j \in p \leftrightarrow \forall i \in p:\langle i, j\rangle \in \sigma)$.
    ${ }^{2}$ This is the 'ideal' situation. If not all questions can be answered, we might say that an optimal discourse is one in which those are answered than can be answered.

[^79]:    ${ }^{3}$ It also needs to be adjusted for some obvious reasons, but in ways which space prohibits detailing here. For one thing, resolutions ought to include the possibility of revision of information, or, rather, exclusion of unreliable information states.

[^80]:    ${ }^{1}$ The last problem can be avoided but we have to assume an operator that applies to syntactically derived relations and cumulates on their both arguments (see Beck and Sauerland 2000 and literature therein). This analysis has been assumed in Sternefeld (1998) and Sauerland (1998). I am assuming that this operation is not possible. Even if we allow it the analysis still faces the two other problems.

[^81]:    ${ }^{1}$ An extended version of the paper also includes predicate logic on partial variable assignments, which might offer an easier way into the format.

[^82]:    ${ }^{2}$ Longer draft with more examples available on request.

[^83]:    * We gratefully thank the audience in the Journée d'étude sur les nominalisations, University of Lille III, june 2009 and in the Séminaire Structure Argumentale et Structure Aspectuelle, University of Paris 8,26 october 2009. We also thank Fiammetta Namer from the Nancy II University for having provided the corpus.

[^84]:    ${ }^{1}$ These examples would also involve, for -age/ -ment pairs, an interplay between the Aktionsart of the verb and the grammatical aspect of the nominalization, which may a priori not hold for -agel-ée.

[^85]:    ${ }^{1}$ These arguments can only be given in their bare essentials here (see Franke, 2009, for the full story).

[^86]:    ${ }^{2}$ As for notation, $\Delta(X)$ is the set of all probability distributions over set $X, Y^{X}$ is the set of all functions from $X$ to $Y, X: Y \rightarrow Z$ is alternative notion for $X \in Z^{Y}$, and $\mathcal{P}(X)$ is the power set of $X$.
    ${ }^{3}$ Notice that this implicitly also commits us to the assumption that all messages are equally costly, or, if you wish, costless.

[^87]:    ${ }^{4}$ Models of this kind are good predictors of laboratory data on human reasoning (see, for instance, Camerer, 2003), but also solve conceptual issues with equilibrium solution concepts (see Crawford, 2003). Both of these aspects make IBR models fit for use in linguistic applications.
    ${ }^{5}$ This is the crucial difference between various IBR models such as given by Camerer et al. (2004), Jäger and Ebert (2009) and Franke (2009), for instance.

[^88]:    ${ }^{6}$ Sets of pure strategies $Z \subseteq X^{Y}$ are represented by listing for each $x \in X$ the set of all $y \in Y$ such that for some strategy $z \in Z$ we have $z(x)=y$.

[^89]:    ${ }^{7}$ In order to make this inference more specific, as it clearly should be, a slightly more careful setup of the reasoning sequence is necessary than given here. But this is a technical problem that does not disturb the conceptual point that of relevance.
    ${ }^{8}$ And with it, in slightly amended form, the syntactic account of Fox (2007).

[^90]:    * I would like to thank Hannes Rieser for giving me access to the Bielefeld SAGA Corpus and Marco Aiello, Michael Moortgat, Yoad Winter and Joost Zwarts for many discussions about semantics, space and gesture.

[^91]:    ${ }^{2}$ If we choose to work with a point-based geometry then $l o c_{\mathrm{e}}$ maps individuals to sets of points.

[^92]:    ${ }^{3}$ A possible counterexample could be for example the arc-like gesture that commonly accompany a generalized quantifier like everyone or everything. However this gesture does not seem to qualify as an iconic one, given that its distribution is quite constrained to the lexical item it accompanies and moreover it is unclear which type of spatial information it is expressing.

[^93]:    ${ }^{4}$ The speaker is also introducing other architectonic features of the church before introducing the two towers.

[^94]:    ${ }^{5}$ Nam in [6] shows how locative prepositions can be equivalently analyzed as operators that generate an intersecting predicate modifier when combined with a noun-phrase or as predicate extensors, i.e. functions that take a predicate of arity $n$ and return as a result a predicate of arity $n+1$.

[^95]:    a. Masha ne byla dolzhna chitat' knigu
    $\neg>\square$
    Masha neg was obliged read book
    b. Masha ne DOLZHNA byla chitat' knigu $\quad \square>\neg ; \neg>\square$

    Masha neg obliged was read book

[^96]:    ${ }^{1}$ The reader is referred to [7] where, independently from us, a number of arguments is provided that English must is a PPI.

[^97]:    ${ }^{1}$ Standard explicatures result from interpreting pronouns and providing spatiotemporal coordinates.

[^98]:    * I want to thank Andreas Blümel, Regine Eckardt, Paula Menéndez-Benito, Manfred Sailer and one anonymous reviewer for their very helpful comments. All mistakes are my own.

[^99]:    ${ }^{1}$ To keep things brief, the adjective counterparts of AOCs differ in that AOCs contribute a CI content to the sentence meaning (Potts 2005), while with evaluative adjectives, the propositional content (as that by AOCs) is an at-issue content (See Bonami and Godard 2008 for more detailed comparisons).

[^100]:    ${ }^{2}$ This is to say, in (9), even B agrees by saying This is indeed sad, it is still not clear that A and B express the same proposition. Rather, they could fairly well take two different judges for whom this is sad and thus express two propositions.

[^101]:    ${ }^{3}$ In her system, as (25) shows, the judge dependency only comes into play by the introduction of $P R O_{J}$, in other words, the judge parameter in the predicate of fun does nothing there. This is different from epistemic modals where the judge dependence comes with the modal verbs.

[^102]:    ${ }^{1}$ Such entailments are discussed in von Fintel and Iatridou 2005. There are further predictions, however, that at first sight are slightly counter-intuitive. For instance, von Fintel and Iatridou discuss an example like (i):

[^103]:    ${ }^{4}$ http://www.maori.org.nz/faq/showquestion.asp?faq=3\&fldAuto=99\&MenuID=3
    ${ }^{5} \mathrm{http}: / /$ www.math.lsa.umich.edu/mmss/coursesONLINE/graph/graph6/index.html
    ${ }^{6}$ It is difficult to extend the above puzzles of minimal and maximal requirement to cases of epistemic modality. This might actually be expected if the analysis of a wide scope minimality operator is on the right track, given the generalisation that epistemic modals tend to take wide scope (von Fintel and Iatridou 2003).

    Consider the following example. Say, you have seen me put 10 marbles in a box, but you do not know how many marbles there were in the box to begin with. Structurally, your knowledge state now resembles that of a minimal requirement scenario: in all compatible worlds, there are (at least) 10 marbles in the box, while in no compatible worlds there are fewer than 10 marbles in the box. Yet, in contrast to the examples given above, we cannot express this knowledge state as (i).

[^104]:    ${ }^{7}$ I am grateful to an anonymous Amsterdam Colloquium reviewer for urging me to attend to the relevance of such data.
    ${ }^{8}$ In fact, an anonymous reviewer suggests that the data extends to cases where minimum is used as a noun, as in (i).

[^105]:    * Thanks to Bernhard Schwarz, Jon Nissenbaum, Alan Bale and Sigrid Beck for their helpful guidance and comments. This research was supported in part by a FQRSC Établisement de nouveau professeur-chercheurs grant awarded to Bernhard Schwarz (FQRSC 2007-NP-114689).

[^106]:    * Thanks to Daniel Büring, Sam Cumming, Roumyana Pancheva and participants of the UCLA Syntax/Semantics Seminar for helpful comments/suggestions. Thanks to Natasha Abner for her help with an ongoing cross-linguistic equatives survey. Please visit http://www.linguistics.ucla.edu/people/rett/survey.doc if you'd like to help.

[^107]:    ${ }^{1}$ It's possible that those NPIs licensed in DE degree contexts are different from those licensed in DE individual contexts, which would explain the any data discussed above (as well as the distribution of Dutch ook maar discussed in Hoeksema, 1983).

[^108]:    ${ }^{3}$ Beaver and Clark (2008) distinguish conventional, free, and quasi-sensitivity.

[^109]:    ${ }^{4}$ We ignore a fourth condition according to which $\llbracket X \rrbracket^{o} \in C$, since we think it is superfluous. While it is unproblematic that the retrieved set $C$ sometimes will contain $\llbracket X \rrbracket^{\circ}$ there are cases in which imposing this as a constraint is implausible, for instance, cases of overt contrast.
    ${ }^{5}$ We ignore issues like tense.

[^110]:    ${ }^{6}$ See Bonomi and Casalegno (1993), Beaver and Clark (2008) for an elegant treatment of focus in event semantics.
    ${ }^{7}$ Here, we ignore intensionality.

[^111]:    ${ }^{8}$ The same point can be made using descriptions with restrictive relative clauses．
    ${ }^{9}$ A is some alternative to German．

[^112]:    ${ }^{10}$ Note that this rests on the assumption that if two different concepts $c 1$ and $c 2$ denote the same individual in a world $w$, then meet $(\operatorname{Sandy}, c 1)$ holds in $w$ iff meet $(\operatorname{Sandy}, c 2)$ holds in $w$.

[^113]:    * This paper has benefited enormously from discussions with Ivano Ciardelli and Jeroen Groenendijk, for which we are very grateful. We would also like to thank Maria Aloni and Kathryn Pruitt for helpful feedback.
    ${ }^{1}$ The semantic significance of these prosodic features has been established experimentally by Pruitt (2007).
    ${ }^{2}$ Previous work on disjunctive questions usually distinguishes block intonation from closed intonation, but does not take the open intonation pattern into account (cf. Bartels, 1999; Han and Romero, 2004a, b; Beck and Kim, 2006).

[^114]:    ${ }^{3}$ This is sometimes taken to be a general argument against 'proposition set' approaches to questions-which include, besides inquisitive semantics, the classical theories of Hamblin (1973), Karttunen (1977), and Groenendijk and Stokhof (1984)—and in favor of alternatives such as the 'structured meaning' approach or the 'orthoalgebraic' approach (cf. Krifka, 2001; Blutner, 2009). Here, we choose not to pursue a full-fledged alternative to the proposition set approach, but rather to extend it in a suitable way.

[^115]:    ${ }^{4}$ Notice that this is reminiscent of what is called non-inquisitive closure in inquisitive semantics (cf. Groenendijk and Roelofsen, 2009), and what is called existential closure in alternative semantics (cf. Kratzer and Shimoyama, 2002).
    ${ }^{5}$ Computing the H -set of a sentence with a focused expression of type $e$ in object position runs into type matching trouble in the present setup. The 'problem' is exactly the same as the one that arises for the interpretation of quantified noun phrases in object position in any system that starts with 'low types' (in particular, (e(et)) for transitive verbs, cf. Heim and Kratzer, 1998). It also has the same solutions: type-lifting, function composition, quantifier raising, or simply starting out with higher types. For simplicity's sake, we will not implement any of these possible solutions here, and simply focus on examples with focused noun phrases in subject position.

[^116]:    ${ }^{6}$ It should perhaps be emphasized that closure is not interpreted here as signaling exhaustivity (as in Zimmermann, 2000). That is, it does not imply that 'nobody else plays the piano' or something of that kind. And this is for a good reason: disjunctive interrogatives with closure intonation generally do not exhibit any exhaustivity effects. Therefore, closure intonation and exhaustivity effects should be seen as (at least partly) independent phenomena.
    ${ }^{7}$ For reasons of space, we cannot spell out explicitly here how the common ground, and updates thereof, are modeled. Groenendijk (2008) discusses the notion of a 'suggestion' that we make use of here in more detail, and provides formal definitions of acceptance and cancellation in the broader context of a dialogue management system.
    ${ }^{8}$ See (Groenendijk, 2008) and (Groenendijk and Roelofsen, 2009) for closely related observations.

[^117]:    ${ }^{3}$ Önnerfors (1997) argues that, in particular, all verb-first declaratives involving sollen as the main verb require an interpretaion of sollen as possibility.
    ${ }^{4}$ Actually, her story is more complex, as the necessity operator present in the imperative clause consists in exhaustified possibility. Nevertheless, this is relevant only in cases where exhaustification is blocked by elements like zum Beispiel 'for example'. In the absence of such elements imperatives contain a (complex) necessity operator and are thus not expected to licenze ruhig on the modal concord approach.

[^118]:    ${ }^{5}$ Ehrich assumes that sollen is ambiguous between expressing necessity and possibility. It is not clear to me how she intends to account for (i) (her (45a)), which she judges as unacceptable. The conflict is not addressed in her paper.
    (i) ${ }^{*} D u$ sollst den Rasen mähen und du sollst den Rasen nicht mähen. you shall the lawn mow and you shall the lawn not mow

[^119]:    ${ }^{6}$ If Kaufmann's (2005) modal analysis of the English simple present were extended to German, the examples in (14)-(16) may not be unmodalized. But they would still contain a necessity operator and should thus not license the presence of ruhig.
    ${ }^{7}$ This is a simplification: the set of salient available actions $A^{x}$ could change as well; also, the context set should consist of world-assignment pairs to capture standard dynamic effects. My representation is inspired by Davis (t.a.), who proposes a similar

[^120]:    analysis for Japanese $y o$. The similarity has been pointed out to me by an anonymus reviewer for 17 th Amsterdam Colloquium.
    ${ }^{8}$ In my implementation, the condition (t.a.) imposes on Japanese yo (his (23a)) reads as in (i) (with the difference that for him, $A_{c}^{x}$ need not be $A_{c^{\prime}}^{x}$ :
    (i) $\quad\left(\exists \alpha \in A_{c^{\prime}}^{x}\right)\left[\left(\forall w_{i}, w_{j} \in C S_{c^{\prime}}\right)\left[\left[\alpha\left(w_{i}\right) \& w_{j}<_{g_{c}^{\prime}\left(w_{j}\right)} w_{i}\right] \rightarrow \alpha\left(w_{j}\right)\right]\right]$.

    If this is correct for yo (cf. McCready 2006 for an analysis that does not display much similarity between ruhig and yo), at least two differences are to be observed:

[^121]:    (a) unlike ruhig, yo does not require $\alpha$ to be mentioned in the sentence; (b) ruhig requires that $\alpha$ become globally optimal.
    ${ }^{9}$ Davis' requirement would make wrong predictions: e.g., an explicit prohibition to take a cookie removes all worlds where both preferences can be fulfilled simultaneously. Afterwards, (if nothing else is prohibited) both taking a cookie and not taking a cookie meet his condition (even if neither is globally optimal). Contrary to fact, ruhig would thus be predicted to be licensed in a prohibition.
    ${ }^{10}$ Note that the inacceptability of ruhig in interrogatives, even if used as indirect speech acts, indicates that the update-conditions imposed by ruhig pertain to the minimal ('automatic') update and ignore additional effects as mediated by pragmatic considerations. I am indebted to Eric McCready (p.c.) for pointing this out.

[^122]:    ${ }^{11}$ Roughly, inducing a change in a modal state of affairs, rather than describing it.

[^123]:    * This research was supported in part by a FQRSC Établisement de nouveau professeurchercheurs grant awarded to the author (2007-NP-114689), and a FQRSC Programme Soutien aux équipes de recherche grant (2010-SE-130906, principal investigator: Lisa Travis).

[^124]:    \|lang\| $=\lambda d . \lambda x . \lambda w . x$ 's length in $w \geq d$

[^125]:    ${ }^{2}$ However, even not being a degree operator, the translations given are mere approximations. Note, for example, that the English translation given in (1) remains acceptable if nongradable TWO-HEADED replaces gradable LONG.

[^126]:    3 Apart from the issue discussed in the next section, a potential problem for this analysis (which it shares with the proposal in [4]) concerns possible licensing by expressions that are non-upward entailing without being downward entailing. The account predicts that a contradiction can be avoided if noch so scopes over a non-upward entailing expression,

[^127]:    whether downward entailing or not. The data do not seem to bear out this predication for noch so. For example, noch so is never licensed by a quantifier like genau drei Studenten 'exactly three students', which is neither upward nor downward entailing.
    4 That degree properties like the ones in (7) and (8) are strictly monotone, even if the scale in question is dense, is proposed explicitly in [8].
    5 [6] makes a similar point (evaluating proposals in [7] and [12]) with regard to the analysis of even.

[^128]:    ${ }^{6}$ The latter assumption follows from the assumption that the set of poems is finite.

[^129]:    * I would like to thank Nicholas Asher, Fritz Hamm, Hans Kamp, Elena Karagjosova, Uwe Reyle, and Antje Roßdeutscher for discussion.
    ${ }^{1}$ In the below discussion of the general semantic properties of because (of), I will mostly use examples involving nominal-complement because of. The overall analysis carries over to sentential-complement because, though. See Section 3 for a difference in interpretation between the two variants, though.

[^130]:    ${ }^{2}$ Thus, the modifier "plain" does not refer to a certain complexity of causal processes, but merely serves to separate this interpretation of because (of) more clearly from the reason interpretation, which is also taken to be a cause of sorts, as will become clear below.
    ${ }^{3}$ It may be noted that - contrary to a suggestion one often encounters - morphophonological considerations, according to which a difference in the availability of phonological reduction could constitute a reflection of a difference in semantic status, do

[^131]:    not provide evidence for any necessity of treating because and because of separately: Data from conversations and informal writing show that both variants are subject to such reduction. Thus, one may find both because or cos on one hand, and because of or cos of on the other.

[^132]:    ${ }^{4}$ The repetition of conditions which can be observed in Figure 2 is indeed intended. However, for reasons of space, it is a matter which I cannot discuss here. See van Genabith et al. (to appear) for details.

[^133]:    ${ }^{1}$ Note that with the definition of POS in (18), differential cases such as (8) and (9) must be handled slightly differently than above. This can be accomplished by defining the comparative morpheme -er in such a way to produce an interval of the same length as the original gap, but lower bounded by 0 . This is worked out in detail in Solt (2009).

[^134]:    ${ }^{2}$ Alternately, the DegP could be analyzed as occuring in the specifier position of some higher functional head in the extended adjectival projection.

[^135]:    ${ }^{3}$ Notice, that necessity of using loops suggests more complex verification strategies, e.g., people can try to pair object or just count all of them and then divide by 2 . There might be no obvious minimal startegy corresponding to the one coded by the automata. The hypothesis would be that if train in using the minimal startegy after a while subjects will improve on parity quantifiers, even performing better than on numerical quantifiers.

[^136]:    ${ }^{1}$ Tatevosov rejects the label 'pluractionality' for characterising the phenomenon he describes. However, the objection he raises concerning the singularity of the participants in the event, applies to event-external pluractionality, and on the contrary, supports a characterisation as event-internal plurality. Another objection he raises is that -kala- does not produce the full spectrum of readings typically associated with pluractionality, and the readings mentioned in the paper appear to be all forms of decrease. Note that having a partial spectrum is rather the standard case for an affix, and that the readings -kala- produces are typical forms of diminutive event-internal plurality.

[^137]:    ${ }^{2}$ This word-formation option is available in other Romance languages, where it appears to be much less productive. Evaluative morphology typically belongs to the nominal domain, but has a variety of uses (Jurafsky, 1996).

[^138]:    ${ }^{3}$ Knocking at the door can be a planned act, indeed semelfactives are not just predicates for unintentional physical acts such as sneezing.

